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Chapter 2

More on Functions

Exercise Set 2.1

- Forx-values from–5 to 1, they-values increase from -3 to 3. Thus the function is increasing on the interval (-5,1).
 - b) Forx-values from 3 to 5, they-values decrease from 3 to 1. Thus the function is decreasing on the interval (3,5).
 - c) Forx-values from 1 to 3,vis 3. Thus the function is constant on (1,3).
- 2.a) Forx-values from 1 to 3, they-values increase from 1 to 2. Thus, the function is increasing on the interval (1,3).
 - b) Forx-values from 5- to 1, they-values decrease from 4 to 1. Thus the function is decreasing on the interval (-5,1).
 - c) Forx-values from 3 to 5, vis 2. Thus the function is constant on (3,5).
- **3.**a) Forx-values from 3- to 1, they-values increase from 4 to 4. Also, forx-values from 3 to 5, the *y*-values increase from 2 to 6. Thus the function is increasing on (-3,-1) and on (3,5).
 - b) Forx-values from 1 to 3, they-values decrease from 3 to 2. Thus the function is decreasing on the interval (1,3).
 - c) Forx-values from-5 to-3,*y* is 1. Thus the function is constant on (-5,-3).
- 4.a) Forx-values from 1 to 2, they-values increase from 1 to 2. Thus the function is increasing on the interval (1,2).

 b) Forx-values from 5-to 2,-they-values decrease from 3 to 1. Forx-values from 2-to 1, they-values decrease from 3 to 1. And forx-values from 3 to 5,

they-values decrease from 2 to 1. Thus the function

is decreasing on (-5,-2), on (-2,1), and on (3,5).

c) For*x*-values from 2 to 3,*y* is 2. Thus the function isconstant on (2,3).

5.a) Forx-values from– ∞ to–8, they-values increase

from–∞to

2. Also, forx-values from-3 to-2, the *y*-values increase from-2 to 3. Thus the function is increasing on $(-\infty, -8)$ and on (-3, -2).

- b) Forx-values from-8 to-6, they-values decrease from 2to-2. Thus the function is decreasing on the interval (-8,-6).
- c) Forx-values from-6 to-3,yis-2. Also, forx-values from-2 to ∞ ,yis 3. Thus the function is constant on (-6,-3) and on (-2, ∞).

- **6.**a) Forx-values from 1 to 4, they-values increase from 2 to 11. Thus the function is increasing on the interval (1,4).
 - b) Forx-values from-1 to 1, they-values decrease from 6 to 2. Also, forx-values from 4 to∞, they- values decrease from 11 to-∞. Thus the function is decreasing on (-1,1) and on (4,∞).
 - c) Forx-values from-∞to-1,vis 3. Thus the func- tion is constant on(-∞,-1).
- **7.**The*x*-values extend from–5 to 5, so the domain is

[-5,5]. They-values extend from-3 to 3, so the range is [-3,3].

- 8.Domain: [-5,5]; range: [1,4]
- **9.**The*x*-values extend from−5 to−1 and from 1 to 5, so the domain is[−5,−1]∪[1,5].

They-values extend from-4 to 6, so the range is [-4,6].

- **10.**Domain: [-5,5]; range: [1,3]
- **11.**The*x*-values extend from–∞to∞, so the domain is (–∞,∞).

They-values extend from– ∞ to 3, so the range is (– ∞ ,3].

- **12.**Domain: (-∞,∞); range: (-∞,11]
- **13.** From the graph we see that a relative maximum value of the function is 3.25. It occurs at*x*= 2.5. There is no relative minimum value.

The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point, the graph decreases. Thus the function is increasing on $(-\infty, 2.5)$ and is decreasing on $(2.5, \infty)$.

14. From the graph we see that a relative minimum value of 2 occurs atx= 1. There is no relative maximum value.

The graph starts falling, or decreasing, from the left and stops decreasing at the relative minimum. From this point, the graph increases. Thus the function is increasing on $(1,\infty)$ and is decreasing on $(-\infty,1)$.

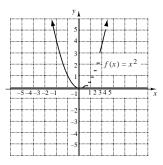
15. From the graph we see that a relative maximum value of the function is 2.370. It occurs atx = 0.667. We also see that a relative minimum value of 0 occurs atx = 2.

The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point it decreases to the relative minimum and then increases again. Thus the function is increasing on $(-\infty, -0.667)$ and on $(2,\infty)$. It is decreasing on (-0.667, 2).

16. From the graph we see that a relative maximum value of 2.921 occurs atx= 3.601. A relative minimum value of 0.995 occurs atx= 0.103.

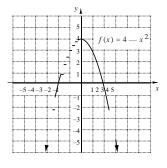
The graph starts decreasing from the left and stops decreasing at the relative minimum. From this point it increases to the relative maximum and then decreases again. Thus the function is increasing on (0.103,3.601) and is decreasing on $(-\infty, 0.103)$ and on $(3.601, \infty)$.

17.

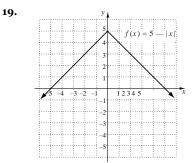


The function is increasing on $(0,\infty)$ and decreasing on $(-\infty,0)$. We estimate that the minimum is 0 at x=0. There are nomaxima.

18.

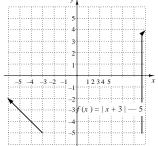


Increasing: $(-\infty, 0)$ Decreasing: $(0,\infty)$ Maximum: 4 atx= 0 Minima: none

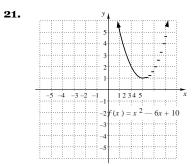


The function is increasing on $(-\infty, 0)$ and decreasing on $(0, c_{2})$. We estimate that the maximum is 5 at x = 0. There are nominima.

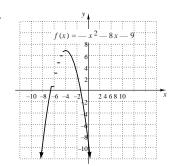




Increasing: $(-3,\infty)$ Decreasing: $(-\infty,-3)$ Maxima: none Minimum:-5 atx=-3



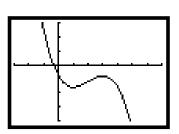
The function is decreasing on $(-\infty,3)$ and increasing on (3,2). We estimate that the minimum is 1 at x=3. There are no maxima.



Increasing: $(-\infty, -4)$ Decreasing: $(-4, \infty)$ Maximum: 7 atx=-4Minima: none

23.

22.

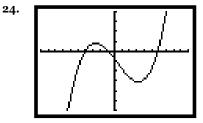


Beginning at the left side of the window, the graphfirst

drops as we move to the right. We see that the function is

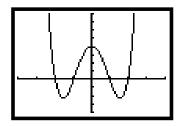
25.

decreasing on $(-\infty, 1)$. We thenfind that the function is increasing on (1, 3) and decreasing again on (3,) "The MAXIMUM and MINIMUM features also show that the relative maximum is–4 atx= 3 and the relative minimum is–8 atx= 1.

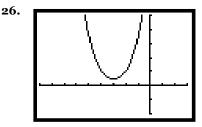


Increasing: (-∞,-2.573), (3.239,∞)

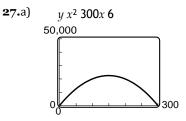
Decreasing: (-2.573,3.239) Relative maximum: 4.134 atx=-2.573 Relative minimum:-15.497 atx= 3.239



We find that the function is increasing on (-1.552,0) and on $(1.552,\infty)$ and decreasing on $-(\infty, -1.552)$ and on (0,1.552). The relative maximum is 4.07 at x=0 and the relative minima are $\frac{2}{2}.314$ at x=1.552 and 2.314 at x=1.552.

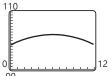


Increasing: $(-3,\infty)$ Decreasing: $(-\infty,-3)$ Relative maxima: none Relative minimum: 9.78 atx=-3



b) 22,506 ata= 150

c) The greatest number of baskets will be sold when \$150 thousand is spent on advertising. For that amount, 22,506 baskets will be sold. **28.**a) *y* 8 80.1*x*² 8 1.2*x* 8 98.6



b) Using the MAXIMUM feature we find that the relative maximum is 102.2 att= 6. Thus, we know that the patient's temperature was the highest at t= 6, or 6 days after the onset of the illness and that the highest temperature was 102.2°F.

29. Graphy=

$$\frac{6x}{x^2 + 1}$$
Increasing: (-1,1)
Decreasing: (-∞,-1), (1,∞)
30. Graphy=

$$\frac{-4}{x^2 + 1}$$
Increasing: (0,∞)
Decreasing: $\sqrt{-\infty,0}$
 $\sqrt{4x^2 + 2}$ for $2x^2$

- **31.** Graphy=x $4-x^2$, for- $2 \le x \le 2$. Increasing: (-1.414,1.414) Decreasing: (-2,-1.414), (1.414,2)
- **32.**Graph*y*=-0.8x $\overline{9-x^2}$, for $-3 \le x \le 3$. Increasing: (-3,-2.121), (2.121,3) Decreasing: (-2.121,2.121)
- *33.* If *x*= the length of the rectangle, in meters, then the <u>480–2x</u> width is 2 , or 240–x. We use the formula Area = length×width:

$$A(x) = x(240-x)$$
, or
 $A(x) = 240x-x_2$

34. Let *h*= the height of the scarf, in inches. Then the length of the base = $2h \neq -2$.

$$A(h) = \frac{1}{2}(2h-7)(h)$$

$$A(h) = h 2 - \frac{7}{2}h$$

35. After *t*minutes, the balloon has risen 120tft. We use the Pythagorean theorem. $[d(t)]^2 = (120t)^2 + 400^2$

 $d(t) = (120t)^2 + 400^2$

We considered only the positive square root since distance must be nonnegative.

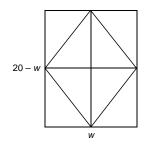
36. Use the Pythagorean theorem.

 $[h(d)]^2 + (3700)^2 = d_2$ $[h(d)]^2 = d_2 - 3700^2$

$$h(d) = \int_{d^2}^{\sqrt{--}} d^2 3700 \, {}^2\text{Taking the}$$
positive square root

37. Let*w*= the width of the rectangle. Then the

length = $\frac{40-2w}{2}$, or 20-w. Divide the rectangle into quadrants as shown below.



In each quadrant there are two congruent triangles. One triangle is part of the rhombus and both are part of the rectangle. Thus, in each quadrant the area of the rhombus is one-half the area of the rectangle. Then, in total, the area of the rhombus is one-half the area of the rectangle.

$$A(w) = \frac{1}{2}(20-w)(w)$$
$$A(w) = 10w - \frac{w^2}{2}$$

38. Let *w*= the width, in feet. Then the length =

or 23–w.

$$A(w) = (23-w)w$$

 $A(w) = 23w-w^{2}$

39. We will use similar triangles, expressing all distances in

feet. 6 in. = $\frac{1}{2}$ ft,sin. = $\frac{s}{12}$ ft, and dyd = 3dft We have

$$\frac{3d}{3} = 2^{\frac{1}{2}}$$

$$s$$

$$7 TZ_{1}$$

$$\frac{12}{3} \cdot 3d = 7 \cdot 2$$

$$\frac{3d}{4} = \frac{7}{2}$$

$$\frac{3d}{4} = \frac{7}{2} \cdot 7$$

$$\frac{3d}{4} = \frac{7}{2} \cdot 7$$

$$\frac{3d}{4} = \frac{7}{2} \cdot 7$$

$$d(s) = \frac{\int_{-\infty}^{s} \frac{14}{s}}{\frac{14}{s}}$$

40. The volume of the tank is the sum of the volume of a sphere with radius*r* and a right circular cylinder with radius*r* and height 6ft.

$$V(r) = \frac{4}{3}\pi r_3 + 6\pi r_2$$

41.a) If the length =*x*feet, then the width = 30–*x*feet.

$$A(x) = x(30-x)$$

 $A(x) = 30x-x = 2$

b) The length of the rectangle must be positive and less than 30 ft, so the domain of the function is $\{x|0 < x < 30\}$, or (0,30).

c) We see from the graph that the maximum value of the area function on the interval (0,30) appears to be 225 whenx= 15. Then the dimensions that yield the maximum area are length = 15 ft and width = 30–15, or 15 ft.

42.a)
$$A(x) = x(360-3x)$$
, or $360x-3x = 2$
360

b) The domain is
$$x < -3$$
, or

{x|0 < x < 120}, or (0,120). The maximum value occurs when

- c) The maximum value occurs when = 60 so the width of each corral should be 60 yd and the total length of the two corrals should be 360 3 60, or 180 yd.
- 43.a) If the height of thefile isxinches, then the widthis 14-2xinches and the length is 8 in. We use the formula Volume = length width height tofind the volume of thefile.

$$V(x) = 8(14-2x)x$$
, or
 $V(x) = 112x-16x = 2$

b) The height of thefile must be positive and less than half of the measure of the long si de of the pie ce of

11

plastic. Thus, the domain is
$$x \ 0 < x < \frac{14}{2}$$
, or $\{x \mid 0 < x < 7\}$.
c) $y \ 112x \ 16x^2$



d) Using the MAXIMUM feature, we find that the maximum value of the volume function occurs when x= 3.5, so there is should be 3.5 in tail.

44.a) When a square with sides of lengthxis cut from each corner, the length of each of the remaining sides of the piece of cardboard is 12–2*x*. Then the dimensions of the box arexby 12–2*x*by 12–2*x*. We

use the formula Volume = length×width×height tofind the volume of the box:

$$V(x) = (12-2x)(12-2x)(x)$$
$$V(x) = (144-48x+4x^{2})(x)$$

$$V(x) = (144x - 48x + 4x^{2})(x)$$
$$V(x) = 144x - 48x + 4x^{3}$$

This can also be expressed as $V(x) = 4x(x-6)^2$, or $V(x) = 4x(6-x)^2$.

b) The length of the sides of the square corners that are cut out must be positive and less than half the length of a side of the piece of cardboard. Thus, the domain of the function $is\{x|0 < x < 6\}$, or (0,6).

- c) y 8 4x(6 8 x)² 200
- d) Using the MAXIMUM feature, we find that the maximum value of the volume occurs when x = 2. When x = 2, $12 - 2x = 12 - 2 \cdot 2 = 8$, so the dimensions that yield the maximum volume are 8 cm by 8 cm by 2 cm.
- 45.a) The length of a diameter of the circle (and a diagonal of the rectangle) is 2.8, or 16 ft. Let/=

the length of the rectangle. Use the Pythagorean theorem to write*l*as a function of*x*.

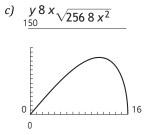
> $x_2 + l_2 = 16^2$ $x_2 + l_2 = 256$ $l_2 = 256 x_{-2}$

l= 256-x 2 Since the length must be positive, we considered only the positive square root.

Use the formula Area = length width tofind the area of the rectangle:

 $A(x) = x \sqrt[4]{256 - x^2}$

b) The width of the rectangle must be positive and less than the diameter of the circle. Thus, the domain of the function is $\{x | 0 < x < 16\}$, or (0, 16).

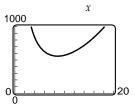


d) Using the MAXIMUM feature, we find that the max-

imum are√a occurs whenxis about 11.314. Whenx≈

main of the function is $\{x | x > 0\}$, or $(0, \infty)$. c) $y 2.5x^2 \frac{3200}{2}$

b) The length of the base must be positive, so the do-



d) Using the MIMIMUM feature, we find that the minimum cost occurs when *x*≈8.618. Thus, the dimensions that minimize the cost are about

8.618 ft by 8.618 ft by $\frac{320}{(8.618)^2}$, or about 4.309 ft.

47.
$$g(x) = \begin{cases} x + 4, \text{for } x \le 1, \\ 8 - x, \text{for } x > 1 \end{cases}$$

Since $-4 \le 1, q(-4) = -4 + 4 = 0$.

Since $0 \le 1, g(0) = 0 + 4 = 4$. Since $1 \le 1, q(1) = 1 + 4 = 5$. Since 3 > 1, g(3) = 8 - 3 = 5.

$$48.f(x) = \begin{bmatrix} 3, \text{for} x \le -2, \\ 0 \end{bmatrix} \frac{1}{2}$$

$$2^{x+6}, \text{for} x > -2$$

$$f(-5) = 3$$

$$f(-2) = 3$$

$$1$$

$$f(0) = 2 \cdot 0 + 6 = 6$$

$$f(2) = 2 \cdot 2 + 6 = 7$$

$$49.h(x) = \begin{bmatrix} -3x - 18, \text{for} x < -5, \\ 1, \text{for} -5 \le x < 1, \\ x + 2, \text{for} x \ge 1 \end{bmatrix}$$

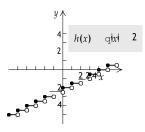
Since -5 is in the interval [-5,1], h(-5) = 1. Since 0 is in the interval [-5,1],h(0) = 1.

11.314, $256-x^2 \approx 256-(11.314)^2 \approx 11.313$. Thus, the dimensions that maximize the area are about 11.314 ft by 11.313 ft. (Answers may vary slightly due to rounding differences.)

64. $f(x) = \frac{1}{[x]} = \frac{1}{2}$

This function can be defined by a piecewise function with an infinite number of statements:

$$f(x) = \begin{array}{c} 2, f_2^{1} \text{or} -1 \le x < 0, \\ 2, f_0^{1} \text{or} 0 x \le 1, \\ -1_{1_2} \text{for} 1 \le x < 2, \\ -1, \text{for} 2 \le x < 3, \\ \end{array}$$



65.From the graph we see that the domain is $(-\infty,\infty)$ and the range is $(-\infty,0)\cup[3,\infty)$.

66.Domain: $(-\infty,\infty)$; range: $(-5,\infty)$

- **67.** From the graph we see that the domain is $(-\infty,\infty)$ and the range is $[-1,\infty)$.
- **68.**Domain: (∞,∞); range: (–∞,3)
- **69.**From the graph we see that the domain is () and the range is $\{y|y \le -2or \ y = -1or \ y \ge 2\}$.
- **70.**Domain: $(-\infty,\infty)$; range: $(-\infty,-3] \cup (-1,4]$
- 71.From the graph we see that the domain is ($-\infty,\infty$) and the range is 524

$$\{-,-,\}$$
. An equation for the function is:
-2, forx <2,
 $f(x) = -5$, forx = 2,
4, forx >2

72.Domain: $(-\infty,\infty)$; range:{ $y|y=-3or y \ge 0$ }

$$g(x) = \begin{array}{c} -3, \text{for } x < 0, \\ x, \text{for } x \ge 0 \end{array}$$

73.From the graph we see that the domain is $(-\infty, -3)$ and the range is $(-\infty, -1]$ (2ρ). Finding the slope of each segment and using the slope-intercept or point-slope formula, we find that an equation for the function is:

$$g(x) = \begin{cases} x, \text{for } x \leq -1, \\ 2, \text{for } 1 < x \geq x, \\ x, \text{for } x > 2 \end{cases}$$

This can also be expressed as follows:

74. Domain: $(-\infty,\infty)$; range: $y{y= 2\sigma r y \ 0 \ge An}$ equation for the function is:

$$h(x) = \frac{|x|, \text{for } x < 3,}{-2, \text{for } x \ge 3}$$

This can also be expressed as follows:

$$h(x) = \begin{array}{l} -x, \text{for } x \leq 0, \\ x, \text{for } 0 < x < 3, \\ -2, \text{for } x \geq 3 \\ \text{It can also be expressed as follows:} \end{array}$$

-x, for x < 0,

$$h(x) = x, \text{for } 0 \le x < 3,$$

-2, for $x \ge 3$

75. From the graph we see that the domain is [5,3] and the range is (3,5). Finding the slope of each segment and using the slope-intercept or point-slope formula, we find that an equation for the function is:

$$x + 8, \text{for} - 5 \le x < -3 \\
 h(x) = 3, \text{for} - 3 \le x \le 1, \\
 3x - 6, \text{for} 1 < x < 3$$

76.Domain: [−4,∞); range: [−2,4]

$$f(x) = \begin{array}{l} -2x-4, \text{for} -4 \le x \le -1, \\ x-1, \text{for} -1 < x < 2, \\ 2, \text{for} x \ge 2 \end{array}$$

This can also be expressed as:

$$f(x) = \begin{array}{l} -2x-4, \text{for} -4 \le x < -1, \\ x-1, \text{for} -1 \le x < 2, \\ 2, \text{for} x \ge 2 \end{array}$$

77.
$$f(x) = 5x 2-7$$

a) $f(-3) = 5(-3)^2 - 7 = 5 \cdot 9 - 7 = 45 - 7 = 38$
b) $f(3) = 5 \cdot 3^2 - 7 = 5 \cdot 9 - 7 = 45 - 7 = 38$
c) $f(a) = 5a 2 - 7$

d)
$$f(-a) = 5(-a)^2 - 7 = 5a^2 - 7$$

78.
$$f(x) = 4x^{3} - 5x$$

a) $f(2) = 4 \cdot 2^{3} - 5 \cdot 2 = 4 \cdot 8 - 5 \cdot 2 = 32 - 10 = 22$
b) $f(-2) = 4(-2)^{3} - 5(-2) = 4(-8) - 5(-2) = -32 + 10 = -22$

c)
$$f(a) = 4a \ 3-5a$$

d) $f(-a) = 4(-a) \ ^3-5(-a) = 4(-a \ 3)-5(-a) = -4a3 + 5a$

79. Firstfind the slope of the given line.

The slope of the given line is 8. The slope of a line perpendicular to this line is the opposite of the reciprocal of 8, or -.

g(x) =	<i>x</i> ,for <i>x</i> ≤ −1, 2,for−1< <i>x</i> <2,
	<i>x</i> ,for <i>x</i> ≥2

$$y-y = m(x-x = 1)$$

$$y-1 = -\frac{1}{[x-(-1)]}$$

$$y-1 = -\frac{1}{8}(x+1)$$

$$y-1 = -\frac{1}{8}x-\frac{1}{8}$$

$$y-1 = -\frac{1}{8}(x+1)$$

$$x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{2} -\frac{9}{8}$$

$$\frac{1}{2}x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{2} -\frac{9}{8}$$

$$\frac{1}{2}x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{2} -\frac{9}{8}$$

$$\frac{1}{8}x-\frac{1}{8}$$

$$\frac{9}{2}x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{2}x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{2}x+\frac{1}{8} = -\frac{1}{8}$$

$$\frac{9}{8}x-\frac{1}{8}$$

$$\frac{9}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}x-\frac{1}{8}$$

$$\frac{1}{8}x-\frac{1}{8}x$$

Relative maximum:-9.008 atx=-0.985

400

Relative minimum:-12.992 atx= 0.985

83.a) The function C(t) can be defined piecewise. 2,for 0< *t* <1, \exists 4, for $1 \le t < 2$,

$$C(t) = \bigcup_{i=1}^{n-1} 6, \text{for } 2 \le t < 3,$$

We graph this function.

4 tb) From the definition of the function in part (a), we see that it can be written as C(t) = 2[[t]] + 1, t > 0.

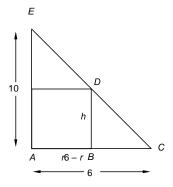
84. If
$$[[x+2]] = 3$$
, then $3 + 2 < 2$, or $- \le - \le -$

86.a) The distance from *A*toSis 4–*x*. Using the Pythagorean theorem, we find that the

> distance fromStoCis $1 + x\sqrt{2}$. Then $C(x) = 3000(4-x)+5000 \frac{1+x^2}{1+x^2}$, or 12,000-3000x + 5000 $1 + x^2$.

b) Use a graphing <u>calculator</u> to graphy= 12,000-3000x+5000 1 + x^2 in a window such as [0,5,10,000,20,000], Xscl = 1, Yscl = 1000. Using the MINIMUM feature, we find that cost is minimized when *x*= 0.75, so the line should come to shore 0.75 mi fromB.

87.a) We add labels to the drawing in the text.



We write a proportion involving the lengths of the sides of the similar trianglesBCDandACE. Then we solve it forh.

$$\frac{h}{6-r} = \frac{10}{6}$$

$$h = \frac{10}{6}(6-r) = \frac{5}{6}(6-r)$$

$$3605 \qquad 3$$

$$h = \frac{-r}{303}$$

$$Thus, h(r) = \frac{-5r}{3}$$

$$V = \pi r 2h$$

$$30-5r$$

$$V(r) = \pi r 2 \qquad 3$$
Substituting forh
We first express rin terms of h.
$$h = \frac{30-5r}{3}$$

$$h = \frac{30-5r}{5}$$

$$5r = 30-3h$$

$$r = \frac{30-3h}{5}$$

$$V = \pi r 2h$$

$$\frac{30-3h}{5} = 2$$

$$V(h) = \pi \qquad 5 \qquad h$$

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b)

c)

–5≤x <−4. The possible inputs forxare
$\{x -5\leq x<-4\}.$
85. If [[<i>x</i>]] ² = 25, then [[<i>x</i>]]= 5 or [[<i>x</i>]] = 5. For

 $- \le 5 - x < 4$, [[x]] = 5. For ≤ x < 6, [[x]] = 5. Thus, the possible inputs for xare $\{x|-5 \le x < -40r5 \le x < 6\}$. Substituting for *r* We can also write $V(h) = \pi h \frac{30-3h^2}{5}$. Exercise Set 2.2

1.
$$(f+g)(5) = f(5) + g(5)$$

 $= (5^2 - 3) + (2 \cdot 5 + 1)$
 $= 25 - 3 + 10 + 1$
 $= 33$
2. $(fg)(0) = f(0) \cdot g(0)$
 $= (0^2 - 3)(2 \cdot 0 + 1)$
3. $(fg)(1) = f(1) g(1)$
 $-3(1) = -3$
 $= ((-1)^2 - 3) - (2(-1) + 1)$
 $= -2 - (-1) = -2 + 1$
 $= -1$
4. $(fg)(2) = f(2) \cdot g(2)$

$$= (2^2 - 3)(2 \cdot 2 + 1)$$

= $1 \cdot 5 = 5$

1

5. ()
$$\frac{1}{f/g} = \frac{f - \frac{1}{2}}{g - \frac{1}{2}}$$

 $= \frac{-\frac{1}{2} - \frac{1}{2}}{g - \frac{1}{2}}$
 $= \frac{-\frac{1}{2} - \frac{1}{2} - \frac{3}{2}}{\frac{1}{1} - \frac{3}{2}}$
 $= \frac{\frac{4}{3} - \frac{3}{2}}{-\frac{1}{1} + 1}$
 $= \frac{4}{0}$

Since division by 0 is not defined, $(f/g) - \frac{1}{2}$ does not exist.

6.
$$(f-g)(0) = f(0) - g(0)$$

= $(0^2 - 3) - (2 \cdot 0 + 1)$
= $-3 - 1 = -4$
7. $(fg) -\frac{1}{2} = f -\frac{1}{2} \cdot g -\frac{1}{2}$

$$= -\frac{1^{2}}{2} - 3 \quad 2 \quad -\frac{1}{2} + 1$$
$$= -\frac{11}{4} \cdot 0 = 0$$
$$\sqrt[4]{-1} f(-\frac{\sqrt{3}}{2}) - \frac{1}{2} + 1$$

9. (g-f)(-1) = g(-1)-f(-1) $= [2(-1) + 1] - [(-1)^{2} - 3]$ =(-2+1)-(1-3)=-1-(-2) = -1 + 2= 1 **10.** $(g/f) - \frac{1}{2} = \frac{g - \frac{1}{2}}{f - \frac{1}{2}}$ $= \frac{2+1}{-\frac{1}{2}-3} \\ = \frac{0}{-\frac{11}{4}} \\ -\frac{1}{4}$ = 0 11. (h-g)(-4) = h(-4) - g(-4)= $(-4 + 4)^{\sqrt{4-1}}$ = $0 - \sqrt{-5}$ Since $\sqrt[]{-5}$ is not a real number, (h-g)(-4) does not exist. $12. (gh)(10) = g(10) \cdot h(10) = 10 - 1(10 + 4)$ = 9(14)= 3.14 = 42**13.** $(g/h)(1) = \frac{g(1)}{k(1)}$ $= \frac{1}{\sqrt{1+4}}$ $= \frac{0}{5} = 0$ **14.** $(h/g)(1) = \frac{\overset{5}{h(1)}}{\overset{1}{g(1)}} = \sqrt[3]{\frac{1+4}{\sqrt{\frac{1+4}{5}}}}$ = 0

Since division by 0 is not defined, (h/g)(1) does not exist. **15.** $(g+h)(1) = g(1)_{/} + h(1)$

$$= \sqrt{11 + (1 + 4)}$$

8.
$$(f/g)(-3) = \frac{\sqrt{g(-3)}}{g(-3)^2 - 3}$$

 $= \frac{\sqrt{g(-3)^2 - 3}}{2(-3)^2 - 3}$
 $= (3 + 4)^3 1$
 $= 7\sqrt{2}$
 $-2 3 + 1$

17.f(x) = 2x + 3g(x) = 3 - 5x

- a) The domain of *f* and of *g* is the set of all real numbers, or (-∞,∞). Then the domain of *f*+*g*, *f*-*g*, *ff*, 3
 - and *fg* is also $(-\infty,\infty)$. For *f/g* we must exclude

5

since
$$3 = 0$$
. Then the domain of f/g is
 $-\infty, \frac{33}{5}, 0, \infty$. For g/f we must exclude
 $3 = 3$

$$-\frac{1}{2} \operatorname{since}_{\underline{3}} f^{-} = \frac{0}{2}$$
. The domain of g/f is
$$-\infty, -\frac{1}{2} \cup -\frac{1}{2}, \infty$$
.

b)
$$(f+g)(x) = f(x) + g(x) = (2x+3) + (3-5x) = -3x+6$$

 $(f-g)(x) = f(x)-g(x) = (2x+3)-(3-5x) = 2x+3-3+5x=7x$
 $(fg)(x) = f(x) \cdot g(x) = (2x+3)(3-5x) = 6x-10x + 9x+9$

$$(ff)(x) = f(x) \cdot f(x) = (2x+3)(2x+3) =$$

$$4x^{2} + 12x + 9$$

$$(f/g)(x) = \frac{f(x)}{2x + 3} = \frac{2x + 3}{3 - 5x}$$

$$(g/f)(x) = \frac{g(x)}{2x + 3} = \frac{3 - 5x}{3 - 5x}$$

18.f(x) = -x + 1, g(x) = 4x - 2

a) The domain of
$$f, g, f+g, f-g, fg$$
, and ff is

$$(-\infty,\infty)$$
. Since $g_{2} = 0$, the domain of f/g is
 $-\infty, 1 \cup \infty$. Since $f(1) = 0$, the domain of $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$

b)
$$(f+g)(x) = (-x+1) + (4x-2) = 3x-1$$

$$(f-g)(x) = (-x+1)-(4x-2) = -x+1-4x+2 = -5x+3 + 6 2$$

$$(fg)(x) = (-x+1)(4x-2) = -4x - 2 x-(ff)(x) = (-x+1)(-x+1) = x - 2x+1 - \frac{-x+1}{2}$$

$$(f/g)(x) = -\frac{-x+1}{2}$$

$$(f/g)(x) = -\frac{4x-2}{2}$$

$$(f/g)(x) = -\frac{4x-2}{2}$$

$$g/f x - x + \frac{1}{\sqrt{-2}}$$

$$19.() = -3, () = -44$$

 $\int f x \quad x - g x \qquad x$

a) Any number can be an input in*f*, so the domain of *f* is the set of all real numbers, or (-∞,∞).

The domain of f/g is the set of all numbers in the domains of f and g, excluding those for which g(x) = 0. Since g(-4) = 0, the domain of f/g is $(-4,\infty)$.

The domain of *g*/*f* is the set of all numbers in

the domains of *g* and *f*, excluding those for which f(x) = 0. Since f(3) = 0, the domain of *g*/f is $[-4,3] \cup (3,\infty)$.

b)
$$(f+g)(x) = f(x) + g(x) = x-3 + \sqrt{x+4}$$

$$(ff)(x) = f(x) = (x_3)^2 = x_{2-6x+9}$$

$$(f/g)(x) = \frac{f(x)}{g(x)} = \frac{x-3}{\sqrt{x+4}}$$
$$(g/f)(x) = \frac{g(x)}{f(x)} = \frac{x-3}{x-3}$$
$$\sqrt{----}$$

20. f(x) = x + 2, g(x) = x - 1

a) The domain offis (-∞,∞). The domain ofg consists of all the values of for whichx-1 is nonnegative, or [1,∞). Then the domain of f+g,f-g, and fg is [1,∞). The domain offf is (-∞,∞). Sinceg(1) = 0, the domain off/g is (1,∞). Sincef(-2) = 0 and-2 is not in the

domain of *g*, the domain of *g*/*f* is [1, ∞).

b)
$$(f+g)(x) = x+2 + \frac{x-1}{\sqrt{x+1}}$$

 $(f-g)(x) = x+2 + \sqrt{x+1}$
 $fg(x) = (x+2) - \sqrt{x+1}$
 $(ff)(x) = (x+2)(x+2) = x + 4x + 4$
 $(f/g)(x) = \sqrt{\frac{x+2}{\sqrt{x-1}}}$
 $(f/g)(x) = (x+2)(x+2) = x + 4x + 4$

$$(g/f)(x) = \frac{1}{x+2}$$
21. $f(x) = 2x-1, g(x) = -2x$ 2

a) The domain of *f* and of *g* is (−∞,∞). Then the domain of *f*+*g*, *f*−*g*, *fg*, and *f* f is (−∞,∞).

For *f/g*, we must exclude 0 since g(0) = 0. The domain of *f/g* is $(-\infty, 0) \cup (0, \infty)$. For *g/f*, we must exclude 1 since 1 = 0. The domain of

$$g/f_{1S} = -\infty, \frac{1}{2} \cup \frac{1}{2}, \infty$$

The domain of *g* consists of all values of *x* for which *x*+4 is nonnegative, so we have $x+4\ge 0$, or $x\ge -4$. Thus, the domain of *g* is $[-4,\infty)$.

The domain of $f+g_{,f}g_{,}$ and fg is the set of all numbers in the domains of both f and g. This is $[-4,\infty)$.

The domain of *f* is the domain of *f*, or $(-\infty,\infty)$.

b)
$$(f+g)(x) = f(x) + g(x) = (2x-1) + (-2x = 2) =$$

 $-2x_2 + 2x-1$
 $(f-g)(x) = f(x) - g(x) = (2x-1) - (-2x = 2) =$
 $2x_2 + 2x-1$
 $(fg)(x) = f(x) \cdot g(x) = (2x-1)(-2x = 2) =$
 $-4x_3 + 2x_2$
 $(ff)(x) = f(x) \cdot f(x) = (2x-1)(2x-1) =$
 $4x_2 - 4x + 1$
 $(f/g)(x) = \frac{f(x)}{f(x)} = \frac{2x-1}{g(x)}$
 $(g/f(x)) = \frac{g(x)}{f(x)} = \frac{-2x^2}{2x-1}$

22. f(x) = x 2 - 1, g(x) = 2x + 5

a) The domain of *f* and of *g* is the set of all real numbers, or (−∞,∞). Then the domain of *f*+*g*,*f*−*g*,

fgandffis ($-\infty,\infty$). Since $g = \frac{5}{5} = 0$, the

domain of f/g is $-\infty, -2 \cup -2, \infty$. Since f(1) = 0 and f(-1) = 0, the domain of g/f is $(-\infty, -1) \cup (-1, 1) \cup (1, \infty)$.

b) (f+g)(x) = x - 1 + 2x + 5 = x + 2x + 4 (f-g)(x) = x - 1 - (2x + 5) = x - 2x - 6 (fg)(x) = (x - 1)(2x + 5) = 2x + 5x - 2x - 5 $(ff)(x) = (x - 1)^{2} = x + 2x - 2x + 1$ x - 1

$$(f/g)(x) = \frac{2x+5}{2x+5}$$

 $(g/f)(x) = \frac{2x+5}{\sqrt{2x+5}}$

- **23.** f(x) = x-3, g(x) = x+3
 - a) Sincef(x) is nonnegative for values of xin [3,)_∞ this is the domain off. Sinceg(x) is nonnegative for values of xin [-3,∞), this is the domain of g. The domain of f+g, f-g, and fg is the intersection of the domains of f and g, or [3,∞). The domain

offfis the same as the domain off, or $[3,\infty)$. For f/g, we must exclude-3 sinceg(-3) = 0. This is not in $[3, \frac{1}{2}]$ so the domain of f/g is [3,]. For g/f, we must exclude 3 since f(3) = 0. The domain

ofg/fis (3,∞).
b)
$$(f+g)(x) = f(x) + g(x) = \sqrt{x-3+x+3}$$

 $(f-g)(x) = f(x) - g(x) = \sqrt{x-3-x+3}$
 $(fg)(x) = f(x) \cdot g(x) = \sqrt{x-3-x+3} = \sqrt{2-9-x+3}$
 $(ff)(x) = f(x) f(x) = 3 \qquad 3-x-x-x-1 - 1$
 $(f/g)(x) = \sqrt{\frac{x-3}{\sqrt{x+3}}}$
 $(g/f)(x) = \sqrt{\frac{x+3}{\sqrt{x+3}}}$
 $(g/f)(x) = \sqrt{\frac{x+3}{\sqrt{x+3}}}$

24. f(x) = x, g(x) = 2-x

a) The domain offis $[0, \infty)$. The domain ofgis $(-\infty, 2]$. Then the domain off+g_if g, and fgis [0,2]. The domain offfis the same as the domain off, $[0, \Im]$. Sinceg(2) = 0, the domain of f/gis [0,2]. Sincef(0) = 0, the domain of g/fis (0,2].

b)

25. f(x) = x + 1, g(x) = |x|

26. f(x) = 4|x|, g(x) = 1-x

a) The domain of *f* and of *g* is $(-\infty,\infty)$. Then the domain of f+g, f-g, fg, and ff is $(-\infty,\infty)$.

For f/g, we must exclude 0 since g(0) = 0. The domain of f/g is $(-\infty, 0) \cup (0, \infty)$. For g/f, we

must exclude-1 since f(-1) = 0. The domain of g/f is $(-\infty, -1) \cup (-1, \infty)$.

- b) (f+g)(x) = f(x) + g(x) = x + 1 + |x| (f-g)(x) = f(x) - g(x) = x + 1 - |x| $(fg)(x) = f(x) \cdot g(x) = (x + 1) |x|$ $(ff)(x) = f(x) \cdot f(x) = (x + 1)(x + 1) = x + 2x + 1$ $(f/g)(x) = \frac{x + 1}{|x|}$ $(g/f)(x) = \frac{|x|}{x + 1}$
- a) The domain of f and of g is $(-\infty, \rightarrow)$ Then the

domain of f+g, f-g, fg, and ff is $(-\infty, \infty)$. Since

g(1) = 0, the domain of f/g is $(-\infty, 1) \cup (1, -)$ Since f(0) = 0, the domain of g/f is $(-\infty, 0) \cup (0, \infty)$.

b) (f+g)(x) = 4|x|+1-x(f-g)(x) = 4|x|-(1-x) = 4|x|-1+x

$$\begin{array}{c} ()() = 4 (1) = 4 4 \\ fg x |x| -x |x| - x |x| - x|x| \\ (ff)(x) = 4|x| \cdot 4|x| = 16x 2 \\ \hline 4|x| \end{array}$$

$$(f/g)(x) = \underbrace{1-x}_{1-x} \\ (g/f)(x) = -4|x|$$

27. f(x) = x g(x) = 2x + 5x - 3

a) Since any number can be an input for eitherforg, the domain off,g,f+g,f-g,fg, andffis the set of all real numbers, or (-∞,∞).

Sinceg(-3) = 0 andg 2
a) 11

-∞,- ∪ -³, 2 ∪ 2,∞. Sincef(0) = 0, the domain of g/fis (-∞,0)∪(0,∞).
(f+g)(x) =f(x)+g(x) =x 3+2x2+5x-3

(f-g)(x) =f(x)-g(x) =x 3-(2x2+5x-3) = x3-2x 2-5x+3

$$(f+g)(x) = \sqrt{x} + \sqrt{2} x$$

$$(f g)(x) = \sqrt{x} + \sqrt{2} - x^{-1}$$

$$(fg)(x) = \overline{x} \cdot \sqrt{2} - x^{-2}$$

$$(ff)(x) = \sqrt{x} \cdot \sqrt{x} - x^{2} = |x|$$

$$(f/g)(x) = \sqrt{x} \cdot \sqrt{x} - x^{2} = |x|$$

$$(f/g)(x) = \sqrt{x} - x^{-1}$$

$$(g/f)(x) = \sqrt{x} - x^{-1}$$

 $(fg)(x) = f(x) \cdot g(x) = x \quad 3(2x_2 + 5x - 3) =$ $(ff) f(x)^5 = f(x)^4 \cdot f(x)^3 = x \quad 3 \cdot x \quad 3 = x \quad 6$ $() ()^{-f(x)} = \underline{x_3}$

$$\begin{array}{cccc}
f/g & g(x) & 2x^2 + 5x - 3\\ ()(& g(x) & 2x^2 + 5x - 3\\ g/f & z & zx - 5x - 3\\ g/f & z & z^3\\ f(x) & z & z^3\end{array}$$

28. f(x) = x 2 - 4, g(x) = x 3

The domain of and of is (). Then the domain of +, f, $g \rightarrow \infty, \infty$). Since f g f - gfg, and ff is $(-\infty, \infty)$ g(0) = 0, the domain of f/g is $(-\infty, 0) \cup (0, \infty)$. Since f(-2) = 0 and f(2) = 0, the domain of g/f

is $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$. b) $(f_{7}g)_{5} x_{3} \overline{x}_{3} - 4 + 4 \cdot 3 x_{3} \circ r_{3}^{2} \circ r_{3}^{2} + x^{2} - 4 + x^{2} - 4$

$$\begin{aligned} & (fg)(x) = (x_2 - 4)(x_3) = x 5 - 4x 3\\ & (ff)(x) = (x_2 - 4)(x_2 - 4) = x 4 - 8x 2 + 16\\ & (f/g)(x) = \frac{x_2 - 4}{x^{3}}\\ & ()() = \\ & g/fx & \overline{x^2 - 4}\\ & 4 & 1 \end{aligned}$$

- **29.** f(x) = x + 1, g(x) = 6 x
 - a) Sincex+ 1 = 0 whenx=-1, we must exclude
 -1 from the domain off. It is (-∞,-1)∪(-1,∞). Since 6-x= 0 whenx= 6, we must exclude 6 from the domain ofg. It is (-∞,6)∪(6,∞). The domain

off+g,f g, and fg is the intersection of the

domains of f and g, or $(-\infty, -1) \cup (-1, 6) \cup (6, \circ)$. The domain of *f* is the same as the domain of *f*, or $(-\infty, -1) \cup (-1, -1) \cup (-1, -1)$.

of x for which g(x) = 0 or f(x) = 0, the domain of f/gandg/f is $(-\infty, -1) \cup (-1, 6) \cup (6, \infty)$.

b)
$$(f+g)(x) = f(x) + g(x) = \frac{4}{x+1} + \frac{1}{6-x}$$

 $(\frac{4}{x+1} + \frac{1}{6-x})$
 $(f-g)(x) = f(x) - g(x) = \frac{4}{x+1} - \frac{4}{6-x}$
 $(fg)(x) = f(x) \cdot g(x) = x+1 \cdot 6-x = (x+1)(6-x)$
 $(fg)(x) = f(x) \cdot f(x) = \frac{4}{x+1} \cdot \frac{4}{x+1} = (x+1)^2, \text{ or }$
 $\frac{16}{x^2+2x+1}$
 $(f/g)(x) = \frac{x^4}{x+1} = \frac{4}{6-x} \cdot \frac{4(6-x)}{4}$
 $(f/g)(x) = \frac{\frac{1}{6-x}}{4} = \frac{1}{6-x} \cdot \frac{x+1}{4} = \frac{x+1}{4(6-x)}$
 $(g/f)(x) = \frac{\frac{1}{6-x}}{x+1} = \frac{1}{6-x} \cdot \frac{x+1}{4} = \frac{x+1}{4(6-x)}$
 $x+1$

b)
$$(f+g)(x) = 2x 2^{-\frac{2}{2}}$$

+
 $(f-g)(x) = 2x 2^{-\frac{2^{x-5}}{x-5}}$
 $(f_g)(x) = 2x^{\frac{2^2}{x-5}} = \frac{4x^2}{x-5}$
 $(ff)(x) = 2x 2 \cdot 2x 2 = 4x^4$
 $(f/g)(x) = \frac{2x}{x-2} = 2x^2 \cdot \frac{x-5}{x-5} = x^2(x-5) = x^3 - 5x^2$

a) Since f(0) is not defined, the domain of f is

 $(-\infty,0)\cup(0,\infty)$. The domain of g is $(-\infty,\infty)$. Then the domain of f+g, f g+g, and f is

 $(-\infty, 0)$ $(0, \Rightarrow$ Sinceg(3) = 0, the domain of f/g is $(-\infty, 0)$ (0, 3) $(3, \Rightarrow$ There are no values of x for which f(x) = 0, so the domain of g/f is $(-\infty, 0) \cup (0, \infty)$.

$$(f+g)(x) = f(x) + g(x) = \frac{1}{x^3} + x^3$$

X

$$(f-g)(x) = f(x)-g(x) = \frac{1}{x} - (x-3) = \frac{1}{x^{-1}} - x+3$$

$$(fg)(x) = f(x) \cdot g(x) = \frac{1}{x} \cdot (x-3) = \frac{x-3}{x}, \text{ or } 1-\frac{3}{x^{-1}}$$

$$(ff)(x) = f(x) \cdot f(x) = {x \cdot 1 \cdot 1} = {x \cdot x \cdot x^2}$$

 $f(x) = {x \cdot x \cdot x^2 \cdot x^2}$

$$(f/g)(x) = \overset{g(x)}{=} \overset{x = 1}{=} \overset{x = 3}{=} \overset{x =$$

a) The domain of f(x) is $[-6,\infty)$. The domain of g(x) is $(-\infty,0)\cup(0,\infty)$. Then the domain of f+g, f-g, and fg is $[-6,0)\cup(0,\infty)$. The domain of ff

is $[-6,\infty)$. Since there are no valuesofxfor which g(x) = 0, the domain of f/g is $[-6,0] \cup (0,\infty)$. Since f(-6) = 0, the domain of g/f is $(-6,0) \cup (0,\infty)$.

b)
$$(f+g)(x) =$$

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 $\sqrt[4]{x+6+1}$

х

30. $f(x) = 2x 2, g(x) = \frac{1}{2}$ a) The domain of $f(5,\infty,\infty)$. Since x = 5, the domain of $g(5,\infty)$. Then the

> domain of f+g, f-g, and fg is $(-\infty, 5) \cup (5, \infty)$. The domain of ff is $(-\infty, 2)$. Since there are no values of x for which g(x) = 0, the domain of f/g.

> is $(-\infty,5)\cup(5,\infty)$. Since f(0) = 0, the domain of g/f is $(-\infty,0)\cup(0,5)\cup(5,\infty)$.

$$(f-g)(x) = \sqrt[\sqrt{x}+6-\frac{1}{\sqrt{x}}]_{x+6}$$

$$(fg)(x) = \sqrt[\sqrt{x+6}]_{x+6} \frac{1}{\sqrt{x}+6}$$

$$(ff)(x) = \sqrt[\sqrt{x+6}]_{x+6} \frac{1}{\sqrt{x}+6}$$

$$(f/g)(x) = \frac{\sqrt[n]{x+6}}{\frac{1}{x}} = \sqrt[n]{x+6} \cdot \frac{x}{1} = x \sqrt[n]{x+6}$$

$$(g/f)(x) = \underbrace{\sqrt{\frac{1}{x}}}_{=} = \frac{1}{\cdot} \cdot \underbrace{\sqrt{\frac{1}{x}}}_{=} = \underbrace{\sqrt{\frac{1}{x}}}_{=}$$

v+ 6

$$x+6 \quad x \quad x+6 \quad x \quad x+6$$
33. $f(x) = \frac{3}{x-2}$, $g(x) = \sqrt[\gamma]{x-1}$

v+ 6

a) Since *f*(2) is not defined, the domain of *f* is $(-\infty, 2)$ $\Downarrow 2$, \oiint Since g(x) is nonnegative for values of xin [1,), this is the domain of g. The domain of *f*+*g*, *f*, *g*, and *f* g is the intersection of the domains of f and g, or [1,2) (2,). The domain offfis the same as the domain off, or $(-\infty,2)$ (2,) For f/g, we must exclude 1 since g(1) = 0, so the domain of f/g is (1,2) (2, j). There are no values of *x* for which f(x) = 0, so the domain of g/f is $[1,2) \cup (2,\infty)$.

$$\frac{f(x)}{g(x)} = \frac{x^{-2}}{g(x)} = \frac{x^{-2}}{\sqrt{-2}} \frac{x^{-2}}{(x^{-2})^2}$$

$$(f/g)(x) = \frac{g(x)}{g(x)} = \frac{x^{-1}}{\sqrt{-1}} = (x^{-2}) \frac{\sqrt{-1}}{\sqrt{-1}}$$

$$) = \frac{g(x)}{\sqrt{-1}} = \frac{x^{-1}}{x^{-1}} = \frac{(x^{-2})^2 x^{-1}}{3}$$

$$34 \cdot f(x) = \frac{2}{4-x} g(x) = \frac{2}{x-1}$$

a) The domain of f is $(-\infty, 4) \cup (4, \infty)$. The domain of g is $(-\infty, 1) \cup (1, \infty)$. The domain of f+g, f-g, and *fg* is $(-\infty, 1) \cup (1, 4) \cup (4, \infty)$. The domain of *ff* is $(-\infty, 4) \cup (4, \infty)$. The domain of *f/g* and of g/f is $(-\infty, 1) \cup (1, 4) \cup (4, \infty)$.

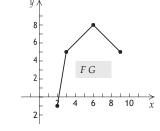
b)
$$(f+g)(x) = \frac{2}{4-x} + \frac{5}{x-1}$$

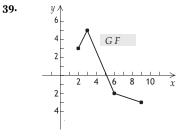
 $(f-x) = \frac{2}{4-x} + \frac{5}{x-1}$
 $(fg)(x) = \frac{2}{4-x} + \frac{5}{2} + \frac{10}{x-1}$
 $(ff)(x) = \frac{4-x}{2} + \frac{x-1}{2} = \frac{(4-x)(x-1)}{(4-x)^2}$
 $4-x + 4-x + (4-x)^2$
 $(f/g)(x) = \frac{4}{4-x} = \frac{2(x-1)}{2}$

35. From the graph we see that the domain of *F* is [2,11] and the domain of *G* is [1,9]. The domain of *F*+*G* is the set

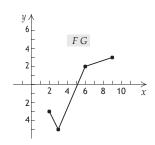
of numbers in the domains of both*F*and*G*. This is [2,9].

- **36.** The domain of *F* **G** and *FG* is the set of numbers in the domains of bothFandG. (See Exercise 33.) This is [2,9]. The domain of *F*/*G* is the set of numbers in the domains of bothFandG, excluding those for whichG= 0. Since G > 0 for all values of x in its domain, the domain of F/Gis [2,9].
- **37.** The domain of G/F is the set of numbers in the domains of bothFandG(See Exercise 33.), excluding those for which F = 0. Since F(3) = 0, the domain of G/F is $[2,3) \cup (3,9]$.
- 38.





40.



41. From the graph, we see that the domain of *F* is [0,9] and the domain of G is [3,10]. The domain of F+G is the set

of numbers in the domains of both*F*and*G*. This is [3,9].

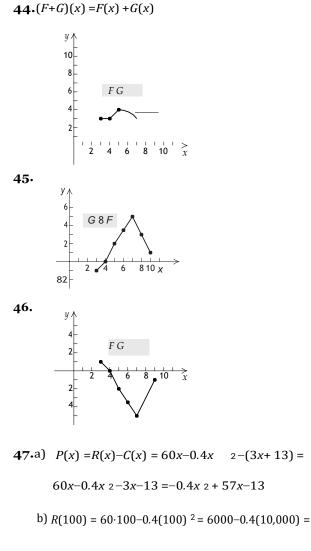
42. The domain of *F*-*G* and *FG* is the set of numbers in the domains of bothFandG. (See Exercise 39.) This is [3,9].

$$\frac{5}{x-1} = \frac{5(4-x)}{(g/f)(x)} = \frac{5}{\frac{x-1}{4-x}} = \frac{5(4-x)}{2(x-1)}$$

The domain of F/G is the set of numbers in the domains of both Fand G, excluding those for which G= 0. Since

G > 0 for all values of x in its domain, the domain of F/G is [3,9].

43. The domain of *G*/*F* is the set of numbers in the domains of both*F* and *G*(See Exercise 39.), excluding those for which F = 0. Since F(6) = 0 and F(8) = 0, the domain of *G*/*F* is [3,6) \cup (6,8) \cup (8,9].



6000-4000 = 2000C(100) = 3.100 + 13 = 300 + 13 = 313

P(100) = R(100) - C(100) = 2000 - 313 = 1687

- **48.**a) $P(x) = 200x x \ 2 (5000 + 8x) = 200x x \ 2 5000 8x = -x \ 2 + 192x 5000$
 - b) $R(175) = 200(175) 175^2 = 4375$

C(175) = 5000 + 8.175 = 6400 P(175) = R(175) - C(175) = 4375 - 6400 = -2025(We could also use the function found in part (a) to find P(175).)

$$f(x+h) = 3(x+h)-5 = 3x+3h-5$$

$$f(x+h)-f(x) = \frac{3x+3h-5-(3x-5)}{h}$$

$$= \frac{3x+3h-5-(3x-5)}{h}$$

$$= \frac{3h}{h} = 3$$
50. $f(x) = 4x-1$

$$f(x+h)-f(x) = \frac{4(x+h)-1-(4x-1)}{h} = \frac{4(x+h)-1-(4x-1)}{h} = \frac{4x+4h-1-4x+1}{h} = \frac{4h}{h} = 4$$
51. $f(x) = 6x+2$

$$f(x+h) = 6(x+h) + 2 = 6x+6h+2$$

$$f(x+h) = 6(x+h) + 2 = 6x+6h+2$$

$$f(x+h) = 6(x+h) + 2 = 6x+6h+2$$

$$f(x+h) = 6(x+h) + 3 = (5x+3) = \frac{6h}{h} = 6$$
52. $f(x) = 5x+3$

$$f(x+h)-f(x) = \frac{5(x+h)+3-(5x+3)}{h} = \frac{5x+5h+3-5x-3}{h} = \frac{5h}{h} = 5$$
53. $f(x) = 5x+3$

$$f(x+h) = \frac{1}{3} (x+h) + 1 = \frac{1}{3} x^{+} \frac{3}{3} h + 1$$

$$f(x+h) = \frac{1}{3} (x+h) + 1 = \frac{1}{3} x^{+} \frac{3}{3} h + 1$$

$$f(x+h) = \frac{1}{3} (x+h) + 1 = \frac{1}{3} \frac{x+3}{h} + 1$$

$$f(x+h) = \frac{1}{3} \frac{1}{x+3} \frac{1}{h+1} - \frac{1}{3} \frac{x+1}{h}$$

$$h = \frac{1}{3} \frac{1}{1} \frac{1}{h} \frac{1}{3} \frac{1}{1} = \frac{1}{2} \frac{1}{h} \frac{1}{3} \frac{1}{3} \frac{1}{1} = \frac{1}{2} \frac{1}{h} \frac{1}{3} \frac{1}{1} = \frac{1}{h} \frac{1}{3}$$
54. $f(x) = -\frac{1}{2} \frac{1}{x+7} \frac{1}{2} - 7$

$$f(x+h) = f(x) = \frac{1}{h} \frac{1}{2} - \frac{1}{2} \frac{1}{h} = \frac{1}{h} \frac{1}{h} = \frac{1}{2} \frac{1}{h} \frac{1}{h} = \frac{1}{2} \frac{1}{h} \frac{1}{h} = \frac{1}{2} \frac{1}{h} \frac{1}{h} = \frac{1}{2} \frac{1}{h} \frac{1}{h} = \frac{1}{2} \frac{1}{h} \frac{1}{h} = \frac{1}{h} \frac{1}{h} = \frac{1}{h} \frac{1}{h} = \frac{1}{h} = \frac{1}{h} \frac{1}{h} = \frac{1}{h} =$$

 $49 \cdot f(x) = 3x - 5$

$$55 \cdot f(x_{j}) = \frac{1}{3x}$$

$$f(x+h) = \frac{1}{3(x+h) - 1} = \frac{1}{3(x+h) - 3x_{-}}$$

$$h \qquad h$$

$$= \frac{1}{3(x+h) - 3x_{-}} = \frac{1}{3x_{+} + h}$$

$$= \frac{3(x+h) - 3x_{-}}{x - h}$$

$$= \frac{3x(x+h) - 3x(x+h)}{h}$$

$$= \frac{3x(x+h) - 3x(x+h)}{h}$$

$$= \frac{3x(x+h) - 3x(x+h)}{h}$$

$$= \frac{3x(x+h) - 3x(x+h)}{h}$$

$$= \frac{3x(x+h) - 3x(x+h) - 1}{h}$$

$$= \frac{1}{3x(x+h) - h}$$

$$= \frac{1}{3x(x+h) - h}$$

$$= \frac{1}{3x(x+h)}$$

$$56.f(x) = \frac{-}{2x}$$

$$\frac{f(x+h)-f(x)}{h} = \frac{2(x+h)}{h} = \frac{2(x+h)}{h} = \frac{2(x+h)}{h} = \frac{2(x+h)}{h} = \frac{x^2 - 1x + h}{h} = \frac{x^2 - 1x + h}{h} = \frac{2(x+h)}{h} = \frac{2(x+h)}{h} = \frac{2(x+h)}{h} = \frac{2x(x+h)}{h} = \frac{2x(x+h)}{h} = \frac{-h}{h} = \frac{-h}{2x(x+h)} \cdot \frac{1}{h} = \frac{-1}{2x(x+h)}, \text{ or } -\frac{1}{2x(x+h)}$$

57
$$f(x) = \frac{1}{4x}$$

$$f(x+h) = -4(+) + \frac{1}{x h} = \frac{1}{4(x+h)} = -\frac{1}{4x} + \frac{1}{4x} + \frac{1}{h} = -\frac{1}{4(x+h)} + \frac{1}{x - \frac{1}{4x} + \frac{x+h}{x+h}} = \frac{-\frac{1}{4(x+h)} + \frac{1}{x} + \frac{x}{x+h}}{-\frac{1}{4x(x+h)} + \frac{1}{x} + \frac{x}{x+h}} = \frac{-\frac{1}{4x(x+h)}}{h} = \frac{-\frac{1}{4x(x+h)}}{h} = \frac{-\frac{1}{4x(x+h)}}{h}$$

$$58.f(x) = \frac{1}{x}$$

$$-\frac{1}{x} = \frac{-1}{x} = -\frac{1}{x}$$

$$f(x+h)-f(x) = x+h \quad x =$$

$$\frac{1x^{h}}{-\frac{1x^{h}}{x+h} \cdot x^{-1} - \frac{1}{x} \cdot \frac{x+h}{x+h}} = \frac{1}{-\frac{1}{x(x+h)}} = \frac{1}{x(x+h)} = \frac{1}{x(x+h)} = \frac{1}{x(x+h)}$$

$$\frac{1}{x(x+h)} = \frac{1}{x(x+h)} = \frac{1}{x(x+h)} = \frac{1}{x(x+h)} = \frac{1}{x(x+h)}$$

$$59.f(x) = x + 1$$

$$f(x+h) = (x+h)^{2} + 1 = x^{2} + 2xh+h^{2} + 1$$

$$\frac{f(x+h)-f(x)}{h} = \frac{x^{2} + 2xh+h^{2} + 1 - (x^{2} + 1)}{h}$$

$$= \frac{x^{2} + 2xh+h^{2} + 1 - x^{2} - 1}{h}$$

$$= \frac{2xh+h^{2}}{h}$$

$$= \frac{h(2x+h)}{h}$$

$$= \frac{h(2x+h)}{h}$$

$$= 2x+h$$
60. $f(x) = x \ 2-3$

$$\frac{f(x+h)-f(x)}{h} = \frac{(x+h)^2 - 3 - (x \ 2-3)}{h} = \frac{x^2 + 2xh + h \ 2 - 3 - x \ 2 + 3}{h} = \frac{2xh + h \ 2}{h} = \frac{h(2x+h)}{h} =$$

h

$$\frac{x^2 + 2xh + h \cdot 2 - 3 - x \cdot 2 + 3}{h} = \frac{2xh + h \cdot 2}{h} = \frac{h(2)}{h}$$

$$2x + h$$

$$61.f(x) = 4-x_2$$

$$f(x+h) = 4-(x+h) \qquad {}^{2} = 4-(x_{2}+2xh+h_{2}) = 4-x_{2}-2xh-h_{2}$$

$$\frac{f(x+h)-f(x)}{h} = 4-x \frac{2-2xh-h 2-(4-x 2)}{h}$$

$$= \frac{4-x 2-2xh-h^{2} - 4+x 2}{h}$$

$$= \frac{-2xh-h 2}{h} = \frac{h/(-2x-h)}{h/}$$

$$= -2x-h$$
62. $f(x) = 2-x 2$

$$\frac{f(x+h)-f(x)}{h} = 2-(x+h)^{2} - (2-x 2)$$

$$= \frac{-2x-h}{h}$$

$$\frac{\frac{h}{2-x^2-2xh-h^2-2+x^2}}{h} = \frac{-2xh-h^2}{h} = -\frac{h}{h}$$

$$\frac{h(-2x-h)}{h} = -2x-h$$

$$= \underbrace{\frac{h}{4x(x+h)}}_{h} \underbrace{\frac{1}{h}}_{h} = \underbrace{\frac{h/\cdot 1}{4x(x+h)\cdot h/}}_{h} = \underbrace{\frac{1}{4x(x+h)}}_{h}$$

h63.f(x) = 3x 2-2x+1 f(x+h) = 3(x+h) 2-2(x+h) + 1 = 3(x2+2xh+h 2)-2(x+h) + 1 =

$$3x_{2} + 6xh + 3h_{2} - 2x - 2h + 1$$

$$f(x) = 3x_{2} - 2x + 1$$

$$f(x+h) = f(x)$$

$$h = \frac{1}{2}$$

$$3x_{2} + 6xh + 3h_{2} - 2x - 2h + 1) - (3x_{2} - 2x + 1)$$

$$\frac{1}{3x_{2} + 6xh + 3h_{2} - 2x - 2h + 1 - 3x_{2} + 2x - 1}{h} = \frac{1}{2}$$

$$\frac{3x_{2} + 6xh + 3h_{2} - 2x - 2h + 1 - 3x_{2} + 2x - 1}{h} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h} = \frac{h(6x + 3h^{-2})}{h - 1} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h} = \frac{h(6x + 3h^{-2})}{h - 1} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h} = \frac{h(6x + 3h^{-2})}{h - 1} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h} = \frac{h(6x + 3h^{-2})}{h - 1} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h} = \frac{h(6x + 3h^{-2})}{h - 1} = \frac{1}{2}$$

$$\frac{6xh + 3h_{2} - 2h}{h - 1} = \frac{6x + 3h - 2}{h - 1}$$

$$\frac{64.f(x)}{h} = 5x_{2} + 4x$$

$$\frac{f(x+h) - f(x)}{h} = \frac{(5x + 10xh + 5hz + 4x + 4h) - (5x + 4x)}{h} = \frac{10x + 5h + 4}{h}$$

$$\frac{65.f(x)}{h} = 4 + 5|x|$$

$$\frac{f(x+h) - f(x)}{h} = \frac{4 + 5|x + h| - (4 + 5|x|)}{h}$$

$$\frac{66.f(x)}{h} = \frac{2|x| + 3x}{h}$$

$$\frac{f(x+h) - f(x)}{h} = \frac{(2|x + h| + 3x + 3h) - (2|x| + 3x)}{h} = \frac{2|x + h| - 2|x| + 3h}{h}$$

$$\frac{67.f(x)}{h} = x_{3}$$

$$\frac{f(x+h) - f(x)}{h} = x_{3} + 3x2h + 3xh + 2h_{3} - x_{3} = \frac{3x^{2}h + 3xh + 2h_{3}}{h} = \frac{h(3x^{2} + 3xh + h_{2})}{h} = \frac{h^{2}}{h^{2}}$$

$$\frac{h^{2}}{h^{2}} = \frac{x^{3} - x}{h^{2}} + \frac{h^{3}}{h^{2}} - \frac{(x + h)^{3} - 2(x + h) - (x - 2x)}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 3x + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} = \frac{x^{3} + 3x2h + 3xh + 2h_{3} - 2x - 2h - x + 2x}{h} =$$

 $\frac{3x_{2}h+3x_{h2}+h_{3}-2h}{h(3x_{2}+3x_{h}+h_{2}-2)} = \frac{h(3x_{2}+3x_{h}+h_{2}-2)}{h(3x_{2}+3x_{h}+h_{2}-2)} = \frac{h(3x_{2}+3x_{h}+h_{2}-2)}{h(3x_{2}+3x_{h}+h_{2}-2)}$

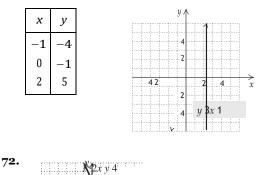
<u>x+h-4</u> <u>x-4</u> x+h+3 h x+3(x+h-4)(x+3)-(x-4)(x+h+3)h(x+h+3)(x+3) $x_{2}+h_{x}-4x+3x+3h-12-(x+h_{x}+3x-4x-4h-12)$ h(x+h+3)(x+3) $x_2 + hx - x + 3h - 12 - x$ 2 - hx + x + 4h + 12 $\begin{array}{r} h(x+h+3)(x+3)\\ \hline 7h & h\\ = \cdot \end{array}$ h(x+h+3)(x+3) h(x+h+3)(x+3)7 (x+h+3)(x+3)Х 70.f(x) =2-xx+h f(x+h)-f(x)2 - (x+h)2-xh h (x+h)(2-x)-x(2-x-h)(2-x-h)(2-x)h $2x - x_2 + 2h - hx - 2x + x_2 + hx$ (2-x-h)(2-x)h 2h(2-x-h)(2-x) h_{2h} (2-x-h)(2-x)(2-x-h)(2-x)h

71.Graph*y***=** 3*x***-**1.

We find some ordered pairs that are solutions of the equation, plot these points, and draw the graph.

When*x*=-1,*y*= 3(-1)-1 =-3-1 =-4. When*x*= 0,*y*= 3·0-1 = 0-1 =-1.

When $x = 2, y = 3 \cdot 2 - 1 = 6 - 1 = 5$.



4

69. $\begin{pmatrix} h & h \\ 3x_2 + 3xh + h & 2 - 2 \\ \end{pmatrix} = \frac{x}{f} \frac{4}{x+3}$ $\frac{f(x+h) - f(x)}{h} = \frac{x+h-4}{h} \frac{x-4}{x+3} = \frac{x+h+3}{h}$ 7**3.**Graph*x*–3*y*= 3.

First wefind thex- andy-intercepts.

$$x - 3 \cdot 0 = 3$$

x= 3

Thex-intercept is (3,0).

0–3*y*= 3

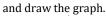
- -3y=3
- y=-1They-intercept is (0,-1).

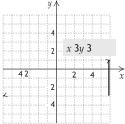
We find a third point as a check. We let *x* = 3 and solve for *y*.

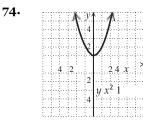
-3-3*y*= 3

-3y=6

Another point on the graph is (-3,-2). We plot the points







75. Answers may vary; $f(x) = \frac{1}{x+7}$, $g(x) = \frac{1}{x-3}$

76. The domain of h+f,h-f, and hfconsists of all numbers that are in the domain of bothhandf, or{-4,0,3}.The domain of h/fconsists of all numbers that are in the

The domain of h/f consists of all numbers that are in the domain of both h and f, excluding any for which the value of f is 0, or $\{-4, 0\}$.

77. The domain of h(x) is $x = \frac{7}{3^{-1}}$, and the domain of g(x)

is{x | x = 3}, so $\frac{7}{3}$ and 3 are not in the domain of (h/g)(x). We must also exclude the value of x for which g(x) = 0.

$$\frac{x^4-1}{5x-15} = 0$$

 $x_4 - 1 = 0$ Multiplying by 5x - 15 $x_4 = 1$ $x = \pm 1$

Exercise Set 2.3

1.
$$(f^{\circ}g)(-1) = f(g(-1)) = f(-1)^{2} - 2(-1) - 6) = f(1 + 2 - 6) = f(-3) = 3(-3) + 1 = -9 + 1 = -8$$

2. $(g^{\circ}f)(-2) = g(f(-2)) = g(3(-2) + 1) = g(-5) = (-5)^{2} - 2(-5) - 6 = 25 + 10 - 6 = 29$
3. $(h^{\circ}f)(1) = h(f(1)) = h(3 \cdot 1 + 1) = h(3 + 1) = h(4) = 4^{3} = 64$
4. $(g^{\circ}h) = \frac{1}{g} = \frac{1}{h} = \frac{1}{2} = \frac{1}{g} = \frac{1}{g}$

Then the domain of $(h/g)(x)$ is x x = 7 and $x = -1$ and $x = 1$, or						
xx ⁷ and	x 3ar	nd x = -1 and	x 1	, or		
3		77				
(-∞,-1)∪(-1,2	1) ∪	$1, \frac{1}{3} \cup \frac{1}{3}, \frac{3}{3}$	∪ (3, ∘	∞).		

 $4 \qquad 5 \ 4$ $(g \circ f)(x) = g \qquad 5^{X} = 4 - 5^{X} = x$ The domain of f and of g is $(-\infty, \infty)$, so the domain of $f \circ g$ and of $g \circ f$ is $(-\infty, \infty)$.

19.
$$(f \circ g)(x) = f(g(x)) = f(3x \ 2 - 2x - 1) = 3x \ 2 - 2x - 1 + 1 = 3x2 - 2x$$

 $(g \circ f)(x) = g(f(x)) = g(x+1) = 3(x+1) \ 2 - 2(x+1) - 1 = 3(x2 + 2x + 1) \ 2(x+1) \ 1 = 3x \ 2 + 6x + 3 \ 2x \ 2 - 1 = -3x2 + 4x$
The domain of a_fnd of is_g($-\infty,\infty$), so the domain of

 $f \circ gand \circ fg \circ fis (-\infty,\infty).$ **20.** $(f \circ g)(x) = f(x + 5) = 3(x + 5) - 2 = 3x + 15 - 2 = 3x + 13$

3x + 13 2 2 $(g \circ f)(x) = g(3x-2) = (3x-2) + 5 = 9x - 12x + 4 + 5 = 9x - 12x + 12x +$

The domain of f and of g is $(-\infty,\infty)$, so the domain of $f^{\circ}g$ and of $g^{\circ}f$ is $(-\infty,\infty)$.

- **21.** $\left(\int_{0}^{\infty} g \right) (x) = \int_{0}^{\infty} g (x) = \int_{0}^{\infty} f (4x-3) = \int_{0}^{\infty} f (4x-3) = \int_{0}^{\infty} g (4x-3) = 1 = 0$
 - $(g \circ f)(x) = g(f(x)) = g(x -3) = 4(x -3) 3 =$
 - $4x_2 12 3 = 4x_2 15$
 - The domain of f and of g is $(-\infty,\infty)$, so the domain of $f^{\circ}g$ and of $g^{\circ}f$ is $(-\infty,\infty)$.
- **22.** $(f \circ g)(x) = f(2x-7) = 4(2x-7)$ $^{2}-(2x-7) + 10 =$ $(4x^{2}-\overline{112x}+496^{-(2x-7)}+10) = 16x \ _{2}-114x+213$

 $(g \circ f)(x) = g(4x \circ 2 - x + 10) = 2(4x \circ 2 - x + 10) - 7 =$ The domain of $f^{2} = 2(4x \circ 2 - x + 10) - 7 = 2(4x \circ 2 - x + 10) - 7 =$

$$f \circ g \text{ and } ofg \circ f \text{ is } (-\infty, \infty).$$
23. $(f \circ g)(x) = f(g(x)) = f$

$$\frac{1}{x} = \frac{4}{1-5 \cdot 1} = \frac{4}{1-5} = \frac{4}{1-5x} = \frac{4}{1-5x} = \frac{4}{1-5x} = \frac{4}{1-5x} = \frac{1}{1-5x} = \frac{1-5}{1-5x} = \frac{1}{1-5x} = \frac{1}{1-5x}$$

The domain of *f* is $x \ x \ \overline{5}$ and the domain of *g* is $\{x \mid x \ 0\}$. Consider the domain of $f \circ g$. Since 0 is not in $\underline{1}$ the domain of *g*, 0 is not in the domain of *f* og. Since 5 is not in the domain of *f*, we know that g(x) cannot be 1.

The domain of f is $\{x | x = 0\}$ and the domain of g is $\frac{1}{2}$

x x = 2. Consider the domain of $f \circ g$. Since 1

off is now to the domain of f is never 0, so the domain of f is $\frac{1}{2}$, or

$$-\infty, -1$$
 $-1, \infty$.

 $2 \stackrel{\cup}{\sim} 2$ Now consider the domain of . Since 0 is not in the domain of $g^{\circ}f$ f, then 0 is not in the domain of $g^{\circ}f$. Also, since $-\frac{1}{2}$ is not in the domain of g, we find the value(s) of xfor which $f(x) = -\frac{1}{2}$.

$$6 = 1$$

$$\begin{array}{c} * & 2^{*} \\ -12 = x \end{array}$$
Then the domain of *g*° *f* is
$$\begin{array}{c} x = -12 \text{ and } x = 0 \\ x = x \end{array}$$
, or

$$(-\infty, -12) \cup (-12, 0) \cup (0, \infty).$$
25. $(f \circ g)(x) = f(g(x)) = f \qquad \frac{x+7}{3} =$

$$3\frac{x+7}{3} -7 = x+7-7 = x$$

$$(3x - 7) + 7$$

$$(g \circ f)(x) = g(f(x)) = g(3x-7) =$$

$$3 =$$

$$\frac{3x}{3} = x$$

The domain of f and of g is $(-\infty,\infty)$, so the domain of $f \circ g$ and of $g \circ f$ is $(-\infty,\infty)$.

26.
$$(f \circ g)(x) = f(1.5x + 1.2) = \frac{2}{3}(1.5x + 1.2)_{-5} \frac{4}{5}$$

 $x + 0.8 = \frac{4}{5} = x$

5

We find the value (s) of x for which $g(x) = \frac{1}{5}$.

$$\frac{1}{x} = \frac{1}{5}$$

0

5 = xMultiplying by 5x

Thus 5 is also not in the domain of $f^{\circ}g$. Then the domain of $f^{\circ}g$ is $\{x | x = 0 \text{ and } x = 5\}$, or $(-\infty, 0) \cup (0, 5) \cup (5, \infty)$.

Now consider the domain of $g \circ f$. Recall that $\frac{1}{1}$ is not in the domain of f, so it is not in the domain of $g \circ f$. Now

is not in the domain of gbut f(x) is never 0, so the domain

of
$$g \circ f$$
 is $x x = \frac{1}{5}$, or $-\infty$, $\overline{5} \cup 5'^{\infty}$.

$$(g \circ f)(x) = g \qquad \frac{2}{3}x - \frac{4}{3} = 1.5 \frac{2}{3}x - \frac{4}{5} + 1.2 = 3 \frac{5}{3}x - 1.2 + 1.2 = x$$

The domain of *f* and of *g* is $(-\infty,\infty)$, so the domain of $f^{\circ}g$ and of $g^{\circ}f$ is $(-\infty,\infty)$.

27.
$$(f \circ g)(x) = f(g(x)) = f(\stackrel{\vee}{*}) = 2 \stackrel{\vee}{x+1} (g \circ f)(x) = g(f(x)) = g(2x+1) = \stackrel{\sqrt}{2x+1}$$

The domain of f is $(-\infty,\infty)$ and the domain of g is $\{x | x \ge 0\}$. Thus the domain of $f^{\circ}g$ is $\{x | x \ge 0\}$, or $[0,\infty)$.

Now consider the domain of $g \circ f$. There are no restrictions on the domain of f, but the domain of $g is \{x | x \ge 0\}$. Since

$$f(x) \stackrel{\text{O for}}{=} x \ge - \frac{1}{2}, \text{ the domain of } g \circ f^{\text{S}} \qquad x \ge -\frac{1}{2},$$

or $-\frac{1}{2}, \infty$.

 $(-\infty,\infty)$. Since $g(x) \ge 0$ when $x \le 3$, the domain of $f \circ g$

is $-\infty, \frac{2}{3}$.

Now consider the domain of $g \circ f$. Since the domain of $f \circ f$ is $\{x | x \ge 0\}$ and the domain of $g \circ f$. Since the domain of $g \circ f$. Since the domain of $f \circ f$ is the domain of $g \circ f$.

of $g \circ f$ is $\{x | x \ge 0\}$, or $[0, \infty)$.

29. $(f \circ g)(x) = f(g(x)) = f(0.05) = 20$

$$(g \circ f)(x) = g(f(x)) = g(20) = 0.05$$

The domain of *f* and of *g* is $(-\infty,\infty)$, so the domain of

$$f \circ gand of g \circ f is \sqrt{-\infty, \infty}).$$
30. $(f \circ g)(x) = (\overset{4}{x})^{4} = x$

$$(g \circ f)(x) = \overset{4}{x^{4}} = |x|$$

The domain of f is $(-\infty, \infty)$ and the domain of g is

 $\{x | x \ge 0\}$, so the domain of $f^{\circ}gis\{x | x \ge 0\}$, or $[0, \infty)$. Now consider the domain of $g^{\circ}f$. There are no restrictions on the domain of $fand f(x) \ge 0$ for all values of x, so the domain is $(-\infty,\infty)$.

31. $(f \circ g)(x) = f(g(x)) = f(x \circ 2 - 5) =$

The domain of $fis{x | x \ge -5}$ and the domain of $gis_{(-\infty,\infty)}$. Since $2 \ge 0$ for all values of x, then $2-5 \ge -5$

for all values of x and the domain of $g \circ f$ is $(-\infty, \infty)$.

Now consider the domain of $f^{\circ}g$. There are no restrictions on the domain of g, so the domain of $f^{\circ}g$ is the same as the domain of $f_{\star}[x | x \ge -5]$, or $[-5, \infty)$.

32.
$$(f \circ g)(x) = (\int_{x+2}^{y} x + 2)^{5} - 2 = x + 2 - 2 = x$$

$$(g \circ f)(x) = {\stackrel{\sqrt{5}}{5}} *^{5} - 2 + 2 = {\stackrel{\sqrt{5}}{5}} *^{5} = x$$

The domain of *f* and of *g* is $(-\infty,\infty)$, so the domain of $f^{\circ}g$ and of $g^{\circ}f$ is $(-\infty,\infty)$.

33.
$$(f \circ g)(x) = f(g(x)) = f(\sqrt[3]{3-x}) = (\sqrt[3]{3-x})^2 + 2 = 3 - x + 2 = 5 - x$$

 $(g \circ f)(x) = g(f(x)) = g(x + 2) = 3 - (x^2 + 2) = 3 -$

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34.
$$(f \circ g)(x) = f(x^2 - 25) = 1 - (x^2 - 25)^2 = 1 - (x^2 - 25) = 1 - (x^2 - 25)^2 = 1 - (x^2 - 25) = 1$$

The domain of *f* is $(-\infty,\infty)$ and the domain of *g* is $\{x | x \le -5 \text{ or } x \ge 5\}$, so the domain of $f \circ g$ is

$$\{x | x \le -5 \text{ or } x \ge 5\}$$
, or $(-\infty, -5] \cup [5, \infty)$.

Now consider the domain of $g \circ f$. There are no restrictions on the domain of f and the domain of g is $\{x | x \le -5 \text{ or } x \ge 5\}$, so we find the values of x for which $f(x) \le \sqrt{5}$ or $f(x) \ge 5$. We see that 1-x $2 \le -5$ when $x \le -6$ or $x \ge 6$ and 1-x $2 \ge 5$ has no solution,

so the domain of
$$g \circ f$$
 is $\{x \mid x \leq -$ for $x \geq$ 6}, or $(-\infty, -6] \cup [6,\infty)$.
35. $(f \circ g)(x) = f(g(x)) = f$ $1 =$ $1+x =$

$$\frac{1-\begin{array}{c}1\\1+x\\1+x\end{array}}{1} = \begin{array}{c}\frac{1+x-1}{1+x}\\\frac{1}{1+x}\end{array} = \\ \frac{x1+x}{1+x} = \\ \frac{x1+x}{1+x} = \\ \frac{1-x}{1+x} = \\ \frac{1-x}{x} = \\ \frac{1-x}{x} = \\ \frac{1}{1-x} = \\ \frac{1-x}{x} = \\ \frac{1}{1-x} = \\ \frac{1-x}{x} = \\ \frac{1}{1-x} = \\ \frac{1}$$

The domain of f is $\{x | x = 0\}$ and the domain of g is

 $\{x | x - 1\}$, so we know that -1 is not in the domain of $f^{\circ}g$. Since 0 is not in the domain of f, values of x for which g(x) = 0 are not in the domain of $f^{\circ}g$. But g(x) is never 0, so the domain of $f^{\circ}g$ is $\{x | x = -1\}$, or $(-\infty, -1) \cup (-1, \infty)$. Now consider the domain of $g^{\circ}f$. Recall that 0 is not in

the domain of *f*. Since -1 is not in the domain of *g*, we know that g(x) cannot be -1. We find the value(s) of *x* for which f(x) = -1. 1-x = 1-

x 1-x=-xMultiplying byx 1 = 0 False equation We see that there are no values of x for which f(x) = -1,

 $\sqrt[\sqrt{\frac{\sqrt{1-x^2}}{1-x^2}} = \sqrt[\sqrt{1-x^2}]{gis}$

 $-\infty,\infty$) and the domain of $\{x \mid x \leq 3\}$, so the domain of $f^{\circ}gis\{x \mid x \leq 3\}$, or $(-\infty,3]$.

Now consider the domain of $g \circ f$. There are no restrictions on the domain of f and the domain of g is $\{x | x \le 3\}$, so

we find the values of x for which $f(x) \le 3$. We see that $x_2 + 2 \le 3$ for $-1 \le x \le 1$, so the domain of $g^\circ f$ is

 $\{x \mid -1 \le x \le 1\}$, or [-1,1].

so the domain of $g \circ f \underset{X+2}{\text{is}\{x \perp X\}} = 0$, or $(-\infty, 0) \cup (0, \infty)$.

36.
$$(f \circ g)(x) = f$$

$$= \frac{1}{1} = \frac{x + 2}{1}$$

$$= \frac{1}{\frac{x + 2 - 2x}{x}} = \frac{-x + 2}{x}$$

$$= 1 \cdot \frac{x}{-x + 2} = \frac{-x}{-x + 2}, \text{ or } \frac{x}{2-x}$$

$$()() = -1 = \frac{x - 2}{x - 2}$$

$$g \circ f x = \frac{x - 2}{1 + 2x - 4} = \frac{x - 2}{2x - 3}$$

$$= \frac{x - 2}{x - 2 - 4} = \frac{x - 2}{x - 2}$$

$$= \frac{2x - 3}{x - 2 - 4} = \frac{x - 2}{x - 2}$$

$$= \frac{2x - 3}{x - 2} = 2x - 3$$

$$x - 2 = 1$$

1

The domain of f is $\{x | x = 2\}$ and the domain of g is

 $\{x | x = 0\}$, so 0 is not in the domain of $f \circ g$. We find the value of $f \circ g$. We find the value of $f \circ g$.

$$= 2$$

$$x$$

$$x + 2 = 2x$$

$$2 = x$$

Then the domain of $f^{\circ}g$ is $(-\infty, 0) \cup (0, 2) \cup (2, \infty)$.

Now consider the domain of $g \circ f$. Since the domain of f is $\{x | x = 2\}$, we know that 2 is not in the domain of $g \circ f$.

Since the domain of g is $\{x \mid x \in 0\}$, we find the value of x for which f(x) = 0.

$$\frac{1}{x-2} = 0$$
$$1 = 0$$

We get a false equation, so there are no such values. Then the domain of $g \circ f$ is $(-\infty, 2) \cup (2, \infty)$.

37. $(f \circ g)(x) = f(g(x)) = f(x+1) =$

 $(x+1)^{3}-5(x+1)^{2}+3(x+1)+7 =$ x3+3x2+3x+1-5x 2-10x-5+3x+3+7 = x3-2x 2-4x+6 $(g^{\circ}f)(x) = g(f(x)) = g(x - 3-5x + 3x + 7) =$

 $x_3-5x + 3x + 7 + 1 = x_3-5x + 3x + 8$ The domain of *f* and of *g* is $(-\infty,\infty)$, so the domain of

 $f \circ gand \ ofg \circ fis (-\infty,\infty).$ **38.** $(g \circ f)(x) = x + 2x^2 - 3x - 9 - 1 = x^3 + 2x^2 - 3x - 10$ $(g \circ f)(x) = (x - 1)^3 + 2(x - 1)^2 - 3(x - 1) - 9 = x^3 - 3x^2 + 3x - 1 + 2x^2 - 4x + 2 - 3x + 3 - 9 = x^3 - x^2 - 4x - 5$ The domain of f and of g is $(-\infty,\infty)$, so the domain of $f \circ gand \ ofg \circ fis (-\infty,\infty).$

39. $h(x) = (4 + 3x)^{5}$ This is 4 + 3x to the 5th power. The most obvious answer is f(x) = x 5 and g(x) = 4 + 3x.

$$42.f(x) = \sqrt{\frac{1}{x}}, g(x) = 3x + 7$$

$$43.f(x) = \frac{x-1}{x+1}, g(x) = x = 3$$

$$44.f(x) = |x|, g(x) = 9x = 2-4$$

$$45. () = \frac{6}{7}, () = 2 + \frac{x}{3}, \frac{1}{7}, \frac{x}{7}, \frac{g(x)}{7}, \frac{g(x)}{7}, \frac{2}{7}, \frac{x}{3}$$

$$46.f(x) = x + \frac{4}{7}, g(x) = \frac{x-3}{\sqrt{-5}}, \frac{x-5}{\sqrt{-5}}$$

$$47.f(x) = \sqrt{x}, g(x) = x + \frac{2}{7}, \frac{x}{7}, \frac{g(x)}{7}, \frac{x}{7}, \frac{g(x)}{7}, \frac{x}{7}, \frac{x}{7}, \frac{x}{7}, \frac{g(x)}{7}, \frac{x}{7}, \frac{x}{7}$$

51.a) Use the distance formula, distance = rate × time. Substitute 3 fortherateand*t* for time.

 $f(x) = 2x + 5x_2g(x) = (x-1)^{1/3}$

r(t) = 3t

- b) Use the formula for the area of a circle. $A(r) = \pi r 2$
- c) $(A \circ r)(t) = A(r(t)) = A(3t) = \pi(3t)$ ² = $9\pi t_2$

This function gives the area of the ripple in terms of time*t*.

52.a)
$$= 2$$

 $h r$
 $S(r) = 2\pi r(2r) + 2\pi r 2$
 $S(r) = 4\pi r 2 + 2\pi r 2$
 $S(r) = 6\pi r 2$

b)
$$r = \frac{h}{2}$$

 $S(h) = 2\pi - \frac{h}{2} + 2\pi - \frac{h}{2}$
 $S(h) = \pi h + 2\pi - \frac{1}{2}$
 πh^2
 $S(h) = \pi h^2 + \frac{1}{2}$
 $S(h) = \frac{3}{2} \pi h^2$

53.The manufacturer chargesm+ 2 per drill. The chain store sells each drill for 150%(m+ 2), or 1.5(m+ 2), or 1.5m+ 3. Thus, we haveP(m) = 1.5m+ 3.

54.
$$f(x) = (t \circ s)(x) = t(s(x)) = t(x-3) = x-3+4=x+1$$

We have $f(x) = x+1$.

55. Equations (*a*)–(*f*) are in the formy=mx+b, so we can Copyright © 2013 Pearson Education, Inc.

40
$$f(x) = \sqrt[3]{x,g(x)} = x - 8$$

41 $h(x) = \frac{1}{(x-2)^4}$

This is 1 divided by (x-2) to the 4th power. One obvious answer is $f(x) = \frac{1}{x}$ and g(x) = x-2. Another possibility is $f(x) = \frac{1}{x}$ and $g(x) = (x-2)^{4}$. read they-intercepts directly from the equations. Equations (g) and (h) can be written in this form $asy=\frac{2}{3}x-2$ and y=-2x+3, respectively. We see that only equa-

tion (c) hasy-intercept (0,1).

56. None (See Exercise 55.)

57. If a line slopes down from left to right, its slope is negative. The equations*y*=*mx*+*b*for which*m*is negative are (b),

(d), (f), and (h). (See Exercise 55.)

58. The equation for which *m* is greatest is the equation with

the steepest slant. This is equation (b). (See Exercise 55.)

- **59.** The only equation that has (0,0) as a solution is (a).
- **60.** Equations (c) and (g) have the same slope. (See Exercise 55.)
- **61.** Only equations (c) and (g) have the same slope and differenty-intercepts. They represent parallel lines.
- **62.** The only equations for which the product of the slopes is -1 are (a) and (f).
- 63. Only the composition (c p)(a) makes sense. It represents the cost of the grass seed required to seed a lawn with area a.
- **64.** Answers may vary. One example is f(x) = 2x + 5 and x 5

 $g(x) = \frac{1}{2}$. Other examples are found in Exercises 17, 18, 25, 26, 32 and 35.

Chapter 2 Mid-Chapter Mixed Review

- 1. The statement is true. See page 162 in the text.
- 2. The statement is false. See page 177 in the text.
- **3.** The statement is true. See Example 2 on page 185 in the text, for instance.
- 4.a) Forx-values from 2 to 4, they-values increase from 2 to 4. Thus the function is increasing on the interval (2,4).
 - b) Forx-values from–5 to–3, they-values decrease from 5 to 1. Also, forx-values from 4 to 5, theyvalues decrease from 4 to–3. Thus the function is decreasing on (–5,–3) and on (4,5).
 - c) Forx-values from-3 to-1,vis 3. Thus the function is constant on (-3,-1).
- 5. From the graph we see that a relative maximum value of

6.30 occurs at x=-1.29. We also see that a relative minimum value of -2.30 occurs at x=1.29.

The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point it decreases to the relative minimum and then increases again. Thus the function is increasing on $(-\infty, -1.29)$

and on $(1.29,\infty)$. It is decreasing on (-1.29,1.29).

6. Thex-values extend from−5 to−1 and from 2 to 5, so the domain is [-5,-1]∪[2,5]. They-values extend from -3 to 5, so the range is [-3,5].

$$7 \cdot A(h) = {}^{-1}(h_2)h$$

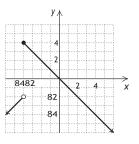
$$\mathbf{8.()} = \begin{bmatrix} x-5, \text{for } x \le -3, \\ 2x+3, \text{for } -3 < x \le 0, \\ fx \qquad \Box \\ 1 \\ \overline{2x} = 1 \end{bmatrix}$$

$$L_2$$
 x,forx >0

Since $-5 \le -3$, f(-5) = -5 - 5 = -10. Since $-3 \le -3$, f(-3) = -3 - 5 = -8. Since $-3 < -1 \le 0$, f(-1) = 2(-1) + 3 = -2 + 3 = 1. Since 6 > 0, $f(6) = \frac{1}{2}$, 6 = 3. x + 2, for x < -4.

$$9.g(x) = \begin{array}{c} x + 2, \text{for } x < -x \\ -x, \text{for } x \ge -4 \end{array}$$

We create the graph in two parts. Graphg(x) = x + 2 for inputs less than-4. Then graphg(x) = -x for inputs greater than or equal to-4.



10.
$$(f+g)(-1) = f(-1) + g(-1)$$

= $[3(-1)-1] + [(-1)^2 + 4]$
= $-3-1 + 1 + 4$
= 1

11.
$$(fg)(0) = f(0) \cdot g(0)$$

= $(3 \cdot 0 - 1) \cdot (0^{-2} + 4)$
= $-1 \cdot 4$
12. $()(3) = (3) \quad (3)$
 $g - f \quad g \quad -f$
= $(3^2 + 4) - (3 \cdot 3 - 1)$
= $9 + 4 - (9 - 1)$
= $9 + 4 - 9 + 1$

= 5

13.
$$(g/f)$$
 $\frac{1}{3} = \frac{g \frac{1}{3}}{f \frac{1}{3}}$
 $\frac{1^2}{3} + 4$
 $A(h) = \frac{1}{2}h_2 - h$

$$= \frac{1}{3 \cdot \frac{1}{3} - 1} \\ = \frac{9}{1 - 1} \\ - \frac{37}{2 - 9} \\ = \frac{37}{2 - 9}$$

—

Since division by 0 is not defined, $(g/f) \frac{1}{3}$ does not exist.

14.f(x) = 2x + 5,g(x) = -x - 4

a) The domain of f and of g is the set of all real numbers, or (-∞,∞). Then the domain of f+g, f-g, fg, and f f is also (-∞,∞).
For f/g we must exclude-4 sinceg(-4) = 0. Then the domain of f/g is (-∞,-4)∪(-4,∞).

For g/f we must exclude $-\frac{5}{2}$ since f = 0.

Then the domain of*g/f*is

$$-\infty, -\frac{5}{2} \cup -\frac{5}{2}, \infty$$

b) (
$$f+g)(x) = f(x)+g(x) = (2x+5)+(-x-4) = x+1$$

(f-g)(x) = f(x) g(x) = (2x+5) (x - 4) =
$$2x+5+x+4 = 3x+9$$

(fg)(x) = f(x) · g(x) = (2x+5)(-x-4) =
$$-2x2 - 8x - 5x - 20 = -2x \quad 2 - 13x - 20$$

$$(g/f) = \begin{cases} g(x) & -x-4 \\ g(x) & -\frac{x-4}{2} \\ f(x) & 2x+5 \end{cases}$$
15. $f(x) = x-1, g(x) = \sqrt[4]{x+2}$

a) Any number can be an input for *f*, so the domain of *f* is the set of all real numbers, or (−∞,∞).

The domain of *g* consists of all values for which x+2 is nonnegative, so we have $x+2\ge 0$, or $x\ge -2$, or $[-2,\infty)$. Then the domain of f+g, f-g, and fg is $[-2,\infty)$.

The domain of ff is $(-\infty,\infty)$.

Since
$$g(-2) = 0$$
, the domain of f/g is $(-2, \infty)$.

Since
$$f(1) = 0$$
, the domain of g/f is $[-2, 1] \cup (1, \infty)$.

b)
$$(f+g)(x) = f(x) + g(x) = x-1 + x+2$$

 $(f-g)(x) = f(x)-g(x) = x-1 - \sqrt{x+2}$
 $(fg)(x) = f(x) \cdot g(x) = (x-1) \sqrt{x+2}$
 $(ff)(x) = f(x) \cdot f(x) = (x-1)(x-1) = x^2 - x - x + 1 = x^2 - 2x + 1$
 $(f/g)(x) = \frac{f(x)}{g(x)} = \sqrt[x]{x+2}$
 $(g/f)(x) = x - 1$
 $(g/f)(x) = x - 1$
 $f(x) = x - 1$
 $f(x) = x - 1$

$$\frac{f(x+h)-f(x)}{h} = \frac{4(x+h)-3-(4x-3)}{h} = \frac{4x+4h-3-4x+3}{4h}$$

Now consider the domain of $g \circ f$. Since the inputs of g must be nonnegative, we must have $3x+2\ge 0$, or $x\ge -\frac{2}{3}$.

Thus the domain of $g \circ f$ is $-\frac{2}{3}, \infty$.

- 24. The graph of y= (h g)(x) will be the same as the graph of y=h(x) moved downbunits.
- 25. Under the given conditions, (f+g)(x) and (f/g)(x) have different domains ifg(x) = 0 for one or more real numbers x.
- **26.** If f and g are linear functions, then any real number can be an input for each function. Thus, the domain of $f^{\circ}g$ =
- the domain of $g \circ f = (-\infty, \infty)$ 27. This approach is not valid. Consider Exercise 23 on page

188 in the text, for example. Since $(f \circ g)(x) = \frac{4x}{x-5}$

an examination of only this composed function would lead to the incorrect conclusion that the domain of $f^\circ g$ is $(-\infty,5)\cup(5,\infty)$. However, we must also exclude from the domain of $f^\circ g$ those values of x that are not in the domain

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 $\begin{array}{c} = & = 4 \\ h & h \end{array}$

of *g*. Thus, the domain of $f^{\circ}g$ is $(-\infty, 0) \cup (0, 5) \cup (5, \infty)$.

Exercise Set 2.4

1. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would not coincide, so the graph is not symmetric with respect to the*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would coincide, so the graph is symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

2. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would not coincide, so the graph is not symmetric with respect to the*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would coincide, so the graph is symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

3. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would coincide, so the graph is symmetric with respect tothe*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

4. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would not coincide, so the graph is not symmetric with respect to the*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

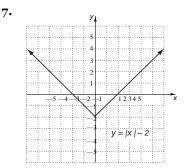
5. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would not coincide, so the graph is not symmetric with respect to the*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

6. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would coincide, so the graph is symmetric with respect tothe*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would coincide, so the graph is symmetric with respect to they-axis. If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.



The graph is symmetric with respect to the *y*-axis. It is not symmetric with respect to the *x*-axis or the origin.

Test algebraically for symmetry with respect to the x-axis:

y = x - 2	Original equation
y = x - 2	Replacingyby—y
	a. 1.4 .

y = -|x| + 2 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test algebraically for symmetry with respect to they-axis:

y = x - 2	Original equation
y = -x - 2	Replacingxby—x

y = |x| - 2 Simplifying

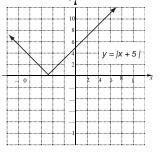
The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test algebraically for symmetry with respect to the origin:

y = x - 2	Original equation
-y = -x - 2	Replacingxby—xand
	yby-y
-y = x - 2	Simplifying
y = - x + 2	

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.





The graph is not symmetric with respect to the*x*-axis, the *y*-axis, or the origin.

Test algebraically for symmetry with respect to the x-axis:

y = |x + 5| Original equation

$$-y = |x + 5|$$
Replacingyby $-y$

$$y = -|x + 5|$$
Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Test algebraically for symmetry with respect to they-axis:

```
y = |x + 5| Original equation
```

y = |-x + 5|Replacingxby-x

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test algebraically for symmetry with respect to the origin:

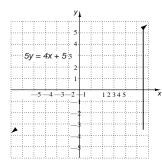
y = |x + 5| Original equation

-y = |-x + 5|Replacing*x*by-xand*y*by-y

y = -|-x + 5|Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.





The graph is not symmetric with respect to the*x*-axis, the *y*-axis, or the origin.

Test algebraically for symmetry with respect to thex-axis:

5y=4x+5Original equation5(-y)=4x+5Replacingyby-y-5y=4x+5Simplifying5y=-4x-5

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Test algebraically for symmetry with respect to they-axis:

5y= 4x+ 5 Original equation

5y=4(-x) + 5 Replacing xby-x

5y = -4x + 5 Simplifying

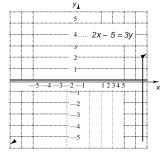
The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test algebraically for symmetry with respect to the origin:

5y=4x+5 Original equation 5(-y)=4(-x)+5 Replacingxby-xand yby-y -5y=-4x+5 Simplifying 5y=4x-5

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.





The graph is not symmetric with respect to the*x*-axis, the *y*-axis, or the origin.

Te stalgebraically for symmetry with respect to the x-axis:

2x-5 = 3yOriginal equation

2x-5 = 3(-y) Replacing/by-y

-2x+5 = 3ySimplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Testalgebraically for symmetry with respect to the y-axis:

2x-5 = 3yOriginal equation

2(-x)-5 = 3yReplacingxby-x

-2x-5 = 3ySimplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*y*-axis.

Testalgebraically for symmetry with respect to theorigin:

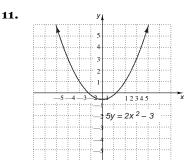
2x-5 = 3yOriginal equation

2(-x)-5 = 3(-y) Replacing *x*by-*x*and *y*by-*y*

$$-2x-5 = -3y$$
Simplifying

$$2x + 5 = 3y$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.



The graph is symmetric with respect to the y-axis. It is not symmetric with respect to the x-axis or the origin.

Test algebraically for symmetry with respect to the *x*-axis: $5y=2x \ 2-3$ Original equation

$5(-y) = 2x_2 - 3$	Replacingyby-y
$-5y = 2x_2 - 3$	Simplifying
$5y = -2x_2 + 3$	

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Test algebraically for symmetry with respect to the y-axis:

 $5y = 2x \ 2 - 3$ Original equation

 $5y=2(-x)^2-3$ Replacing xby-x

5y = 2x 2 - 3

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test algebraically for symmetry with respect to the origin:

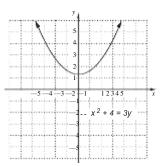
 $5y= 2x \ 2-3$ Original equation $5(-y) = 2(-x)^2 - 3$ Replacingxby-xand yby-y

$$-5y = 2x_{2}^{2} - 3$$

 $5y = -2x_{2}^{2} + 3$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

12.



The graph is symmetric with respect to the y-axis. It is not symmetric with respect to the x-axis or the origin.

Test algebraically for symmetry with respect to the x-axis:

 $x_2 + 4 = 3y$ Original equation

 $x_2 + 4 = 3(-y)$ Replacing y by -y

 $-x_2 - 4 = 3y$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test algebraically for symmetry with respect to they-axis:

 $x_2 + 4 = 3y$ Original equation

 $(-x)^2 + 4 = 3y$ Replacingxby-x x₂ + 4 = 3y

The last equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Test algebraically for symmetry with respect to the origin: $x_2 + 4 = 3y$ Original equation $(-x)^2 + 4 = 3(-y)$ Replacingxby-xand yby-y $x_2 + 4 = -3y$ Simplifying

$$-x_2 - 4 = 3y$$

The last equation is not equivalent to the original equation,

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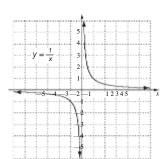
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13.



The graph is not symmetric with respect to the -axis or

the y-axis. It is symmetric with respect to the origin.

Test algebraically for symmetry with respect to the _-axis:

$$y = \frac{1}{x}$$
Original equation
$$1$$

$$-y = \frac{1}{x}$$
Replacing/by-y
$$y = -\frac{1}{x}$$
Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test algebraically for symmetry with respect to they-axis:

$$y = \frac{1}{x}$$
 Original equation

$$y = \frac{1}{-x}$$
 Replacingxby-x

$$y = -\frac{1}{x}$$
 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*y*-axis. Test algebraically for symmetry with respect to the origin:

$$y = \frac{1}{x}$$
Original equation
$$y = \frac{1}{-x}$$
Replacing x by - x and y by - y
$$y = \frac{1}{x}$$
Simplifying

not symmetric with respect to the origin.

14.

metric with respect to the origin.

last equa tion is equi vale nt to the origi nal equa tion, so the grap h is sym metr ic with resp ect to the origi n.

Th e gr

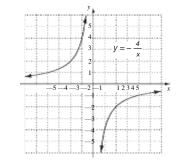
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sy m Test algebraically for symmetry with respect to thex-axis:

$$y=-\frac{4}{2}$$
 Original equation
 x
 $-y=-\frac{4}{x}$ Replacing/by-y
 $y=\frac{4}{x}$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis. Test algebraically for symmetry with respect to the*y*-axis:

$$y=- \begin{array}{c} 4 \\ - \end{array} \quad \text{Original equation} \\ y=- \begin{array}{c} x \\ -x \\ y=- \end{array} \quad \text{Replacingxby-x} \\ y= \begin{array}{c} 4 \\ -x \\ y=- \end{array} \quad \text{Simplifying} \end{array}$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis. Test algebraically for symmetry with respect to the origin:

$$y = -\frac{4}{x}$$
Original equation
$$-y = -\frac{-x}{4}$$
Replacing x by - x and y by - y
$$y = -\frac{4}{x}$$
Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

15. Test for symmetry with respect to the*x*-axis:

5x-5y=0 Original equation

5x-5(-y) = 0 Replacing y by -y

$$5x + 5y = 0$$
 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to they-axis:

5x-5y=0 Original equation

$$5(-x)-5y=0$$
 Replacing $xby-x$

-5x-5y=0 Simplifying

5x + 5y = 0

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test for symmetry with respect to the origin:

5x-5y=0 Original equation

$$5(-x)-5(-y) = 0$$
 Replacing x by $-x$ and
 y by $-y$
 $-5x+5y=0$ Simplifying
 $5x-5y=0$

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin. The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Test for symmetry with respect to they-axis:

6x+7y=0 Original equation 6(-x) + 7y=0 Replacingxby-x 6x-7y=0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:

6x + 7y = 0 Original equation

6(-x) + 7(-y) = 0 Replacing *x*by - *x*and

yby—y6x+ 7y= 0 Simplifying The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

17. Test for symmetry with respect to the*x*-axis: $3x_2-2y = 3$ Original equation

 $3x_2-2(-y)^2 = 3$ Replacing/by-y

 $3x_2-2y_2 = 3$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the*x*-axis. Test for symmetry with respect to the*y*-axis:

16. Test for symmetry with respect to thex-axis: 6x+7y=0 Original equation 6x+7(-y) = 0 Replacing/by-y 6x-7y=0 Simplifying $3x_2-2y = 3$ Original equation $3(-x)^2-2y = 3$ Replacingxby-x $3x_2-2y = 3$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test for symmetry with respect to the

origin: $3x_2-2y = 3$ Original equation $3(-x)^2-2(-y)^2 = 3$ Replacingxby-x andyby-y $3x_2-2y = 3$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

18. Test for symmetry with respect to thex-

axis:5*y*= 7x = 2-2xOriginal equation

 $5(-y) = 7x^{2}$ -2xReplacing/by-y $5y=-7x^{2} + 2x$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Test for symmetry with respect to they-

axis:5*y*= 7*x* $_2$ -2*x*Original equation

 $5y=7(-x)^2-2(-x)$ Replacingxb $y-x5y=7x^2+2x$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin: $5y=7x \ 2-2x$ Original equation

$$5(-y) = 7(-x)^2 - 2(-x) \operatorname{Replacing} x \operatorname{by} - x$$

and $v \operatorname{by} - v$

-5y = 7x + 2xSimplifying

 $5y = -7x \ _2 - 2x$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

19. Test for symmetry with respect to thex-axis:

y = |2x| Original equation

-y = |2x|Replacing/by-y

y = -|2x|Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test for symmetry with respect to they-axis:

y = |2x| Original equation

$$y=|2(-x)|$$
Replacing x by $-x$

y = |-2x|Simplifying

y = |2x|

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:

y = |2x| Original equation

-y=|2(-x)|Replacingxby-xandyby-y

-y=|-2x|Simplifying

-y=|2x|

```
y = -|2x|
```

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

20. Test for symmetry with respect to thex-axis:

 $y_3 = 2x_2$ Original equation $(-y)^3 = 2x_2$ Replacing/by-y $-y_3 = 2x_2$ Simplifying $y_3 = -2x_2$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test for symmetry with respect to they-axis:

 $y_3 = 2x_2$ Original equation $y_3 = 2(-x)^2$ Replacingxby- xy_3

= 2*x*₂ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:

 $y_{3} = 2x_{2}$ Original equation $(-y)^{3} = 2(-x)^{2}$ Replacing x by -x and y by -y $-y_{3} = 2x_{2}$ Simplifying $y_{3} = -2x_{2}$ The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

21. Test for symmetry with respect to thex-axis:

2x4 + 3 = y 2Original equation $2x4 + 3 = (-y)^2$ Replacingyby-y2x4 + 3 = y 2Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the *x*-axis.

Test for symmetry with respect to they-axis:

 $2x_4 + 3 = y_2$ Original equation

 $2(-x)^4 + 3 = y_2$ Replacing x by $-x_2$ $2x_4 + 3 = y_2$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the y-axis.

Test for symmetry with respect to the origin: $2x_4 + 3 = y_2$ Original equation

 $2(-x)^4 + 3 = (-y)^2$ Replacing x by -xand y by -y $2x_4 + 3 = y_2$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

22. Test for symmetry with respect to the*x*-axis:

 $2y_2 = 5x_2 + 12$ Original equation

 $2(-y)^2 = 5x_2 + 12$ Replacing/by-y $2y_2 = 5x_2 + 12$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to thex-axis.

Testfor symmetry with respect to they-axis:

 $2y_2 = 5x_2 + 12$ Original equation $2y_2 = 5(-x)^2 + 12$ Replacingxby-x

 $2y_2 = 5x_2 + 12$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:

 $2y_2 = 5x_2 + 12$ Original equation $2(-y)^2 = 5(-x)^2 + 12$ Replacingxby-x andyby-y $2y_2 = 5x_2 + 12$ Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

23. Test for symmetry with respect to the*x*-axis:

$3y_3 = 4x_3 + 2$	Original equation
$3(-y)^3 = 4x_3 + 2$	Replacingyby–y
$-3y_3 = 4x_3 + 2$	Simplifying
3уз =-4х з -2	

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Testfor symmetry with respect to they-axis:

$$3y_3 = 4x_3 + 2$$
 Original equation

$$3y_3 = 4(-x)^3 + 2$$
 Replacingxby-x

 $3y_3 = -4x_3 + 2$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test for symmetry with respect to the origin: $3y_3 = 4x_3 + 2$ Original equation

 $3(-y)^3 = 4(-x)^3 + 2$ Replacingxby-x

$$-3y_3 = -4x_3 + 2$$
 and $yby-y$ Simplifying

3*y*₃ = 4*x*₃-2

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

24. Test for symmetry with respect to the*x*-axis:

3x = |y| Original equation

3x = |-y|Replacing/by-y

3x = |y|Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the*x*-axis.

Test for symmetry with respect to they-axis:

3x = |y| Original equation

3(-x) = |y|Replacingxby-x

-3x = |y|Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test for symmetry with respect to the origin:

3x = |y| Original equation 3(-x) = |-y| Replacing x by -x and y by -y

-3x = |y|Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

25. Test for symmetry with respect to thex-axis:

xy= 12 Original equation

x(-y) = 12	Replacingyby–y
<i>-xy</i> = 12	Simplifying

xy=-12

The last equation is not equivalent to the original equation,

so the graph is not symmetric with respect to the*x*-axis. Test for symmetry with respect to the*y*-axis:

xy= 12 Original equation -xy= 12 Replacingxby-x

xy = -12 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

26.Test for symmetry with respect to the*x*-axis:

xy-x 2 = 3 Original equation x(-y)-x 2 = 3 Replacing/by-y

 $xy+x_2 = -3$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis. Test for symmetry with respect to the*y*-axis:

 $xy-x_2 = 3$ Original equation

-xy-(-x) = 3 Replacingxby-x xy+x = -3 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test for symmetry with respect to the origin:

xy-x = 3 Original equation

$$-x(-y)-(-x)^2 = 3$$
 Replacing *x*by-*x*and

$$xy - x = 3$$
 Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

2

 $-\frac{7}{2},0$

1,-<u>3</u> 8 ,0

7

2,0

27.*x*-axis: Replace/with-*y*; (-5,-6)

y-axis: Replacexwith-x; (5,6)

Origin: Replacexwith-xandywith-y; (5,-6)

28.*x*-axis: Replace*y*with–*y*;

7

y-axis: Replace*x*with–*x*;

Origin: Replace*x*with–*x*and*y*with–*y*;

29.*x*-axis: Replace*y*with–*y*; (–10,7) *y*-axis: Replace*x*with–*x*; (10,–7) Origin: Replace*x*with–xand*y*with–*y*; (10,7)

30.*x*-axis: Replace*y* with–*y*;

y-axis: Replace*x*with–*x*; $-1, \frac{3}{8}$

Test for symmetry with respect to the origin: *xy*= 12 Original equation

Orig in: Repl acex with -xan dyw

ith-

y;

31.*x*-axis: Replaceywith–*y*; (0,4) *y*-axis: Replacexwith–*x*; (0,–4) Origin: Replacexwith–xandywith–*y*; (0,4)

32.*x*-axis: Replace*y*with–*y*; (8,3)

y-axis: Replace*x*with–*x*; (–8,–3)

Origin: Replacexwith-xandywith-y; (-8,3)

-x(-y) = 12 Replacingxby-xandyby-y
xy= 12 Simplifying

33. The graph is symmetric with respect to the*y*-axis, so the function is even.

<u>3</u>

- **34.** The graph is symmetric with respect to the*y*-axis, so the function is even.
- **35.** The graph is symmetric with respect to the origin, so the function is odd.
- **36.** The graph is not symmetric with respect to either the*y*-axis or the origin, so the function is neither even nor odd.
- **37.** The graph is not symmetric with respect to either theyaxis or the origin, so the function is neither even nor odd.
- 38. The graph is not symmetric with respect to either they-

axis or the origin, so the function is neither even nor odd.

39.
$$f(x) = -3x + 2x$$

 $f(-x) = -3(-x)^3 + 2(-x) = 3x - 2x$
 $-f(x) = -(-3x + 2x) = 3x - 2x$
 $f(-x) = -f(x)$, so f is odd.

40. f(x) = 7x + 4x - 2 $f(-x) = 7(-x)^3 + 4(-x) - 2 = -7x + 4x - 2$ -f(x) = -(7x + 4x - 2) = -7x + 2

f(x) f(-x), so f is not even. f(-x) - f(x), so f is not odd.

Thus, f(x) = 7x + 4x - 2 is neither even nor odd.

1

41.
$$f(x) = 5x + 2x4 - 1$$

 $f(-x) = 5(-x)^2 + 2(-x)^4 - 1 = 5x + 2x4 - 1$
 $f(x) = f(-x)$, sofis even.

42.
$$f(x) = x + \frac{1}{2}$$

x

1

43.
$$f(x) = x \ 17$$

 $f(-x) = (-x)^{17} = -x \ 17$
 $-f(x) = -x \ 17$
 $f(-x) = -f(x)$, so f is odd.
44. $f(x) = \frac{3}{3}x$

f(-x) = (-x) - |(-x)| = -x - |x|

46.
$$f(x) = \frac{1}{\frac{x^2}{x^2}} = \frac{1}{(-x)^2} = \frac{1}{x^2}$$

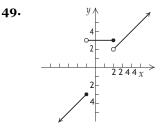
$$f(x) = f(-x)$$
, so f is even.

47.
$$f(x) = 8$$

 $f(-x) = 8$
 $f(x) = f(-x)$, sofis even.
48. $f(x) = \sqrt{x^2 + 1}$

$$f(-x) = (-x)^2 + 1 = x^2 + 1$$

f(x) = f(-x), sofis even.



50. Let = the price of a ticket to the closing *Familiarize* t

ceremonies. Then t+ 325 = the price of a ticket to the opening ceremonies. Together, the two tickets cost t+ (t+ 325) = 2t+ 325.

Translate. The total cost of the two tickets is \$1875, so we have the following equation.

$$2t + 325 = 1875$$

Carry out. We solve the equation. 2*t*+ 325 = 1875

Then t+ 325 = 775 + 325 = 1100.

Check. \$1100 is \$325 more than \$775 and \$775 +\$1100 = \$1875, so the answer checks.

State. A ticket to the opening ceremonies cost \$1100, and a ticket to the closing ceremonies cost \$775.

51.
$$f(x) = x$$
 $10-x^2$
 $f(-x) = -x \sqrt{10-(-x)^2} = -x \sqrt{10-x^2}$
 $-f(x) = -x 10-x^2$
Since $f(-x) = -f(x)$, f is odd.
52. $x^2 + 1$

$$f(x) = \frac{1}{x^3 + 1}$$

$$f(-x) = \frac{(-x)^2 + 1}{(-x)^3 + 1} = \frac{x^2 + 1}{-x^3 + 1}$$

$$x^2 + 1$$

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-f(x) = -(x-|x|) = -x+|x| $f(x) \quad f(-x), \text{ sofis not even.}$ $f(-x) \quad -f(x), \text{ sofis not odd.}$ Thus, f(x) = x - |x| is neither even nor odd. $-f(x) = -\frac{1}{x^3 + 1}$ Since f(x) = f(-x), f is not even. Since f(-x) - f(x), f is not odd. Thus, $f(x) = \frac{x^2 + 1}{x^3 + 1}$ is neither even nor odd. **53.** If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would coincide, so the graph is symmetric with respect tothe*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

54. If the graph were folded on the*x*-axis, the parts above and below the*x*-axis would not coincide, so the graph is not symmetric with respect to the*x*-axis.

If the graph were folded on they-axis, the parts to the left and right of they-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

55. See the answer section in the text.

$$56.0(-x) = \frac{f(-x)-f(-(-x))}{2} = \frac{f(-x)-f(x)}{2},$$

$$\frac{f(x)-f(-x)}{2} = \frac{f(-x)-f(x)}{2},$$

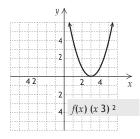
$$-O(x) = -\frac{2}{2} = \frac{2}{2}.$$
 Thus,

O(-x) = -O(x) and O is odd.

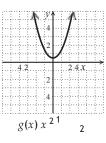
- **57.**a), b) See the answer section in the text.
- **58.**Let f(x) = g(x) = x. Now f and g are odd functions, but (fg)(x) = x = (fg)(x). Thus, the product is even, so the statement is false.
- **59.** Let f(x) and g(x) be even functions. Then by definition, f(x) = f(x) and g(x) = g(x). Thus, (f+g)(x) = f(x) + g(x) = f(x) + g(x) = (f+g)(x) and f+g is even. The statement is true.
- **60.** Let f(x) be an even function, and let g(x) be an odd function. By definition f(x) = f(x)- and g(x) = g(x), or g(x) = -g(x). Then fg(x) = f(x) g(x) = f(x) - (-g(-x)) = f(x) - g(x) - g(x) = f(x) - g(x) - g(x) = f(x) - g(x) = f(x) - g(x) = f(x) - g(x) = g(x) = g(x) - g(x) = g(x) =

Exercise Set 2.5

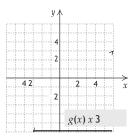
1. Shift the graph of f(x) = x 2 right 3 units.



2. Shift the graph of $g(x) = x 2 u p \frac{1}{2}$ unit.



3. Shift the graph of g(x) = x down 3 units.

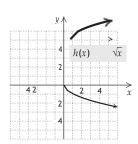


4. Reflect the graph of g(x) = xacross the x-axis and then

shift it down 2 units.

					:
H					
	2				
4.2			141		→
	2				
	4				
		[]		k	
g(x)	x 2				

 $\sqrt[n]{xacross}$ the*x*-axis.



5. Reflect the graph of h(x) =

 $g(x) \quad \sqrt{x} \quad 1$

6. Shift the graph of g(x) =

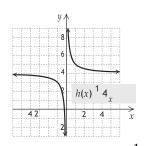
			y]				[
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			2				
							[
	12				24	х	
			~				[
 			2	 			
 		 	2	 			
 		 	2	 			

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 $\sqrt[n]{xright 1 unit.}$

7. Shift the graph of
$$h(x) = \frac{1}{2}$$
 up 4 units.

х



8. Shift the graph of g(x) =

 $\frac{1}{r}$ right 2 units.

	У 4 2	
12	2	$\begin{array}{c} 244x \\ g(x) \\ x 2 \end{array}$

9. First stretch the graph of h(x) =xvertically by multiplying eachy-coordinate by 3. Then reflect it across the *x*-axis and shift it up 3 units.

	y /	<u>►</u>
	7	
		h(x) 3x 3
	2	
4 2		2 4 x
42	2	2.4.x
42	2	2.4.x
42	2 4	

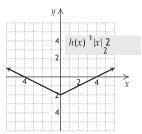
10. First stretch the graph of *f*(*x*) =*x*vertically by multiplying eachy-coordinate by 2. Then shift it up 1 unit.

y 4	
4.2	24 <i>x</i> >
(x) 2x	

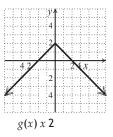
f(x) 2x 1

11. First shrink the graph of h(x) = |x| vertically by multiply-

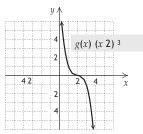
ing eachy-coordinate by
$$\frac{1}{2}$$
. Then shift it down 2 units.



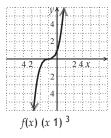
12.Reflect the graph of g(x) = x across thex-axis and shift it up 2 units.



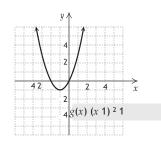
13. Shift the graph of g(x) = x 3 right 2 units and reflect it across the *x*-axis.



14. Shift the graph of f(x) = x 3 left 1 unit.

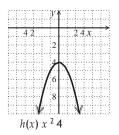


15. Shift the graph of $g(x) = x^2$ 2 left 1 unit and down 1 unit.

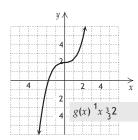


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16. Reflect the graph of $h(x) = x_2$ across the *x*-axis and down 4 units.



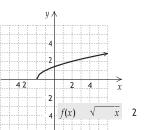
17. First shrink the graph of g(x) = x 3 vertically by multiplying each*y*-coordinate by $\frac{1}{3}$. Then shift it up 2 units.



18. Reflect the graph of $h(x) = x \exists across the y-axis.$

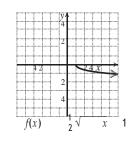
4	Υ.
2	
.42 .2 .4 .4 .4	x) ³

19. Shift the graph of
$$f(x) =$$



First shift the graph of $f(x) = \sqrt[\gamma]{xright 1}$ unit. Shrink it vertically by multiplying eachy-coordinate by $\frac{1}{a}$ and then reflect it across the x-axis. 2

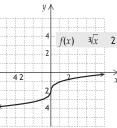
xleft 2 units.



21. Shift the graph of f(x) =

 $\sqrt[3]{x}$ down 2 units.

 $\sqrt[\gamma]{x}$ left 1 unit.



22. Shift the graph of h(x) =

 $\begin{array}{c} y^{y} \\ z^{2} \\ z^{2} \\ z^{2} \\ z^{2} \\ z^{4} \\ h(x) \sqrt[3]{x} 1 \end{array}$

23. Think of the graph of f(x) = |x|. Since g(x) = f(3x), the graph of g(x) = |3x| is the graph of f(x) = |x| shrunk horizontally by dividing each $\frac{1}{2}$

coordinate by 3 or multiplying eachx-coordinate by $\frac{1}{3}$.

24. Think of the graph of $g(x) = \sqrt[\gamma]{3} x$. Since $f(x) = \frac{1}{2}g(x)$, the

graph of
$$f(x) = \frac{1}{2} \sqrt[3]{xis}$$
 the graph of $g(x) = \frac{\sqrt[3]{xshrunk}}{1}$

vertically by multiplying eachy-coordinate by

25. Think of the graph of $f(x) = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$. Since $f(x) = \begin{bmatrix} 2 \\ 7 \end{bmatrix}$. Since $f(x) = \begin{bmatrix} 2 \\ 7 \end{bmatrix}$.

the graph of $h(x) = \underline{is}$ the graph of $f(x) = \underline{stretched}_X$ vertically by multiplying eachy-coordinate by 2.

26. Think of the graph of g(x) = |x|. Since f(x) = g(x-3)-4, the graph of f(x) = |x-3|-4 is the graph of g(x) = |x|

shifted right 3 units and down 4 units.

27. Think of the graph of $(x) = \sqrt[4]{x}$ Since f(x) = 3 $(y) = \sqrt[4]{x}$, the graph of f(x) = 3 x^{-5} is the graph of g(x) = xstretched vertically by multiplying eachy-coordinate by 3 and then shifted down 5 units.

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 $\frac{1}{x}$. Since f(x) = 5 - g(x), or **28.** Think of the graphofg(x) =

f(x) = -g(x) + 5, the graph of $f(x) = 5 - \frac{1}{x}$ is the graph

 $ofg(x) = {}^{1}$ -reflected across the *x*-axis and then shifted up 5 units.

29. Think of the graph of f(x) = |x|. Since g(x) = |x| $f_3 = 4$, the graph of g(x) = 3x - 4 is the graph of f(x) = x stretched horizontally by multiplying eachx-

coordinate by 3 and then shifted down 4 units. **30.** Think of the graph of g(x) = x 3. Since

 $f(x) = \frac{2}{3}g(x)-4$, the graph of $f(x) = \frac{2}{3}x_3-4$ is the graph of g(x) = x 3 shrunk vertically by multiplying each 2 *y*-coordinate by $_{3}$ -and then shifted down 4 units.

31. Think of the graph of g(x) = x 2. Since $f(x) = -g(x_{-5})$,

the graph of $f(x) = -\frac{4}{4}(x-5)$ 2 is the graph of g(x) = x 2 shifted right 5 units, shrunk vertically by multiplying each *y*-coordinate by $\overline{4}$, and reflected across the*x*-axis.

- **32.** Think of the graph ofg(x) = x 3. Since $f(x) = g(x)_{-} 5$, the graph of $f(x) = (x)^3 5$ is the graph of $g(x) = x^3$ reflected across they-axis and shifted down 5 units.
- **33.** Think of the graph of $g(x) = \frac{1}{x}$. Since $f(x) = \frac{1}{x}$

g(x+3) + 2, the graph of $f(x) = \frac{1}{x+3} + 2$ is the graph

of $g(x) = \frac{s}{x}$ hifted left 3 units and up 2 units.

34. Think of the graph $\oint f_X$) = $\bigvee_{\mathcal{X}}$ Since g(X) = f(-X) + 5, the scale of x is the graph of $f(x) = \sqrt{x}$

-axis and shifted up 5 units

35. Think of the graph of f(x) = x 2. Since h(x) = -f(x-3) +

5, the graph of $h(x) = (x-3)^2 + 5$ is the graph of $f(x) = (x-3)^2 + 5$ x2 shifted right 3 units, reflected across thex-axis, and shifted up 5 units.

- **36.** Think of the graph of g(x) = x 2. Since f(x) = 3g(x+4)-3, the graph of $f(x) = 3(x+4)^2 - 3$ is the graph of $g(x) = x^2$ shifted left 4 units, stretched vertically by multiplying each y-coordinate by 3, and then shifted down 3 units.
- **37.** The graph of y=g(x) is the graph of y=f(x) shrunk vertically by a factor of . Multiply theycoordinate by

40.The graph of *y*=*g*(*x*) is the graph of *y*=*f*(*x*) shrunk 1 horizontally. The x-coordinates of y=g(x) are the 4 correspondingx-coordinates ofy=f(x

), so we divide the or multiply it by $\frac{1}{434}$. *x*-coordinate by 4

- **41.** The graph of y=g(x) is the graph of y=f(x) shifted down 2 units. Subtract 2 from they-coordinate: (-12,2).
- **42.** The graph of y=g(x) is the graph of y=f(x) stretched horizontally. The x-coordinates of y=g(x) are twice the corresponding*x*-coordinates of y=f(x), so we multiply

or divide it by $\frac{1}{24-4}$. thex-coordinate by 2

- **43.** The graph of y=g(x) is the graph of y=f(x) stretched vertically by a factor of 4. Multiply they-coordinate by 4: (-12, 16).
- **44.** The graph of y=g(x) is the graph y=f(x) reflected across thex-axis. Reflect the point across thex-axis:

(-12,-4).

- 45.g(x) = x + 4 is the function f(x) = x + 3 shifted up 1 unit, sog(x) = f(x) + 1. Answer B is correct.
- **46.** If we substitute 3*x*for*x*in*f*, we get 9*x* 2 + 3, so g(x) = f(3x). Answer D is correct.
- 47. If we substitute x-2 for x in f, we get (x-2)³ + 3, so g(x) = f(x-2). Answer A is correct.
- **48.** If we multiply $x_2 + 3$ by 2, we get $2x_2 + 6$, so g(x) = 2f(x). Answer C is correct.

49.Shape:h(x) = x = 2

Turnh(x) upside-down (that is, reflect it across thexaxis):g(x) = -h(x) = -x2

2 Shiftg(x) right 8 units: f(x) = g(x-8) = -(x-8)

50.Shape_h (,) = Shifth(x) left 6 units:g(x) = h(x+6) =

Shiftq(x) down 5 units: f(x) = q(x) - 5 =x+ 6-5

51.Shape:h(x) = |x|Shifth(x) left 7 units:g(x) = h(x+7) = |x+7|

Shiftg(x) up 2 units: f(x) = g(x) + 2 = |x + 7| + 2

52.Shape:*h*(*x*) =*x* 3 Turnh(x) upside-down (that is, reflect it across thexaxis): $g(x) = -h(x) = -x^{3}$ Shift 3

hift
$$g(x)$$
 right 5 units: $f(x) = g(x-5) = -(x-5)$

53.Shape:
$$h(x) =$$

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 $\frac{\frac{2}{1}}{\frac{2}{2}}$: (_12,2). **38.**The graph of y=g(x) is the graph of y=f(x) shifted

right 2 units. Add 2 to the x-coordinate: (-10,4).

39. The graph of y=g(x) is the graph of y=f(x) reflected across they-axis, so we reflect the point across they-axis:

(12,4).

Shrink

h(x) vertically by a factor of that is,

multiply each function value by $\begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$

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 $g(x) = {}_{2}h(x) = {}_{2} \cdot , \text{ or } {}_{2x}$ Shiftg(x) down 3 units:f(x) = g(x) - 3 =

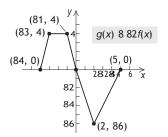
 $\frac{1}{2x}$ -3

54.Shape:h(x) = x = 22 Shifth(x) right 6 units:g(x) = h(x-6) = (x-6)Shift*q*(*x*) up 2 units: f(x) = g(x) + 2 = (x-6) $^{2} + 2$ **55.**Shape:m(x) = x = 2Turn*m*(*x*) upside-down (that is, reflect it across the*x*axis):h(x) = -m(x) = -x2 2 Shifth(x) right 3 units:g(x) = h(x-3) = -(x-3)Shiftg(x) up 4 units: f(x) = g(x) + 4 = -(x-3) $^{2}+4$ **56.**Shape:h(x) = |x|Stretch h(x) horizontally by a factor of 2 that is, multiply each*x*-value by $\frac{1}{2}:g(x) = h$ $\frac{1}{2}x = \frac{1}{2}x$ Shiftg(x) down 5 units:f(x) = g(x) - 5 =57.Shape: $m(x) = \sqrt[\gamma]{x}$ Reflectm(x) across the y-axis: h(x) = m(-x) =Shifth(x) left 2 units:g(x) = h(x+2) =Shiftg(x) down 1 unit:f(x) = g(x) - 1 =-(x+2)-1**58.**Shape:h(x) = \overline{x} 1

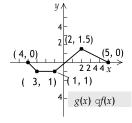
Reflect h(x) across the x-axis: g(x) = -h(x) = -Shift g(x) up 1 unit: f(x) = g(x) + 1 = - $\frac{1}{x} + 1$

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59. Eachy-coordinate is multiplied by–2. We plot and connect (–4,0), (–3,4), (–1,4), (2,–6), and (5,0).

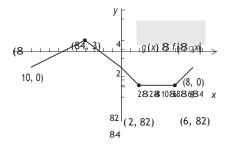


60. Eachy-coordinate is multiplied by $\frac{1}{2}$. We plot and connect



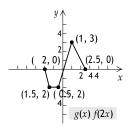
61. The graph is reflected across the*y*-axis and stretched horizontally by a factor of 2. That is, each¹*x*-coordinate is multiplied by 2

- or divided by $-\frac{1}{2}$. We plot and connect (8,0), (6,-2), (2,-2), (-4,3), and (-10,0).



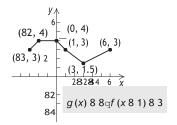
62. The graph is shrunk horizontally by a factor of 2. That is, eachx-coordinate is divided by 2 or multiplied by 1 We plot and connect (-2,0), (-1.5,-2), (-0.5,-2), (1,3),

and (2.5,0).

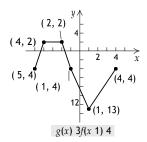


63. The graph is shifted right 1 unit so each*x*-coordinate is increased by 1. The graph is also reflected across the*x*-axis, shrunk vertically by a factor of 2, and shifted up 3

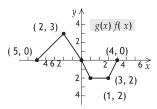
units. Thus, eachy-coordinate is multiplied by
$$-\frac{1}{2}$$
 and then increased by 3. We plot and connect (-3,3), (2,4),



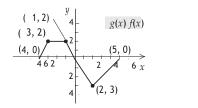
64. The graph is shifted left 1 unit so each*x*-coordinate is decreased by 1. The graph is also reflected across the *x*-axis, stretched vertically by a factor of 3, and shifted down 4 units. Thus, each*y*-coordinate is multiplied by–3 and then decreased by 4. We plot and connect (–5,–4), (–4,2), (–2,2), (1,–13), and (4,–4).



65. The graph is reflected across the*y*-axis so each *x*-coordinate is replaced by its opposite.

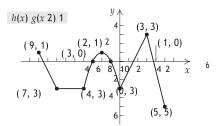


66. The graph is reflected across the*x*-axis so each *y*-coordinate is replaced by its opposite.

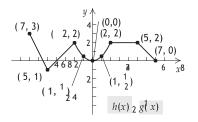


67. The graph is shifted left 2 units so each*x*-coordinate is decreased by 2. It is also reflected across the*x*-axis so each *y*-coordinate is replaced with its opposite. In addition, the graph is shifted up 1 unit, so each*y*-coordinate is then increased by 1.

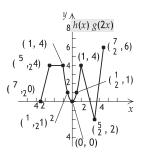
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68. The graph is reflected across they-axis so each *x*-coordinate is replaced with its opposite. It is also shrunk vertically by a factor of _, so eachy-coordinate is multi-2plied by 2-(or divided by 2).

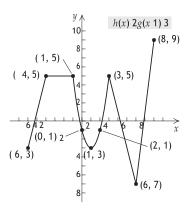


69.The graph is shrunk horizontally. The*x*-coordinates of y=h(x) are one-half the corresponding*x*-coordinates of y=g(x).



70. The graph is shifted right 1 unit, so eachx-coordinate is increased by 1. It is also stretched vertically by a factor of 2, so eachy-coordinate is multiplied by 2 or divided

by $\overline{2}$. In addition, the graph is shifted down 3 units, so eachy-coordinate is decreased by 3.



71.g(x) = f(-x) + 3

The graph of g(x) is the graph of f(x) reflected across the *y*-axis and shifted up 3 units. This is graph (f).

$$72.g(x) = f(x) + 3$$

The graph of g(x) is the graph of f(x) shifted up 3 units. This is graph (h).

 $73 \cdot g(x) = -f(x) + 3$

The graph of g(x) is the graph of f(x) reflected across the *x*-axis and shifted up 3 units. This is graph (f).

$$74 \cdot g(x) = -f(-x)$$

The graph of g(x) is the graph of f(x) reflected across the *x*-axis and the *y*-axis. This is graph (a).

$$75 \cdot g(x) = \frac{1}{3} f(x-2)$$

The graph of g(x) is the graph of f(x) shrunk vertically by a factor of 3 that is, eachy-coordinate is multiplied 1

by _and then shifted right 2 units. This is graph (d).

 $76.g(x) = \frac{1}{3}f(x) - 3$

The graph of g(x) is the graph of f(x) shrunk vertically by a factor of 3 that is, eachy-coordinate is multiplied

by
$$\overline{3}$$
 and then shifted down 3 units. This is graph (e).
77. $g(x) = \frac{1}{3}f(x+2)$

The graph of g(x) is the graph of f(x) shrunk vertically by a factor of 3 that is, eachy-coordinate is multiplied

by $\frac{1}{3}$ and then shifted left 2 units. This is graph (c).

78.g(x) = -f(x+2)

The graph of g(x) is the graph f(x) reflected across the *x*-axis and shifted left 2 units. This is graph (b).

$$79.f(-x) = 2(-x)^{4} - 35(-x)^{3} + 3(-x) - 5 = 2x4 + 35x3 - 3x - 5 = g(x)$$

80
$$f(-x) = (-x)^{4} - x^{2} + (x)^{2} + (x$$

81. The graph of f(x) = x 3-3x 2 is shifted up 2 units. A formula for the transformed function is q(x) = f(x) + 2, org(x) = x 3 - 3x 2 + 2.

82.Eachy-coordinate of the graph of f(x) = x 33x 2 is mul-

tiplied by $\frac{1}{2}$. A formula for the transformed function is $h(x) = \frac{1}{2}f(x)$, $\operatorname{or} h(x) = \frac{1}{2}(x_3 - 3x_2)$.

- **83.** The graph of f(x) = x 3-3x 2 is shifted left 1 unit. A formula for the transformed function is k(x) = f(x+1), $ork(x) = (x+1)^{3}-3(x+1)^{2}$.
- **84.** The graph of f(x) = x 3 3x 2 is shifted right 2 units and up 1 unit. A formula for the transformed function is t(x) = f(x-2) + 1, ort(x) = (x-2) $^{3}-3(x-2)^{2}+1$.

85. Test for symmetry with respect to thex-axis.

y = 3x - 3Original equation

```
-y = 3x - 3
             Replacingyby-y
```

```
y=-3x + 3 Simplifying
```

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Test for symmetry with respect to they-axis.

y = 3x - 3Original equation

 $y=3(-x)^4-3$ Replacing xby-x

y = 3x - 3Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Test for symmetry with respect to the origin:

v = 3x 4 - 3

 $-y=3(-x)^4-3$ Replacing xby-xand vby-v

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

86. Test for symmetry with respect to thex-axis.

 $y_2 = x$ Original equation

 $(-y)^2 = x \operatorname{Replacing} y \operatorname{by} - y$ *y*² =*x*Simplifying The last equation is equivalent to the original equation, so

the graph is symmetric with respect to thex-axis.

Test for symmetry with respect to they-axis:

 $y_2 = x$ Original equation

 $y_2 = -x \operatorname{Replacing} x \operatorname{by} -x$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Test for symmetry with respect to the origin:

 $y_2 = x$ Original equation

 $(-y)^2 = -x \operatorname{Replacing} x \operatorname{by} -x \operatorname{and}$

yby-y

 $y_2 = -x$ Simplifying

The last equation is not equivalent to the original equation,

so the graph is not symmetric with respect to the origin. **87.**Test for symmetry with respect to the -axis:

2x-5y=0 Original equation

2x-5(-y) = 0 Replacing yby -y

2x + 5y = 0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis. Test for symmetry with respect to they-axis:

2 5 = 0 Original equation

-y = 3x 4 - 3

x-y2(-x)-5y= 0 Replacingxby-x -2x-5y= 0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the

origin:2x-5y=0 Original equation 2(-x)-5(-y) = 0 Replacingxby-xand yby-y-2x+5y=0y=-3x + 3 Simplifying

2x-5y=0 Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

88. Let m = the number of Madden games sold, in millions. Then 3m-1 = the number of Wii Fit games sold.

Solve: 3*m*-1 = 3.5

m= 1.5 million games

89. *Familiarize*. Let*g*= the total amount spent on gift cards, in billions ofdollars.

Translate.

\$5 billion is 6% of total amount spent

5 = $0.06 \cdot g$

Carry out. We solve the equation.

 $5 = 0.06 \cdot g$ $\frac{5}{0.06} = g$ $83.3 \approx g$

Check. 6% of \$83.3 billion is 0.06(\$83.3 billion) = \$4.998 billion≈\$5 billion. (Remember that we rounded the value of *g*.) The answer checks.

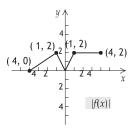
State. About \$83.3 billion was spent on gift cards.

90. Let*n*= the number of tax returns e-filed in 2005, in millions.

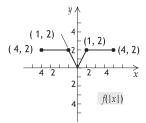
Solve:*n*+ 0.439*n*= 98.3

n≈68.3 mllion returns

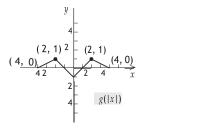
91. Each point for which *f*(*x*)<0 is reflected across the *x*-axis.



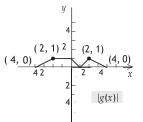
92. The graph of y=f(x) consists of the points of y=f(x) for which x ⊕ along with their reflections across the y-axis.



93. The graph of *y*=*g*(*x*|) consists of the points of *y*=*g*(*x*) for which *x* ⊉ along with their reflections across the *y*-axis.



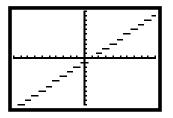
94. Each point for which*g*(*x*)<0 is reflected across the*x*-axis.



95. Think of the graph of g(x) = int(x). Since

$$f(x) = g \quad x_{-} \quad \frac{1}{2}$$
, the graph of $f(x) = int \quad x_{-} \quad \frac{1}{2}$ is the

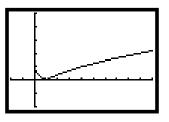
graph of g(x) = int(x) shifted right ¹ unit. The domain is the set of all real numbers; the ra²nge is the set of all integers.



96. This function can be defined piecewise as follows:

$$f(x) = \frac{\Box}{\Box} - (\neg x - 1), \text{ for } 0 \le x < 1,$$
$$\Box_{\sqrt{x-1}, \text{ for } x \ge 1,}$$

Think of the graph of $g(x) = \sqrt[\gamma]{x}$. First shift it down 1 unit. Then reflect across thex-axis the portion of the graph for which 0 < x < 1. The domain and range are both the set of nonnegative real numbers, or $[0,\infty)$.



97. On the graph of y = 2f(x) each y-coordinate of y=f(x) is multiplied by 2, so (3,4 \cdot 2), or (3,8) is on the transformed graph.

On the graph of y = 2 + f(x), each y-coordinate of y = f(x) is increased by 2 (shifted up 2 units), so (3,4 + 2), or (3,6) is on the transformed graph.

On the graph of *y*=*f*(2*x*), each*x*-coordinate of *y*=

f(x) is multiplied by $\frac{1}{2}$ (or divided by 2), so $\frac{1}{2}$ · 3,4 , or

 $\frac{3}{2}$,4 is on the transformed graph.

Λ

The graph of $y=f(x \ 3)$ is the graph of y=f(x) shifted right 3 units. Thus we shift each of the zeros of f(x) 3 units right to find the zeros of $f(x \ 3)$. They are 2.582 + 3, or 0.418; 0 + 3, or 3; and 2.582 + 3, or 5.582.

The graph of y=f(x+8) is the graph of y=f(x) shifted 8 units left. Thus we shift each of the zeros of f(x) 8 units left tofind the zeros of f(x+8). They are -2.582-8, or -10.582; 0-8, or -8; and 2.582-8, or -5.418.

Exercise Set 2.6

 $\begin{array}{ll} \mathbf{1.} & y = kx \\ & 54 = k \cdot 12 \end{array}$

 $\frac{54}{12} = k, \text{ or } k = \frac{9}{2}$ The variation constant is $\frac{9}{2}$, or 4.5. The equation of variation is $y = \frac{9}{x}$, or y = 4.5x.

1

2. y = kx0.1 = k(0.2)

 $\frac{1}{2} = kVariation constant$

Equation of variation: $y = 2^{x}$, or y = 0.5x.

3. $y = \frac{k}{x}$

$$3 = \frac{11}{12}$$

36 = k

The variation constant is 36. The equation of variation is $y = \frac{36}{2}$.

 $4 \cdot y = \frac{k}{\overline{x}}$

$$12 = \frac{k}{5}$$

60 = kVariation constantEquation of variation: $y = \frac{60}{2}$

5.
$$y = kx$$

$$1 = k - \frac{1}{4}$$

 $4 = k$

The variation constant is 4. The equation of variation is y=4x.

6. $y = \frac{1}{x}$

y=7. 32 = 1 $\cdot 32 = k$ 8 4 = kThe variation constant is 4. The equation of variation is $\begin{array}{c} 4 \end{array}$ x 8. y = kx $3 = k \cdot 33$ ¹=*k*Variation constant 1 Equation of variation:y= 11 ^x 9. y = kx<u>3</u> $=k\cdot 2$ 4 13 . 3 =k2 =k8 3 The variation constant is $\frac{1}{8}$. The equation of variation is <u>3</u> $y = \frac{x}{8}$ **10.** $y = \frac{k}{x}$ $\frac{1}{k}$ 5 35 7 =*k*Variation constant 7 Equation of variation:*y*= х 11. y=1.8 = 0.3 0.54 = kThe variation constant is 0.54. The equation of variation $isy = \frac{0.54}{2}$ x 12. y=kx 0.9 = k(0.4)9 = kVariation constant 4 Equation of variation: $y = \frac{9}{x_{1}} x_{2} \text{ or } y = 2.25x$ 0.1 = k

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 $\begin{array}{c} 0.5\\ 0.05 = k \text{Variation constant}\\ \text{Equation of variation:} y = \underbrace{\begin{array}{c} 0.05\\ x \end{array}}_{x} \end{array}$

13. Let *S*= the sales tax and *p*= the purchase price. S=kp Svaries directly as *p*. 17.50 = $k \cdot 260$ Substituting 0.067 \approx kVariation constant *S*= 0.067*p*Equation of variation *S*= 0.067(21) Substituting

S≈1.41 The sales tax is \$1.41.

14. Let *W*= the weekly allowance and *a*= the child's age.

W=ka $4.50 = k \cdot 6$ 0.75 = k

W= 0.75aW= 0.75(11)W= \$8.25k

 $W = \frac{1}{L}$ Wvaries inversely as *L*. 1200 = $\frac{k}{8}$ Substituting

9600 =*k*Variation constant 9600

$$\begin{array}{c} W = & & \text{Equation of variation} \\ W = & \frac{9600}{14} & \text{Substituting} \\ W \approx 686 \end{array}$$

A 14-m beam can support about 686 kg.

16.

$$t = \frac{-}{r}$$

$$5 = \frac{-k}{80}$$

$$400 = r$$

$$t = \frac{400}{r}$$

$$\frac{400}{r}$$

$$t = \frac{70}{70}$$

$$t = \frac{40}{70}, \text{ or } 5 \frac{5}{2} \text{ hr}$$

k

7 7 **17.** Let *F*= the number of grams of fat and *w*= the weight. *F*=*kw F* varies directly as *w*. $60 = k \cdot 120$ Substituting <u>60</u> = *k*, or Solving for *k* 120

 $\frac{1}{2} = \frac{1}{2}$ $F = \frac{1}{2}$ $\frac{1}{2}$ $F = \frac{1}{2}$ $\frac{1}{2}$ $F = \frac{1}{2}$ $\frac{1}{2}$ $F = \frac{1}{2}$

$$\frac{29}{19,011,000} = k \text{Variation constant}$$

$$N = \frac{19,011,000}{29} P$$

$$N = \frac{19,011,000}{19,011,000} \cdot 4,418,000 \text{ Substituting}$$

$$N \approx 7$$

Colorado has 7 representatives.

19.
$$T = \frac{k}{p}$$
 Tvaries inversely as *P*.
 $5 = \frac{k}{7}$ Substituting

35 =*k*Variation constant

,

 $T = \begin{array}{c} 35 \\ - \end{array} \quad Equation of variation$ $T = \begin{array}{c} P \\ 35 \\ 10 \end{array} \quad Substituting$

T= 3.5 It will take 10 bricklayers 3.5 hr to complete the job.

20.
$$t = \frac{k}{r}$$

$$45 = \frac{k}{600}$$
27,000 = k
$$t = \frac{27,000}{1000}$$

$$t = \frac{27,000}{1000}$$

$$t = 27 \text{ min}$$
21.
$$d = km \, d \text{varies directly asm.}$$

$$40 = k \cdot 3 \text{ Substituting}$$

$$\overline{3} = k \text{Variation constant}$$

$$d = \frac{40}{3} \cdot 5 = \frac{200}{3} \text{ Substituting}$$

$$F = \frac{1}{2} \cdot 180 \text{ Substituting}$$

The maximum daily fat intake for a person

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0

weighing 180lb is 90g.

 $\begin{array}{c} 2\\ d = 66 \frac{2}{3^{-}}\\ A 5 \text{-kg mass will stretch the spring } 66^{2} \frac{\text{cm.}}{3}\\ \textbf{22.} \qquad f = kF\\ 6.3 = k \cdot 150\\ 0.042 = k\\ f = 0.042F\\ f = 0.042(80)\\ f = 3.36\end{array}$

XZ

5wp

29.
$$P = \frac{k}{W}$$
 Protestinversely as W .
 $330 = \frac{k}{3.2}$ Substituting28. $y = kx = 2$
 $\frac{5}{2} = k^{-3} = 3^{-2}$
 $\frac{2}{3} = k^{-3}$ 1056 = k/Variation constant
1056 $y = \frac{2}{3x}$ 1056 = k/Variation constant $1 = k$ 105 = k/Variation constant $1 = k$ $\frac{2}{3} = k/95$ Substituting $1 = k$ $\frac{105}{5} = k$ $1 = k$ $M = \frac{2}{5}$ Substituting $1 = k$ $0.15 = k$ $0.015 = k$ $0.15 = k$ $0.0015 = k$ $10 = k$ $1 = k$ $10 = k$ $2 = k \frac{23}{2}$ $2 = k \frac{2}{3}$ $3 = \frac{2}{3}$ $\frac{2}{3} = k \frac{3}{3}$ $3 = \frac{2}{3}$ $\frac{2}{3} = k \frac{3}{3}$ <

34. $y = \kappa^2 - \frac{1}{W^2}$ Copyright © 2013 Pearson Education, Inc.

$$0.15 = 0.01k$$

$$\frac{12}{5} = k \cdot 16.3$$

$$0.15 = 5^{2}$$

$$0.01 \quad k \quad 5^{2} = k \cdot 15 = k$$
The equation of variation is y= 15x 2.
$$y = \frac{5}{4} = \frac{5}{4} = k$$

$$y = \frac{5}{4} =$$

35.
$$I = \frac{k}{d^2}$$

$$90 = \frac{k}{5^2}$$
 Substituting

$$90 = \frac{k}{25}$$

$$2250 = k$$

The equation of variation is $I = \frac{2250}{d^2}$
Substitute 40 for *l* and find *d*.

$$40 = \frac{2250}{d^2}$$

$$40d_2 = 2250$$

$$d^2$$

$$d^2$$

d= 7.5

The distance from 5 m to 7.5 m is 7.5–5, or 2.5 m, so it is 2.5 m further to a point where the intensity is 40 W/m^2 .

36. *D=kAv*

 $222 = k \cdot 37.8 \cdot 40$

$$\frac{37}{252} = k$$

$$\frac{252}{51v}$$

$$\frac{51v}{v \approx 57.4 \text{ mph}}$$
37. $d = kr = 2$

$$200 = k \cdot 60^{-2} \text{ Substituting}$$

$$200 = 3600k$$

$$200 = 3600k$$

$$200 = k$$

$$\frac{200}{3600} = k$$

$$\frac{1}{18} = k$$
The equation of variation is $d = \frac{1}{r_2}$.
$$18$$
Substitute 72 for dand findr.
$$72 = \frac{1}{r_2}$$

$$1296 = r = 2$$

$$36 = r$$
A car can travel 36 mph and still stop in 72 ft.
38. $W = -\frac{k}{(3978)^2}$

$$3,481,386,480 = k$$

$$W = \frac{3,481,386,480}{(3481,386,480)}$$

$$W = \frac{3,481,386,480}{(3481,386,480)}$$

kR **39.**E= Ι Wefirstfindk. Substituting <u>k·93</u> 3 89 = . 215.2 215.2 215.2 =*k*Multiplying by 3.89 93 93 9≈*k* 9*R* The equation of variation is*E*= Substitute 3.89 for and 238 for I $3.89 = \frac{9R}{238}^{E}$ Iand solve forR $\frac{3.89(238)}{9}$ =*R*Multiplying by 238 9 103≈*R* Bronson Arroyo would have given up about 103 earned runs if he had pitched 238 innings. **40.** $V = \frac{kT}{k}$ Р $231 = \frac{k 42}{20}$ 110 = k $V=\frac{110T}{P}$ $V=\frac{110\cdot 30}{2}$ 15 *V*= 220 cm ³ 41.parallel 42.zero 43.relative minimum

44.odd function

45. inverse variation

46.a)
$$7xy=14$$

 $y=\frac{2}{x}$
Inversely
b) $x-2y=12$
 $y=\frac{x}{2}-6$
Neither

c) -2x+y=0y=2xDirectly 3

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(3978 + 200)² *W*≈199 lb

d)
$$x = \frac{y}{4}$$

 $y = \frac{x}{3} + \frac{x}{3}$
Directly

e)
$$\frac{x}{y} = 2$$

 $y = \frac{1}{2}x$
Directly

47.Let*V* represent the volume and *p* represent the price of a jar of peanut butter.

$$\pi \frac{3}{2}$$
 (5) = k(2.89) Substituting

3.89 π =kVariation constant

 $V= 3.89\pi p$ Equation of variation

$$\pi(1.625)^2(5.5) = 3.89\pi p$$
Substituting

3.73≈p

n 2

If cost is directly proportional to volume, the larger jar should cost \$3.73.

Now let *W* represent the weight and *p* represent the price of a jar of peanut butter.

W=kp

18 = k(2.89) Substituting

6.23≈kVariation constant

W= 6.23*p*Equation of variation

28 = 6.23pSubstituting

If cost is directly proportional to weight, the larger jar should cost \$4.49. (Answers may vary slightly due to rounding differences.)

kp²

48.
$$Q = \frac{1}{q^3}$$

*Q*varies directly as the square of *p* and inversely as the cube of *q*.

49.We are toldA=kd 2, and we know $A=\pi r$ 2 so we have: $kd2=\pi r$ 2

$$kd_{2} = \pi \frac{d^{2}}{2} r = \frac{d^{2}}{2}$$
$$kd_{2} = \frac{\pi d_{2}}{\frac{4}{\pi}}$$

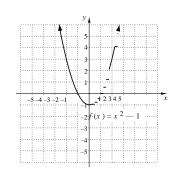
Chapter 2 Review Exercises

- **1.** This statement is true by the definition of the greatest integer function.
- **2.** Thes statement is false. See Example 2(b) in Section 2.3 in the text.
- **3.** The graph of *y*=*f*(*x d*) is the graph of *y*=*f*(*x*) shifted right *d*units, so the statement is true.

- 5.a) Forx-values from-4 to-2, they-values increase from 1 to 4. Thus the function is increasing on the interval (-4,-2).
 - b) Forx-values from 2 to 5, they-values decrease from 4 to 3. Thus the function is decreasing on the interval (2,5).
 - c) Forx-values from-2 to 2,*y* is 4. Thus the function is constant on the interval (-2,2).
- 6.a) Forx-values from-1 to 0, they-values increase from

3 to 4. Also, forx-values from 2 to ∞ , they-values increase from 0 to ∞ . Thus the function is increasing on the intervals (-1,0), and (2, ∞).

- b) Forx-values from 0 to 2, they-values decrease from 4 to 0. Thus, the function is decreasing on the interval (0,2).
- c) Forx-values from $-\infty$ to -1, *y* is 3. Thus the function is constant on the interval $(-\infty, -1)$.

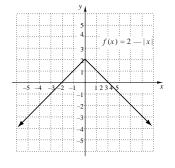


The function is increasing on $(0, \Rightarrow)$ and decreasing on $(-\infty, 0)$. We estimate that the minimum value is 1-at

x= 0. There are no maxima.



7.

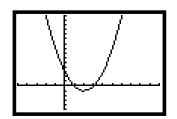


The function is increasing on $(-\infty, 0)$ and decreasing on

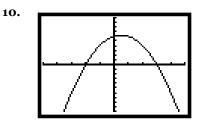
The graph of y= f(x) is the reflection of the graph of y=f(x) across thex-axis, so the statement is true.

 $(0,\infty)$. We estimate that the maximum value is 2 at x=0. There are no minima.

9.

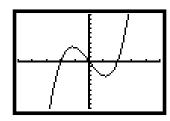


We find that the function is increasing on (2,) and decreasing on $(-\infty, 2)$. The relative minimum is 1 atx=2. There are nomaxima.

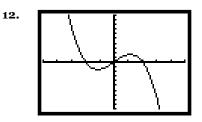


Increasing: $(-\infty, 0.5)$ Decreasing: $(0.5, \infty)$ Relative maximum: 6.25 atx= 0.5Relative minima: none

11.



We find that the function is increasing on $(-\infty, -1.155)$ and on $(1.155, \infty)$ and decreasing on (-1.155, 1.155). The relative maximum is 3.079 at x=-1.155 and the relative minimum is -3.079 at x=1.155.



We find that the function is increasing on (1.455, 1.155) and decreasing on $(-\infty, -1.155)$ and on (1.155,). The relative maximum is 1.540 at x= 1.155 and the relative minimum is -1.540 at x= -1.155.

13. If*l*= the length of the tablecloth, then the width is

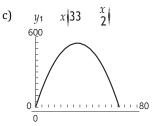
 $\frac{20-2l}{\text{wid}^2}$, or 10–*l*. We use the formula Area = length× wid²th.

A(l) =l(10–l),or A(l) = 10l–l 2

14. The length of the rectangle is 2 . The width is the second $\frac{x}{x}$

coordinate of the point (x, y) on the circle. The circle has center $(0, \underline{0})$ and radius 2, so its equation is $x_2 + y_2 = 4$ and $y = 4 - x\sqrt{\frac{2}{2}}$. Thus the area of the rectangle is given by $A(x) = 2x 4 - x^2$.

b) The length of the side parallel to the garagemust be positive and less than 66 ft, so the domain of the function is $\{x | 0 < x < 66\}$, or (0,66).



d) By observing the graph or using the MAXIMUM feature, we see that the maximum value of the function occurs when x=33. When x=33, then $33-\frac{x}{2}=33-\frac{33}{2}=33-16.5=16.5$. Thus the dimensions that yield the maximum area are 33 ft by 16.5 ft.

16.a) Leth= the height of the box. Since the volume is 108 in³, wehave:

$$108 = x \cdot x \cdot h$$
$$108 = x \cdot 2h$$
$$\frac{108}{x^2} = h$$

Nowfind the surface area.

$$S=x^{2} + 4 \cdot x \cdot h$$

$$S(x) = x^{2} + 4 \cdot x$$

$$\vdots$$

$$S(x) = x^{2} + \frac{432}{x}$$

$$x^{2}$$

b) xmust be positive, so the domain is $(0,\infty)$.

c) From the graph, we see that the minimum value of the function occurs when x = 6 in. For this value of x,

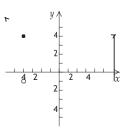
$$h = \frac{108}{x^2} = \frac{108}{6^2} = \frac{108}{36} = 3 \text{ in.}$$

$$\Box$$

$$= \frac{1}{17.} \text{ ()} = \frac{1}{1} \text{ for } \underline{x} - 4,$$

 $\begin{cases} f x & -\frac{1}{2}x + 1, \text{ for } x > -4 \\ \text{We create the graph in two parts. Graph} f(x) = -x \text{ for } \end{cases}$

inputs less than or equal to-4. Then graph $f(x) = \frac{1}{2}x+1$ for inputs greater than-4.



$$A(x) = x 33 - \frac{2}{2}, \text{er}$$
$$A(x) = 33x - \frac{x^2}{2}$$

$$\mathbf{18.} f(x) = \begin{bmatrix} x_3, \text{for } x < -2, \\ \Box \\ = \sqrt{\frac{|x|, \text{for } -2 \le x \le 2,}{\sqrt{-x-1}, \text{for } x > 2}} \end{bmatrix}$$

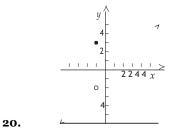
We create the graph in three parts. Graphf(x) = x 3 for inputs less than—2. Then graphf(x) = |x| for inputs greater than or equal $\sqrt[40-2]$ and less than or equal to 2. Finally graphf(x) = x-1 for inputs greater than 2.

$$y = \frac{y}{2}$$

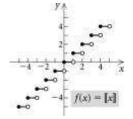
$$\frac{y}{2}$$

We create the graph in two parts. Graph $f(x) = \frac{x_2 - 1}{x + 1}$

for all inputs except-1. Then graphf(x) = 3 for x = -1.



f(x) = [[x]]. See Example 9 on page 166 of the text.



21.f(x) = [[x-3]]

This function could be defined by a piecewise function with an infinite number of statements.

$$f(x) = \frac{-3, \text{for } 0 \le x < 1, \\ -3, \text{for } 0 \le x < 2, \\ 1, \text{for } 2 \le x \le 3, \\ \vdots \\ \vdots \\ \vdots \\ 22.f(x) = \begin{bmatrix} x3, \text{for } x < 2, \\ 1, \text{for } 2 \le x \le 3, \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ z = \frac{1}{2} \int_{x}^{2} \int_{x}^$$

 $= 0 \cdot (4-1)$ Copyright © 2013 Pearson Education, Inc. **26.** $(f+g)(-1) = f(-\underline{1}) + g(-1)$ = $\sqrt{-1}^{-2} + ((-1)^{2} - 1)$ = -3 + (1-1)

Since $\sqrt[9]{-3}$ is not a realnumber, (f+g)(-1) does not exist.

27.
$$f(x) = \frac{4}{x^2}g(x) = 3 2x$$

a) Division by zero is undefined, so the domain of *f* is {x | x = 0}, or (-∞,0)∪(0,∞). The domain of *g* is the set of all real numbers, or (-∞,∞).

The domain of f+g, f-g and fg is $\{x \mid x = 0\}$,

or $(-\infty, 0) \cup (0, \infty)$. Since g = 0, the domain 2

off/gis
$$x x = 0$$
 and $x = \frac{3}{2}$, or
 $(-\infty, 0) \cup 0, \frac{33}{2} \cup \frac{3}{2}, \infty$.
b) $(-+)() = \frac{4}{x^2} + (3 \ 2x) = \frac{4}{x^2} + 3 \ 2x$
 $(f-g)(x) = \frac{4}{x^2} - (3-2x) = \frac{4}{x^2} - 3 + 2x$
 $(fg)(x) = \frac{4}{x^2}(3-2x) = \frac{12}{x^2} - \frac{8}{x}$
 $\frac{4}{x^2}$

$$(f/g)(x) = \frac{x^2}{(3-2x)} = \frac{4}{x^2(3-2x)}$$

28.a) The domain of $f_{,g,f+g,f-g,}$ and f_{g} is all real numbers, or $(-\infty,\infty)$. Since $g = \frac{1}{2} = 0$, the domain

(f/g)(x) = 2x-1

29.
$$P(x) = R(x) - C(x)$$

= (120x-0.5x 2)-(15x+6)
= 120x-0.5x 2-15x-6
=-0.5x 2 + 105x-6

30.
$$f(x) = 2x + 7$$

$$\frac{f(x+h) - f(x)}{h} = \frac{2(x+h) + 7 - (2x+7)}{h} = \frac{h}{2x + 2h + 7 - 2x - 7} = \frac{2h}{2} = 2$$

f(x+h)-f(x) = 3-x + 2-2xh-h + 2-(3-x + 2)

38. $(h \circ g)(2) = h(g(2)) = h(2^2 + 4) = h(4 + 4)$ $h(8) = 3 - 8^3 = 3 - 512 = -509$ **39.** $(f \circ f)(x) = f(f(x)) = f(2x-1) = 2(2x-1)-1 =$

$$4x - 2 - 1 = 4x - 3$$

40. $(h \circ h)(x) = h(h(x)) = h(3-x \quad 3) = 3-(3-x \quad 3)^3 =$ $3-(27-27x \quad 3+9x_6-x \quad 9) = 3-27+27x \quad 3-9x \quad 6+x \quad 9 =$ $-24+27x_3-9x \quad 6+x \quad 9 =$ **41.**a) $f() = (3 \quad 2) =$

$${}^{\circ}g x \quad f - x \qquad (3-2x)^{2} \\ 4 \qquad 4 \qquad 8 \\ g {}^{\circ}f(x) = g \qquad \frac{1}{x^{2}} = 3-2 \qquad x^{2} = 3-\frac{1}{x^{2}} \\ h \qquad h \qquad 31.f(x) = 3-x^{2}$$

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b) The domain of $fis{x|x = 0}$ and the domain of g

2

$$f(x+h) = 3-(x+h)$$
 $^{2} = 3-(x^{2}+2xh+h^{2}) =$

$$\begin{array}{cccc} 3 & 2 & 2 \\ -x & -2xh-h \end{array}$$

is the set of all real numbers. Tofind the domain of $f \circ g$, we find the values of $x \circ g$ which g(x) = 0. Since 3-2x=0 when x=, the domain of $f \circ g$ 3 2 :-

is
$$3 - 3$$

 $x x = 2$, or $-\infty$, $2 \cup 2, \infty$. Since

_

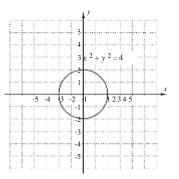
any real number can be an input forg, the domain of $g \circ f$ is the same as the domain of f, $\{x | x = 0\}$, α (-∞,0)∪(0,∞).

$$\begin{array}{l} \textbf{42.a} \quad f \circ g(x) = f(2x-1) \\ &= 3(2x-1)^2 + 4(2x-1) \\ &= 3(4x_2 - 4x + 1) + 4(2x-1) \\ &= 12x_2 - 12x + 3 + 8x - 4 \\ &= 12x_2 - 4x - 1 \\ (g \circ f)(x) = g(3x + 4x) \\ &= 2(3x_2 + 4x) - 1 \\ &= 6x_2 + 8x - 1 \end{array}$$

- b) Domain of f= domain of g= all real numbers, so domain of $f \circ g$ = domain of $g \circ f$ = all real numbers, or $(-\infty,\infty)$.
- **43** f(x) = x, g(x) = 5x + 2. Answers may vary.

44.f(x) = 4x + 9, g(x) = 5x-1. Answers may vary.

45•*x*
2
 +*y* $_{2}$ = 4



The graph is symmetric with respect to the *x*-axis, the *y*-axis, and the origin.

Replacey with y to test algebraically for symmetry with respect to thex-axis.

$$x_2 + (-y)^2 = 4$$

$$x_2 + y_2 = 4$$

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to thex-axis. Replace with to test algebraically for symmetry with

x -x respect to the *y*-axis.

$$(-x)^2 + y_2 = 4$$

 $x_2 + y_2 = 4$

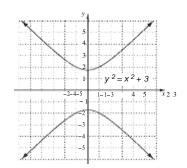
The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Replace*x* and *x* and *y* with *y* to test for symmetry with respect to the origin.

$$(-x)^2 + (-y)^2 = 4$$

x2 +y 2 = 4

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to the origin. **46.** $y^2 = x_2 + 3$



The graph is symmetric with respect to the *x*-axis, the *y*-axis, and the origin.

Replacey with y to test algebraically for symmetry with respect to the x-axis.

$$(-y)^2 = x + 3$$

 $y_2 = x + 3$

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to the*x*-axis.

Replacex with *x* to test algebraically for symmetry with respect to the *y*-axis.

$$y_2 = (-x)^2 + 3$$

$$y_2 = x + 3$$

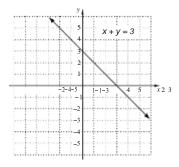
The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Replace*x* and *x* and *y* with *y* to test for symmetry with respect to the origin.

$$(-y)^2 = (-x)^2 + 3$$

 $y_2 = x + 3$

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.



The graph is not symmetric with respect to the *x*-axis, the *y*-axis, or the origin.

Replacey with y to test algebraically for symmetry with respect to thex-axis.

x-y=3

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Replace*x* with *x*to test algebraically for symmetry with respect to the *y*-axis.

-x+y=3

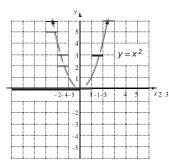
Replacexand–xandy with -y to test for symmetry with respect to the origin.

-x-y=3

x+y=-3

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

48. *y*=*x* 2



The graph is symmetric with respect to the y-axis. It is not symmetric with respect to the x-axis or the origin.

Replacey with y to test algebraically for symmetry with respect to the x-axis.

 $-y=x_2$ $y=-x_2$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the*x*-axis.

Replace*x* with *-x*to test algebraically for symmetry with respect to the *y*-axis.

y= (-x)² y=x²

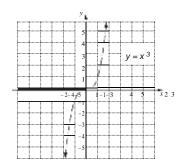
The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Replace*x* and *x* and *y* with *y* to test for symmetry with respect to the origin.

 $-y = (-x)^{2}$ $-y = x^{2}$ $y = -x^{2}$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

49. *у*=х з



The graph is symmetric with respect to the origin. It is not symmetric with respect to the*x*-axis or the*y*-axis.

Replacey with y to test algebraically for symmetry with respect to the x-axis.

-*у=х* з *у=-х* з

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to thex-axis.

Replacexwith-xto test algebraically for symmetry with respect to they-axis.

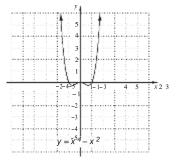
y= (−*x*) ³ *y*=−*x* з

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to they-axis.

Replacexand—xandy with —y to test for symmetry with respect to the origin.

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

50.*y*=*x* 4 –*x* 2



The graph is symmetric with respect to the y-axis. It is not symmetric with respect to the x-axis or the origin.

Replacey with y to test algebraically for symmetry with respect to the x-axis.

$$-y=x 4 - x 2$$

 $y=-x 4 + x 2$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to

thex-axis. Replacexwith– to test algebraically for symmetry with

respect to the x y-axis.

 $y = (-x)^4 - (-x)^2$

y=*x* 4 –*x* 2

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis.

Replacexand–xandywith–yto test for symmetry with respect to the origin.

 $-y = (-x)^4 - (-x)^2$

$$-y=x 4 - x 2$$

 $y=-x 4 + x 2$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

- **51.** The graph is symmetric with respect to the*y*-axis, so the function is even.
- **52.** The graph is symmetric with respect to the*y*-axis, so the function is even.
- **53.** The graph is symmetric with respect to the origin, so the function is odd.
- **54.** The graph is symmetric with respect to the*y*-axis, so the function is even.

55.
$$f(x) = 9-x = 2$$

 $f(-x) = 9-(-x = 2) = 9-x = 2$
 $f(x) = f(-x)$, so fis even.

56.
$$f(x) = x \cdot 3 - 2x + 4$$

 $f(-x) = (-x)^3 - 2(-x) + 4 = -x \cdot 3 + 2x + 4$

$$f(x) f(-x), \text{sofis not even.}$$

$$-f(x) = -(x - 2x + 4) = -x + 2x - 4$$

$$f(-x) - f(x), \text{sofis not odd.}$$

Thus, $f(x) = x \cdot 3 - 2x + 4$ is neither even or odd.

57.
$$f(x) = x 7 - x 5$$

 $f(-x) = (-x)^{7} - (-x)^{5} = -x^{7} + x^{5}$ f(x) f(-x), so f is not even. $-f(x) = -(x^{7} - x^{5}) = -x^{7} + x^{5}$

f(-x) = -f(x), so f is odd.

58. f(x) = |x|

f(-x) = |-x| = |x| $f(x) = f(\sqrt{x}), \text{ sofis even.}$

60.
$$f(x) = \frac{10x}{x^2 + 1}$$

$$f(-x) = \frac{10(-x)}{(-x)^2 + 1} = -\frac{10x}{x^2 + 1}$$

$$f(x) = -\frac{1}{x^2+1}$$

f(-x) = -f(x), so f is odd.

61.Shape:
$$g(x) = x$$
 2
Shift $g(x)$ left 3 units: $f(x) = g(x+3) = (x+3)$ 2

62.Shape:*t*(*x*) = *x* Turn*t*(*x*) upside down (that is, reflect it across the*x*-axis):

$$h(x) = -t(x) = -\frac{\sqrt{-x}}{x}.$$

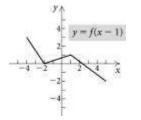
Shifth(x) right 3 units: $g(x) = h(x-3) = -\sqrt{-x-3}.$

Shift
$$g(x)$$
 up 4 units: $f(x) = g(x) + 4 = -x - 3 + 4$.

63.Shape:h(x) = |x|

Stretch*h*(*x*) vertically by a factor of 2 (that is, multiply each function value by 2):g(x) = 2h(x) = 2|x|. Shift*g*(*x*) right 3 units:f(x) = g(x-3) = 2|x-3|.

64. The graph is shifted right 1 unit so each*x*-coordinate is increased by 1. We plot and connect (-4,3), (-2,0), (1,1) and (5,-2).



65. The graph is shrunk horizontally by a factor of 2. That is, each*x*-coordinate is divided by 2. We plot and connect

$$-\frac{5}{2}$$
, $3, -\frac{3}{2}, 0, (0,1)$ and $(2, -2)$.



66. Each -coordinate is multiplied by 2. We plot and con-



59.
$$f(x) = 16-x^2$$

 $f(-x) = \overline{16-(-x^2)} = \sqrt[4]{16-x^2}$
 $f(x) = f(-x)$, sofis even.

67. Eachy-coordinate is increased by 3. We plot and connect (-5,6), (-3,3), (0,4) and (4,1).

3^{*x*}

$$y = 3 + f(x)$$

68. y=kx

100 = 25x

$$4 = x$$

Equation of variation:y = 4x

6 = 9x2 =*x*Variation constant 2 Equation of variation: = $\frac{3}{2}$

$$y = \frac{k}{x}$$

$$100 = \frac{k}{25}$$

2500 = kEquation of variation:y=²⁵⁰⁰ х

71.
$$y = \frac{k}{k}$$

9 54 =*k*Variation constant 54 Equation of variation:y= x

72.
$$y = \frac{k}{x^2}$$
$$12 = \frac{k}{2^2}$$
$$48 = k$$
$$y = \frac{48}{-1}$$
$$x^2$$

kxz2 **73**. v=w 1 2 k(16) 2 2 = 2 = 0.2 $2 = \frac{4k}{0.2}$ 2 = 20k $\hat{1}_{=k}$ 10 1 *xz*2 *y*= $\overline{10} w$ $t=\frac{k}{k}$ 74. k 35 = 800 28,000 = k $t = \frac{28,000}{2}$ 28,000 t= 1400 *t*= 20 min 75. N= ka 87 =k·29 3 = kN=3aN = 3.25N = 75Ellen's score would have been 75 if she had answered 25 questions correctly. P=kC 2 76. $180 = k \cdot 6^2$ 5 =*k*Variation constant *P*= 5*C* 2 Variation equation $P = 5 \cdot 10^{2}$ P=500 watts $\sqrt{}$ $77 \cdot f(x) = x + 1, g(x) =$ х The domain of *f* is $(-\infty,\infty)$, and the domain of *g* is $[0,\infty)$.

To find the domain of $(g \circ f)(x)$, we find the values of xfor which $f(x) \ge 0$.

x+ 1≥0

 $x \ge -1$

Thus the domain of (g f)(x) is [1,]. Answer A is correct.

78. For b > 0, the graph of y = f(x) + b is the graph of y = f(x)shifted upbunits. Answer C is correct.

79. The graph of $g(x) = -\frac{1}{2}f(x) + 1$ is the graph of y=f(x)shrunk vertically by a factor of $\frac{1}{2}$, then reflected across the *x*-axis, and shifted up 1 unit. The correct graph is B.

- Reflect the graph of y=f(x) across the x-axis and then across the y-axis.

82.
$$f(x) = 4x \ 3-2x+7$$

a) $f(x) + 2 = 4x \ 3-2x+7 + 2 = 4x \ 3-2x+9$
b) $f(x+2) = 4(x+2)^{3}-2(x+2) + 7$
 $= 4(x3 + 6x2 + 12x+8)-2(x+2) + 7$
 $= 4x3 + 24x2 + 48x + 32-2x-4 + 7$
 $= 4x3 + 24x2 + 46x + 35$
c) $f(x) + f(2) = 4x \ 3-2x+7 + 4\cdot2^{3}-2\cdot2 + 7$
 $= 4x3 - 2x + 7 + 32 - 4 + 7$
 $= 4x3 - 2x + 42$

f(x) + 2 adds 2 to each function value; f(x+2) adds 2 to each input before the function value is found; f(x) + f(2) adds the output for 2 to the output forx.

- 83. In the graph of y=f(cx), the constant cstretches or shrinks the graph of y=f(x) horizontally. The constant ciny=cf(x) stretches or shrinks the graph of y=f(x) vertically. For y=f(cx), the x-coordinates of y=f(x) are divided byc; for y=cf(x), the y-coordinates of y=f(x) are multiplied byc.
- **84.** The graph of f(x) = 0 is symmetric with respect to the *x*-axis, the *y*-axis, and the origin. This function is both even and odd.
- **85.** If all of the exponents are even numbers, then f(x) is an even function. If a = 0 and all of the exponents are odd

numbers, then f(x) is an odd function.

86.Let y(x) = kx 2. Then $y(2x) = k(2x)^2 = k \cdot 4x$ 2 = $4 \cdot kx$ 2 = $4 \cdot y(x)$. Thus, doubling xcauses y to be quadrupled.

87.Lety=k xandx=
$$\frac{k_2}{z}$$
. Theny=k $\frac{k_2}{z}$, or $y = z$,

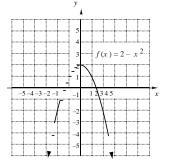
soyvaries inversely asz.

Chapter 2 Test

- **1.**a) Forx-values from-5 to-2, they-values increase from-4 to 3. Thus the function is increasing on the interval (-5,-2).
 - b) Forx-values from 2 to 5, they-values decrease from 2 to–1. Thus the function is decreasing on the

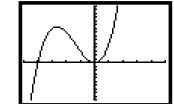
interval (2,5).

2.



The function is increasing on $(-\infty, 0)$ and decreasing on $(0, c_0)$. The relative maximum is 2 at x= 0. There are no minima.





We find that the function is increasing on– $(\infty, -2.667)$ and on $(0,\infty)$ and decreasing on (-2.667,0). The relative maximum is 9.481 at–2.667 and the relative minimum is 0 at x=0.

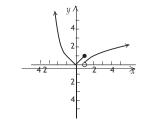
4. If b= the length of the base, in inches, then the height = 4b-6. We use the formula for the area of a triangle,

$$A = 2 \frac{bh}{bh}$$

 $A(b) = \frac{1}{b}(4b \ 6)$, or
 $2 - \frac{bh}{bh}$

$$A(b) = 2b_2 - 3b$$

$$\mathbf{5.f}(x) = \begin{bmatrix} |x|, \text{for} - 1 \le x \le 1, \\ |x|, \text{for} - 1 \le x \le 1, \\ -\sqrt{\frac{1}{x-1, \text{for} x > 1}} \end{bmatrix}$$



6.Since $-1 \le -\frac{7}{5} \le 1$, $f = -\frac{7}{5} = -\frac{7}{5} = \frac{7}{5}$

Since
$$-4 < -1$$
, $f(-4) = (-4)^{2} = 16$
7. $(f+g)(-6) = f(-6) + g(-6) = (-6)^{2} - 4(-6) + 3 + -(-6) = (-6)^{2} = (-6)^{2} - 4(-6) + 3 + -(-6) = (-6)^{2} = (-6)^{2} - 4(-6) + 3 + -(-6)^{2} = (-6)^{2} - 4(-6)^{2} + 3(-6)^{2} + (-6)^{2} = (-6)^{2} - 4(-6)^{2} + 3(-6)^{2} + (-6)^{2} = (-6)^{2} - 4(-6)^{2} + 3(-6)^{2} + (-6)^{2} = (-6)^{2} - 4(-6)^{2} + 3(-6)^{2} + (-6)^{2} = (-6)^{2} - 4(-6)^{2} + (-6)^{2} + (-6)^{2} + (-6)^{2} = (-6)^{2} - 4(-6)^{2} + (-6)^{2} + (-6)^{2} + (-6)^{2} + (-6)^{2} = (-6)^{2} - (-6)^{2} + (-6)^{$

c) Forx-values from-2 to

2,yis 2. Thus the

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function is constant on the interval (-2,2).

$$36 + 24 + 3 + \sqrt{3}$$

 $3 + 6 = 63 + \sqrt{9} = 63 + 3 = 66$

8.
$$(f-g)(-1) = f(-1)-g(-1) =$$

 $(-1)^2 - 4(-1) + 3 - 3 - (-1) =$
 $1 + 4 + 3 - \sqrt[3]{3} + 1 = 8 - \sqrt[3]{-2} = 6$
 $4 = 8$
9. $(fg)(2) = f(2) \cdot g(2) = (2^2 - 4 \cdot 2 + 3)(\sqrt[3]{3} - 2) =$
 $(4 - 8 + 3)(\sqrt[4]{1}) = -1 \cdot 1 = -1$
10. $(f/g)(1) = \frac{f(1)}{g(1)} = \frac{1^2 - 4 \cdot 1 + 3}{\sqrt{3} - 1} = \frac{1 - 4 + 3}{\sqrt{3}} = \frac{0}{\sqrt{2}} = 0$

- **11.** Any real number can be an input for f(x) = x2, so the domain is the set of real numbers, or $(-\infty,\infty)$.
- **12.** The domain of $g(x) = x \overline{3}$ is the set of real numbers for which x-3 \ge 0, or x \ge 3. Thus the domain is { $x | x \ge$ 3}, or [3,∞).
- **13.** The domain of *f*+*g* is the intersection of the domains of fandg. This is $\{x | x \ge 3\}$, or $[3, \infty)$.
- **14.** The domain of *f*-*g* is the intersection of the domains of fandg. This is $\{x | x \ge 3\}$, or $[3, \infty)$.
- **15.** The domain of *fg* is the intersection of the domains of *f* and g. This is $\{x | x \ge 3\}$, or $[3, \infty)$.
- **16.** The domain of *f*/*g* is the intersection of the domains of *f* and *q*, excluding those *x*-values for which q(x) = 0. Since x-3 = 0 when x= 3, the domain is (3, ∞).

$$17.(f+g)(x) = f(x) + g(x) = x \qquad 2 + \sqrt[7]{x-3}$$

$$18.(f-g)(x) = f(x) - g(x) = x \qquad 2 - \sqrt[7]{x-3}$$

$$19.(fg)(x) = f(x) \cdot g(x) = x \qquad \frac{\sqrt[7]{x-3}}{2 \cdot x-3}$$

$$20.(f/g)(x) = \frac{f(x)}{g(x)} = \frac{\sqrt{x-3}}{\sqrt{x-3}}$$

$$1$$

21. $f(x) = 2\overline{x} + 4$ 1 1 $f(x+h) = \frac{1}{2}(x+h) + 4 = \frac{1}{2}x + \frac{1}{2}h + 4$

h

$$\frac{f(x+h)-f(x)}{2} = \frac{1}{2}x + \frac{1}{2}h + 4 - \frac{1}{2}x + 4$$

$$1 \quad 1 \quad 1 \\ - \quad - \\ = \frac{2^{x+2} + 2^{h+4-2x-4}}{1_{h}}$$
$$= \frac{2}{h} = \frac{1}{2^{h}} \cdot \frac{1}{h} = \frac{1}{2} \cdot \frac{h}{h} = \frac{1}{2}$$

2

22.
$$f(x) = 2x \ 2-x+3$$

 $f(x+h)=2(x+h)^2-(x+h)+3=2(x_2+2xh+h_2)-x-h+3=$

 $2x_2 + 4xh + 2h_2 - x - h + 3$

 $f(x+h)-f(x) = 2x^2+4xh+2h^2-x-h+3-(2x^2-x+3)$

h

$$2x_2 + 4xh + 2h_2 - x_h + 3 - 2x_2 + x - 3$$

h

$$= \frac{4xh+2h_2-h}{h}$$
$$= \frac{h}{h/(4x+2h_1)}$$
$$= \frac{h/(4x+2h_1)}{h/}$$
$$= 4x+2h-1$$

- **23.** $(g \circ h)(2) = g(h(2)) = g(3 \cdot 2 2 + 2 \cdot 2 + 4) =$ $g(3\cdot 4 + 4 + 4) = g(12 + 4 + 4) = g(20) = 4\cdot 20 + 3 =$ 80 + 3 = 83
- **24.** $(f \circ g)(-1) = f(g(-1)) = f(4(-1) + 3) = f(-4 + 3) =$ $f(-1) = (-1)^2 - 1 = 1 - 1 = 0$
- **25.** $(h \circ f)(1) = h(f(1)) = h(1 \ ^2 1) = h(1 1) = h(0) =$ $3 \cdot 0^2 + 2 \cdot 0 + 4 = 0 + 0 + 4 = 4$

26.
$$(g \circ g)(x) = g(g(x)) = g(4x+3) = 4(4x+3) + 3 = 16x+12+3 = 16x+15$$

$$\int_{X^2-4}^{Y^2-4} f_{X}g x fg x fx x^2 - \frac{1}{x^2-4}$$

$$(g \circ f)(x) = g(f(x)) = g(\sqrt[\gamma]{x-5}) = (\sqrt[\gamma]{x-5})^2 + 1 = x-5 + 1 = x-4$$

28. The inputs for f(x) must be such that $x-5\geq 0$, or $x\geq 5$. Then for $(f \circ g)(x)$ we must have $g(x) \ge 5$, or $2 + 1 \ge 5$, or

 $x_2 \ge 4$. Then the domain of $(f \circ g)(x)$ is $(-\infty, -2] \cup [2, \infty)$. Since we can substitute any real number forxing, the

domain of $(g \circ f)(x)$ is the same as the domain of f(x), [5,∞).

29. Answers may vary.f(x) = x + 4g(x) = 2x-7

30.*y*=*x* 4-2*x* 2

Replacey with y to test for symmetry with respect to thex-axis. -y=x 4 - 2x 2

$y = -x + 2x_2$

The resulting equation is not equivalent to the original Copyright © 2013 Pearson Education, Inc.

equation, so the graph is not symmetric with respect to the x-axis.

Replacexwith–xto test for symmetry with respect to they-axis.

$$y = (-x)^{4} - 2(-x)^{2}$$

$$y = x^{4} - 2x^{2}$$

The resulting equation is equivalent to the original equation, so the graph is symmetric with respect to they-axis. Replacexwith xandy with yto test for symmetry with respect to the origin.

$$-y = (-x)^{4} - 2(-x)^{2}$$

-y=x 4 - 2x 2
y=-x 4 + 2x2
regular g equation is not equivalent to the origin

The resulting equation is not equivalent to the original

equation, so the graph is not symmetric with respect to the origin.

31.
$$f(x) = \frac{2x}{x^2 + 1}$$

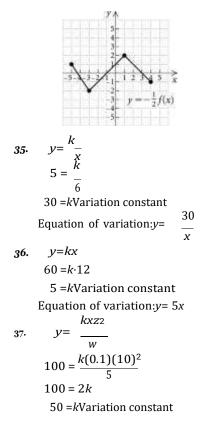
$$f(x) = \frac{2(-x)}{(-x)^2 + 1} = \frac{2x}{x^2 + 1}$$

$$f(x) = f(-x), \text{ sofis not even.}$$

$$\frac{-2x}{-f(x) = -x^2 + 1}$$

$$f(-x) = -f(x), \text{ sofis odd.}$$
32. Shape: $h(x) = x = 2$
Shift $h(x)$ right 2 units: $g(x) = h(x-2) = (x-2)$
Shift $g(x)$ down 1 unit: $f(x) = (x-2) = 2^{-1}$
33. Shape: $h(x) = x = 2$
Shift $h(x)$ left 2 units: $g(x) = h(x+2) = (x+2) = 2^{-1}$
Shift $g(x)$ down 3 units: $f(x) = (x+2) = 2^{-1}$

2



38. *d=kr* ²

$$200 = k \cdot 60^{2}$$

$$\frac{1}{18} = k \text{Variation constant}$$

$$d = \frac{1}{18} r^{2}$$
Equation of variation
$$d = \frac{1}{18} \cdot 30^{2}$$

$$d = 50 \text{ ft}$$

39. The graph of g(x) = 2f(x)-1 is the graph of y=f(x)

stretched vertically by a factor of 2 and shifted down 1 unit. The correct graph is C.

40. Each*x*-coordinate on the graph of y=f(x) is divided by $\underline{-3}$

3 on the graph of
$$y=f(3x)$$
. Thus the point 3, 1, or $(-1,1)$ is on the graph of $f(3x)$.

 $y = \frac{50xz_2}{w}$ Equation of variation

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