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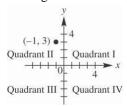
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Chapter 2 GRAPHS AND FUNCTIONS

Section 2.1 Rectangular Coordinates and Graphs

The point (-1, 3) lies in quadrant \underline{II} in the rectangular coordinate system.



The point $(4, \underline{6})$ lies on the graph of the equation y = 3x - 6. Find the *y*-value by letting x = 4 and solving for *y*.

3461266

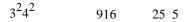
Any point that lies on the x-axis has

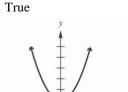
y-coordinate equal to 0.

The *y*-intercept of the graph of y = -2x + 6 is (0, 6).

The x-intercept of the graph of 2x + 5y = 10 is (5, 0). Find the x-intercept by letting y = 0 and solving for x.

2*x* 5 0 10 2 *x* 10 *x* 5

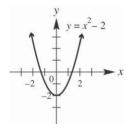




The distance from the origin to the point (-3, 4) is $\underline{5}$. Using the distance formula, we have

$$d(P,Q) (30)^2 (40)^2$$

True



9. False. The midpoint of the segment joining

(0,0) and (4,4) is

$$\frac{40}{10}$$
, $\frac{40}{10}$, $\frac{4}{10}$, $\frac{$

2 2

2 2

False. The distance between the point (0,0) and (4,4) is

$$\frac{d(P, Q)\sqrt{(4\,0)^2 (4\,0)^2}}{\sqrt{616}} \sqrt{\frac{4^2 4^2}{32 4^2}}$$

Any three of the following:

2,5,1,7,3,9,5,17,6,21

Any three of the following:

3,3,5, 21, 8,18,4, 6,0, 6

Any three of the following: (1999, 35), (2001, 29), (2003, 22), (2005, 23), (2007, 20), (2009, 20)

Any three of the following:

2002, 86.8, 2004, 89.8, 2006, 90.7,

2008, 97.4, 2010, 106.5, 2012,111.4,

2014, 111.5

P(-5, -6), Q(7, -1)

(a)
$$d(P,Q) \frac{[7-(-5)]^2 [1-(-6)]^2}{\sqrt{12^2} 5^2 \sqrt{169} 13}$$

The midpoint M of the segment joining points P and Q has coordinates

$$P(-4, 3), Q(2, -5)$$

$$d(P,Q) \quad [2 - (-4)]^{2} \quad (-5 - 3)^{2}$$

$$\sqrt{2 \quad (-8)^{2}} \quad \sqrt{100} \quad 10$$

The midpoint M of the segment joining points P and Q has coordinates

$$-42$$
, $3(-5)$, 2 , 2

2, 2, 2, 2, 1, 1.

P(8, 2), Q(3, 5)

$$d(P,Q) = (3-8)^{2} (5-2)^{2}$$

$$5^{2} 3^{2}$$

$$259 = 34$$

The midpoint M of the segment joining points P and Q has coordinates

$$\frac{83}{2}$$
, $\frac{25}{11}$, $\frac{11}{7}$.

$$P(-8,4), Q(3,-5)$$

(a)
$$d(P, Q) = 3 + 8 = 54$$

$$\sqrt{1^2 (-9)^2} = \sqrt{12181}$$

The midpoint M of the segment

joining points P and Q has coordinates

$$-83, 4(-5)$$
 5, 1.

$$P(-6, -5), Q(6, 10)$$

$$d(P, Q) = [6 - (-6)]^2 = [10 - (-5)]^2$$
 the length 2017 Pearson Education, Inc.

The midpoint M of the segment joining points N and N are coordinates

$$\sqrt[3]{1}\sqrt{2}$$
 4 5(-5)

The midpoint M of the segment joining points P and Q has coordinates

$$\frac{\sqrt{157}}{\sqrt{157}} \sqrt{\frac{8\sqrt{3}(-3)}{3}} \sqrt{2}$$

$$\frac{4\sqrt{1}}{2}, \frac{7\sqrt{3}}{2} = 27, \frac{7}{2}$$

Label the points A(-6, -4), B(0, -2), and C(-10, 8). Use the distance formula to find the length of each side of the triangle.

$$\sqrt[2]{2^2 \cdot 15^2} \quad \sqrt{144 \cdot 225}$$

$$d(A, B) \sqrt{\frac{[0-(-6)]}{2} \sqrt{-2-(-4)}}$$

The midpoint M of the segment joining points P and Q has coordinates

$$\frac{-6.6}{5}$$
, $\frac{-5.10}{0}$, $\frac{0}{5}$, $\frac{5}{0}$, $\frac{5}{0}$.

$$P(6, -2), Q(4, 6)$$

(a)
$$d(P, Q) = (4\sqrt{-6})^2 = [6 - (-2)]^2$$

$$\sqrt{-2)^2 8^2} = \sqrt{-6}$$

$$464 = 682\sqrt{7}$$

The midpoint M of the segment joining points P and Q has coordinates

$$d(B,C) = \sqrt{\frac{(-10-0)^2 [8-(-2)]^2}{\sqrt{10)^2} 10^2}} = \sqrt{\frac{100100}{\sqrt{100100}}}$$

$$d(A,C) \sqrt{[-10-(-6)]^2 [8-(-4)]^2} \sqrt{(-4)^2 12^2} \sqrt{16 144} \sqrt{160}$$

$$\sqrt{}^2 \sqrt{}^2 \sqrt{}^2$$
Because $40 \quad 160 \quad 200$,

triangle ABC is a right triangle.

Chapter 2 Graphs and Functions Label the points A(-2, -8), B(0, -4), and C(-4, -7). Use the distance formula to find

the length of each side of the triangle. d(A,

B)
$$[0-(-2)]^2 [-4-(-8)]^2$$

$$\sqrt[4^2 4^2]{4 \cdot 16} \sqrt[40]{0}$$

$$d(B,C) \sqrt{\frac{-4-0}{2} [-7-(-4)]^2}$$

$$\sqrt[4]{2} (-3)^2 \sqrt{169}$$

$$d(A,C) \sqrt{[-4-(-2)]^{2}[-7-(-8)]^{2}} \sqrt{[-2)^{2} 1^{2}} \sqrt{41} \sqrt{41}$$

Because $(\frac{1}{9})^2$ ($20\sqrt{25}$ 20 25 5^2 , triangle *ABC* is a right triangle.

Label the points A(-4, 1), B(1, 4), and

$$C(-6, -1)$$
.

$$d(A, B) \sqrt{1 - (-4)]^2 \sqrt{4 - 1}^2}$$

$$5^2 3^2 \qquad 259 \ 34$$

$$d(B,C) = \sqrt{\frac{(-6-1)^2 (-1-4)^2}{\sqrt{-7)^2 (-5)^2}}} \sqrt{\frac{1-49 25}{49 25}} \sqrt{\frac{1-49 25}{74}} \sqrt{\frac{1-49 25}{74}}} \sqrt{\frac{1-49 25}{74}} \sqrt{\frac{1-49 25}{74}} \sqrt{\frac{1-49 25}{74}}} \sqrt{\frac{1-$$

$$d(A,C) \sqrt{[-6-(-4)]^{2}(-1-1)^{2}} \sqrt{-2)^{2}(-2)^{2}} \sqrt{448} \sqrt{8} \sqrt{-2}$$

Because $()^2 ()^2 (74)^2$ because

8 34 42 74, triangle *ABC* is not a right triangle.

Label the points A(-2, -5), B(1, 7), and C(3, 15).

$$d(A, B) = \sqrt{\frac{[1-(2)]^2}{\sqrt[3]{212^2}}} = \sqrt{\frac{[7(5)]^2}{9144}} \sqrt{\frac{153}{153}}$$

$$d(B,C) \sqrt{12} \frac{2 \ 65}{\sqrt{-3)^2 \ (-11)^2}}$$
9121 130

$$\frac{d(A,C)}{\sqrt{3^{2}9^{2}}} \sqrt{\frac{981}{981}} \sqrt{\frac{9}{9}}$$

Because
$$40$$
 90 130 , triangle

ABC is a right triangle.

Label the points A(-7, 4), B(6, -2), and C(0, -15).

$$d(A, B) \sqrt{6-7} \quad \begin{array}{c} 2 & 4 & 2 \\ \sqrt{3^2 + 6^2} & \sqrt{2} & \sqrt{2} \\ 169 & 36 & 205 \end{array}$$

410

Because
$$\sqrt{205}^2$$
 $\sqrt{205}^2$ $41\sqrt[3]{2}$,

triangle ABC is a right triangle.

Label the given points A(0, -7), B(-3, 5), and C(2, -15). Find the distance between each pair of points.

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d(B,C) (31) 2 (157) $_{2}$

$$\sqrt{\frac{1}{2} \cdot 8^{2}} \sqrt{464} \cdot 68$$

$$d(A,C) \sqrt{[3(2)]^{2}} \sqrt{15(5)}^{2}$$

$$\sqrt{25400} \sqrt{425}$$

Because
$$($$
 $)^2$ $($ $\sqrt{425}$ 2 because

68 153 221 425 , triangle ABC is not a

right triangle.

27. Label the points A(-4, 3), B(2, 5), and C(-1, -6).

$$d(A,B) \sqrt{2--4} \frac{2_{53}}{\sqrt{6^2 2^2}} \sqrt{\frac{2_{53}}{364}} \sqrt{\frac{2}{40}}$$

$$d(B,C) \sqrt{\frac{2-3}{3}} \frac{2-15-5}{2}$$

$$\sqrt[3]{\frac{2}{2}-20} \sqrt{\frac{2}{2}} 25400$$

$$425 517$$

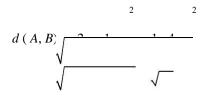
$$\sqrt[2]{\frac{2}{2}-8^2} d(A,C) \sqrt{20} 15-7\sqrt{1}$$

$$2^2-8^2 682 17$$

Because d(A, B) d(A, C) d(B, C) or 3 2 51 he points are collinear.

Label the points A(-1, 4), B(-2, -1), and

C(1, 14). Apply the distance formula to each pair of points.



$$d(B,C)\sqrt{1--2} \qquad 14--1$$

$$\sqrt[2]{2 \quad 15^2} \qquad \sqrt{234} \quad 3\cancel{2}6$$

$$2 \qquad 2$$

$$d(A,C) \qquad \sqrt{1-1-14-4} \qquad \sqrt{2}$$

$$2^{2} \quad 10^{2} \qquad \sqrt{104} \quad 2 \quad 26$$

Because $\sqrt{26}$ 2 3 2 he points are collinear.

Label the points A(0, 9), B(-3, -7), and C(2, 19).

$$d(A, B) \sqrt{-3 - 0)^{2} (-7 - 9)^{2}}$$

$$\sqrt{-3)^{2} (-16)^{2}} \sqrt{9 \cdot 256}$$

$$265 \quad 16.279$$

$$d(B,C) \sqrt{\frac{2-3}{\sqrt{19-7}}} \sqrt{\frac{2}{\sqrt{5^2 26^2}}} \sqrt{\frac{25676}{\sqrt{701} 26.476}}$$

$$d(A,C) \sqrt{\frac{2-0^2 19-9^2}{\sqrt{10^2}}} \sqrt{4100}$$

$$10.198$$

Because d(A, B) d(A, C) d(B, C)

or
$$\sqrt{265}$$
 $\sqrt{04}$ $70\sqrt{1}$

$$d(A,C) \sqrt{\frac{1--1}{2} - 11 - 3} \sqrt{\frac{1--1}{2} - 11 - 3} \sqrt{\frac{1}{2} - 8^2} \sqrt{\frac{464}{464}}$$

68 8.2462

Because d(A, B) + d(A, C) d(B, C)

or
$$\sqrt{241}$$
 $\sqrt{565}$

15.5242 8.2462 23.7697 23.7704 23.7697,

the three given points are not collinear. (Note,

however, that these points are very close to lying on a straight line and may appear to lie on a straight line when graphed.)

Label the points A(-7, 4), B(6,-2), and C(-1,1).

$$d(B,C) = \begin{cases} 205 & 14.3178 \\ \sqrt{16} & 2 & 2 \\ \sqrt{16} & 1 - 2 \\ \sqrt{16} & 2 & 2 \end{cases}$$

58 7.6158
$$d(A, C)\sqrt{1 - -7} \qquad 14$$

$$\sqrt{6^2 - 3^2} \qquad \sqrt{369}$$

$$\sqrt{56^2 - 3^2} \qquad \sqrt{369}$$

$$\sqrt{56^2 - 3^2} \qquad \sqrt{369}$$
Because $d(B, C) + d(A, C) \ d(A, B)$ or

58 45 205

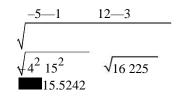
7.6158 6.7082 14.3178 14.3240 14.3178,

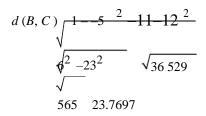
16.279 10.198 26.476, **32.** Label the points A(-1, -3), B(-5, 12), and 26.477 26.476, C(1, -11). the three given points are not collinear (Note 17) Pearson Education, Inc.

however, that these points are very close to lying on a straight line and may appear to lie on a straight line when graphed.)

the three given points are not collinear. (Note, however, that these points are very close to lying on a straight line and may appear to lie on a straight line when graphed.)

d(A, B)





Label the given points A(-4, 3), B(2, 5), and C(-1, 4). Find the distance between each pair of points.

$$\sqrt{\frac{2}{4(A,B)}} \sqrt{\frac{2}{2-4}} \sqrt{\frac{2}{2}} \sqrt{\frac{2-2}{2}}$$

$$d(A,B) 2--4 53 62$$

$$d(B,C) \sqrt{\frac{(12)^2 (45)^2}{\sqrt{2} \sqrt{2} \sqrt{\sqrt{100}}}} \sqrt{\frac{100}{2}}$$
3 (-1) 91 10

$$d(A,C) \sqrt{\frac{1-4}{\sqrt{2}} + \frac{4}{2} 3} \sqrt{\frac{3}{2} + \frac{1}{2} 10}$$
3 1 91 10

Because d(B, C) d(A, C) d(A, B) or $\sqrt{10} \sqrt{10} 2 10$, the points are collinear.

Chapter 2 Graphs and Functions Midpoint (5, 8), endpoint (13, 10)

The other endpoint has coordinates (-3, 6). Midpoint (-7, 6), endpoint (-9, 9)

$$\frac{-9x}{-7} - 7 \quad \text{and} \qquad \frac{9y}{6} = 6$$

$$\frac{2}{-9x - 14} \quad \text{and} \qquad 9y = 12$$

$$x - 5 \quad \text{and} \qquad y = 3.$$

The other endpoint has coordinates (-5, 3). Midpoint (12, 6), endpoint (19, 16)

The other endpoint has coordinates (5, -4).

Midpoint (-9, 8), endpoint (-16, 9)

$$\frac{-16 x}{-9}$$
 and $\frac{9 y}{8}$ 8
 $\frac{2}{-16 x - 18}$ and $\frac{2}{9 y 16}$
 $x - 2$ and $y 7$

The other endpoint has coordinates (-2, 7). Midpoint (a, b), endpoint (p, q)

The other endpoint has

coordinates (2a p, 2b q).

The endpoints are (2006, 7505)

and (2012, 3335)

$$\frac{2006\ 2012}{22}\ , \frac{7505\ 3335}{22}$$

2009, 5420

According to the model, the average national advertising revenue in 2009 was \$5420 million. This is higher than the actual value of

\$4424 million.

The points to use are (2011, 23021) and (2013, 23834). Their midpoint is

In 2012, the poverty level cutoff was approximately \$23,428.

(a) To estimate the enrollment for 2003,

use the points (2000, 11,753) and (2006, 13,180)

The enrollment for 2003 was about 12,466.5 thousand.

To estimate the enrollment for 2009, use the points (2006, 13,180) and (2012, 14,880)

2009, 14030

The enrollment for 2009 was about 14,030 thousand.

The midpoint M has

$$\frac{}{} x x y y$$
coordinates 1 2,2 1 2.2

Midpoint 6a, 6b, endpoint 3a, 5b

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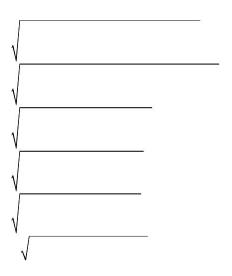
The other endpoint has coordinates (9a, 7b).

The endpoints of the segment are (1990, 21.3) and (2012, 30.1).

$$M = \frac{1990\ 2012}{2}, \frac{21.3\ 30.9}{2}$$

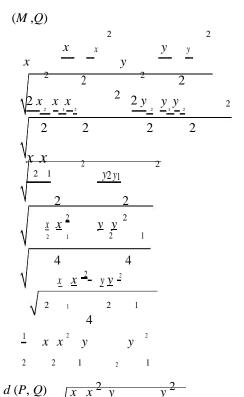
2001, 26.1

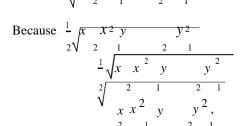
The estimate is 26.1%. This is very close to the actual figure of 26.2%.



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(continued)





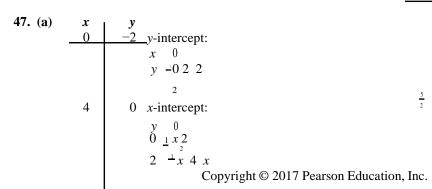
this shows d(P, M)d(M, Q) d(P, Q) and d(P, M) d(M, Q).

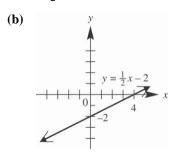
The distance formula,

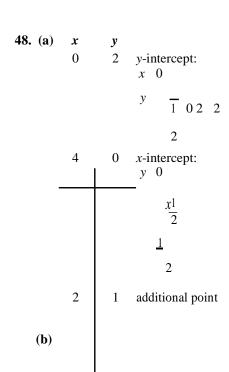
$$d = \sqrt{x_2 - x_1} \quad (y_2 - y_1), \quad \text{can be written}$$

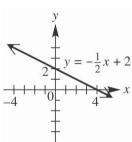
as
$$d [(x_2-x_1) (y_2-y_1)]$$
.

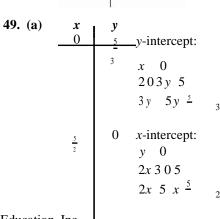
In exercises 47-58, other ordered pairs are possible.

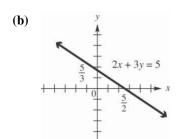










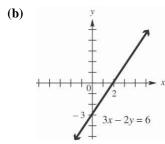


Chapter 2 Graphs and Functions

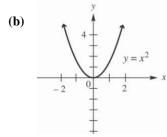
Chapter 2 Graphs and Function		
50. (a)	x	у
	0	−3 y-intercept:
		<i>x</i> 0
		302y6
		2 y 6 y 3
	2	0 <i>x</i> -intercept:
		y 0
		3 <i>x</i> 2 0 6
		3r 6 r 2

3x 6 x 2

3 additional point



51. (a) $\begin{array}{c|cccc} x & y & \\ \hline 0 & 0 & x \text{- and } y \text{-intercept:} \\ & 0 & 0^2 \\ \hline 1 & 1 & \text{additional point} \\ \hline -2 & 4 & \text{additional point} \\ \end{array}$

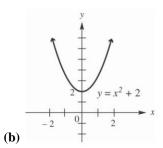


52. (a) $\begin{array}{c|cccc} x & y \\ \hline 0 & 2 & y\text{-intercept:} \\ & & x & 0 \\ & & y & 0^2 & 2 \\ & & y & 0 & 2 & y & 2 \\ \hline -1 & 3 & additional point \\ 2 & 6 & additional point \\ \end{array}$

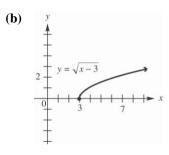
no x-intercept:

$$y \ 0 \ 0 \ x^2 \ 2$$

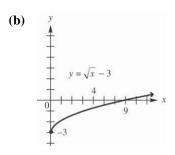
 $2 \ x^2 \ 2 \ x \sqrt{}$

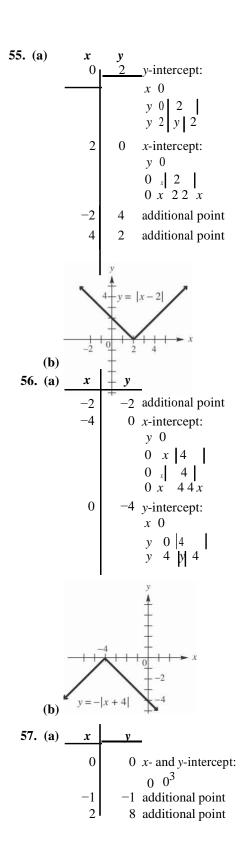


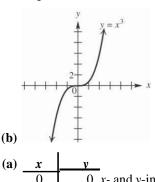
no y-intercept: $x \ 0 \ y \qquad \sqrt{0 \ 3 \ y} \ 3 \qquad \sqrt{}$

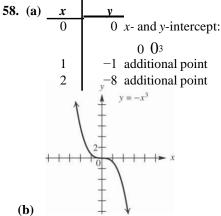


54. (a) $\begin{array}{c|cccc} x & y & \\ \hline 0 & -3 & y\text{-intercept:} \\ & & \sqrt{y} & 0 & 3 \\ & & \sqrt{y} & 0 & 3 \\ & & y & 0 & 3 & y & 3 \\ \hline 4 & -1 & additional point \\ & 0 & x\text{-intercept:} & y \\ & & 0 & \\ & & \sqrt{y} & 0 & 3 & \\ & & 0 & x & 3 & \\ & & 3 & \sqrt{y} & x & \\ \hline \end{array}$









Points on the *x*-axis have *y*-coordinates equal to 0. The point on the x-axis will have the same x-coordinate as point (4, 3). Therefore, the line will intersect the x-axis at (4, 0).

Points on the y-axis have x-coordinates equal to 0. The point on the y-axis will have the same y-coordinate as point (4, 3). Therefore, the line will intersect the y-axis at (0, 3).

Because (a, b) is in the second quadrant, a is negative and b is positive. Therefore, (a, -b) will have a negative x-coordinate and a negative y-coordinate and will lie in quadrant III.

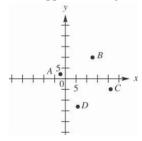
(-a, b) will have a positive *x*-coordinate and a positive *y*-coordinate and will lie in quadrant I. (-a, -b) will have a positive *x*-coordinate and a negative *y*-coordinate and will lie in quadrant IV.

(b, a) will have a positive *x*-coordinate and a negative *y*-coordinate and will lie in quadrant IV.

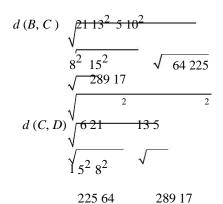
Chapter 2 Graphs and Functions

62. Label the points A(2, 2), B(13,10),

C (21, 5), and D(6, 13). To determine which points form sides of the quadrilateral (as opposed to diagonals), plot the points.



Use the distance formula to find the length of each side.

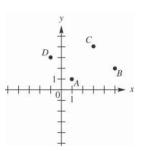


 $d(D,A) = \sqrt[2]{\frac{2}{6} - \frac{2}{2}} 13$ $\sqrt[8^2]{15^2}$ $64 \ 225 = \sqrt{289} \ 17$

Because all sides have equal length, the four points form a rhombus.

To determine which points form sides of the

quadrilateral (as opposed to diagonals), plot the points.



$$d(B,C) = 3 \cdot 5^{2} \cdot 4 \cdot 2^{2}$$

$$\sqrt{22^{2}} \qquad \sqrt{44} \quad 8\sqrt{4^{2} \cdot 1^{2}}$$

$$\sqrt{4^{2} \cdot 1^{2}} \qquad \sqrt{161} \qquad 17$$

$$d(D,A) \sqrt{\frac{161}{11}} \qquad 13$$

$$\sqrt{2^{2}} \qquad \sqrt{2^{2} \cdot 44} \qquad 8\sqrt{2^{2}}$$

Because d(A, B) = d(C, D) and d(B, C) = d(D, A), the points are the vertices of a parallelogram. Because $d(A, B) \neq d(B, C)$, the points are not the vertices of a rhombus.

For the points A(4, 5) and D(10, 14), the difference of the x-coordinates is 10 - 4 = 6 and the difference of the

y-coordinates is 14 - 5 = 9. Dividing these differences by 3, we obtain 2 and 3,

respectively. Adding 2 and 3 to the x and y coordinates of point A, respectively, we obtain B(4+2, 5+3) or B(6, 8). Adding 2 and 3 to the x- and y- coordinates of

point B, respectively, we obtain

C(6+2, 8+3) or C(8, 11). The desired points are B(6, 8) and C(8, 11).

We check these by showing that

$$d(A, B) = d(B, C) = d(C, D)$$
 and that

$$d(A, D) = d(A, B) + d(B, C) + d(C, D).$$

$$d(A, B) = \sqrt{64} + 8\sqrt{5} - \sqrt{2}$$

$$\sqrt{2} + \sqrt{2} + \sqrt{2}$$

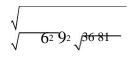
$$\sqrt{2} + \sqrt{3} + \sqrt{49} + \sqrt{13}$$

$$d(B, C) = 86^{2} + 118^{2}$$

$$2^2 \ 3^2$$
 4 9 13

$$d(C,D) = \sqrt{\frac{10.8^2 \cdot 14.11^2}{\sqrt{2^2} \cdot \sqrt{3^2 \cdot 49}}} \sqrt{\frac{10.8^2 \cdot 14.11^2}{\sqrt{3^2 \cdot 49}}}} \sqrt{\frac{10.8^2 \cdot 14.11^2$$

$$d(A, D) 104^2 145^2$$



 $\sqrt{117}\sqrt{9(13)}$ 3 $\sqrt{8}$ d(A, B), d(B, C), and d(C, D) all have the same measure and d(A, D) = d(A, B) + d C + d(C, D) Because $\sqrt{8}$ 13 13 13.

Use the distance formula to find the length of each side.

$$d(A, B) \int_{\sqrt{2}1^2}^{51^2 21^2} \sqrt{161} 1\sqrt{1}$$

Section 2.2 Circles

The circle with equation $x^2 y^2$ 49 has center with coordinates (0, 0) and radius equal to 7.

The circle with center (3, 6) and radius 4 has equation $x 3^2 y 6 16$.

The graph of $x 4^2 y 7^2 9$ has center with

coordinates (4, -7).

The graph of x^2 y 5^2 9 has center with

coordinates (0, 5).

This circle has center (3, 2) and radius 5. This is graph B.

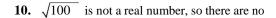
This circle has center (3, -2) and radius 5. This is graph C.

This circle has center (-3, 2) and radius 5. This is graph D.

This circle has center (-3, -2) and radius 5. This is graph A.

The graph of x^2 y^2 0 has center (0, 0) and radius 0. This is the point (0, 0). Therefore,

there is one point on the graph.

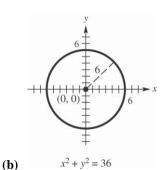


points on the graph of x^2 y^2 100.

(a) Center (0, 0), radius 6

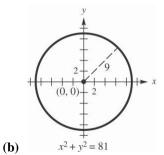
$$\sqrt{0^2 y 0^2 6}$$

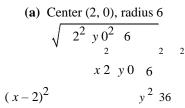
 $0^2 y 0^2 6^2 x^2 y^2 36$

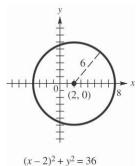


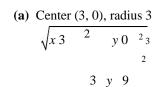
(a) Center (0, 0), radius 9

$$\sqrt{\begin{array}{cccc}
0^2 & y & 0^2 & 9 \\
0^2 & y & 0^2 & 9^2 & x^2 & y^2 & 81
\end{array}}$$

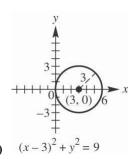


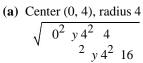


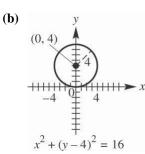




(b)

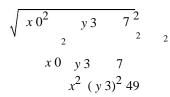


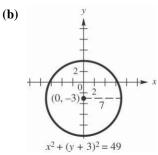




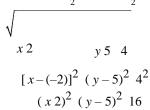
Chapter 2 Graphs and Functions

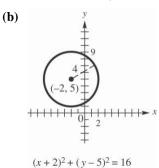
16. (a) Center (0, -3), radius 7



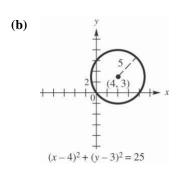


17. (a) Center (-2, 5), radius 4

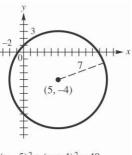




18. (a) Center (4, 3), radius 5 $\sqrt{x} \frac{4^2 y 3^2 5}{4^2 y 3^2 5^2}$ $4^2 y 3^2 25$



(b)

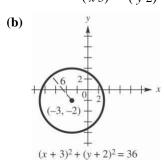


 $(x-5)^2 + (y+4)^2 = 49$

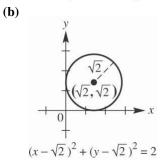
20. (a) Center (-3, -2), radius 6

$$\sqrt{x 3^2 y 2 6}_2$$

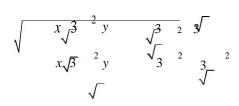
 $x 3 y 2 6 2$
 $(x 3)^2 (y 2)^2 36$



21. (a) Center $2\sqrt{2}$, radius \sqrt{x} $\sqrt{x} \frac{2^2 y}{\sqrt{2}^2 y} \frac{2^2}{\sqrt{2}^2 2}$



22. (a) Center $\sqrt[3]{}$, radius $\sqrt{3}$

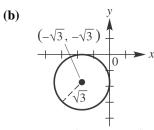


$$\sqrt{x \, 5^2} \qquad y \, 4 \qquad 7^2$$

$$(x-5)^2 \left[y - (-4) \right]^2 \, 7^2$$

$$(x-5)^2 \left(y \, 4 \right)^2 \, 49$$

$$x = 3^2 y \qquad \mathcal{F}^2 3$$



- $(x + \sqrt{3})^2 + (y + \sqrt{3})^2 = 3$
- (a) The center of the circle is located at the midpoint of the diameter determined by the points (1, 1) and (5, 1). Using the midpoint formula, we have

$$C = \frac{15}{1}, \frac{11}{1}$$
 3,1. The radius is

2 2

one-half the length of the diameter:

$$r^{\frac{1}{\sqrt{5}}\sqrt{5}} 1^2 11^2 2$$

2

The equation of the circle is

$$x 3^{2} y 1^{2} 4$$

Expand $x 3^2 y 1^2 4$ to find the

equation of the circle in general form:

$$x 3^{2} y 1^{2} 4$$

 $x^{2} 6x 9 y^{2} 2 y 1 4$
 $x^{2} y^{2} 6x 2 y 6 0$

(a) The center of the circle is located at the midpoint of the diameter determined by

the points (-1, 1) and (-1, -5). Using the midpoint formula, we have

$$C = \frac{1(1)}{1}, \frac{1(5)}{1}, \frac{1}{2}$$

2

The radius is one-half the length of the diameter:

$$r$$
 $\frac{1}{\sqrt{11}}$ $\frac{2}{513}$

The equation of the circle is $x 1^2 v 2^2 9$

(b) Expand $x 1^2$ $y 2^2$ 9 to find the equation

(a) The center of the circle is located at the midpoint of the diameter determined by the points (-2, 4) and (-2, 0). Using the midpoint formula, we have

$$C = \frac{2(2)}{2}, \frac{40}{2}, \frac{2}{2}$$

The radius is one-half the length of the diameter:

$$r = \frac{1}{2}\sqrt{22}$$

The equation of the circle is $2^2 \text{ y } 2^2 \text{ 4}$

Expand
$$x 2^2 y 2^2 4$$
 to find the

equation of the circle in general form:

$$x^2$$
 y^2 4x 4 y 4 0

(a) The center of the circle is located at the midpoint of the diameter determined by the points (0, -3) and (6, -3). Using the midpoint formula, we have

$$06 3(3)$$
 $C 2' 2 3,3.$

The radius is one-half the length of the diameter:

$$r \frac{1}{2} \sqrt{60^2 \ 3 \ 3^2 \ 3}$$

The equation of the circle is $x \cdot 3 + y \cdot 3 = 9$

Expand $x 3^2 y 3^2 9$ to find the equation of the circle in general form:

of the circle in general form: Copyright © 2017 Pearson Education, Inc.

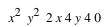
 x^{2} y^{2} 6 x 8 y 9 0 $x^2 6 x 9 y^2 8 y 16 -9 9 16_2$ Co m ple te the squa re on \boldsymbol{x} an d y se pa rat ely x

x 2

6 x

y 2

8 y



Yes, it is a circle. The circle has its center at (-3, -4) and radius 4.

Chapter 2 Graphs and Functions

$$x^2$$
 y^2 $8x - 6y$ 160
Complete the square on x and y separately.

$$x^2 8x y^2 - 6y 16$$

$$x^2$$
 8x 16 y^2 - 6 y 9 - 16 16 9

$$4^2 v - 3^2 9$$

Yes, it is a circle. The circle has its center at (-4, 3) and radius 3.

$$x^2$$
 y^2 4 x 12 y 4

 x^2 y^2 4 x 12 y 4 Complete the square on x and y separately.

$$x^2 - 4x y^2 12y - 4$$

 $x^2 - 4x 4 y^2 12y 36 - 4436$

$$x-2^{2}$$
 y 6^{2} 36

Yes, it is a circle. The circle has its center at

$$x^2$$
 $y^2 - 12 \times 10 \text{ y} - 25$

(2, -6) and radius 6. x^2 $y^2 - 12 \times 10 \times y - 25$ Complete the square on x and y separately.

$$x^2 - 12x y^2 10 y - 25$$

$$x^2 - 12 \times 36 \text{ y}^2 10 \text{ y} 25$$

$$-25\ 36\ 25$$
$$x - 6^2 y\ 5^2\ 36$$

Yes, it is a circle. The circle has its center at (6, -5) and radius 6.

$$4x^2$$
 $4x^2$ $4x - 16x - 190$

Complete the square on x and y separately.

$$4 x^{2} x^{\frac{1}{4}} 4 y^{\frac{2}{4}} - 4 y 4$$

$$4x^{\frac{1}{2}}$$
 $4y-2^{2}36$

$$x = \frac{1}{2} y - 2^2 = 9$$

Yes, it is a circle with center $\frac{1}{2}$, 2 and

radius 3.

$$9x^{\frac{2}{2}}9y-1^{2}$$
 36
 $\frac{2}{2}$ 2 2 2
 x^{3} $y-1$ 4 3

Yes, it is a circle with center $\frac{2}{3}$, 1 and

radius 2.

$$x^2$$
 y^2 2 $x - 6$ y 14 0

Complete the square on x and y separately.

$$x^2 2x y^2 - 6y - 14$$

$$x^{2}$$
 2 x 1 y 2 - 6 y 9 - 14 1 9
x 1 y - 3 - 4

The graph is nonexistent.

$$x^2$$
 y^2 4 $x - 8$ y 32 0

Complete the square on x and y separately.

$$x^{2} + 4x + y^{2} - 8y - 32$$
 $x^{2} + 4x + 4y^{2} - 8y + 16$
 $-32 + 416$
 $x + 2 + y - 4 + -11$

The graph is nonexistent.

$$x^2$$
 y^2 6x 6 y 18 0

 x^2 y^2 6x 6 y 18 0 Complete the square on x and y separately.

The graph is the point (3, 3).

$$x^2$$
 y^2 4 x 4 y 8 0

Complete the square on x and y separately.

$$x^2 + 4x + y^2 + 4y + 8$$

The graph is the point (-2, -2).

37.
$$9x^2$$
 $9y^2$ $6x6y230$

32.
$$9x^2$$
 $9y^2$ $12x - 18y - 230$

Complete the square on x and y separately. $9 x^2 6x 9 y^2 6y 23$

Complete the square on x and y separately.

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$$9x^{2} \stackrel{4}{=} x_{3} 9y^{2} - 2y 23$$

$$9x^{2} \stackrel{4}{=} x_{3} \stackrel{4}{=} 9y^{2} - 2y 1$$

$$239^{\frac{4}{=}} 91$$

$$y^{2} = x \quad 9 \quad y^{2} = y \quad 23$$

$$x^{2} = x \quad y^{2} \quad y^{2} = y \quad 23$$

$$x^{2} = x \quad y^{2} \quad y^{2} = y \quad y^{2} = y$$

$$4x^2 4y^2 4x4y7 0$$

Complete the square on *x* and *y* separately.

$$4x^{2} x 4y^{2} y 7$$

$$4x^{2} x 1 4y^{2} - y 1$$

$$4x^{2} x 1 4y^{2} - y 1$$

$$4x^{2} x 1 4y^{2} - y 1$$

$$4x^{2} x 1 4y - 12 9$$

$$x 1^{2} y - 12 2$$

$$x 1 4y - 12 2$$

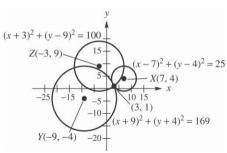
Yes, it is a circle with center $\frac{1}{2}$, $\frac{4}{2}$ and

radius
$$\frac{3}{2}$$
.

The equations of the three circles are $(x7)^2 (y4)^2 25$,

$$(x9)^2 (y4)^2$$
 169, and

 $(x \ 3)^2 (y \ 9)^2 \ 100$. From the graph of the three circles, it appears that the epicenter is located at (3, 1).



Check algebraically:

$$(x7)^{2} (y4)^{2} 25 (3$$

 $7)^{2} (14)^{2} 25$
 $4^{2} 3^{2} 25 25 25$
 $(x9)^{2} (y4)^{2} 169$

$$(3 9)^2 (1 4)^2 169$$

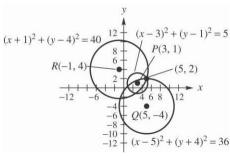
 $12^2 5^2 169 169 169$

$$(x3)^2 (y9)^2 100$$

 $(33)^2 (19)^2 100$
 $6^2 (8)^2 100 100 100$

(3, 1) satisfies all three equations, so the

epicenter is at (3, 1).



Check algebraically:

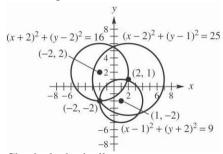
$$(x3)^{2}(y1)^{2} 5$$

(53) $(21) 5$

$$(x 1)^2 (y 4)^2 40 (5$$

 $1)^2 (2 4)^2 40$
 $6^2 (2)^2 40 40 40$
(5, 2) satisfies all three equations, so the epicenter is at (5, 2).

From the graph of the three circles, it appears that the epicenter is located at (-2, -2).



Check algebraically:

$$(x 2) (y 1) 25$$

$$(2 2) {}_{2} (2 1)^{2} 25$$

$$(4) (3) 25$$

$$25 25$$

$$(x 2) (y 2) 16$$

$$(2\ 2)^2\ (2\ 2)^2\ 16$$
 $0\ (4)$
 16

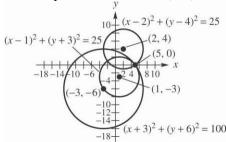
The three equations are $(x \ 3)^2 (y \ 1)^2 \ 5$, $(x \ 5)_2 (y \ 4)_2 \ 36$, and Copyright © 2017 Pearson Education, Inc.

 $(x \, 1)^2 \, (y \, 4)^2 \, 40$. From the graph of the three circles, it appears that the epicenter is located at (5, 2).

16
$$(x \, 1)^2 (y \, 2)^2 \, 9 (2$$
 $1)^2 (2 \, 2)^2 \, 9 (3)^2 \, 0^2 \, 9$
 $9 \, 9$
 $(-2, -2)$ satisfies all three equations, so the epicenter is at $(-2, -2)$.

Chapter 2 Graphs and Functions

From the graph of the three circles, it appears that the epicenter is located at (5, 0).



Check algebraically:

$$(x2)^{2} (y4)^{2}$$
25 (5
2)² (04)²
25
3² (4)²
25
25
(x1)² (y3)² 25

$$(51)^2 (03)^2 25$$

 $4^2 3^2 25$

25
$$(x 3)^{2} (y 6)^{2} 100$$

$$(5 3)^{2} (0 6)^{2} 100$$

$$8^{2} 6^{2} 100$$

$$100 100$$
(5, 0) satisfies all three equations, so the

epicenter is at (5, 0).

The radius of this circle is the distance from the center C(3, 2) to the *x*-axis. This distance

is 2, so
$$r = 2$$
.
 $(x-3)^2 (y-2)^2 2^2$
 $(x-3)^2 (y-2)^2 4$

The radius is the distance from the center C(-4, 3) to the point P(5, 8).

$$[5-(-4)]^2 (8-3)^2$$

$$9^{2} 5^{2} \sqrt{106}$$

The equation of the circle is

$$[x - (-4)]^{2} (y - 3)^{2}$$

$$(x4)^{2} (y - 3)^{3} 106$$

$$\begin{array}{r}
 1 x^2 3 x^2 16 \\
 1 2x x^2 9 6 x x^2 16 \\
 2 x^2 8x 10 16 \\
 2 x^2 8x 6 0 \\
 x^2 4 x 3 0
 \end{array}$$

To solve this equation, we can use the quadratic formula with a = 1, b = -4, and = -3.

Because x = y, the points are

Let P(-2, 3) be a point which is 8 units from Q(x, y). We have

$$d(P,\sqrt{Q})2x^{2} = 3y^{2} = 8$$

$$2x^{2} + 3y^{2} = 64.$$
Because $x + y = 0$, $x = -y$. We can either

for x. Substituting

because x + y = 0, x = -y. We can either

for y we solve the following:
$$2 x^2$$
 $3 x$ $_2 64$

substitute x for y or y

To solve this equation, use the quadratic formula with a = 2, b = 10, and c = -51.

$$10\sqrt{10^242}$$
 51

 $\begin{array}{c|c}
2 \\
\underline{10\ 100\ 408} \\
4 \\
\text{n, Inc 10.}
\end{array}$

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x

Label the points
$$P(x, y)$$
 and $Q(1, 3)$.
If $d(P, Q) = 4$, $\sqrt[4]{x^2 + 3y^2 + 4}$

$$1 x^2 3 y^2$$
 16.
If $x = y$, then we can either substitute x for y or y for x. Substituting x for y we solve the following:

Because
$$y x$$
 the points are

$$\frac{5127\sqrt{5127}}{2}$$
 and $\frac{-512}{2}, \frac{127}{2}, \frac{1}{2}$

Let P(x, y) be a point whose distance from A(1,0) is 100 and whose distance from B(5, 4) is $\sqrt[4]{n} \cdot d(P, A) = 10\sqrt{\text{so}}$

$$\sqrt{(1 x)^2 (0 y)^2} \sqrt{10}$$

$$(1 x)^2 y^2 10. d(P, B) \sqrt{0}, \text{ so}$$

$$\sqrt{(5 x) (4 y)} \sqrt{10}$$

$$(5 x)^2 (4 y)^2 10. \text{ Thus,}$$

$$(1 x)^2 y^2 (5 x)^2 (4 y)^2$$

$$1 2x x^{2} y^{2}$$

$$25 10 x x^{2} 16 8 y y^{2}$$

$$1 2x 41 10x 8 y$$

Substitute 5 - x for y in the equation $(1 x)^2 y^2$ 10 and solve for x.

$$(1 x)^2 (5 x)^2 10$$

 $1 2x x^2 25 10x x^2 10$
 $2x^2 12 x 26 10 2 x^2 12x 16 0$
 $x^2 6x 80 (x 2)(x 4) 0$
 $x 2 0 \text{ or } x 4 0$

To find the corresponding values of y use the equation y = 5 - x. If x = 2, then y = 5 - 2 = 3.

If
$$x = 4$$
, then $y = 5 - 4 = 1$. The points satisfying the conditions are $(2, 3)$ and $(4, 1)$.

The circle of smallest radius that contains the

points A(1, 4) and B(-3, 2) within or on its boundary will be the circle having points A and B as endpoints of a diameter. The center will be M, the midpoint:

The radius will be the distance from M to either *A* or *B*:

$$d(M, A) [1(1)]^2 (43)_2$$

Label the points A(3, y) and B(-2, 9). If d(A, B) = 12, then

$$\sqrt{2 \, 3^2 \, 9 \, y^2 \, 12}$$

$$\sqrt{5^2 \, 9 \, y^2 \, 12}$$

$$5^2 \, 9 \, y^2 \, 12^2$$

$$y^2$$
 18 y 38 0

 y^2 18 y 38 0 Solve this equation by using the quadratic formula with a = 1, $\vec{b} = -18$, and $\vec{c} = -38$:

The values of y are 9
$$\sqrt{119}$$
 and 9 $\sqrt{119}$.

Because the center is in the third quadrant, the radius is $2\sqrt{a}$ and the circle is tangent to both

axes, the center must be at
$$(2, 2)$$
.

Using the center-radius of the equation of a circle, we have $\sqrt{}$

Let P(x, y) be the point on the circle whose distance from the origin is the shortest. Complete the square on x and y separately to write the equation in center-radius form:

$$x 16x y 14 y 88 0$$

 $x^2 16 x 64 y^2 14 y 49$

$$\begin{array}{c}
88 \ 64 \ 49 \\
(x \ 8)^2 \ (y \ 7)^2 \ 25 \\
\text{Sol}_{2}^{14} \xrightarrow{\text{the celiter is}} (8,47) \ \text{and the radius is 5.}
\end{array}$$

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$$\sqrt[4]{\frac{\sqrt{2^21^2}}{\sqrt{41}}} \sqrt{41} \sqrt{5}$$

The equation of the circle is

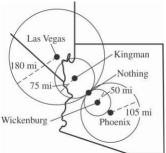
$$x = 1$$
 $2 \times 3^2 \times 5^2$

$$x 1^2 y 3^2 = 5$$
.

Chapter 2 Graphs and Functions

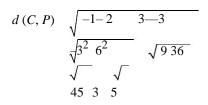
Using compasses, draw circles centered at Wickenburg, Kingman, Phoenix, and Las Vegas with scaled radii of 50, 75, 105, and 180 miles respectively. The four circles should

intersect at the location of Nothing.



The midpoint *M* has coordinates

Use points C(2, -3) and P(-1, 3).





The radius is 3 **55.** Use points C(2, -3) and Q(5, -9).

The radius is 3



56. Use the points P(-1, 3) and Q(5, -9).

Because
$$d(P, Q) \sqrt{5-1}^2 -9-3^2$$

$$\sqrt{2 -12^2} \sqrt{36144} = 180$$

Label the endpoints of the diameter P(3, -5) and Q(-7, 3). The midpoint M of the segment joining P and Q has coordinates

$$2$$
 , 2 2 , 2 $(-2, -1)$.

The center is C(-2, -1). To find the radius, we can use points C(-2, -1) and P(3, -5)

$$\frac{d(C, P) \sqrt{3 - 2^{2} - 5 - 1}}{\sqrt{5^{2} - 4^{2} \sqrt{2516}}} = 4\sqrt{-5}$$

We could also use points C(-2, -1).and Q(-7, 3).

$$d(C,Q) \sqrt{7--2} \qquad 2 3-1 \qquad 2 \\ \sqrt{5^2 4^2} \qquad \sqrt{25 \ 16} \quad \sqrt{41}$$

We could also use points P(3, -5) and

Q(-7, 3) to find the length of the diameter. The

length of the radius is one-half the length of the diameter.

$$d(P,Q) \sqrt{\int_{Q} \sqrt{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q} \sqrt{\int_{Q}$$

The center-radius form of the equation of the circle is

$$[x-(-2)]^2 [y-(-1)]^2$$
 ($x^2 = (x^2)^2 (y^2)^2 = (x^2)^2$

59. Label the endpoints of the diameter P(-1,2) and Q(11,7). The midpoint M of the segment joining P and Q has coordinates

$$\frac{1}{2} \frac{11}{2} \frac{27}{2} \frac{9}{2} = 5,$$

The center is C 5, 2 . To find the radius, we Copyright © 2017 Pearson Education, Inc. $\frac{1}{2}$

f, the radius is
$$\frac{1}{2} d(P, Q)$$
. Thus 2
$$\frac{1}{r} = 6.5 \text{ } 5. \text{ } \sqrt{}$$

The center-radius form for this circle is (
$$(x-2)^2 (y 3)^2 (3 5)^2 \sqrt{ }$$
$$(x-2)^2 (y 3)^2 45.$$

can use points C 5, $\frac{9}{-}$ and P(-1, 2).

$$d(C, P) = \sqrt{\begin{array}{ccccc} 5 - 1 & 2 & 2 & 2 \\ \sqrt{} & - & 2 & 2 & 2 \\ 6 & & & 6 & & \\ \end{array}}$$

$$d(C, Q) \sqrt{5 \cdot 11^{2} \cdot \frac{9}{2} - 7^{2}} \sqrt{\frac{6^{2} \cdot 5^{2}}{13}}$$

(continued on next page)

(continued)

Using the points P and Q to find the length of the diameter, we have

$$dP, Q \sqrt{111^2 27^2} \sqrt{\frac{12^2}{16913}} 5^2$$

$$dP, Q = \frac{1}{13} \frac{13}{13}$$

The center-radius form of the equation of the circle is

$$x 5^2 y^{\frac{9}{2}} 2^{\frac{13}{2}} 2$$
 $x 5^2 y^{\frac{9}{2}} 2^{\frac{169}{2}}$

60. Label the endpoints of the diameter P(5, 4) and Q(-3, -2). The midpoint M of the segment joining P and Q has coordinates 5(3), 4(2) 1,1.

The center is C(1, 1). To find the radius, we can use points C(1, 1) and P(5, 4).

We could also use points C(1, 1) and Q(-3, -2).

$$d(C,Q)\sqrt{\frac{1}{3}} \frac{1-2}{\sqrt{4^23^2}} \frac{1-2}{\sqrt{25}}$$

Using the points P and Q to find the length of

the diameter, we have
$$\frac{2}{dP}$$
, $\frac{2}{\sqrt{8^26^2}}$ $\frac{42}{\sqrt{100}}$

$$\frac{1}{2} d(P, Q) = \frac{1}{2} 105$$

The length of the diameter PQ is

$$\sqrt{15^2 \, 41^2}$$
 $\sqrt{4^2 3^2}$ $\sqrt{25} \, 5.$

The length of the radius is $2^{\frac{1}{5}} \cdot 5^{\frac{5}{5}} \cdot 2$

The center-radius form of the equation of the circle is

$$x \ 3^2 \ y_{\underline{5}_2} \ \underline{5}_2$$

Label the endpoints of the diameter P(-3, 10) and Q(5, -5). The midpoint M of the segment joining P and Q has coordinates <u>35</u> <u>10(5)</u>

The center C is 1, 52. The length of the diameter PQ is

$$\sqrt{\frac{35^2 \cdot 105^2}{8^2 \cdot 15^2}}$$

$$\sqrt{-17}$$

The length of the radius is $\frac{21}{17}$ 17 $\frac{17}{17}$. 2 The center-radius form of the equation of the

circle is

$$x 1$$
 $y 2 2 4$

$$x 1^2 y^{\frac{1}{2}} = \frac{289}{}$$

Section 2.3 **Functions**

1. The domain of the relation

3, 5, 4, 9, 10, 13 is
$$3, 4, 10$$
.

- **2.** The range of the relation in Exercise 1 is <u>5, 9,</u>13.
- **3.** The equation y = 4x 6 defines a function with $x 1^2 v 1^2 5^2$

2 The center-radius form of the equation of the circle is Copyright © 2017 Pearson Education, Inc.

independent variable \underline{x} and dependent variable y.

$$x 1^2 y 1^2 25$$

Label the endpoints of the diameter P(1, 4) and Q(5, 1). The midpoint M of the

segment joining P and Q has coordinates

$$\frac{15}{5}$$
, $\frac{41}{5}$ 3, $\frac{5}{5}$.

The center is $C 3, \frac{5}{2}$.

The function in Exercise 3 includes the ordered pair (6, 18).

5. For the function fx + 4x = 2,

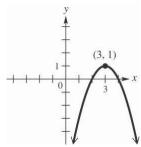
6. For the function gx x, g9 9 3.

7. The function in Exercise 6, gx x, has domain 0, .

Chapter 2 Graphs and Functions

8. The function in Exercise 6, g(x) x, has range $\underline{0}$.

For exercises 9 and 10, use this graph.



The largest open interval over which the function graphed here increases is , 3.

The largest open interval over which the function graphed here decreases is 3, .

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{5, 3, 4, 7\}$$
 x-values $\{1, 2, 9, 8\}$ *y*-values

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{8, 5, 9, 3\}$$
 x-values $\{0, 7, 3, 8\}$ *y*-values

Two ordered pairs, namely (2, 4) and (2, 6), have the same *x*-value paired with different *y*-values, so the relation is not a function.

Two ordered pairs, namely (9, -2) and (9, 1), have the same *x*-value paired with different *y*-values, so the relation is not a function.

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{-3, 4, -2\}$$
 x-values $\{1, 7\}$ *y*-values

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{-12, -10, 8\}$$
 x-values $\{5, 3\}$ *y*-values

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{3, 7, 10\}$$
 x-values $\{-4\}$ *y*-values

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{-4, 0, 4\}$$
 x-values $\{\sqrt{2}\}$ y-values

Two sets of ordered pairs, namely (1, 1) and (1, -1) as well as (2, 4) and (2, -4), have the same x-value paired with different y-values, so the relation is not a function.

domain: {0, 1, 2}; range: {-4, -1, 0, 1, 4}

The relation is not a function because the *x*-value 3 corresponds to two *y*-values, 7 and 9. This correspondence can be shown as follows.

$$\{2, 3, 5\}$$
 x-values $\{5, 7, 9, 11\}$ y-values domain: $\{2, 3, 5\}$; range: $\{5, 7, 9, 11\}$

The relation is a function because for each different *x*-value there is exactly one *y*-value.

domain: {2, 3, 5, 11, 17}; range: {1, 7, 20}

The relation is a function because for each different *x*-value there is exactly one *y*-value.

domain: {1, 2, 3, 5}; range: {10, 15, 19, 27}

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{0, -1, -2\}$$
 x-values \downarrow \downarrow \downarrow $\{0, 1, 2\}$ *y*-values

Domain: $\{0, -1, -2\}$; range: $\{0, 1, 2\}$

The relation is a function because for each different *x*-value there is exactly one *y*-value. This correspondence can be shown as follows.

$$\{0, 1, 2\}$$
 x-values $\downarrow \downarrow \downarrow \lbrace 0, -1, -2 \rbrace$ *y*-values

Domain: $\{0, 1, 2\}$; range: $\{0, -1, -2\}$ The

relation is a function because for each different year, there is exactly one number for visitors.

domain: {2010, 2011, 2012, 2013} range: {64.9, 63.0, 65.1, 63.5}

The relation is a function because for each basketball season, there is only one number for attendance. domain: {2011, 2012, 2013, 2014} range: {11,159,999, 11,210,832, 11,339,285, 11,181,735}

This graph represents a function. If you pass a vertical line through the graph, one *x*-value corresponds to only one *y*-value.

domain: , ; range: ,

This graph represents a function. If you pass a vertical line through the graph, one *x*-value corresponds to only one *y*-value.

domain:,; range:, 4

This graph does not represent a function. If you pass a vertical line through the graph, there are places where one value of *x* corresponds to two values of *y*.

domain: 3, ; range:,

This graph does not represent a function. If

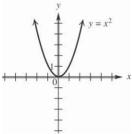
you pass a vertical line through the graph, there are places where one value of *x* corresponds to two values of *y*. domain: [-4, 4]; range: [-3, 3]

This graph represents a function. If you pass a vertical line through the graph, one *x*-value corresponds to only one *y*-value.

domain: , ; range: ,

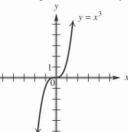
This graph represents a function. If you pass a vertical line through the graph, one *x*-value corresponds to only one *y*-value. domain: [–2, 2]; range: [0, 4]

 $y \ x^2$ represents a function because y is always found by squaring x. Thus, each value of x corresponds to just one value of y. x can be any real number. Because the square of any real number is not negative, the range would be zero or greater.



domain:,; range: 0,

 x^3 represents a function because y is always found by cubing x. Thus, each value of x corresponds to just one value of y. x can be any real number. Because the cube of any real number could be negative, positive, or zero, the range would be any real number.



domain:,; range:,

The ordered pairs (1, 1) and (1, -1) both

6
satisfy $x \ y$. This equation does not

represent a function. Because *x* is equal to the sixth power of *y*, the values of *x* are nonnegative. Any real number can be raised to the sixth power, so the range of the relation

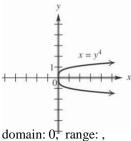
 $x = y^{6}$

is all real numbers.

domain: 0, range:,

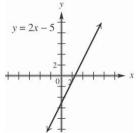
Chapter 2 Graphs and Functions The ordered pairs (1, 1) and (1, -1) both

satisfy x y^4 . This equation does not represent a function. Because x is equal to the fourth power of y, the values of x are nonnegative. Any real number can be raised to the fourth power, so the range of the relation is all real numbers.



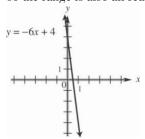
y 2x 5 represents a function because y is found by multiplying x by 2 and subtracting 5. Each value of x corresponds to just one value of y. x can be any real number, so the domain is all real numbers. Because y is twice x, less 5, y also may be any real number, and

x, less 5, y also may be any real numbers.



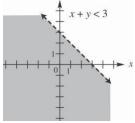
domain: , ; range: ,

6x 4 represents a function because y is found by multiplying x by -6 and adding 4. Each value of x corresponds to just one value of y. x can be any real number, so the domain is all real numbers. Because y is -6 times x, plus 4, y also may be any real number, and so the range is also all real numbers.



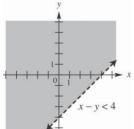
domain: , ; range: ,

By definition, y is a function of x if every value of x leads to exactly one value of y. Substituting a particular value of x, say 1, into x + y < 3 corresponds to many values of y. The ordered pairs (1, -2), (1, 1), (1, 0), (1, -1), and so on, all satisfy the inequality. Note that the points on the graphed line do not satisfy the inequality and only indicate the boundary of the solution set. This does not represent a function. Any number can be used for x or for y, so the domain and range of this relation are both all real numbers.



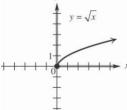
domain:,; range:,

By definition, y is a function of x if every value of x leads to exactly one value of y. Substituting a particular value of x, say 1, into x - y < 4 corresponds to many values of y. The ordered pairs (1, -1), (1, 0), (1, 1), (1, 2), and so on, all satisfy the inequality. Note that the points on the graphed line do not satisfy the inequality and only indicate the boundary of the solution set. This does not represent a function. Any number can be used for x or for y, so the domain and range of this relation are both all real numbers.



domain: , ; range: ,

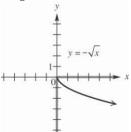
41. For any choice of x in the domain of y √, there is exactly one corresponding value of y, so this equation defines a function. Because the quantity under the square root cannot be negative, we have x 0. Because the radical is nonnegative, the range is also zero or greater.



domain: $0\downarrow$; range: 0,

For any choice of x in the domain of $x\sqrt{\text{there}}$ is exactly one corresponding

value of y, so this equation defines a function. Because the quantity under the square root cannot be negative, we have x 0. The outcome of the radical is nonnegative, when you change the sign (by multiplying by -1), the range becomes nonpositive. Thus the range is zero or less.

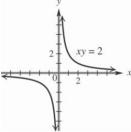


domain: 0, ; range: , 0

43. Because xy = 2 can be rewritten as $y = \frac{2}{x}$

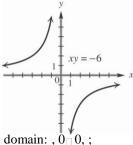
we can see that y can be found by dividing x into 2. This process produces one value of y

for each value of x in the domain, so this equation is a function. The domain includes all real numbers except those that make the denominator equal to zero, namely x = 0. Values of y can be negative or positive, but never zero. Therefore, the range will be all real numbers except zero.



domain: 0_0 , ; range: 0_0 ,

Because xy = -6 can be rewritten as $y \in x$ we can see that y can be found by dividing x into -6. This process produces one value of y for each value of x in the domain, so this equation is a function. The domain includes all real numbers except those that make the denominator equal to zero, namely x = 0. Values of y can be negative or positive, but never zero. Therefore, the range will be all real numbers except zero.



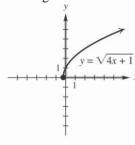
range:, 0 0,

For any choice of x in the domain of y 4x there is exactly one

corresponding value of *y*, so this equation defines a function. Because the quantity under

the square root cannot be negative, we have 4 x 1 0 4 x 1 x $\frac{1}{2}$. Because the radical is

nonnegative, the range is also zero or greater.



domain: 1, ;4_range: 0,

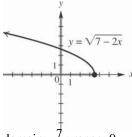
Chapter 2 Graphs and Functions

For any choice of x in the domain of

 $\sqrt{2x}$ there is exactly one corresponding value of y, so this equation defines a function. Because the quantity under the square root cannot be negative, we have

$$72 \times 02 \times 7 \times \frac{7}{}$$

Because the radical is nonnegative, the range is also zero or greater.



domain: $\frac{7}{}$; range: 0,

47. Given any value in the domain of $y = \frac{2}{x} 3$, we

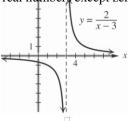
find *y* by subtracting 3, then dividing into 2. This process produces one value of *y* for each

value of *x* in the domain, so this equation is a function. The domain includes all real

numbers except those that make the denominator equal to zero, namely x = 3. Values of y can be negative or positive, but

never zero. Therefore, the range will be all

real numbers except zero.



domain:, 3 3,;

range: , 0 0,

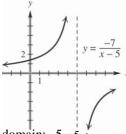
48. Given any value in the domain of

$$y_{-1}$$
, we

x 5

find y by subtracting 5, then dividing into -7. This process produces one value of y for each value of x in the domain, so this equation is a function. The domain includes all real numbers except those that make the denominator equal to zero, namely x = 5.

Values of *y* can be negative or positive, but never zero. Therefore, the range will be all real numbers except zero.



domain: , 5 5

range: , 0 0,

B. The notation *f*(3) means the value of the dependent variable when the independent variable is 3.

Answers will vary. An example is: <u>The cost of gasoline</u> depends on <u>the number of gallons</u> <u>used; so cost</u> is a function of <u>number of gallons</u>.

$$g x x^2 + 4 x + 1$$
 53.

54.
$$g x x^2 4x 1$$

 $g 10 10^2 410 1$
 $100 40 1 59$

55.
$$f \times 3x = 4$$
 $f = 3 = 4 = 143$

56.
$$f \stackrel{?}{=} 3 \stackrel{?}{=} 474 \stackrel{11}{=} 11$$

$$g x x^2 4 x 1$$

57.

58.
$$g x x^2 4x 1$$

$$g \perp \frac{1}{4} 2 \quad 4 \pm 1_{4}$$

$$\frac{1}{16} \frac{11}{16} \frac{1}{1}$$

$$\int x 3x 4$$

59. *f p* 3 *p* 4

$$g x x^2 4x 1 g k k^2$$

$$\begin{array}{c}
4k 1 \\
fx 3x 4
\end{array}$$

$$\begin{array}{c}
x 3 x 4 3x 4 \\
gx x^2 4 x 1
\end{array}$$

$$fx \ 3x \ 4$$
 $fx \ 2 \ 3x \ 2 \ 4$
 $3x \ 6 \ 4 \ 3x \ 2$
 $fx \ 3x \ 4$

68. (a)
$$f = 2.5$$
 (b) $f = 1.11f = 1$

70. (a)
$$f = 13$$
 (b) $f = 13$

71. (a)
$$f23f20$$
 (b) $f04f4$

72. (a)
$$f12$$
 (b) $4f00$

73. (a)
$$f12$$
 (b) $f02$ (c) $f23$ (d)

(a)
$$x 4 y 8$$

 $8 4 y x$
 $4 y$
 8
 4
 y
 $y \pm x + 2fx^{-1} x + 2$

(b)
$$f3 \stackrel{1}{=} 32^{\frac{1}{3}}2^{\frac{1}{3}}8^{\frac{1}{8}}5$$

79. (a)
$$y^2x^2 - 3x$$
 $y^2x - x^3$

$$f x^2 x^2 x^3$$

80. (a)
$$y 3x^2 2x$$

 $y 3x^2 x 2$
 $fx 3x^2 x 2$

(b)
$$f 3 33^2 3 2$$

81. (a)
$$\begin{array}{c} 4 x 3 y 8 \\ 4 x 3 y 8 \\ 4 x 8 3 y \end{array}$$

- 76. (a) f^2 3 (b) f^0 3 (c) f^1 3 (d) f^4 3

83. *f* 3 4

Chapter 2 Graphs and Functions

Because $f 0.2 \ 0.2^2 \ 3 \ 0.2 \ 1$

= 0.04 + 0.6 + 1 = 1.64, the height of the rectangle is 1.64 units. The base measures 0.3 - 0.2 = 0.1 unit. Because the area of a rectangle is base times height, the area of this rectangle is 0.1(1.64) = 0.164 square unit.

f 3 is the y-component of the coordinate, which is -4.

2 is the y-component of the coordinate, which is -3.

- **87.** (a) 2, 0
- **(b)** , 2

0,

- **88.** (a) 3, 1
- **(b)** 1,
- (c) , 3
- **89.** (a) , 2;2,
 - **(b)** 2, 2
- (c) none
- **90.** (a) 3, 3
- **(b)** ,3; 3,

none

(a) 1, 0; 1,

,1;0,1

none

- (a), 2; 0, 2 (b) 2, 0; 2,
 - (c) none
- (a) Yes, it is the graph of a function.

[0, 24]

When t = 8, y = 1200 from the graph. At 8 A.M., approximately 1200 megawatts is being used.

The most electricity was used at 17 hr or 5 P.M. The least electricity was used at 4 A.M.

f 12 1900

At 12 noon, electricity use is about 1900 megawatts.

increasing from 4 A.M. to 5 P.M.; decreasing from midnight to 4 A.M. and from 5 P.M. to midnight

(a) At t = 2, y = 240 from the graph. Therefore, at 2 seconds, the ball is 240 feet high.

At y = 192, x = 1 and x = 5 from the graph. Therefore, the height will be 192 feet at 1 second and at 5 seconds.

The ball is going up from 0 to 3 seconds and down from 3 to 7 seconds.

The coordinate of the highest point is (3, 256). Therefore, it reaches a maximum height of 256 feet at 3 seconds.

At x = 7, y = 0. Therefore, at 7 seconds, the ball hits the ground.

(a) At t = 12 and t = 20, y = 55 from the graph. Therefore, after about 12 noon until about 8 P.M. the temperature was over 55°.

At t = 6 and t = 22, y = 40 from the graph. Therefore, until about 6 A.M. and after 10 P.M. the temperature was below 40°.

The temperature at noon in Bratenahl, Ohio was 55°. Because the temperature in Greenville is 7° higher, we are looking for the time at which Bratenahl, Ohio was at or above 48°. This occurred at approximately 10 A.M and 8:30 P.M.

The temperature is just below 40° from midnight to 6 A.M., when it begins to rise until it reaches a maximum of just below 65° at 4 P.M. It then begins to fall util it reaches just under 40° again at midnight.

(a) At t = 8, y = 24 from the graph.

Therefore, there are 24 units of the drug in the bloodstream at 8 hours.

The level increases between 0 and 2 hours after the drug is taken and decreases between 2 and 12 hours after the drug is taken.

The coordinates of the highest point are (2, 64). Therefore, at 2 hours, the level of the drug in the bloodstream reaches its greatest value of 64 units.

After the peak, y = 16 at t = 10. 10 hours – 2 hours = 8 hours after the peak. 8 additional hours are required for the level to drop to 16 units. When the drug is administered, the level is 0 units. The level begins to rise quickly for 2 hours until it reaches a maximum of 64 units. The level then begins to decrease gradually until it reaches a level of 12 units, 12 hours after it was administered.

Section 2.4 Linear Functions

B; f(x) = 3x + 6 is a linear function with y-intercept (0, 6).

H; x = 9 is a vertical line.

C; f(x) = -8 is a constant function.

G; 2x - y = -4 or y = 2x + 4 is a linear equation with x-intercept (-2, 0) and y-intercept (0, 4).

A; f(x) = 5x is a linear function whose graph

passes through the origin, (0, 0). f(0) = 5(0) = 0.

6. D; $f(x) x^2$ is a function that is not linear.

m-3 matches graph C because the line falls rapidly as x increases.

m = 0 matches graph A because horizontal lines have slopes of 0.

m = 3 matches graph D because the line rises rapidly as x increases.

m is undefined for graph B because vertical lines have undefined slopes.

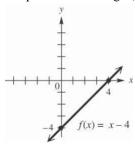
$$f(x) x-4$$

Use the intercepts.

$$f(0) \ 0 - 4 - 4 : y$$
-intercept

$$0 x - 4 x 4 : x$$
-intercept

Graph the line through (0, -4) and (4, 0).



The domain and range are both,.

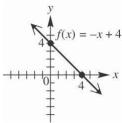
$$f(x) - x 4$$

Use the intercepts.

$$f(0) = 0.44 : y$$
-intercept

$$0 - x 4 \times 4 : x$$
-intercept

Graph the line through (0, 4) and (4, 0).



The domain and range are both, .

13. $f(x) = \frac{1}{2}x - 6$

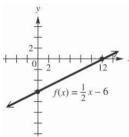
Use the intercepts.

1

$$f(0) \ 2 \ 0 \ -6 - 6$$
: y-intercept

$$\frac{1}{2}x - 66\frac{1}{6}x x^{2}12$$
: x-intercept

Graph the line through (0, -6) and (12, 0).



The domain and range are both, .

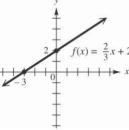
14.
$$f(x) \stackrel{2}{=} x 2$$

Use the intercepts.

$$f(0) \stackrel{?}{=} 022 : y$$
-intercept

$$0 = \frac{2}{3} \times 2 = \frac{2}{3} \times 3 = \frac{2}{3} \times 1 = \frac{2}{3} \times$$

Graph the line through (0, 2) and (-3, 0).

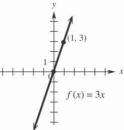


The domain and range are both,.

Chapter 2 Graphs and Functions

f(x) 3x

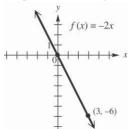
The *x*-intercept and the *y*-intercept are both zero. This gives us only one point, (0, 0). If x = 1, y = 3(1) = 3. Another point is (1, 3). Graph the line through (0, 0) and (1, 3).



The domain and range are both,.

$$x - 2x$$

The *x*-intercept and the *y*-intercept are both zero. This gives us only one point, (0, 0). If x = 3, y = -2(3) = -6, so another point is (3, -6). Graph the line through (0, 0) and (3, -6).



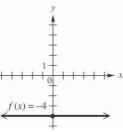
The domain and range are both, .

f(x) - 4 is a constant function.

17.

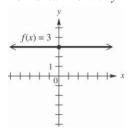
The graph of f(x) 4 is a horizontal line

with a y-intercept of -4.



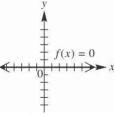
domain:,; range: $\{-4\}$

f(x) 3 is a constant function whose graph is a horizontal line with y-intercept of 3.



domain:,; range: {3}

f(x) 0 is a constant function whose graph is the x-axis.



domain:,; range: {0}

fx 9x

The domain and range are both, .

4 *x* 3 *y* 12

Use the intercepts.

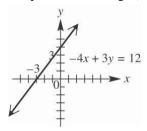
4 0 3 y 12 3 y 12

4 : *y*-intercept

4 *x* 3 0 12 4*x* 12

x 3 : x-intercept

Graph the line through (0, 4) and (-3, 0).



The domain and range are both, .

2x 5 y 10; Use the intercepts.

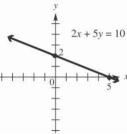
205 y 105 y 10

2 : y-intercept

2 x 5 0 10 2 x 10

x 5 : x-intercept

Graph the line through (0, 2) and (5, 0):



The domain and range are both,.

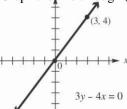
3 y 4x 0

Use the intercepts.

3 y 4 0 0 3 y 0 y 0 : y-intercept

 $3 \ 0 \ 4x \ 0 \ 4x \ 0 \ x \ 0$: *x*-intercept The graph has just one intercept. Choose an additional value, say 3, for *x*.

Graph the line through (0, 0) and (3, 4):



The domain and range are both,.

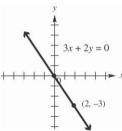
3x 2y 0

Use the intercepts.

 $3x \ 2 \ 0 \ 0 \ 3x \ 0 \ x \ 0 : x$ -intercept

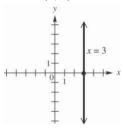
The graph has just one intercept. Choose an additional value, say 2, for *x*.

Graph the line through (0, 0) and (2, -3):



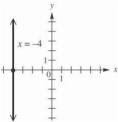
The domain and range are both,.

x = 3 is a vertical line, intersecting the x-axis at (3, 0).



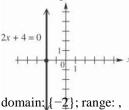
domain: {3}; range:,

x = -4 is a vertical line intersecting the x-axis at (-4, 0).



domain: $\{-4\}$; range:,

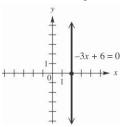
2x + 4 = 0 2 x 4 x 2 is a vertical line intersecting the x-axis at (-2, 0).



3x 60 - 3x 6 x 2

is a vertical

line intersecting the x-axis at (2, 0).

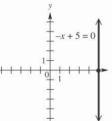


domain: {2}; range:,

29. *x* 5 0 *x* 5

is a vertical line

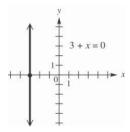
intersecting the x-axis at (5, 0).



domain: {5}; range:,

Chapter 2 Graphs and Functions 3 x 0 x 3 is a vertical line

intersecting the *x*-axis at 3, 0.



domain: $\{-3\}$; range:,

y = 5 is a horizontal line with y-intercept 5.

Choice A resembles this.

y = -5 is a horizontal line with y-intercept -5.

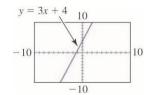
Choice C resembles this.

x = 5 is a vertical line with x-intercept 5.

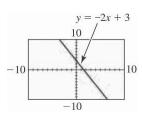
Choice D resembles this.

x = -5 is a vertical line with x-intercept

−5. Choice B resembles this.



35.



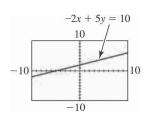
36.

37.
$$3x + 4y = 6$$

$$-10$$

$$-10$$

38.



40. The pitch or slope is $\frac{1}{4}$. If the rise is 4 feet

then $\frac{1}{4}$ rise $\frac{1}{x}$ $\frac{1}$

Through (2, -1) and (-3, -3)

rise of 4 feet.

Let
$$x_1 = 2$$
, $y_1 = -1$, $x_2 = -3$, and $y_2 = -3$.

Then rise y - 3 - (-1) - 2 and run x - 3 - 2 - 5.

rise
$$\underline{y}$$
 $\underline{-2}$ $\underline{2}$

The slope is m run x -5. 5

Through (-3, 4) and (2, -8)

Let $x_1 = 3$, $y_1 = 4$, $x_2 = 2$, and $y_2 = 8$.

Then rise y - 8 - 4 - 12 and run x - 2 - (3) - 5.

The slope is m run x 5 .5

Through (5, 8) and (3, 12)

Let x_1 5, y_1 8, x_2 3, and y_2 12.

Then rise y 12 8 4 and run x 3 5 2.

The slope is $m = \frac{\text{rise } y}{\text{run}} = \frac{4}{x} = 2$

Through (5, -3) and (1, -7)

Let x_1 5, y_1 -3, x_2 1, and y_2 -7.

Then rise y -7 - (-3) -4 and run x 1 - 5 -4.

The slope is $m = \frac{y}{x} = \frac{4}{4} = 1$.

45. Through (5, 9) and (-2, 9) $m^{\frac{y}{2}} \frac{y_2 y_1}{y_1} = \frac{9-9}{0} = 0$

46. Through (-2, 4) and (6, 4)

$$m^{\frac{y}{2}} + \frac{y_2}{y_1} + \frac{44}{9} = 0$$

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$$x = \begin{pmatrix} x & x \\ 2 & 1 \end{pmatrix} = 6 (-2) = 8$$

The rise is 2.5 feet while the run is 10 feet so the slope is
$$\frac{2.5}{10}$$
 0.25 25% $\frac{1}{4}$. So A =

0.25, C
$$\stackrel{2.5}{=}$$
 , D = 25%, and E^1 are all expressions of the slope.

Horizontal, through (5, 1)

The slope of every horizontal line is zero, so m = 0.

Horizontal, through (3, 5)

The slope of every horizontal line is zero, so m = 0.

Vertical, through (4, -7)

The slope of every vertical line is undefined; m is undefined.

Vertical, through (– 8, 5)
The slope of every vertical line is undefined; *m* is undefined.

51. (a) y 3x 5

Find two ordered pairs that are solutions to the equation.

If x = 0, then $y = 3 \cdot 0 \cdot 5 \cdot y \cdot 5$.

If
$$x = -1$$
, then $y \ 3 \ 1 \ 5 \ y \ 3 \ 5 \ y \ 2$.

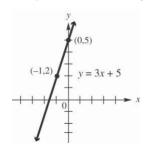
Thus two ordered pairs are (0, 5) and (-1, 2)

m

3.

1

(b)



y 2x 4

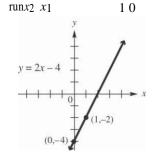
Eindriven offder of pairsethat are solutions to the

$$y = 4$$
. If $x = 1$, then $y = 21 = 4$ 2 4 $y = 2$. Thus two ordered pairs

are 0, 4 and 1, 2.

$$rise y y 2 4 2 -2 1 2.$$



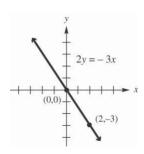


2y 3x

Find two ordered pairs that are solutions to the equation. If x 0, then 2 y 0 y 0.

If
$$y = 3$$
, then $2 \ 3 \ 3x = 6 \ 3x$

(b)



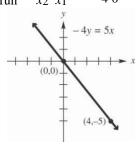
4y 5x

Find two ordered pairs that are solutions to the equation. If x 0, then 4 y 0 y 0.

5. Thus two ordered pairs are 0, 0 and 4, 5.

$$\frac{\text{rise}}{n \quad \text{run}} \frac{y_2 y_1}{x_2} \quad \frac{50}{x_1} \quad \frac{5}{40}$$

(b)



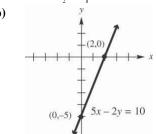
Find two ordered pairs that are solutions to the equation. If x 0, then 5 0 2 y 10

$$y = 5$$
. If $y = 0$, then $5x = 2010$

$5x\ 10 \ x \ 2.$

Thus two ordered pairs are 0, 5 and 2, 0.

$$\frac{\text{rise}}{m} \quad \frac{y}{2} \underbrace{y}_{1} \quad \frac{05}{5} \quad 5 \\
m \quad \text{run} \quad x \quad x \quad 20 \quad 2$$
(b)



- x = 2. Thus two ordered pairs are 0, 0 and
- 2, 3.

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$$\frac{\text{rise}}{m} \frac{y_2 y_1}{\text{run}} \frac{30}{x_2} \frac{3}{x_1} \frac{3}{20} \frac{3}{2}$$

Chapter 2 Graphs and Functions $4x \ 3y \ 12$

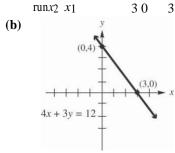
Find two ordered pairs that are solutions to the

equation. If x = 0, then 4 = 0 = 3 y = 12

3 y 12 y 4. If y 0, then

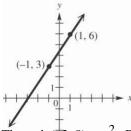
4 x 3 0 12 4 x 12 x 3. Thus two ordered pairs are 0, 4 and 3, 0.

$$\frac{\text{rise } y \ y \quad \underline{044}}{\underline{}} \quad .$$



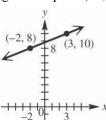
Through (-1, 3), $m^{\frac{3}{2}}$ 2

First locate the point (-1, 3). Because the slope is $2^{\frac{3}{2}}$, a change of 2 units horizontally (2 units to the right) produces a change of 3 units vertically (3 units up). This gives a second point, (1, 6), which can be used to complete the graph.



58. Through (-2, 8), m^{2} . Because the slope is

 $\frac{2}{5}$, a change of 5 units horizontally (to the right) produces a change of 2 units vertically (2 units up). This gives a second point (3, 10), which can be used to complete the graph. Alternatively, a change of 5 units to the left produces a change of 2 units down. This gives the point (-7, 6).

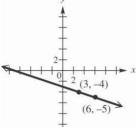


Through (3, -4), $m - \frac{1}{2}$. First locate the point

(3, -4). Because the slope 3 is $-\frac{1}{2}$, a change of

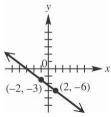
3 units horizontally (3 units to the right) produces a change of -1 unit vertically (1 unit

down). This gives a second point, (6, -5), which can be used to complete the graph.



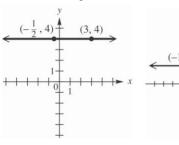
Through (-2, -3), $m - \frac{3}{4}$. Because the slope is $-\frac{3}{4}$ 4 $-\frac{3}{3}$, a change of 4 units horizontally

(4 units to the right) produces a change of -3 units vertically (3 units down). This gives a second point (2, -6), which can be used to complete the graph.



Through $\frac{1}{2}$, 4, m = 0. The graph is ²the horizontal line

through $2,4^{\frac{1}{2}}$.



Exercise 62

Through $^{3}_{-}$, 2, m = 0.

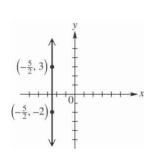
Exercise 61

The graph $\frac{2}{1}$ is the horizontal line through $2^{\frac{3}{1}}$ 2.

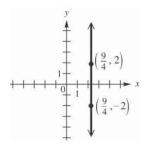
63. Through $\frac{5}{2}$, 3, undefined slope. The slope

is undefined, so the line is vertical, intersecting the x-axis at 5 _0.

2



Through 9 $\bar{,}$ 2 , undefined slope. The slope is undefined, 4 so the line is vertical, intersecting the x-axis at 9 4, 0.



The average rate of change is

$$m \qquad \frac{f \, bf \, a}{b \, a}$$

 $\frac{204}{04}$ $\frac{16}{4}$ \$4 (thousand) per year. The

value of the machine is decreasing \$4000 each year during these years.

The average rate of change is f bf

 $\begin{array}{cc} \underline{200\ 0} & \underline{200} \\ & 4\ 0 & 4 \end{array} \$50 \ \text{per month. The amount}$ saved is increasing \$50 each month during

these months.

- **67.** The graph is a horizontal line, so the average rate of change (slope) is 0. The percent of pay raise is not changing—it is 3% each year.
- **68.** The graph is a horizontal line, so the average rate of change (slope) is 0. That means that the

number of named hurricanes remained the same, 10, for the four consecutive years shown.

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78.8 thousand per year

The number of high school dropouts decreased by an average of 78.8 thousand per year from 1980 to 2012.

Sales of plasma flat-panel TVs decreased by an average of \$513.29 million per year from 2006 to 2013.

(a) The slope of -0.0167 indicates that the average rate of change of the winning time for the 5000 m run is 0.0167 min less. It is negative because the times are generally decreasing as time progresses.

The Olympics were not held during World Wars I (1914–1919) and II (1939–1945). y 0.0167 2000 46.45 13.05 min The model predicts a winning time of 13.05 minutes. The times differ by 13.35 – 13.05 = 0.30 min.

(a) From the equation, the slope is 200.02. This means that the number of radio stations increased by an average of

200.02 per year.

The year 2018 is represented by x = 68. y 200.02 68 2727.7 16, 329.06 According to the model, there will be about 16,329 radio stations in 2018.

73.
$$\frac{f2013f2008}{2013\ 2008}$$

$$2013\ 2008$$

$$\frac{65,318}{5}$$

$$13,063.6$$

The average annual rate of change from 2008 through 2013 is about 13,064 thousand.

74.
$$\frac{f2014f2006}{20142006} \quad \underbrace{\frac{3.744.53}{20142006}}_{0.79}$$

$$\underbrace{\frac{0.099}{20142006}}_{0.099}$$

The average annual rate of change from 2006 through 2014 is about -0.099.

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56.3 138

The average rate of change was -8.17 thousand mobile homes per year.

The negative slope means that the number of mobile homes decreased by an average of 8.17 thousand each year from 2003 to 2013.

76.
$$\begin{array}{r}
f2013f1991 \\
20131991 \\
20131991 \\
35.2 \\
\hline
1.6
\end{array}$$

22

There was an average decrease of 1.6 births per thousand per year from 1991 through

2013.

(a)
$$C \times 10 \times 500$$

 $R \times 35x$
 $P \times R \times C \times 35x \cdot 10x \cdot 500$
 $35x \cdot 10x \cdot 500 \cdot 25x \cdot 500$
 $C \times R \times 10x \cdot 500 \cdot 25x$
 $x \times 20 \text{ units; do not produce}$
 $C \times 150x \cdot 2700$
 $R \times 280x$

(a)

- **(b)** $280 \times 150 \times 2700$ $280 \times 150 \times 2700$
- (c) 130×2700 $C \times R \times X$ $150 \times 2700 \times 280 \times X$ $2700 \times 130 \times X$
- (d) 20.77 x or 21 units

21 units; produce

79. (a)
$$C \times 400x 1650$$

 $R \times 305x$

305*x* 400*x* 1650 305*x* 400 *x* 1650 95*x* 1650

Cx Rx 400 x 1650 305x 95x 1650 0 95x 1650 17.37 units

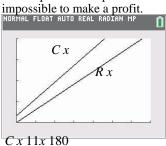
This result indicates a negative "break-

even point," but the number of units

produced must be a positive number. A calculator graph of the lines

$$y$$
1 C x 400 x 1650 and
 y 2 R x 305x in the window

 $[0, 70] \times [0, 20000]$ or solving the inequality 305x 400 x 1650 will show that Rx Cx for all positive values of x (in fact whenever x is greater than -17.4). Do not produce the product because it is



(a) $R \times 20 \times$

 $P \times R \times C \times$

$$\begin{array}{c}
C x R x \\
11x 180 20 x \\
9x \\
20 x
\end{array}$$
20 units; produce

C x R x 220 x 1000 240 x 1000 20x 50 x

The break-even point is 50 units instead of 25

units. The manager is not better off because

twice as many units must be sold before beginning to show a profit.

The first two points are A(0, -6) and B(1, -3).

$$m \frac{3-(-6)}{1-0} \frac{3}{1}$$

The second and third points are B(1, -3) and C(2, 0).

$$2-11$$

If we use any two points on a line to find its slope, we find that the slope is the same in all cases.

The first two points are A(0, -6) and B(1, -3).

$$\frac{d(A, B)}{\sqrt{-0)^2 [-3 - (-6)]^2}}$$
1²3²

$$\sqrt{19\sqrt{-19\sqrt{-10}}}$$

The second and fourth points are B(1, -3) and D(3, 3).

$$d(B, D) = \sqrt{\frac{3-1)^2 [3-(-3)]^2}{\sqrt{\sqrt{2^2 6^2 \sqrt{436}}}}}$$

The first and fourth points are A(0, -6) and D(3, 3).

$$d(A, D) \sqrt{(3-\theta)^2 [3-(-\theta)]^2}$$

$$\sqrt[3]{2} 9^2 \sqrt{981}$$

$$3 10 \sqrt[3]{6} \text{ as yum is } 3 1 \text{ hich/is equal to the answer in Exercise } 88.$$

If points A, B, and C lie on a line in that order, then the distance between A and B added to the distance between \underline{B} and \underline{C} is equal to the distance between \underline{A} and \underline{C} .

91. The midpoint of the segment joining A(0, -6) and G(6, 12) has coordinates

$$\frac{0_{6}}{2}$$
, $\frac{612}{2}$ $\frac{6}{2}$, $\frac{6}{2}$ 3, 3. The midpoint is

M(3, 3), which is the same as the middle entry in the table.

Chapter 2 Quiz (Sections 2.1–2.4)

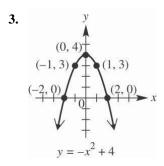
1.
$$d(A, B)\sqrt{\frac{x^2 y}{2^{1}}} \sqrt{\frac{y^2}{8(4)^2 32^2}} \sqrt{\frac{8(4)^2 32^2}{1625 41}}$$

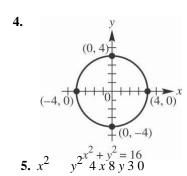
To find an estimate for 2006, find the midpoint of (2004, 6.55) and (2008, 6.97:

The estimated enrollment for 2006 was 6.76 million.

To find an estimate for 2010, find the midpoint of (2008, 6.97) and (2012, 7.50):

The estimated enrollment for 2006 was about 7.24 million.





Complete the square on x and y separately. (x 2 4x 4) (y 2 8 y 16) 3 4 16

$$(x2)^{2} (y4)^{2}$$
 17

92. The midpoint of the segment joining
$$E(4, 6)$$

and
$$F(5, 9)$$
 has coordinates $\frac{45.69}{9}$ 9 $\frac{15}{9}$

$$_{2}$$
, $_{2}$, $_{2}$, $_{2}$ = (4.5, 7.5). If the

x-value 4.5 were in the table, the corresponding *y*-value would be 7.5.

The radius is 17 and the midpoint of the circle is (2, -4).

From the graph, f(-1) is 2.

Domain: (,); range: [0,)

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- 8. (a) The largest open interval over which f is decreasing is (3).
 - **(b)** The largest open interval over which f is increasing is 3, .
 - (c) There is no interval over which the

function is constant.

9. (a)
$$m \frac{11.5}{5.1} \frac{6}{4} \frac{3}{2}$$

(b)
$$m \frac{-44}{1(7)} \frac{0}{6} 0$$

(c)
$$m = \frac{4 \cdot 12 \cdot 16}{6 \cdot 6}$$
 the slope is undefined.

The points to use are (2009, 10,602) and (2013, 15,884). The average rate of change is

The average rate of change was 1320.5 thousand cars per year. This means that the number of new motor vehicles sold in the United States increased by an average of 1320.5 thousand per year from 2009 to 2013.

Section 2.5 Equations of Lines and Linear Models

The graph of the line y 3 4 x 8 has

slope $\underline{4}$ and passes through the point $(8, \underline{3})$.

- **2.** The graph of the line y 2x 7 has slope $\underline{-2}$ and y-intercept $\underline{(0, 7)}$.
- 3. The vertical line through the point (-4, 8) has equation $\underline{x} = -4$.

The horizontal line through the point (-4, 8) has equation y = 8.

For exercises 5 and 6,

$$6x7y07y6xy$$

Any line parallel to the graph of 6 x 7 y 0 Copyright © 2017 Pearson Education, Inc.

$$4x + 3y = 12$$
 or $3y = -4x + 12$ or $y - \frac{4}{3}x + 4$

is graphed in B. The slope is $-3^{\frac{4}{3}}$ and the y-intercept is (0, 4).

$$y - 1 \stackrel{3}{=} x 1$$
 2 is graphed in C. The slope

is $\frac{3}{2}$ and a point on the graph is (1, -1).

y = 4 is graphed in A. y = 4 is a horizontal line with y-intercept (0, 4).

Through (1, 3), m = -2.

Write the equation in point-slope form.

$$y - y_1 m x x_1 y - 3 - 2 x - 1$$

Then, change to standard form.

$$3-2 x 2 2 x y 5$$

Through (2, 4), m = -1

Write the equation in point-slope form.

$$y - y_1 m x x_1 y - 4 - 1x - 2$$

Then, change to standard form.

$$y - 4 - x 2 x y 6$$

Through (-5, 4), $m^{\frac{3}{2}}$ 2

Write the equation in point-slope form.

$$y-4 = x5$$

Change to standard form.

$$2 y - 4 - 3 x 5$$

 $2 y - 8 - 3x - 15$

$$3x \ 2 \ v \ -7$$

4

Through (–4, 3), $m^{\frac{3}{2}}$

Write the equation in point-slope form.

$$y - 3 = \frac{3}{4} \times 4$$

7. $y = \frac{1}{x} x 2$ is graphed in D.

must have slope $\frac{6}{.7}$.

Any line perpendicular to the graph of $6 \times 7 \times 0$ must have slope $\frac{7}{.9}$.

Change to standard form.

4 y 3 3 x 4 4 y 12 3x 12 3x 4 y 24 or 3x 4 y 24

Through (-8, 4), undefined slope Because undefined slope indicates a vertical line, the equation will have the form x = a.

J

The slope is 4 and the y-intercept is (0, 2).

The equation of the line is x = -8.

Through (5, 1), undefined slope This is a vertical line through (5, 1), so the equation is x = 5.

Through (5, -8), m = 0This is a horizontal line through (5, -8), so the equation is y = -8. Through (-3, 12), m = 0

This is a horizontal line through (-3, 12), so the equation is y = 12.

Through (-1, 3) and (3, 4)

First find *m*.

$$m = \frac{4-3}{3-(-1)} \frac{1}{4}$$

Use either point and the point-slope form.

$$y-4 \frac{1}{4}x-3$$

Through (2, 3) and (-1, 2)

First find *m*.

12 3 3

Use either point and the point-slope form.

$$\begin{array}{r}
 3 \frac{1}{3}x - 2 \\
 3 y - 9 & x 2 \\
 3 y & 7 \\
 x 3 y & 7
 \end{array}$$

x-intercept (3, 0), y-intercept (0, -2)

The line passes through (3, 0) and (0, -2). Use these points to find m.

$$m = \frac{-2-0}{0-3} \frac{2}{3}$$
Using slope-intercept form we have $y = x - 2$.

x-intercept (-4, 0), y-intercept (0, 3)

The line passes through the points (-4, 0)

and (0, 3). Use these points to find m.

$$m = \frac{3-0-3}{0-(-4)}$$

Using slope-intercept form we have $4\frac{3}{4}$ x 3.

Vertical, through (-6, 4)

The equation of a vertical line has an equation of the form x = a. Because the line passes through (-6, 4), the equation is

x = -6. (Because the slope of a vertical line is undefined, this equation cannot be written in slope-intercept form.)

Vertical, through (2, 7)

The equation of a vertical line has an equation of the form x = a. Because the line passes through (2, 7), the equation is x = 2. (Because the slope of a vertical line is undefined, this equation cannot be written in slope-intercept form.)

Horizontal, through (-7, 4)

The equation of a horizontal line has an equation of the form y = b. Because the line passes through (-7, 4), the equation is

Horizontal, through (-8, -2)

The equation of a horizontal line has an equation of the form y = b. Because the line passes through (-8, -2), the equation is v = -2.

$$m = 5, b = 15$$

Using slope-intercept form, we have 5x 15.

$$m = -2, b = 12$$

Using slope-intercept form, we have 2 x 12.

Through (-2, 5), slope = -4

$$5 \ 4 \ x \ 2$$

 $5 \ 4 \ x \ 2$
 $5 \ 4 \ x \ 8$
 $y \ 4 \ x \ 3$

Through
$$(4, -7)$$
, slope = -2
7 2 x 4
7 2 x 8
y 2 x 1

slope 0, y-intercept 0,
$$\frac{3}{2}$$

These represent m 0 and b 3 . \bar{z} Using slope-intercept form, we have

$$y \ 0 \ x \ \frac{3}{2} \ y \ \frac{3}{2} \ .$$

32. slope 0, y-intercept 0, $\frac{5}{2}$

These represent m = 0 and $ab = \frac{5}{4}$. Using slope-intercept form, we have

0 x 4 y 4.

The line x + 2 = 0 has x-intercept (-2, 0). It does not have a y-intercept. The slope of his line is <u>undefined</u>. The line 4y = 2 has

y-intercept $0, \frac{1}{2}$. It -does not have an x-

intercept. The slope of this line is $\underline{0}$.

(a) The graph of y = 3x + 2 has a positive slope and a positive y-intercept. These conditions match graph D.

Chapter 2 Graphs and Functions

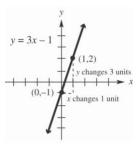
The graph of y = -3x + 2 has a negative slope and a positive y-intercept. These conditions match graph B.

The graph of y = 3x - 2 has a positive slope and a negative y-intercept. These conditions match graph A.

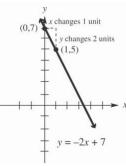
The graph of y = -3x - 2 has a negative slope and a negative y-intercept. These conditions match graph C.

$$y = 3x - 1$$

This equation is in the slope-intercept form, y = mx + b. slope: 3; yintercept: (0, -1)



$$y = -2x + 7$$
 slope: –
2; y-intercept: (0, 7)

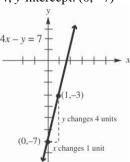


$$4x - y = 7$$

Solve for *y* to write the equation in slope-intercept form.

$$-y - 4 \times 7 y 4x - 7$$
 slope:

4; y-intercept: (0, -7)

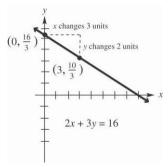


$$2x + 3y = 16$$

Solve the equation for *y* to write the equation in slope-intercept form.

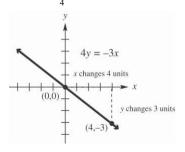
$$3y - 2x 16y - 3x 3^{\frac{2}{3}}$$

slope: $-\frac{2}{3}$; y-intercept: 0, $\frac{16}{3}$



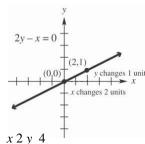
39.
$$4y - 3x \ y - \frac{3}{4} x \text{ or } y = \frac{3}{4} x 0$$

slope: $\frac{3}{2}$; y-intercept (0, 0)



40.
$$2yxy^{\frac{1}{2}}x \text{ or }^2y^{\frac{1}{2}}x0^{-2}$$

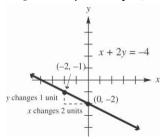
slope is $2^{\frac{1}{2}}$; y-intercept: (0, 0)



Solve the equation for *y* to write the equation in slope-intercept form.

$$2y - x4y - \frac{1}{2}x22$$

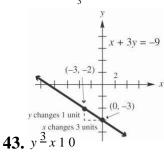
slope: $-2^{\frac{1}{2}}$; y-intercept: (0, -2)



x3y9

Solve the equation for y to write the equation in slope-intercept form. 3y - x9y - x3 slope: $-\frac{1}{2}$

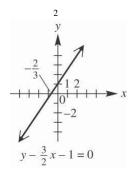
; y-intercept:
$$(0,-3)$$



Solve the equation for *y* to write the equation in slope-intercept form.

$$y \frac{3}{2}x 10 y 2x 1$$

slope: $\frac{3}{2}$; y-intercept: (0, 1)



(a) Use the first two points in the table, A(-2, -11) and B(-1, -8).

When x = 0, y = -5. The y-intercept is (0, -5).

Substitute 3 for m and -5 for b in the slope-intercept form. y mx b y 3x - 5

(a) The line falls 2 units each time the x value increases by 1 unit. Therefore the slope is -2. The graph intersects the y-axis at the point (0, 1) and intersects the x-axis at ¹-2, 0, so the y-intercept is (0, 1) and the x-intercept is ¹, 0.

An equation defining *f* is y = -2x + 1.

(a) The line rises 2 units each time the x value increases by 1 unit. Therefore the slope is 2. The graph intersects the y-axis at the point (0, -1) and intersects the x-axis at $\frac{1}{2}$, 0, so the y-intercept is (0, -1) and the x-intercept is $\frac{1}{2}$, 0.

An equation defining f is y = 2x - 1.

- (a) The line falls 1 unit each time the x value increases by 3 units. Therefore the slope is $\frac{1}{3}$. The graph intersects the y-axis at the point (0, 2), so the y-intercept is (0, 2). The graph passes through (3, 1) and will fall 1 unit when the x value increases by 3, so the x-intercept is (6, 0).
- **(b)** An equation defining f is $y = \frac{1}{x_2} \cdot 2$.
- (a) The line rises 3 units each time the x value increases by 4 units. Therefore the $\frac{3}{2}$

slope is 4. The graph intersects the

y-axis at the point (0, -3) and intersects the x-axis at (4, 0), so the y-intercept is (0, -3) and the x-intercept is 4.

- **(b)** An equation defining f is $y = \begin{bmatrix} 3 \\ 4 \end{bmatrix} x = 3$.
- (a) The line falls 200 units each time the x value increases by 1 unit. Therefore the slope is -200. The graph intersects the y-axis at the point (0, 300) and intersects the x-axis at $\frac{3}{2}$, 0, so the y-intercept is (0, 300) and the x-(0, 300) and the x-(0, 300) and the (0, 300) and (0
- (b) An equation defining f is y = -200x + 300.
- (a) The line rises 100 units each time the x value increases by 5 units. Therefore the slope is 20. The graph intersects the y-axis at the point (0, -50) and intersects the x-axis at $\frac{5}{2}$, 0, so the y-intercept is $\frac{2}{(0, -50)}$ and the x-intercept is $\frac{2}{5}$, 0.

An equation defining *f* is y = 20x - 50.

51. (a) through (-1, 4), parallel to x + 3y = 5Find the slope of the line x + 3y = 5 by writing this equation in slope-intercept form.

The slope is $\frac{1}{2}$.

Because the lines are parallel, $\frac{1}{3}$ is also

the slope of the line whose equation is to be found. Substitute $m = \frac{1}{3}$, x = -1,

and y1 4 into the point-slope form.

$$y-y_1 mx-x_1$$

 $y = 4 + x - 1$
 $y = 4 + x + 1$

$$3y-12-x-1x3y11$$

Solve for y.

(a) through (3, -2), parallel to 2x - y = 5 Find the slope of the line 2x - y = 5 by writing this equation in slope-intercept form.

$$2x-y$$
 5 -y -2 x 5 $2x-5$

The slope is 2. Because the lines are parallel, the slope of the line whose equation is to be found is also 2.

Substitute m = 2, $x_1 \ 3$, and $y_1 \ 2$ into the point-slope form.

$$y-y1$$
 $mx-x1$

$$y \ 2 \ 2 \ x - 3 \ y \ 2 \ 2 \ x - 6$$

-2 $x \ y \ -8$ or $2 \ x - y \ 8$

- **(b)** Solve for y. y = 2x 8
- 53. (a) through (1, 6), perpendicular to 3x + 5y = 1Find the slope of the line 3x + 3y = 1

Find the slope of the line 3x + 5y = 1 by writing this equation in slope-intercept form.

$$3x 5 y 1 5 y -3x 1
y - $\frac{3}{5}x \stackrel{!}{=} 5$$$

This line has a slope of $\frac{3}{2}$. The slope of

$$y-6 \stackrel{5}{=} (x-1)$$
3(y-6)5(x-1)
3y-185x-5
-135x-3y or 5x-3y-13

(b) Solve for y.

$$3 y 5x 13 y \frac{5}{5} x \frac{13}{3}$$

(a) through (-2, 0), perpendicular to

$$8x - 3y = 7$$

Find the slope of the line 8x - 3y = 7 by writing the equation in slope-intercept

form.

$$8x - 3y 7 - 3y - 8x 7
\underline{8} x - 7
33$$

This line has a slope of $\frac{8}{3}$. The slope of

any line perpendicular to this line is $\frac{38}{3}$,

because
$$\frac{8}{3}$$
 $\frac{3}{8}$ 1.

Substitute $m = \frac{3}{2}$, x 2, and into y₁ 0 the point-slope form.

the point-slope form.

$$y-0 = \frac{3}{8}(x 2)$$

 $8y = -3(x 2)$
 $8y = -3x - 63x8y = -6$

Solve for y.

(a) through (4, 1), parallel to y = -5 Because y = -5 is a horizontal line, any line parallel to this line will be horizontal

and have an equation of the form y = b. Because the line passes through (4, 1), the equation is y = 1.

- **(b)** The slope-intercept form is y = 1.
- **56.** (a) through 2, 2, parallel to y = 3. Because y = 3 is a horizontal line, any line parallel to this line will be horizontal and have an equation of the form y = b. Because the line passes through 2, 2, the equation is y = -2.
 - **(b)** The slope-intercept form is y = -2

```
any line perpendicular to this line is \frac{5}{3}, because \frac{2}{3} 1. Substitute m 5

\frac{5}{3} 3

57. (a) through (-5, 6), perpendicular to x = -2.

Because x = -2 is a vertical line, any line perpendicular to this line will be
```

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 x_1 1, and y_1 6 into the point-slope form.

horizontal and have an equation of the form y = b. Because the line passes through (-5, 6), the equation is y = 6.

The slope-intercept form is y = 6.

Through (4, -4), perpendicular to x = 4

Because x = 4 is a vertical line, any line perpendicular to this line will be horizontal and have an equation of the form y = b. Because the line passes through (4, -4), the equation is y = -4.

(a)

The slope-intercept form is y = -4.

(a) Find the slope of the line 3y + 2x = 6.

$$3 y 2x 6 3 y -2x 6$$
 $-\frac{2}{3} x 2$

Thus, $m - \frac{2}{3}$. A line parallel to

3y + 2x = 6 also has slope $-\frac{2}{3}$.

Find the slope of the line 2y - 5x = 1.

$$y \xrightarrow{5} x \xrightarrow{1}$$

Thus, $m = \frac{5}{2}$. A line perpendicular to 2y

2

-5x = 1 will have slope -5, because

$$\frac{5}{2}$$
 - 5 $\frac{2}{}$ -1.

Solve this equation for k.

$$\frac{3}{k} \frac{2}{4} = \frac{2}{5}$$

$$5 k 4 - \frac{3}{5} = 5 k = 4^{\frac{2}{5}}$$

$$k 4 = 5$$

$$2 k 4$$

$$2 k 8$$

$$2 k 7 k 7$$

60. (a) Find the slope of the line 2x - 3y = 4.

$$2x - 3y + 4 - 3y - 2x + 4$$

 $y = 2x - 4$

Thus, $m^{\frac{3}{2}}$.3 A line parallel to

2x - 3y = 4 also has slope $3^{\frac{2}{3}}$. Solve for r using the slope formula.

r 6 4 r 2

Find the slope of the line x + 2y = 1.

Thus, $m^{-\frac{1}{2}}$. A line perpendicular to

the line x + 2y = 1 has slope 2, because $-2^{\frac{1}{2}}(2) - 1$. Solve for r using the slope formula.

(a) First find the slope using the points (0, 6312) and (3, 7703).

$$m = \frac{77036312}{30} = \frac{1391}{3463.67}$$

The *y*-intercept is (0, 6312), so the equation of the line is 463.67 *x* 6312.

The value x = 4 corresponds to the year 2013.

The model predicts that average tuition and fees were \$8166.68 in 2013. This is \$96.68 more than the actual amount.

(a) First find the slope using the points

2

(0, 6312) and (2, 7136).

$$m \frac{7136 6312}{20} \frac{824}{2} 412$$

The y-intercept is (0, 6

e q u a t i o n o f t h e l i n e i s

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The value x = 4 corresponds to the year 2013.

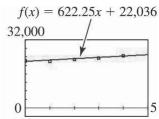
y 412 4 6312 7960

The model predicts that average tuition and fees were \$7960 in 2013. This is \$110 less than the actual amount.

Chapter 2 Graphs and Functions

(a) First find the slope using the points (0, 22036) and (4, 24525).

The y-intercept is (0, 22036), so the equation of the line is y 622.25x 22, 036.



THOOOpe of the line indicates that the average tuition increase is about \$622 per year from 2009 through 2013.

- (b) The year 2012 corresponds to x = 3. $y = 622.25 \ 3 \ 22,036 \ 23,902.75$ According to the model, average tuition and fees were \$23,903 in 2012. This is \$443 more than the actual amount \$23,460.
- (c) Using the linear regression feature, the

equation of the line of best fit is y 653x 21,634.



64. (a) See the graph in the answer to part (b). There appears to be a linear

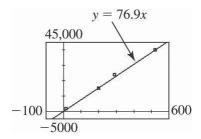
relationship between the data. The farther the galaxy is from Earth, the faster it is

receding.

(b) Using the points (520, 40,000) and (0, 0), we obtain

$$m = \frac{40,000 - 0}{40,000} = 76.9.$$

$$520-0$$
 520 The equation of the line through these two points is $y = 76.9x$.



(c) $76.9 \times 60,000$

$$\begin{array}{ccc} x & \underline{60}, \underline{000} \\ 76.9 & \end{array} \quad x \quad 780$$

According to the model, the galaxy Hydra is approximately 780 megaparsecs away.

(d)
$$A = \frac{9.5 \cdot 10^{11}}{m}$$

$$A = \frac{9.5 \cdot 10^{11}}{76.9} = 1.235 \cdot 10^{-10} = 12.35 \cdot 10^{-9}$$

Using m = 76.9, we estimate that the age of the universe is approximately 12.35 billion years.

(e)
$$A = \frac{9.5 \cdot 10^{11}}{1.9 \cdot 10} = 1.9 \cdot 10$$
 or $19 \cdot 10$

$$A = \frac{9.5 \cdot 10}{100} = 1.9 \cdot 10$$

$$A = \frac{9.5 \cdot 10^{11}}{100} = 1.9 \cdot 10$$

The range for the age of the universe is between 9.5 billion and 19 billion years.

65. (a) The ordered pairs are (0, 32) and (100, 212).

The slope is
$$m = \frac{212-32 - 180 - 9}{100-0 - 100}$$
.
Use $(x, y) = (0, 32)$ and $m = \frac{9}{2}$ in the

point-slope form.

$$y-y1 m(x-x1)$$

 $y-32 \frac{9}{2}(x-0)$
 $y-32 \frac{9}{2}x$

$$y \stackrel{5}{=} x 32 F \stackrel{9}{=} C 32$$

(b) $F \stackrel{9}{=} C 32$ 5F 9C 32 5F 9C 160 9C 5F - 160 $9C 5(F - 32) C \stackrel{5}{=} (F - 32)$

(c) $F C F \stackrel{5}{=} (F-32)$ 9F 5(F-32) 9F 5F-160 4F -160 F -40 $F = C \text{ when } F \text{ is } -40^{\circ}.$ (a) The ordered pairs are (0, 1) and (100, 3.92).

The slope is

$$m = \frac{3.92 - 1}{100 - 0} = \frac{2.92}{100} = 0.0292$$
 and $b = 1$.

Using slope-intercept form we have $y = 0.0292 \times 1$ or $p(x) = 0.0292 \times 1$.

Let
$$x = 60$$
.

$$P(60) = 0.0292(60) + 1 = 2.752$$

The pressure at 60 feet is approximately 2.75 atmospheres.

(a) Because we want to find *C* as a function of *I*, use the points (12026, 10089) and (14167, 11484), where the first component represents the independent variable, *I*. First find the slope of the line.

$$m\, \frac{11484\, 10089}{14167\, 12026\, 2141} \underline{0.6516}$$

Now use either point, say (12026, 10089), and the point-slope form to find the equation.

 $C - 10089 \ 0.6516(I - 12026)$

 $C - 10089\ 0.6516I - 7836$

0.6516I 2253

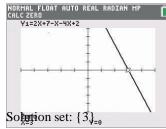
Because the slope is 0.6516, the marginal

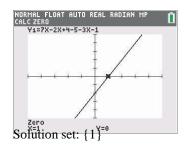
propensity to consume is 0.6516.

D is the only possible answer, because the x-intercept occurs when y = 0. We can see from the graph that the value of the x-intercept exceeds 10.

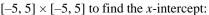
Write the equation as an equivalent equation with 0 on one side: 2 x 7 x 4 x 2 2 x 7 x 4 x 2 0. Now graph y 2x 7 x 4x 2 in the window

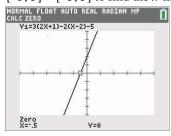
 $[-5, 5] \times [-5, 5]$ to find the *x*-intercept:





Write the equation as an equivalent equation with 0 on one side: 3 2 x 1 2 x 2 5 3 2 x 1 2 x 2 5 0 . Now graph 3 2 x 1 2 x 2 5 in the window





Solution set: $\frac{1}{2}$ or 0.5

Write the equation as an equivalent equation with 0 on one side:

4 x 3 4 2 x 2 x 3 6 x 2 4x 3 4 2 x 2 x 3 6 x 2 0 . Now graph

4x 3 4 2 x 2 x 3 6 x 2 in the

window $[-2, 8] \times [-5, 5]$ to find the *x*-intercept:



Solution set: $\{4\}$ 73. (a) $\begin{array}{r}
2 \times 5 \times 2 \\
2 \times 10 \times 2 \\
\times 2 \\
12 \times \\
\text{Solution set: } \{12\}
\end{array}$

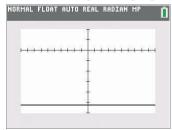
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Answers will vary. Sample answer: The solution does not appear in the standard viewing window x-interval [10, -10]. The minimum and maximum values must include 12.

Rewrite the equation as an equivalent equation with 0 on one side.

6x 18 4x 8 2x 0

Now graph y = -6x - 18 - (-4x + 8 - 2x)in the window $[-10, 10] \times [-30, 10]$.



The graph is a horizontal line that does not intersect the x-axis. Therefore, the solution set

is . We can verify this algebraically.

6 x 18 6x 8 0 26

Because this is a false statement, the

solution set is.

$$A(-1, 4), B(-2, -1), C(1, 14)$$

For *A* and *B*,
$$m = \frac{14}{5} = \frac{5}{5}$$

For *B* and *C*, *m*
$$\frac{14(1)}{15}$$
 5

For A and C,
$$m = \frac{144}{100} = \frac{10}{500} = \frac{1}{500}$$

Since all three slopes are the same, the points are collinear.

$$A(0, -7), B(-3, 5), C(2, -15)$$

For *A* and *B*,
$$m = \frac{5(7)}{12} \frac{12}{4}$$

$$A(-1, -3), B(-5, 12), C(1, -11)$$

For *A* and *B*,
$$m = 12 \cdot (3) \cdot 15 = 5 \cdot (1) = 4$$

For *B* and *C*,
$$m = \frac{1112}{1(5)} = \frac{23}{6}$$

For *A* and *C*,
$$m = \frac{11(3)}{1(1)} \frac{8}{4}$$

Since all three slopes are not the same, the points are not collinear.

$$A(0, 9), B(-3, -7), C(2, 19)$$

For *A* and *B*,
$$m = \frac{7.9 + 16 + 16}{3.0 + 3}$$

For *B* and *C*,
$$m = \frac{19(7)}{2(3)} = \frac{26}{5}$$

For *A* and *C*,
$$m = \frac{199}{20} = \frac{10}{5}$$

Because all three slopes are not the same, the points are not collinear.

79.
$$d(O, P) = (x - 0)^2$$

$$(mx\sqrt{-0)^2}$$

$$\sqrt{\frac{2_1 m^2 x_1^2}{1}}$$

$$\sqrt[4]{\frac{1}{\sqrt{2_1 m^2 x_1^2}}} \frac{1}{1}$$

$$d(O,Q) = (\sqrt{2-0)^2 (m_2 x_2 - 0)^2}$$

$$\int_{0}^{\infty} x_2^{2} m^2 x_2$$

$$d(P,Q)$$
 $(x -x) (mx -mx)$

$$\frac{[d(O, P)]^{2} [d(O, Q)]^{2} [d(P, Q)]^{2}}{\sqrt{\sum_{\substack{X^{2} m^{2}x^{2} \\ 1 & 1 & 1}} x^{2} m^{2} x^{2} x^{2} m^{2} x^{2}}} 2$$

$$\sqrt{\frac{2}{x_2 - x_1}} \frac{2}{m_2 x_2 - m_1 x_1}$$

$$x - x \qquad m x - m x$$

For *B* and *C*, *m* $15.5 \ 20$ 4 Copyright © 2017 Pearson Education, Inc. $x_2 \ 2x_2x_1 \ 1$ $x_2 \ 2x_2x_1 \ 1$ $x_3 \ 2x_2$

For *A* and *C*, *m* $\frac{15(7)}{8}$ 4

20 2

Since all three slopes are the same, the points are collinear.

 $2m_1m_2x_1x_2x_2x_1$ 0

- **83.** $-2m_1m_2 x_1 x_2 2 x_1 x_2 = 0$ $-2 x_1 x_2 (m_1m_2 = 1) = 0$
- **84.** $-2x_1x_2$ (m_1m_2 1) 0 Because x_1 0 and x_2 0, we have m_1m_2 1 0 implying that m_1m_2 -1.

If two nonvertical lines are perpendicular, then the product of the slopes of these lines is -1.

Summary Exercises on Graphs, Circles,

Functions, and Equations

P(3,5), Q(2,3)

$$d(P,Q)\sqrt{(2\ 3)^2\ (3\ 5)^2}$$

$$\sqrt{1^2\ 8^2}$$

$$\sqrt{64\ 65}\sqrt{}$$

The midpoint M of the segment joining points P and Q has coordinates

First find $m: m = \frac{3-5-8}{8}$ 8

Use either point and the point-slope form.
$$-5 \ 8 \ x - 3$$

Change to slope-intercept form.

P(-1, 0), Q(4, -2)

(a)
$$d(P, Q) = \sqrt{4 - (-1)^2 - (-2 - 0)^2}$$

 $\sqrt{54 - (-2)^2}$
 $\sqrt{54}$

The midpoint *M* of the segment joining points *P* and *Q* has coordinates

$$-14, 0(-2)$$
 3.2

(c) First find $m: m^{2-0} \ 2 \ 2$

The midpoint *M* of the segment joining points *P* and *Q* has coordinates

(c) First find m:
$$m = \frac{2-2}{3-2} - \frac{0}{5} = 0$$

All lines that have a slope of 0 are horizontal lines. The equation of a horizontal line has an equation of the form y = b. Because the line passes through (3, 2), the equation is y = 2

through (3, 2), the equation is y = 2.

(a)
$$d(P, Q) = \sqrt{\sqrt{2} - 2\sqrt{2}} = \sqrt{32-2\sqrt{2}}$$

$$\sqrt{\sqrt{\frac{2}{\sqrt{2}}} = \sqrt{\frac{2}{\sqrt{2}}} = \sqrt{\frac{2}{\sqrt{2}}}$$

$$-2 = 2 = 2$$

$$28 = 10$$

The midpoint M of the segment joining points P and Q has coordinates

(c) First find
$$m: m = \frac{3\sqrt{2}2\sqrt{2}}{\sqrt{2}2\sqrt{2}} = \frac{\sqrt{2}}{\sqrt{2}}$$

Use either point and the point-slope form.

$$y - \sqrt{2} 2 \qquad x - 2 2$$
Change to slope-intercept form.
$$y - \sqrt{2} 2 x 4 2 y \sqrt{2} x 5 2 \qquad \sqrt{}$$

(a)
$$d(P, Q) (5-5)^2 [1-(-1)]^2$$

4–15 5

$$\sqrt[4]{\frac{\sqrt{2}}{2^2}}$$
 $\sqrt{04}$ $\sqrt{4}$ 2

Use either point and the point-slope form. y-0 $\stackrel{2}{\overset{\sim}{5}}$ 1

$$y - 0 = 2 x = \frac{1}{5}$$

Change to slope-intercept form.

$$y = \frac{2}{x} x^{\frac{2}{3}}$$

3. P(-2, 2), Q(3, 2)

(a)
$$d(P, Q) = \sqrt{[3 - (-2)]^2 \cdot 2 \cdot 2^2}$$

 $\sqrt{250} = \sqrt{25} \cdot 5$

The midpoint M of the segment joining points P and Q has coordinates

(c) First find m.

m undefined 5-5 0

All lines that have an undefined slope are vertical lines. The equation of a vertical line has an equation of the form x = a. The line passes through (5, 1), so the equation is x = 5. (Because the slope of a vertical line is undefined, this equation cannot be written in slope-intercept form.)

P(1, 1), Q(3, 3)

$$d(P,Q) = (3-1)^{2} (3-1)^{2}$$

$$\sqrt[4]{2} 4^{2}$$

$$\sqrt[4]{616} = \sqrt{32} 4 \sqrt[4]{7}$$

The midpoint *M* of the segment joining points *P* and *Q* has coordinates

$$3 - 1 \ 4$$

First find m: m 1 3-1 4

Use either point and the point-slope form.

$$-11x-1$$

Change to slope-intercept form.

7. $P2 \sqrt[4]{3}$ $Q6 3 5\sqrt{}$

(a)
$$d(P, Q) = \begin{cases} 6.3 - 2 & 3 & 3.5 - 3 & 5 \\ \sqrt{\sqrt{2} \sqrt{2}} & \sqrt{\sqrt{2}} & \sqrt{\sqrt{48}} & 4\sqrt{3} \end{cases}$$

The midpoint *M* of the segment joining points *P* and *Q* has coordinates

$$\frac{\sqrt{2} \cdot 63\sqrt{} \cdot 3\sqrt{535}}{2} \cdot \sqrt{}$$

All lines that have a slope of 0 are horizontal lines. The equation of a horizontal line has an equation of the form y = b. Because the line passes

through 2 $\sqrt{3}$, 3 the equation is

$$P(0, -4), Q(3, 1)$$

$$d(P,Q) \quad (3-0)^{2} \frac{[1-(-4)]^{2}}{\sqrt{925}} \sqrt{925} \quad 34$$

The midpoint *M* of the segment joining points *P* and *Q* has coordinates

(c) First find $m: m = \frac{1-4}{2} = \frac{5}{2}$

30 3

Using slope-intercept form we have $y = \frac{5}{x} - 4$.

9. Through 2,1 and 4, 1

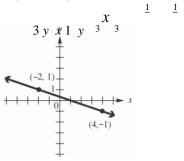
<u>1-1</u> <u>2</u> 1

First find $m: m \ 4 - (-2) \ 6 \ 3$ Use either point and the point-slope form.

$$y - 1$$
 3 $x - 4$

Change to slope-intercept form.

3 y 1 x 4 3 y 3 x 4

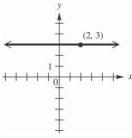


Solution Copyright © 2017 Pearson Education, Inc. 2, 2 43, 5.



the horizontal line through (2, 3)

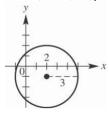
The equation of a horizontal line has an equation of the form y = b. Because the line passes through (2, 3), the equation is y = 3.



the circle with center (2, -1) and radius 3 (

$$(x-2)^2 y - (-1)^2 3^2$$

$$(x-2)^2 (y1)^2 9$$

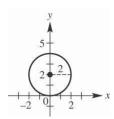


the circle with center (0, 2) and tangent to the

x-axis

The distance from the center of the circle to the *x*-axis is 2, so r = 2.

$$(x-0)^2 (y-2)^2 2^2 x^2 (y-2)^2 4$$

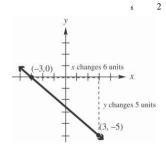


13. the line through (3, 5) with slope $\frac{5}{2}$

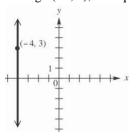
Write the equation in point-slope form.

$$y - 5 = \frac{5}{x_3} = 6$$

Change to standard form.



The equation of a vertical line has an equation of the form x = a. Because the line passes through (-4, 3), the equation is x = -4.



a line through (-3, 2) and parallel to the line 2x + 3y = 6

First, find the slope of the line 2x + 3y = 6 by writing this equation in slope-intercept form.

$$2 \times 3 \times 6 \times 3 \times 2 \times 6 \times 2 \times 2$$

3

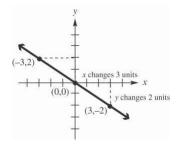
The slope is $\frac{2}{3}$. Because the lines are parallel, $\frac{2}{3}$ is also the slope of the line

whose equation is to be found. Substitute m_3 , $^2*_1 3$, and y_1 2 into the point-slope form.

$$y-y1 mx-x1 y2^{\frac{2}{2}}x3 3$$

$$3 y2 2x33y62x-6$$

$$3 y-2x y^{\frac{2}{2}}x$$



a line through the origin and perpendicular to the line 3x 4y 2

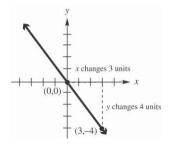
First, find the slope of the line 3x 4 y 2 by writing this equation in slope-intercept form. 3x 4 y 2 4 y -3x 2

This line has a slope of 4 . The slope of any line perpendicular to this line is $\frac{4}{3}$, because

 $\frac{43}{3}$ 1. Using slope-intercept form we have $y \stackrel{4}{=} x \stackrel{0}{=} 0$ or $y \stackrel{4}{=} x$.

(continued on next page)

216 Chapter 2 Graphs and Functions (continued)



$$x^2 + 4x + y^2 + 2y + 4$$

Complete the square on x and y separately.

$$x^2 4x y^2 2y 4$$

$$x^2$$
 4 x 4 y 2 2 y 1 4 4 1

$$x 2^2 y 1^2 9$$

Yes, it is a circle. The circle has its center at

$$(2, -1)$$
 and radius 3.
 $x^2 6x y^2 10 y 36 0$

Complete the square on x and y separately.

$$x^2$$
 6 x y 2 10 y 36

$$x^2$$
 6 x 9 y 2 10 y 25 -36 9 25

$$x 3^2 y 5^2 2$$

No, it is not a circle.

19.
$$x^2$$
 12 x y^2 20 0

Complete the square on x and y separately.

$$x^2 12 x y^2 20$$

$$x^2$$
 12 x 36 y 2 -20 36
x 6^2 y 2 16

Yes, it is a circle. The circle has its center at (6, 0) and radius 4.

20.
$$x^2 \ 2x \ y^2 \ 16y \ 61$$

Complete the square on x and y separately.

$$x^2 \ 2x \ y^2 \ 16 \ y \ 61$$

$$x^2 \ 2 \ x \ y^2 \ 10 \ 0$$

Complete the square on x and y separately.

$$x^2 2 x y^2 10$$

$$x^2$$
 2 x 1 y 2 -10 1

$$x 1^2 y^2 9$$

No, it is not a circle.

$$x^2 y^2 - 8 y 9 0$$

Complete the square on x and y separately.

$$x^2 y^2 - 8y 9$$

$$x^2$$
 $y^2 - 8$ y 16 9 16

$$x^2 y - 4^2$$
 25

Yes, it is a circle. The circle has its center at (0, 4) and radius 5.

The equation of the circle is

$$(x4)^2 (y5)^2 4^2$$
.

Let y = 2 and solve for x:

$$(x4)^{2} (25)^{2} 4^{2}$$

$$(x4) (3) 4 (x4)$$

$$x = 4$$
 $\sqrt{7} x = 4 7 \sqrt{}$

The points of intersection are 4 $\sqrt{7}$, 2 and

24. Write the equation in center-radius form by completing the square on x and y separately:

$$x^2$$
 y^2 10x 24 y 144 0

$$x^{2}$$
 10 x y^{2} 24 y 144 0
(x = 10 x 25) (y= 24 y 144) 25 (x 5) =

$$(y 12)^2 25$$

The center of the circle is (5, 12) and the

radius is 25.2 y y 2 Now use the distance formula to find the distance from the center (5, 12) to the origin:

$$x^{2}$$
 2 x 1 y^{2} 16 y 64 -61 1 64
x 1^{2} y 8^{2} 4

$$\sqrt{\frac{1}{(5\,0)}^2 (12\,0)^2} \sqrt{\frac{25\,144\,13}{13}}$$

Yes, it is a circle. The circle has its center at (-1, -8) and radius 2.

The radius is 5, so the shortest distance from the origin to the graph of the circle is 13–5=8.

(continued on next page)

20 18

10

Section 2.6 Graphs of Basic Functions

$$2 y x^{2} 3 y \frac{1}{2} x$$
 $2 \frac{3}{2} x \text{ can be}$

217

any real number. Because the square of any real number is not negative, $2^{\frac{1}{2}}x^2$ is never negative. Taking the constant term into consideration, range would be 2, .

Each value of x corresponds to just one value of y. x^2 2 y 3 represents a

Graphs of Basic Functions

(a) The equation can be rewritten as

4 6 8 101214161820

1 3 4y x 6 y 4x 4 y 4x 2. x can be any real number, so the domain is all real numbers and the range is also all real numbers.

domain: , ; range: ,

Each value of x corresponds to just one value of y. x 4 y 6 represents a function.

1. The equation $\int_{0}^{\infty} x^{2}$ matches graph E.

The domain is,.

Section 2.6

2. The equation of fx x matches graph G.

The function is increasing on 0, .

3. The equation fx x^3 matches graph A.

The range is,.

Graph C is not the graph of a function. Its equation is $x y^2$.

Graph F is the graph of the identity function. Its equation is f x x.

The equation $fx \ x^{\square}$ matches graph B.

f 1.5 1

(a) The equation can be rewritten as

 v^2 5 x. y can be any real number.

Because the square of any real number is not negative, y^2 is never negative.

Taking the constant term into consideration, domain would be 5, . domain: 5, ; range:,

Because (-4, 1) and (-4, -1) both satisfy the relation, $y^2 x 5$ does not represent a function.

27. (a) $x 2^2 y^2$ 25 is a circle centered at

(-2, 0) with a radius of 5. The domain will start 5 units to the left of -2 and end

7. The equation $\int x_3 x^{\sqrt{}}$ matches graph H.

5 units to the right of -2. The domain will be [-2-5, 2+5] = [-7, 3]. The range

will start 5 units below 0 and end 5 units above 0. The range will be [0-5, 0+5] [-5, 5].

Because (-2, 5) and (-2, -5) both satisfy the relation, $x 2^2 y^2 25$ does not represent a function. No, there is no interval over which the function is decreasing.

8. The equation of $fx \sqrt{x}$ matches graph D.

The domain is 0, .

The graph in B is discontinuous at many points. Assuming the graph continues, the range would be $\{..., -3, -2, -1, 0, 1, 2, 3, ...\}$.

the domain and increase over part of the

domain. They both increase over 0, and

decrease over, 0.

The function is continuous over the entire domain of real numbers . .

The function is continuous over the entire domain of real numbers, .

The function is continuous over the interval 0, .

The function is continuous over the interval 0.

The function has a point of discontinuity at (3, 1). It is continuous over the interval 3 and the interval 3, .

The function has a point of discontinuity at *x* = 1. It is continuous over the interval ,1 and the interval 1, .

$$f(x) \stackrel{\textstyle 2x}{=} if x -1$$

$$\begin{array}{r}
 x - 1 \text{ if } x - 1 \text{ (-} \\
 5) 2(-5) - 10 \\
 \hline
 (b) \\
 \hline
 (-1) 2(-1) -2
 \end{array}$$

$$f(0) = 0 - 1 = -1$$

$$f(3) = 3 - 1 = 2$$

$$f(x) \begin{cases} x - 2 & \text{if } x \\ 3 \\ x & \text{if } x \end{cases} = 5 - 1$$

$$f(-5) = -5 - 2 = -7$$

$$f(-1) = -1 - 2 = -3$$

$$f(0) = 0 - 2 = -2$$

 $f(3) = 5 - 3 = 2$
 $2x \text{ if } x = -4$

19.
$$f(x) - x$$
 if -4×2 if $3x \times 2$

$$-2 x$$
 if $x -3$

$$fx 3x - 1 \text{ if } -3 x 2$$
$$-4x \text{ if } x 2$$

$$f(-5) = -2(-5) = 10$$

$$f(-1) = 3(-1) - 1 = -3 - 1 = -4$$

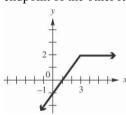
$$f(0) = 3(0) - 1 = 0 - 1 = -1$$

$$f(3) = -4(3) = -12$$

$$x - 1 \text{ if } x 3$$

21.
$$f(x)$$
 2 if x 3

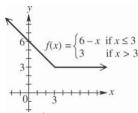
Draw the graph of y = x - 1 to the left of x = 3, including the endpoint at x = 3. Draw the graph of y = 2 to the right of x = 3, and note that the endpoint at x = 3 coincides with the endpoint of the other ray.



$$3$$
 if x 3

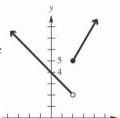
22.
$$f(x) = 6 - x$$
 if $x = 3$

Graph the line y = 6 - x to the left of x = 3, including the endpoint. Draw y = 3 to the right of x = 3. Note that the endpoint at x = 3 coincides with the endpoint of the other ray.



23.
$$f(x) = 4 - x \quad \text{if } x \neq 2$$

Draw the graph of y = 4 - x to the left of x = 2, but do not include the endpoint. Draw the graph of y = 1 + 2x to the right of x = 2, including the endpoint.



$$f(-5) = 2 + (-5) = -3$$

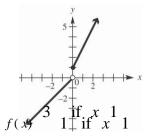
$$f(-1) = -(-1) = 1$$

$$f(0) = -0 = 0$$

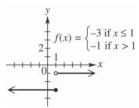
$$\int_{f(x)} 2x 1 \text{ if } x = 0$$

if
$$x = 0$$

Graph the line y = 2x + 1 to the right of x = 0, including the endpoint. Draw y = x to the left of x = 0, but do not include the endpoint.

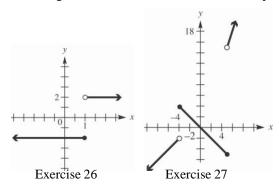


Graph the line y = -3 to the left of x = 1, including the endpoint. Draw y = -1 to the right of x = 1, but do not include the endpoint.



26.
$$f(x)^{2} \inf_{x \to 1} x$$

Graph the line y = -2 to the left of x = 1, including the endpoint. Draw y = 2 to the right of x = 1, but do not include the endpoint.



$$2x$$
 if $x-4$

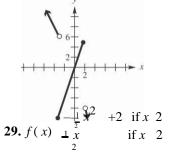
27.
$$f(x) - x$$
 if -4×5 if $3x \times 5$

Draw the graph of y = 2 + x to the left of -4, but do not include the endpoint at x = 4. Draw the graph of y = -x between -4 and 5, including both endpoints. Draw the graph of

$$-2x$$
 if $x - 3$

$$f(x) 3x - 1 \text{ if } -3 x 2$$

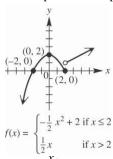
Graph the line y = -2x to the left of x = -3, but do not include the endpoint. Draw y = 3x - 1 between x = -3 and x = 2, and include both endpoints. Draw y = -4x to the right of x = 2, but do not include the endpoint. Notice that the endpoints of the pieces do not coincide.



Graph the curve $y = \frac{1}{x^2}x^2 = 2$ to the left of

x = 2, including the endpoint at (2, 0). Graph the line $y \stackrel{1}{=} x$ to the right of x = 2, but do

not include the endpoint at (2, 1). Notice that the endpoints of the pieces do not coincide.

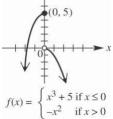


30.
$$f(x)$$
 5 if x 0

Graph the curve $y x^3 = 0$ 5 to the left of x = 0, including the endpoint at (0, 5). Graph the line $y x^2$ to the right of x = 0, but do

not include the endpoint at (0,0). Notice that

the endpoints of the pieces do not coincide.



y = 3x to the right of 5, but do not include the endpoint at x = 5.

31.
$$f(x)$$
 2 if 1 x 0

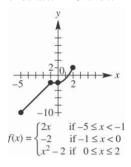
$$x^2$$
 2 if 0 x 2

Graph the line y = 2x between x = -5 and

x = -1, including the left endpoint at (-5, -10), but not including the right endpoint at (-1, -2). Graph the line y = -2 between x = -1 and x = 0, including the left endpoint at (-1, -2) and not including the right endpoint at (0, -2). Note that (-1, -2) coincides with the first two sections, so it is included. Graph

the curve
$$y x^2 2$$
 from $x = 0$ to $x = 2$,

including the endpoints at (0, -2) and (2, 2). Note that (0, -2) coincides with the second two sections, so it is included. The graph ends at x = -5 and x = 2.



32.
$$f(x) = \begin{cases} 0.5x^2 & \text{if } 4 \times 2 \text{ if } 2 \\ x & x & 2 \end{cases}$$

Graph the curve $y = 0.5x^2$ between x = -4

and x = -2, including the endpoints at

(-4, 8) and (-2, 2). Graph the line y x between x = -2 and x = 2, but do not include the endpoints at (-2, -2) and (2, 2). Graph the

curve
$$y x^2 4$$
 from $x = 2$ to $x = 4$,

including the endpoints at (2, 0) and (4, 12). The graph ends at x = -4 and x = 4.

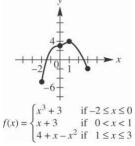
$$x^{3}$$
 3 if 2 x 0
33. $f(x)$ x 3 if 0 x 1
 $4xx^{2}$ if 1 x 3

Graph the curve $y x^3$ 3 between x = -2

and x = 0, including the endpoints at (-2, -5) and (0, 3). Graph the line y = x + 3 between x = 0 and x = 1, but do not include the endpoints at (0, 3) and (1, 4). Graph the curve

 $4 x x^2$ from x = 1 to x = 3, including the endpoints at (1, 4) and (3, -2). The graph

ends at x = -2 and x = 3.



$$2x$$
 if 3×1

34.
$$f(x) x^2 1$$
 if 1×2 $2 \cdot \frac{1}{2} x^3 1$ if 2×3

Graph the curve y = -2x to from x = -3 to = -1, including the endpoint (-3, 6), but not including the endpoint (-1, 2). Graph the

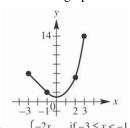
curve
$$y x^2$$
 1 from $x = -1$ to $x = 2$,

including the endpoints 2 (-1, 2) and (2, 5).

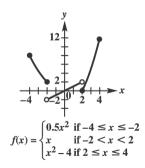
Graph the curve $y = \frac{1}{2}x^3$ 1 from x = 2 to

x = 3, including the endpoint (3, 14.5) but not including the endpoint (2, 5). Because the endpoints that are not included coincide with

endpoints that are included, we use closed dots on the graph.



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 \int

(a) The equation can be rewritten as

4 6 8 101214161820

<u>1</u> <u>6</u> <u>1</u>

3

4 y x 6 y 4x 4 y 4x 2. x can be any real number, so the domain is all real numbers and the range is also all real numbers.

domain:,; range:,

Each value of x corresponds to just one value of y. x 4 y 6 represents a function.

(a) The equation can be rewritten as

 y^2 5 x. y can be any real number.

Because the square of any real number is not negative, y^2 is never negative.

Taking the constant term into consideration, domain would be 5, . domain: 5, ; range: ,

Because (-4, 1) and (-4, -1) both satisfy the relation, $y^2 x 5$ does not represent a function.

27. (a) $x 2^2 y^2$ 25 is a circle centered at

$$2 y x^2 3 y 1x 2 23 x can be$$

217

any real number. Because the square of any real number is not negative, $2^{\frac{1}{2}}x^2$ is never negative. Taking the constant term into consideration, range would be $\frac{3}{2}$, .

domain:,; range: 3,

Each value of x corresponds to just one value of y. x^2 2 y 3 represents a

function. $y \stackrel{1}{=} x^2 \stackrel{3}{=} f_x \stackrel{1}{=} x^2 \stackrel{3}{=} 2$ $f \stackrel{2}{=} 2^2 \stackrel{3}{=} 1_4 \stackrel{3}{=} 4_{\stackrel{3}{=} 1_4} 2$

Section 2.6 Graphs of Basic Functions

1. The equation $\int_{0}^{\infty} x^{2}$ matches graph E.

The domain is , .

2. The equation of fx x matches graph G.

The function is increasing on 0, .

3. The equation fx x^3 matches graph A.

The range is,.

Graph C is not the graph of a function. Its equation is $x y^2$.

Graph F is the graph of the identity function. Its equation is f x x.

The equation $fx \ \mathbb{L}^{\square}$ matches graph B.

f 1.5 1

(-2, 0) with a radius of 5. The domain will start 5 units to the left of -2 and end

7. The equation $\int x_3 x^{\sqrt{}}$ matches graph H.

5 units to the right of -2. The domain will be [-2-5, 2+5] = [-7, 3]. The range

will start 5 units below 0 and end 5 units above 0. The range will be [0-5, 0+5] [-5, 5].

Because (-2, 5) and (-2, -5) both satisfy the relation, $x 2^2 y^2 25$ does not represent a function. No, there is no interval over which the function is decreasing.

8. The equation of $fx \sqrt{x}$ matches graph D.

The domain is 0, .

The graph in B is discontinuous at many points. Assuming the graph continues, the range would be $\{..., -3, -2, -1, 0, 1, 2, 3, ...\}$.

the domain and increase over part of the

domain. They both increase over 0, and

decrease over, 0.

The function is continuous over the entire domain of real numbers . .

The function is continuous over the entire domain of real numbers, .

The function is continuous over the interval 0, .

The function is continuous over the interval 0.

The function has a point of discontinuity at (3, 1). It is continuous over the interval 3 and the interval 3, .

The function has a point of discontinuity at *x* = 1. It is continuous over the interval ,1 and the interval 1, .

$$f(x) \stackrel{\textstyle 2x}{=} if x -1$$

$$\begin{array}{r}
 x - 1 \text{ if } x - 1 \text{ (-} \\
 5) 2(-5) - 10 \\
 \hline
 (b) \\
 \hline
 (-1) 2(-1) - 2
 \end{array}$$

$$f(0) = 0 - 1 = -1$$

$$f(3) = 3 - 1 = 2$$

$$f(x) \begin{cases} x - 2 & \text{if } x \\ 3 & \text{otherwise} \end{cases} 5 - x & \text{if } x \\ f(-5) = -5 - 2 = -7$$

$$f(-1) = -1 - 2 = -3$$

$$f(0) = 0 - 2 = -2$$

 $f(3) = 5 - 3 = 2$
 $2x \text{ if } x = -4$

19.
$$f(x) - x$$
 if -4×2 if $3x \times 2$

$$-2 x$$
 if $x -3$

$$fx 3x - 1 \text{ if } -3 x 2$$

$$-4x \text{ if } x 2$$

$$f(-5) = -2(-5) = 10$$

$$f(-1) = 3(-1) - 1 = -3 - 1 = -4$$

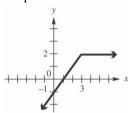
$$f(0) = 3(0) - 1 = 0 - 1 = -1$$

$$f(3) = -4(3) = -12$$

$$x - 1 \text{ if } x 3$$

21.
$$f(x)$$
 2 if x 3

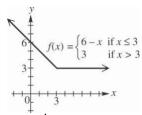
Draw the graph of y = x - 1 to the left of x = 3, including the endpoint at x = 3. Draw the graph of y = 2 to the right of x = 3, and note that the endpoint at x = 3 coincides with the endpoint of the other ray.



3 if x 3

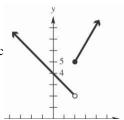
22.
$$f(x) = 6 - x$$
 if $x = 3$

Graph the line y = 6 - x to the left of x = 3, including the endpoint. Draw y = 3 to the right of x = 3. Note that the endpoint at x = 3 coincides with the endpoint of the other ray.



23.
$$f(x) = 4 - x$$
 if $x = 2$

Draw the graph of y = 4 - x to the left of x = 2, but do not include the endpoint. Draw the graph of y = 1 + 2x to the right of x = 2, including the endpoint.



$$f(-5) = 2 + (-5) = -3$$

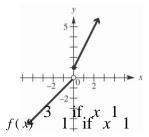
$$f(-1) = -(-1) = 1$$

$$f(0) = -0 = 0$$

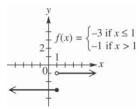
$$\int_{f(x)} 2x 1 \text{ if } x = 0$$

if
$$x = 0$$

Graph the line y = 2x + 1 to the right of x = 0, including the endpoint. Draw y = x to the left of x = 0, but do not include the endpoint.

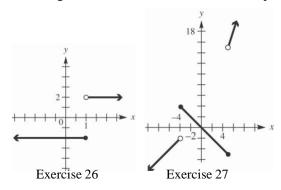


Graph the line y = -3 to the left of x = 1, including the endpoint. Draw y = -1 to the right of x = 1, but do not include the endpoint.



26.
$$f(x)^{2}$$
 if $x = 1$

Graph the line y = -2 to the left of x = 1, including the endpoint. Draw y = 2 to the right of x = 1, but do not include the endpoint.



$$2x$$
 if $x-4$

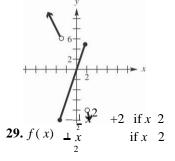
27.
$$f(x) - x$$
 if -4×5 if

Draw the graph of y = 2 + x to the left of -4, but do not include the endpoint at x = 4. Draw the graph of y = -x between -4 and 5, including both endpoints. Draw the graph of

$$-2x$$
 if $x - 3$

$$f(x) 3x - 1 \text{ if } -3 x 2$$

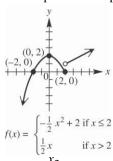
Graph the line y = -2x to the left of x = -3, but do not include the endpoint. Draw y = 3x - 1 between x = -3 and x = 2, and include both endpoints. Draw y = -4x to the right of x = 2, but do not include the endpoint. Notice that the endpoints of the pieces do not coincide.



Graph the curve $y = \frac{1}{x^2}x^2 = 2$ to the left of

x = 2, including the endpoint at (2, 0). Graph the line $y \stackrel{1}{=} x$ to the right of x = 2, but do

not include the endpoint at (2, 1). Notice that the endpoints of the pieces do not coincide.

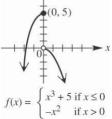


30
$$f(x)$$
 5 if x 0 if x 30

Graph the curve $y x^3 = 0$ 5 to the left of x = 0, including the endpoint at (0, 5). Graph the line $y x^2$ to the right of x = 0, but do

not include the endpoint at (0,0). Notice that

the endpoints of the pieces do not coincide.



y = 3x to the right of 5, but do not include the endpoint at x = 5.

31.
$$f(x)$$
 2 if 1 x 0

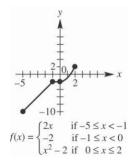
$$x^2$$
 2 if 0 x 2

Graph the line y = 2x between x = -5 and

x = -1, including the left endpoint at (-5, -10), but not including the right endpoint at (-1, -2). Graph the line y = -2 between x = -1 and x = 0, including the left endpoint at (-1, -2) and not including the right endpoint at (0, -2). Note that (-1, -2) coincides with the first two sections, so it is included. Graph

the curve
$$y x^2 2$$
 from $x = 0$ to $x = 2$,

including the endpoints at (0, -2) and (2, 2). Note that (0, -2) coincides with the second two sections, so it is included. The graph ends at x = -5 and x = 2.



32.
$$f(x) = \begin{cases} 0.5x^2 & \text{if } 4 \times 2 \text{ if } 2 \\ x & x & 2 \end{cases}$$

Graph the curve $y = 0.5x^2$ between x = -4

and x = -2, including the endpoints at

(-4, 8) and (-2, 2). Graph the line y x between x = -2 and x = 2, but do not include the endpoints at (-2, -2) and (2, 2). Graph the

curve
$$y x^2 4$$
 from $x = 2$ to $x = 4$,

including the endpoints at (2, 0) and (4, 12). The graph ends at x = -4 and x = 4.

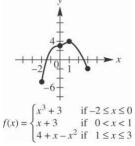
$$x^{3}$$
 3 if 2 x 0
33. $f(x)$ x 3 if 0 x 1
 $4xx^{2}$ if 1 x 3

Graph the curve $y x^3$ 3 between x = -2

and x = 0, including the endpoints at (-2, -5) and (0, 3). Graph the line y = x + 3 between x = 0 and x = 1, but do not include the endpoints at (0, 3) and (1, 4). Graph the curve

 $4 x x^2$ from x = 1 to x = 3, including the endpoints at (1, 4) and (3, -2). The graph

ends at x = -2 and x = 3.



$$2x$$
 if 3×1

34.
$$f(x) x^2 1$$
 if 1×2 $2 \cdot \frac{1}{2} x^3 1$ if 2×3

Graph the curve y = -2x to from x = -3 to = -1, including the endpoint (-3, 6), but not including the endpoint (-1, 2). Graph the

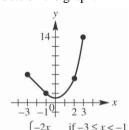
curve
$$y x^2$$
 1 from $x = -1$ to $x = 2$,

including the endpoints 2 (-1, 2) and (2, 5).

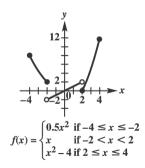
Graph the curve $y = \frac{1}{2}x^3$ 1 from x = 2 to

x = 3, including the endpoint (3, 14.5) but not including the endpoint (2, 5). Because the endpoints that are not included coincide with

endpoints that are included, we use closed dots on the graph.



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The solid circle on the graph shows that the endpoint (0, -1) is part of the graph, while the

open circle shows that the endpoint (0, 1) is not part of the graph. The graph is made up of

parts of two horizontal lines. The function which fits this graph is

$$f(x) - 1 \text{ if } x = 0$$
if $x = 0$.

domain:,; range: $\{-1, 1\}$

36. We see that y = 1 for every value of x except x = 0, and that when x = 0, y = 0. We can write the function as

$$\begin{array}{cccc}
f(x) & 1 & \text{if } x & 0 \\
& 0 & \text{if } x & 0.
\end{array}$$

domain: , ; range: {0, 1}

The graph is made up of parts of two

horizontal lines. The solid circle shows that the endpoint (0, 2) of the one on the left belongs to the graph, while the open circle

the right does not belong to the graph. The function that fits this graph is

$$f(x) = \frac{2}{1} \inf_{x = 1}^{x} x^{0} = 1$$

We see that y = 1 when x = 1 and that y = -1

$$f(x) = 1 \text{ if } x - 1$$

domain: -1 if x = 2.

$$(-,-1]$$
 (2,); range: $\{-1,1\}$

through the points (-1, -1) and (0, 0). The slope is 1, so the equation of this piece is y =x. For x > 0, that piece of the graph is a horizontal line passing through (2, 2), so its

equation is y = 2. We can write the function as

$$f(x) = \begin{cases} x & \text{if } x & 0 \\ 2 & \text{if } x & 0 \\ \text{domain: } (-,) & \text{range: } (,0] & \square\{2\} \end{cases}$$

For x < 0, that piece of the graph is a horizontal line passing though (-3, -3), so the equation of this piece is y = -3. For x = 0, the curve passes through (1, 1) and (4, 2), so the

equation of this piece is \sqrt{x} . We can

Section 2.6 Graphs of Basic Functions For x < 1, that piece of the graph is a curve passes through (-8, -2), (-1, -1) and (1, 1), so

the equation of this piece is $y \sqrt[3]{\sqrt{.}}$. The right

piece of the graph passes through (1, 2) and (2, 3). $m = \frac{23}{12} 1$, and the equation of the

line is y 2 x 1 y x 1. We can write

the function as
$$f(x) = 3x$$
 if $x = 1$

$$x 1 \text{ if } x 1$$

$$x \mid \text{ if } x \mid$$
 domain: $(-,)$ range: $(,1) \mid \boxed{[2,)}$

For all values except x = 2, the graph is a line. It passes through (0, -3) and (1, -1). The slope is 2, so the equation is y = 2x - 3. At x = 2, the graph is the point (2, 3). We can write

the function as
$$f(x)$$
 3 if $x = 2$
2x 3 if $x = 2$

domain:
$$(-,)$$
 range: $(,1) \square (1,)$

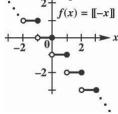
$$f(x) = x^{\text{I}}$$

Plot points.

	-xf(x)	$\mathbf{y} = \mathbf{x}^{\square}$
-2	2	2
−2 −1.5	1.5	1
-1	1	1
-0.5	0.5	0
0	0	0
0.5	-0.5	-1
1	-1	-1
1.5	-1.5	-2
2 More gene	−2 rally to ge	t v = 0 we

$$1 \ x \ 2 \qquad -2 \ x \ 1.$$

Follow this pattern to graph the step function.



write the function as f(x) $\sqrt{\quad}$ if $x \neq 0$ domain: , ; range: $\{...,-2,-1,0,1,2,...\}$ domain: (-,) range: $\{3\} \square [0,)$

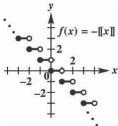
Chapter 2 Graphs and Functions

$$f(x) = x$$

Plot points.

	x		f(x) = x
_			
	-2 -1.5	-2 -2 -1	2 2
	-1	-1	1
	-0.5	-1	1
	0	0	0
	0.5	0	0
	1	1	-1
	1.5	1	-1
	2	2	-2
		l	

Follow this pattern to graph the step function.



domain:,; range: {...,-2,-1,0,1,2,...}

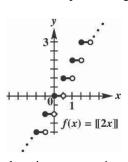
$$f(x) = 2x^{-1}$$

To get y = 0, we need 0 2 x 1 0 x $\frac{1}{x}$.

To get y = 1, we need $1 \ 2 \ x \ 2 \ 1 \ x \ 1$.

To get y = 2, we need 2 2 x 3 1 x - 1.

Follow this pattern to graph the step function.



domain:,; range: {...,-2,-1,0,1,2,...}

$$g(x) = 2 x 1^{$$

To get y = 0, we need

0 2 x 1 1 1 2 x 2
$$\frac{1}{x}$$
 x 1.
To get y = 1, we need

$$12x-1222x31x$$
 2.

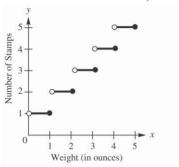
Follow this pattern to graph the step function.

g(x) = [2x - 1]

domain: , ; range: {..., 2,-1,0,1,2,...}

The cost of mailing a letter that weighs more

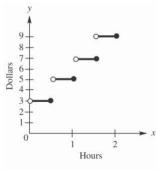
same as the cost of a 2-ounce letter, and the cost of mailing a letter that weighs more than 2 ounces and less than 3 ounces is the same as the cost of a 3-ounce letter, etc.

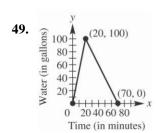


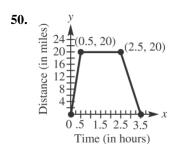
The cost is the same for all cars parking

between $\frac{21}{2}$ hour and 1-hour, between 1 hour

and $1^{\frac{1}{2}}$ hours, etc.







51. (a) For 0 x 8,
$$m = \frac{49.8 \ 34.2}{8.0} 1.95$$
,

so
$$y 1.95x 34.2$$
. For 8 $x 13$, $52.2 49.8$

0.48 , so the equation

is *y* 52.2 0.48(*x* 13) 0.48*x* 45.96

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(b)
$$f(x) = \begin{cases} 1.95x & 34.2 \text{ if } 0 = x \text{ 8} \\ 0.48x & 45.96 \text{ if } 8 = x \text{ 13} \end{cases}$$

When 0×3 , the slope is 5, which means that the inlet pipe is open, and the outlet pipe is closed. When 3×5 , the slope is 2, which means that both pipes are open. When 5×8 , the slope is 0, which means that both pipes are closed. When 8×10 , the slope is -3, which means that the inlet pipe is closed, and the outlet pipe is open.

(a) The initial amount is 50,000 gallons. The final amount is 30,000 gallons.

The amount of water in the pool remained constant during the first and fourth days.

$$f(2)$$
 45, 000; $f(4)$ 40, 000

The slope of the segment between (1, 50000) and (3, 40000) is -5000, so the

water was being drained at 5000 gallons per day.

(a) There were 20 gallons of gas in the tank at x = 3

The slope is steepest between t = 1 and

 $t \approx 2.9$, so that is when the car burned

gasoline at the fastest rate.

55. (a) There is no charge for additional length, units. so we use the greatest integer function.

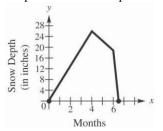
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$$6.5x$$
 if 0 x 4

56. (a)
$$f(x) 5.5x 48 \text{ if } 4 \times 6$$

$$-30 \times 195 \text{ if } 6 \times 6.5$$

Draw a graph of y = 6.5x between 0 and 4, including the endpoints. Draw the graph of y = -5.5x + 48 between 4 and 6, including the endpoint at 6 but not the one at 4. Draw the graph of y = -30x + 195, including the endpoint at 6.5 but not the one at 6. Notice that the endpoints of the three pieces coincide.



From the graph, observe that the snow depth, y, reaches its deepest level (26 in.) when x = 4, x = 4 represents 4 months after the beginning of October, which is the beginning of February.

From the graph, the snow depth *y* is nonzero when *x* is between 0 and 6.5. Snow begins at the beginning of October and ends 6.5 months later, in the middle of April.

Section 2.7 Graphing Techniques

To graph the function $f x x^2 3$, shift the

graph of $y x^2$ down 3 units.

To graph the function $fx x_2 5$, shift the

graph of $y x^2$ up $\underline{5}$ units.

$$f x_{\mathcal{X} 4^2}$$
 is obtained by

The graph of

shifting the graph of $y x^2$ to the left 4 units.

4. The graph of $fx \times 7^2$ is obtained by shifting the graph of $y \sqrt{x^2}$ to the <u>right</u> 7 units.

The cost is based on multiples of two

feet, so
$$f(x)$$
 0.8 $\frac{1}{2}$ if 6 x 18.

(b)
$$\frac{8.5}{100}$$
 0.8(4) \$3.20

$$f(15.2) \quad 0.8 \frac{15.2}{2}$$
 0.8(7) \$5.60

- **5.** The graph of fx x is a reflection of the graph of fx x across the x-axis.
- **6.** The graph of fx x is a reflection of the graph of fx x across the \underline{y} -axis.

Chapter 2 Graphs and Functions

To obtain the graph of $fx ext{ } x ext{ } 2^3 ext{ } 3$, shift the graph of $y ext{ } x^3 ext{ } 2$ units to the left and $\underline{3}$ units down.

To obtain the graph of $fx \times 3^3$ 6, shift the graph of gx^3 2 units to the right and 6 units up.

9. The graph of fx x | is the same as the graph of y x | because reflecting it across the \underline{y} -axis yields the same ordered pairs.

The graph of x y 2 is the same as the graph of x y 2 because reflecting it across the \underline{x} -axis yields the same ordered pairs.

- 11. (a) B; $y(x7)^2$ is a shift of $y(x^2)$, 7 units to the right.
 - (b) D; $y x^2$ 7 is a shift of $y x^2$, 7 units downward.

E; $y 7 x^2$ is a vertical stretch of $y x^2$, by a factor of 7.

- (d) A; $y (x7)^2$ is a shift of $y x^2$, 7 units to the left.
- (e) C; $y x^2$ 7 is a shift of $y x^2$, 7 units upward.
- 12. (a) E; $y = 4^3 \sqrt{x}$ is a vertical stretch of $y = 3\sqrt{x}$, by a factor of 4.

(c) G; $y(x^2)^2$ is a shift of $y(x^2)$, 2 units to the left.

(d) C; $y(x^2)^2$ is a shift of $y(x^2)$, 2 units to the right.

F; $y \ 2x$ is a vertical stretch of $y \ x$, by a factor of 2.

D; $y \times x$ a reflection of $y \times x$, across the x-axis.

- (g) H; $y (x^2)^2 1$ is a shift of $y x^2$, 2 units to the right and 1 unit upward.
- (h) E; $y(x^2)^2 = 1$ is a shift of y^2 , 2 units to the left and 1 unit upward.
- (i) I; $y(x^2)^2 = 1$ is a shift of $y^2 = x^2$, 2 units to the left and 1 unit down.

14. (a) G; y = x 3 is a shift of y = x, 3 units to the left.

- (b) D; $y = x \ 3$ is a shift of $y = x \ 3$ units downward.
- (c) E; $y = \sqrt{x} + 3$ is a shift of $y = x\sqrt{x} + 3$ units upward.

B; $y \ni x$ is a vertical stretch of $y \mid x$, by a factor of 3.

- (e) C; $y x\sqrt{\ }$ is a reflection of $y x\sqrt{\ }$ across the x-axis.
- (f) A; $y = x\sqrt{3}$ is a shift of y = x, $\sqrt{}$

(b) C; $y \ ^3 x \sqrt{}$ is a reflection of $y \ ^3 x$, 3 units to the right. Copyright © 2017 Pearson Education, Inc.

over the *x*-axis.

D;
$$y^3 x \sqrt{s}$$
 a reflection of $y^3 x$, over the y-axis.

- (d) A; $y^3 \sqrt{4}$ is a shift of $y^3 x$, 4 units to the right.
- (e) B; $y = \sqrt[3]{4}$ is a shift of $y = \sqrt[3]{x}$ 4 units down.
- 13. (a) B; $y x^2 2$ is a shift of $y x^2$, 2 units upward.
 - **(b)** A; $y x^2 2$ is a shift of $y x^2$, 2 units downward.

- (g) H; $y = \sqrt{x3/2}$ is a shift of $y = x \sqrt{3}$ units to the right and 2 units upward.
- (h) F; $y = \sqrt{x \cdot 3} \cdot 2$ is a shift of $y = x\sqrt{3} \cdot 3$ units to the left and 2 units upward.
- (i) I; $y = \sqrt{x \cdot 3}$ 2 is a shift of $y = x \cdot \sqrt{x \cdot 3}$ 3 units to the right and 2 units downward.
- **15.** (a) F; $y \neq 2$ is a shift of $y \neq 1$ 2 units to the right.
 - **(b)** C; $y \in [2]$ is a shift of $y \in [3]$ units downward.
 - (c) H; $y \in \mathbb{Z}$ is a shift of $y \in \mathbb{Z}$ units upward.

D; $y \ 2x$ is a vertical stretch of yx by a factor of 2.

G; y = x is a reflection of

x across the x-axis.

(f) A; $y \times |$ is a reflection of $y \times |$ across the y-axis.

E; $y \ 2x$ is a reflection of $y \ 2x$ | |

across the x-axis. y | 2x | is a vertical

stretch of y x by a factor of 2.

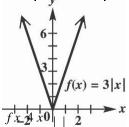
I; $y \times 2 = 2$ is a shift of $y \times 2 = 1$ units to the right and 2 units upward.

B; $y \times 2 = 2$ is a shift of $y \times 2$ units to the left and 2 units downward.

16. The graph of $fx 2x1^3$ 6 is the graph

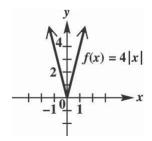
of $f x x^3$ stretched vertically by a factor of 2, shifted left 1 unit and down 6 units. f x 3 x

	. ' '	
x	hxx	fx3x
-2	2	6
-1	1	3
0	0	0
1	1	3
2	v 2	6



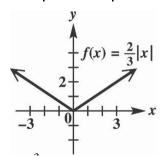
10

,	. 11	.	
x	h x x	fx 4x	
-2	2	8	_
-1	1	4	_
0	0	0	_
1	1	4	_
2	2	8 0	– Copyright © 2017 Pearson Education, Inc



19. f.	$\begin{bmatrix} x & 2 & x \\ 3 & 3 \end{bmatrix}$			
	3			
		1		

x	h x x	$fx^{\frac{2}{3}}x3$
-3	3	2
-2	2	<u>4</u> 3
-1	1	2 <u>3</u>
0	0	0
1	1	2 3
2	2	<u>4</u> <u>3</u>
3	3	2



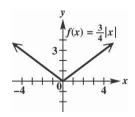
20.
$$fx \stackrel{5}{=} x4$$

0	0	0
1	1	<u>3</u> 4
2	2	<u>3</u> 2
3	3	9 4
4	4	3

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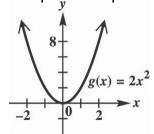
Chapter 2 Graphs and Functions

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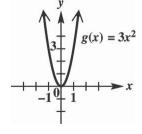
 $fx 2x^2$

x	$h x x^2$	$fx 2x^2$
-2	4	8
-1	1	2
0	0	0
1	1	2
2	4	8



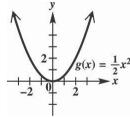
 $f x 3x^2$

х	$h x x^2$	$fx 3x^2$
-2	4	12
-1	1	3
0	0	0
1	1	3
2	4	12



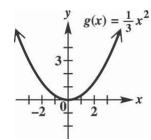
$$fx \pm x^2$$

		2	
	x	$h x x^2$	$fx^{\frac{1}{2}}x^22$
	-2	4	2
	-1	1	1/2
	0	0	0
•	1	1	$\frac{1}{2}$
,	2	4	2

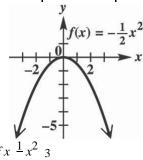


 $fx \frac{1}{2}x^2$

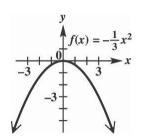
$\int x - x 3$			
x	$h x x^2$	$fx^{\frac{1}{2}}x^23$	
-3	9	3	
-2	4	4/3	
-1	1	1 3	
0	0	0	
1	1	1 <u>3</u>	
2	4	4/3	
3	Q	3	



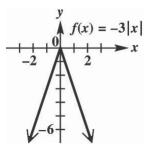
f	$fx \stackrel{1}{=} x^2$ 2				
	х	$h x x^2$	$fx \stackrel{1}{=} \frac{X^2}{2}$		
	-3	9	9		
	-2	4	2		
	-1	1	1 2		
	0	0	0		
	1	1	1 2		
	2	4	2		
	3	9	9 2		



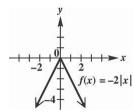
x	$h x x^2$	$fx^{-1}x^2$
-3	9	-3
-2	4	<u>4</u> 3
-1	1	1 3
0	0	0
1	1	1 3
2	4	<u>4</u> 3
3	9	-3



f x 3 x		
x	hxx	$fx \ 3x \ \ $
-2	2	-6
-1	1	-3
0	0	0
1	1 _	-3
2	2	-6



28.	, J x 2	^x	
	x	h x x	fx 2x
	-2	2	-4
	-1	1	-2
	0	0	0
	- 1		

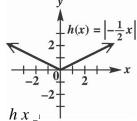


29. $h x^{-1} x$				
	x	fx x	1 1	$\begin{array}{c c} h & x & 2^{\frac{1}{2}} \\ & & \frac{1}{2} & x & 1 \\ & & & & \end{array}$
	-4	4		2
	-3	3		3 2
	-2	2		1
	-1	1		$\frac{1}{2}$
	0	0		0

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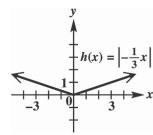
(continued)

x	fx x	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
1	1	1/2
2	2	1
3	3	3 2
4	4 v	2



30.
$$\begin{bmatrix} n & x \\ x \end{bmatrix}^{-1} \begin{bmatrix} 1 \\ 3 \end{bmatrix}$$

	x	$fx \stackrel{!}{=} x \mid 3$	$\begin{array}{c cccc} hx & x & 3 & & \\ & x & 3 & & 3 & \\ & & 3 & & 3 & \end{array}$
	-3	3	1
•	-2	2	2 3
•	-1	1	1 3
	0	0	0
	1	1	1 3
	2	2	2 3
	3	3	1

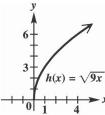


	x	$fx x\sqrt{}$	h x	$\sqrt{4x} 2 x \sqrt{}$
,	0	0	0	
,	1	<u>√</u> 1	_2	
٠	2	2	$2^{\sqrt{2}}$ 2	

x	$fx x\sqrt{}$	h x	$4\sqrt{x} 2x \sqrt{}$
3	$\sqrt{3}$	2	
4	2	4	
$h(x) = \sqrt{4x}$ 1 1 4 x			

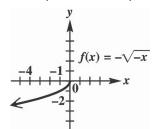
		_
32.	h x	$9\sqrt{x}$
J4.	$n\lambda$	スル

x	$\int fx x\sqrt{}$	$hx 9x - 3x \sqrt{}$
0	0	0
1	1	3
2	$\sqrt{2}$	3
3	$\sqrt{3}$	3
4	2	6



33. fx = x

	٧	
x	$\begin{array}{ccc} h x & x \\ & \sqrt{} \end{array}$	fx x
-4	2	-2
-3	$\sqrt{3}$	J ³
-2	$\sqrt{2}$	$\sqrt{\frac{2}{1}}$
-1	1	-1
0	0	0



x	h x x	$fx x \mid$	
-3	3	-3	
-2	2	-2	
-1	1	-1	
0	0	0	
1	1	-1	
2	2	-2	
3	3	-3	
f(x) = - -x -3 -3 -3 -3			

35. (a) y f x 4 is a horizontal translation of f, 4 units to the left. The point that corresponds to (8, 12) on this translated function would be 8 4,12 4,12.

> f x 4 is a vertical translation of f, 4 units up. The point that corresponds to (8, 12) on this translated function would be 8,12 4 8,16.

 $\frac{1}{4}fx$ is a vertical shrinking of f, by a 1. The point that corresponds factor of

36. (a)

(8, 12) on this translated

function would be 8, 1 412 8, 3.

4 f x is a vertical stretching of f, by a factor of 4. The point that corresponds to (8, 12) on this translated function would be 8, 4 12 8, 48.

$$y \ f(4x)$$
 27. (8) is about our of details

by a factor of 4. The point that corresponds to (8, 12) on this translated function is $8\frac{1}{2}$, 12 2, 12.

 $f^{\perp}x$ is a horizontal stretching of f, by a factor 4 of 4. The point that corresponds to (8, 12) on this translated function is 8 4, 12 32, 12.

Section 2.7 Graphing Techniques

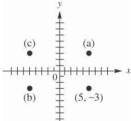
229 (a) The point that corresponds to (8, 12) when reflected across the x-axis would be (8, -12).

> The point that corresponds to (8, 12)when reflected across the y-axis would be (-8, 12).

(a) The point that is symmetric to (5, -3)with respect to the x-axis is (5, 3).

> The point that is symmetric to (5, -3)with respect to the y-axis is (-5, -3).

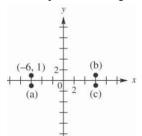
The point that is symmetric to (5, -3)with respect to the origin is (-5, 3).



(a) The point that is symmetric to (-6, 1)with respect to the x-axis is (-6, -1).

> The point that is symmetric to (-6,1) with respect to the y-axis is (6, 1).

The point that is symmetric to (-6, 1) with respect to the origin is (6, -1).



(a) The point that is symmetric to (-4, -2)with respect to the x-axis is (-4, 2).

> The point that is symmetric to (-4, -2)with respect to the y-axis is (4, -2).

The point that is symmetric to (-4, -2) with respect to the origin is (4, 2).

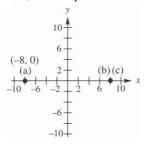
Chapter 2 Graphs and Functions

(a) The point that is symmetric to (-8, 0) with respect to the *x*-axis is (-8, 0) because this point lies on the *x*-axis.

The point that is symmetric to the point

(-8, 0) with respect to the y-axis is (8, 0).

The point that is symmetric to the point (-8, 0) with respect to the origin is (8, 0).



The graph of y = |x - 2| is symmetric with respect to the line x = 2.

The graph of y = -|x + 1| is symmetric with respect to the line x = -1.

$$y x^2 5$$

Replace x with -x to obtain

 $(x)^2$ 5 x^2 5. The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Because *y* is a function of *x*, the graph cannot be symmetric with respect to the *x*-axis. Replace with -x and y with -y to obtain $y(x)^2$ 2 y x^2 2 y x^2 2.

The result is not the same as the original equation, so the graph is not symmetric with

respect to the origin. Therefore, the graph is symmetric with respect to the *y*-axis only.

$$y 2 x^4 3$$

Replace x with -x to obtain

$$2(x)^4 3 2 x^4 3$$

The result is the same as the original equation, so the graph is symmetric with respect to the y-

axis. Because *y* is a function of *x*, the graph cannot be symmetric with respect to the

x-axis. Replace x with -x and y with -y to

obtain $-y 2(x)^4 3 y 2 x^4 3 y 2 x^4 3$. The result is not the same as the original

$$x^2 y^2 12$$

Replace x with -x to obtain

$$(x)^2 y^2 12 x^2 y^2 12$$
.

The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace *y* with –*y* to obtain

$$x^{2} (y)^{2} 12 x^{2} y^{2} 12$$

The result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis. Because the graph is symmetric with respect to the *x*-axis and *y*-axis, it is also symmetric with respect to the origin.

$$v^{2} x^{2} 6$$

Replace x with -x to obtain

$$y^2 x^2 6 y^2 x^2 6$$

The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace y with -y to obtain

$$(y)^2 x^2 6 y^2 x^2 6$$

The result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis. Because the graph is symmetric with respect to the *x*-axis and *y*-axis, it is also symmetric with respect to the origin. Therefore, the graph is symmetric with respect to the *x*-axis, the *y*-axis, and the origin.

$$y + 4x^3 x$$

Replace x with $-x$ to obtain

$$y \ 4(x)$$
 $(x) \ y \ 4(x) x$
 $y \ 4x^3 \ x$.

The result is not the same as the original equation, so the graph is not symmetric with respect to the y-axis. Replace y with -y to

obtain
$$y 4x x y 4x x$$

The result is not the same as the original equation, so the graph is not symmetric with respect to the x-axis. Replace x with -x and y with -y to obtain

$$y \ 4(x)^3 (x) y \ 4(x^3) x$$

equation, so the graph is not symmetric with respect to the origin. Therefore, the graph is symmetric with respect to the *y*-axis only.

The result is the same as the original equation, so the graph is symmetric with respect to the origin. Therefore, the graph is symmetric with respect to the origin only.

$$y x^3 x$$

Replace x with -x to obtain

$$(x)^3 (x) y x^3 x$$
.

The result is not the same as the original

equation, so the graph is not symmetric with respect to the y-axis. Replace y with -y to

obtain y x = x y x = x x. The result

is not the same as the original equation, so the graph is not symmetric with respect to the x-axis. Replace x with -x and y with -y to obtain $y(x)^3(x) y x^3 x y x^3 x$. The

result is the same as the original equation, so

the graph is symmetric with respect to the origin. Therefore, the graph is symmetric with respect to the origin only.

51.
$$y x^2 x 8$$

Replace x with -x to obtain $y(x)^{2}(x)8yx^{2}x8.$

The result is not the same as the original equation, so the graph is not symmetric with

respect to the y-axis. Because y is a function of x, the graph cannot be symmetric with respect to the x-axis. Replace x with -x and y with -y

to obtain
$$y(x)^{2}(x) = 8$$

 $y(x^{2})^{2}(x) = 8$

The result is not the same as the original equation, so the graph is not symmetric with respect to the origin. Therefore, the graph has none of the listed symmetries.

52.
$$y = x + 15$$

Replace *x* with –*x* to obtain (*x*) 15 *y x* 15.

The result is not the same as the original equation, so the graph is not symmetric with respect to the y-axis. Because y is a function of x, the graph cannot be symmetric with respect to the x-axis. Replace x with -x and y with -yto obtain y(x) 15 y x 15. The

result is not the same as the original equation,

so the graph is not symmetric with respect to the origin. Therefore, the graph has none of

the listed symmetries.

Section 2.7 Graphing Techniques
$$fx \ x^5 \ 2x^3$$

The function is odd.

55.
$$fx = 0.5x^4 \ 2x^2 \ 6$$

$$fx = 0.5 x^4 2 x^2 6$$

 $0.5x^4 2x^2 6 fx$

The function is even.

56.
$$fx = 0.75x^2 = x + 4$$

$$fx = 0.75x^2 = x + 4$$

$$0.75x^2 = x + 4$$

$$0.75x^2 = x + 4$$

The function is even.

$$fx x^3 x 9$$

57.
$$fx x^3 x 9$$

 $x x 9 x x 9 x x 9 fx$

The function is neither.

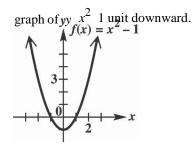
58.
$$fx x^4 5x 8$$

$$fx \quad x^4 \quad 5 \quad x \quad 8$$
$$x^4 \quad 5x \quad 8 \quad fx$$

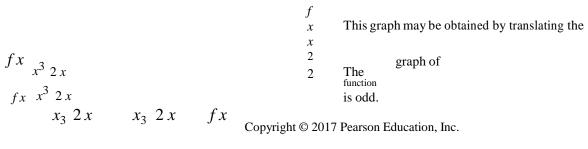
The function is neither.

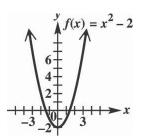
$$\int fx x^2 1$$

This graph may be obtained by translating the



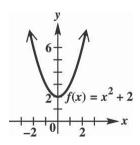
60.





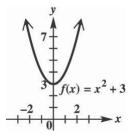
y x² 2 unit s dow nwa rd. Chapter 2 Graphs and Functions $fx x^2 2$

This graph may be obtained by translating the graph of $y x^2 2$ units upward.



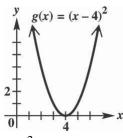
$$fx x^2 3$$

This graph may be obtained by translating the graph of $y x^2 3$ units upward.



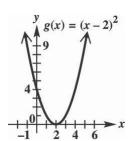
$$g x x 4^2$$

This graph may be obtained by translating the graph of $y x^2 4$ units to the right.



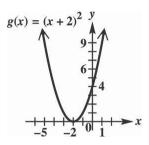
$$g x x 2^2$$

This graph may be obtained by translating the graph of $y x^2$ 2 units to the right.



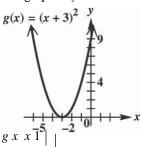
$$g x x 2^2$$

This graph may be obtained by translating the graph of $y x^2 2$ units to the left.

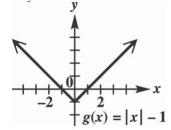


3²

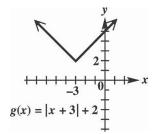
This graph may be obtained by translating the graph of $y x^2 3$ units to the left.



The graph is obtained by translating the graph of $y \neq 1$ unit downward.



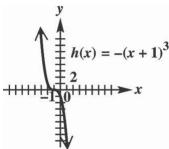
 $g \times x \times 3 = 2$ This graph may be obtained by translating the graph of $y \times 3$ units to the left and 2 units upward.



233

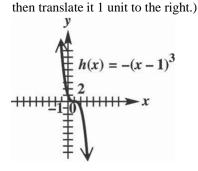
Section 2.7 Graphing Techniques

This graph may be obtained by translating the graph of $y x^3$ 1 unit to the left. It is then reflected across the x-axis.



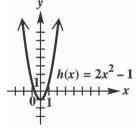
$$hx(x1)^3$$

This graph can be obtained by translating the graph of $y x^3$ 1 unit to the right. It is then reflected across the x-axis. (We may also reflect the graph about the x-axis first and

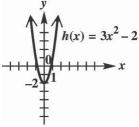


$$h \times 2 x^2 + 1$$

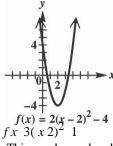
This graph may be obtained by translating the graph of $y x^2 1$ unit down. It is then stretched vertically by a factor of 2.



This graph may be obtained by stretching the graph of $y x^2$ vertically by a factor of 3, then shifting the resulting graph down 2 units.

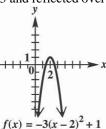


This graph may be obtained by translating the graph of $y x^2$ 2 units to the right and 4 units down. It is then stretched vertically by a factor of 2.



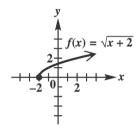
This graph may be obtained by translating the graph of $y x^2 2$ units to the right and 1 unit

up. It is then stretched vertically by a factor of 3 and reflected over the *x*-axis.



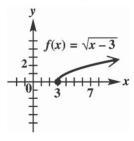
75.
$$fx$$
 $x \ge \frac{x}{\sqrt{x}}$

This graph may be obtained by translating the graph of \sqrt{y} x two units to the left.



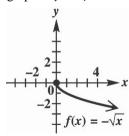
This grades y be obtained by translating the

graph of $y = \sqrt{x}$ three units to the right.



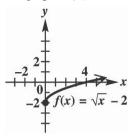
77.
$$fx x$$

This graph may be obtained by reflecting the graph of y x across the x-axis.



78.
$$fx$$
 $x = 0$

This graph may be obtained by translating the graph of $y\sqrt{x}$ two units down.



79.
$$fx = 2 \sqrt{x} = 1$$

This graph may be obtained by stretching the graph of y x vertically by a factor of two

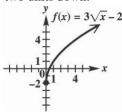
and then translating the resulting graph one unit up.

80.
$$f \times 3$$
 $\times 2$

This graph may be obtained by stretching the

graph of
$$y = \frac{x}{\sqrt{}}$$
 vertically by a factor of

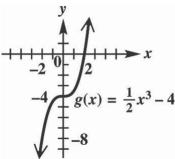
three and then translating the resulting graph two units down.



$$g x \frac{1}{2} x^3 4$$

This graph may be obtained by stretching the graph of $y x^3$ vertically by a factor of $\frac{1}{2}$,

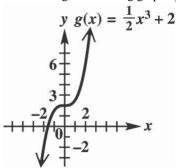
then shifting the resulting graph down four units.

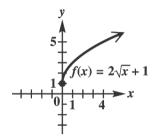


82.
$$g x^{-1} x_3^3 = 2$$

This graph may be obtained by stretching the graph of $y x^3$ vertically by a factor of $\frac{1}{2}$,

then shifting the resulting graph up two units.

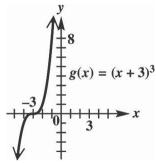




$$g x x 3^3$$

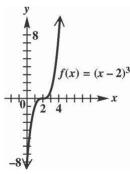
This graph may be obtained by shifting the

graph of $y x^3$ three units left.



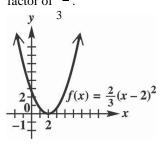
$$fx x 2^3$$

This graph may be obtained by shifting the graph of $y x^3$ two units right.



85.
$$fx = 2x 2_3^2$$

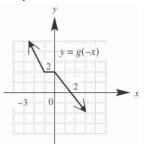
This graph may be obtained by translating the graph of $y x^2$ two units to the right, then stretching the resulting graph vertically by a factor of $\frac{2}{3}$.



Because g(x) x x f(x), the graphs are the same.

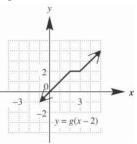
87. (a)
$$y = g(-x)$$

The graph of g(x) is reflected across the y-axis.



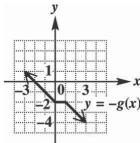
$$y = g(x - 2)$$

The graph of g(x) is translated to the right 2 units.



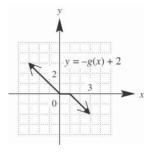
$$y = -g(x)$$

The graph of g(x) is reflected across the *x*-axis.



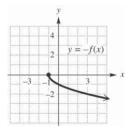
$$y = -g(x) + 2$$

The graph of g(x) is reflected across the *x*-axis and translated 2 units up.



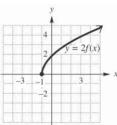
88. (a) y f x

The graph of f(x) is reflected across the *x*-axis.



y 2 f x

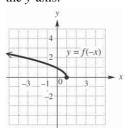
The graph of f(x) is stretched vertically by a factor of 2.



y f x

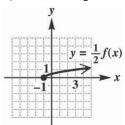
The graph of f(x) is reflected across

the y-axis.



(d)
$$y = \frac{1}{2} f^{y}$$

The graph of f(x) is compressed vertically by a factor of $\frac{1}{2}$.



It is the graph of fx xtranslated 1 unit to

90. It is the graph of
$$gx$$

x translated 4 units

to the left, reflected across the *x*-axis, and translated two units up. The equation is

$$\chi \sqrt{x \ 4 \ 2}$$
.

91. It is the graph of $fx \sqrt{x}$ translated one

unit right and then three units down. The equation is $y \sqrt{x \cdot 13}$.

92. It is the graph of fx x | | translated 2 units

to the right, shrunken vertically by a factor of $\frac{1}{2}$, and translated one unit down. The equation is $y + x = 2 \cdot 1$

It is the graph of $g \times \blacksquare$ translated 4 units

to the left, stretched vertically by a factor of 2, and translated four units down. The equation is $y \ 2\sqrt{x} \ 4$.

It is the graph of $fx \ x \mid$ reflected across

the x-axis and then shifted two units down. The equation is $y \times 2$.

Because f(3) = 6, the point (3, 6) is on the graph. Because the graph is symmetric with respect to the origin, the point (-3, -6) is on the graph. Therefore, f(-3) = -6.

Because f(3) = 6, (3, 6) is a point on the graph. The graph is symmetric with respect to the y-axis, so (-3, 6) is on the graph. Therefore, f(-3) = 6.

97. Because f(3) = 6, the point (3, 6) is on the graph. The graph is symmetric with respect to the line x = 6 and the point (3, 6) is 3 units to

the left of the line x = 6, so the image point of (3, 6), 3 units to the right of the line x = 6 is (9, 6). Therefore, f(9) = 6.

98. Because f(3) = 6 and f(-x) = f(x), f(-3) = f(3). Therefore, f(-3) = 6.

99. Because (3, 6) is on the graph, (-3, -6) must also be on the graph. Therefore, f(-3) = -6.

100. If f is an odd function, f(-x) = -f(x). Because f(3) = 6 and f(-x) = -f(x), f(-3) = -f(3). Therefore, f(-3) = -6.

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the left, reflected across the *x*-axis, and translated 3 units up. The equation is $y \mid x \mid |3$.

$$f(x) = 2x + 5$$

Translate the graph of f(x) up 2 units to obtain the graph of

$$t(x)(2 \times 5)22 \times 7.$$

Now translate the graph of t(x) = 2x + 7 left 3 units to obtain the graph of g(x) 2(x3) 7 2 x 6 7 2x 13.

(Note that if the original graph is first translated to the left 3 units and then up 2 units, the final result will be the same.)

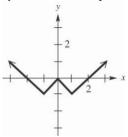
$$f(x) = 3 - x$$

Translate the graph of f(x) down 2 units to

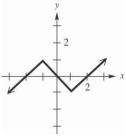
obtain the graph of t(x) (3 x) 2 x 1. Now translate the graph of t x x 1 right 3 units to obtain the graph of g(x) (x 3) 1 x 3 1 x 4.

(Note that if the original graph is first translated to the right 3 units and then down 2 units, the final result will be the same.)

(a) Because f(-x) = f(x), the graph is symmetric with respect to the y-axis.

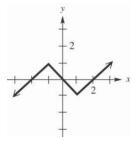


Because f(-x) = -f(x), the graph is symmetric with respect to the origin.

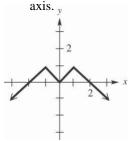


104. (a) f(x) is odd. An odd function has a graph

symmetric with respect to the origin. Reflect the left half of the graph in the origin.



f(x) is even. An even function has a graph symmetric with respect to the *y*-axis. Reflect the left half of the graph in the *y*-axis.



Chapter 2 Quiz (Sections 2.5-2.7)

1. (a) First, find the slope: *m*

Choose either point, say, (-3, 5), to find the equation of the line: $y ext{ 5 } 2(x(3)) y 2(x 3) ext{ 5}$ $2x ext{ 11}$.

To find the *x*-intercept, let y = 0 and solve for x: $0.2 x 11 x \frac{11}{x}$. The 2 *x*-intercept is $\frac{11}{x}$.

Write 3x - 2y = 6 in slope-intercept form to find its slope: $3x \ 2y \ 6y \ ^{\frac{3}{2}}x \ 3$.

Then, the slope of the line perpendicular to this graph is $\frac{2}{3}$. $y \ 4^{\frac{2}{3}}(x \ 3(6))$

$$y = \frac{2}{3}(x 6)) 4 y = \frac{2}{3}x$$

- **3.** (a) x 8 (b) y 5
- **4.** (a) Cubing function; domain: (,); range: (,); increasing over (,).
 - (b) Absolute value function; domain:(,); range: [0,); decreasing over(, 0); increasing over (0,)

Cube root function: domain: (,);

range: (,) ; increasing over
 (,) .

$$fx = 0.40 x^{1} = 0.75$$

$$f 5.5 \ 0.40 \ 5.5 \ 0.75$$

 $0.40 \ 5 \ 0.75 \ 2.75$

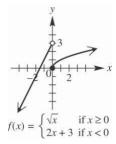
A 5.5-minute call costs \$2.75.

6.
$$f(x) = x\sqrt{1 + (x^2 + x^2)^2}$$
 if $x = 0$

For values of x < 0, the graph is the line y = 2x + 3. Do not include the right endpoint

(0, 3). Graph the line $y \times x$ for values of

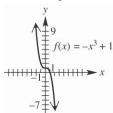
 $x \ge 0$, including the left endpoint (0, 0).



$$f(x) x^{3} 1$$

Reflect the graph of $f(x) x^3$ across the

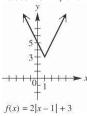
x-axis, and then translate the resulting graph one unit up.



8.
$$f(x) 2x | 13 |$$

Shift the graph of f(x) |x| one unit right,

stretch the resulting graph vertically by a factor of 2, then shift this graph three units up.



9. This is the graph of
$$g(x) = x$$
, translated

four units to the left, reflected across the *x*-axis, and then translated two units down.

The equation is
$$y = \begin{cases} \sqrt{x} & 42 \end{cases}$$

10. (a)
$$fx x^2 7$$

Replace x with $-x$ to obtain

$$x(x)^{2}7 f$$

$$xx^{2}7fx$$

The result is the same as the original function, so the function is even.

$$fx x^3 x 1$$

Replace x with -x to obtain

The result is not the same as the original equation, so the function is not even. Because $fx ext{ } fx$, the function is

not odd. Therefore, the function is neither even nor odd.

$$\begin{array}{ccc}
fx & x^{101} & x^{99} \\
\text{Replace } x & \text{with } -x & \text{to obtain} \\
& & & & & & & & & & & \\
101 & & & & & & & & & \\
\end{array}$$

$$fx x$$
 x

$$\chi^{101} \chi^{99}$$

Because f(-x) = -f(x), the function is odd.

Section 2.8 Function Operations and Composition

In exercises 1–10, $fx = x \cdot 1$ and $gx = x^2$.

212 7

$$212^{2}$$

$$212^2$$
 12

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5.
$$f g 2 fg 2 f2^2 2^2 15$$

6.
$$g^{-1} f^2 g f^2 g^2 1^2 1^2 9$$

f is defined for all real numbers, so its domain is

g is defined for all real numbers, so its domain

is,.

f + g is defined for all real numbers, so its domain is , .

f

10. g is defined for all real numbers except those

values that make $g \times 0$, so its domain is $0 \cup 0$, .

In Exercises 11–18, f(x) x^2 3 and g(x) 2x 6.

$$(f g)(5) f(5) g(5)$$

 $[(5)^2 3] [2(5) 6]$

28 16 44

$$[(1)^2 \ 3] [2(1) \ 6]$$

484

$$(f g)(4) f(4) g (4)$$

$$[(4)^{2} 3] [2(4) 6]$$

$$19 (2) 21$$

$$(fg)(4) f(4) g (4)$$

(fg)(4) f(4) g(4)

19 (2) 38

$$(fg)(3) f(3) g(3)$$

$$[(3)^{2} 3] [2(3) 6]$$

$$12 12 144$$

$$f$$
 $\underline{f(1)}$ $(\underline{1})^2 \underline{3}$ $\underline{4} \underline{1}$ $\underline{}$

17. (1)
$$g$$
 $g(1)$ $2(1) 6$ $8 2$ f $f(5)$

$$(f g)(x) f(x) g(x) (3x 4) (2 x 5) x 9 (fg)(x) f(x) g(x) (3x 4)(2 x 5) 6x2 15x 8x 20 6x2 7 x 20$$

$$f(x)f(x) = 3x4$$

$$g(x) = 2x5$$

The domains of both f and g are the set of all real numbers, so the domains of f + g, f - g, and fg are all, . The domain of f is the g set

of all real numbers for which

gx 0. This is the set of all real numbers except $\frac{5}{2}$, which is written in interval notation

as
$$,\frac{5}{1} = \frac{5}{2}, \dots$$

20.
$$f(x) = 6 - 3x, g(x) = -4x + 1 (fg)(x)f(x)g(x)$$

$$(6 3x) (4x 1)$$

$$7 x 7$$

$$(f g)(x)f(x)g(x)$$

$$(6 3x) (4 x 1) x 5$$

$$(fg)(x)f(x)g(x) (6 3x)(4 x 1)$$

$$2$$

$$24x 6 12x 3x$$

$$12 x^2 27 x 6$$

$$f(x) f(x) g(x) (6 3x)$$

$$(x) g(x) 4x 1$$

The domains of both f and g are the set of all real numbers, so the domains of f + g, f - g, and fg are all, . The domain of

 g^f is the set of all real numbers for which g x 0. This is the set of all real numbers

1

except 4, which is written in interval notation

as
$$-$$
, $\frac{1}{2}$ $\frac{1}{2}$,...
 $f(x) 2 x^2 3x$, $g(x) x^2 x 3 (fg)(x)$
 $(2 x^2 3x) (x^2 x 3)$
 $(2 x^2 3x) (x^2 x 3)$

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 $\frac{(5)^{\frac{2}{3}}}{(2x^2 3x)(x^2 x 3)}$

19.
$$f(x) 3x4, g(x) 2x5$$

 $(f g)(x) f(x) g(x)$
 $(3x4) (2x5) 5x1$

$$2x^2 3x x^2 x 3$$
$$x^2 2x 3$$

(continued on next page)

Chapter 2 Graphs and Functions (continued)

$$(fg)(x)f(x)g(x)$$

$$(2x^{2} 3x)(x^{2} x 3)$$

$$2x^{4} 2x^{3} 6x^{2} 3x^{3} 3x^{2} 9x$$

$$2x^{4} 5x^{3} 9x^{2} 9x$$

$$f(x)$$

$$g(x) x^{2} x 3$$

The domains of both f and g are the set of all real numbers, so the domains of f+g, f-g, and fg are all , . The domain of

 $-g^f$ is the set of all real numbers for which

 $g \times 0$. If $x^2 \times 30$, then by the quadratic formula $x^{1 i 11}$. The <u>equation</u> has no real solutions. There are no real numbers which make the denominator zero.

Thus, the domain of f is also , .

$$f(x) 4x^{2} 2x, g(x) x^{2} 3x 2 (f$$

$$g)(x) f(x) g(x)$$

$$(4x^{2} 2x) (x^{2} 3x 2)$$

$$5x^{2} x 2$$

$$(f g)(x) f(x) g(x)$$

$$(4x^{2} 2x) (x^{2} 3x 2)$$

$$4x^{2} 2x x^{2} 3x 2$$

$$3x^{2} 5x 2$$

$$(fg)(x) f(x) g(x)$$

$$(4 x2 2 x)(x2 3x 2)$$

$$4x4 12 x3 8x2 2x3 6 x2 4 x$$

$$4x4 10 x3 2 x2 4 x$$

$$\frac{f}{g} \qquad \frac{f(x)}{g} \qquad \frac{4x^{-2}2x}{3x^2}$$

$$g \qquad g(x) \qquad x^2 \quad 3x \quad 2$$

The domains of both f and g are the set of all

23.
$$f(x) = \sqrt{4x \, 1}, g(x) = \frac{1}{x}$$

$$(f g)(x) f(x) g(x) = \sqrt{4x \, 1} = \frac{1}{x}$$

$$(f g)(x) f(x) g(x) = \sqrt{4x \, 1} = \frac{1}{x}$$

$$(fg)(x) f(x) g(x) = \sqrt{4x \, 1} = \frac{1}{x}$$

$$f(x) = \frac{f(x)}{x} = \frac{4x \, 1}{x} = \sqrt{4x \, 1}$$

$$g(x) = \frac{1}{x} = \frac{1}{x}$$

Because $4 \times 104 \times \sqrt{x4}$, the domain of f is $^{1}4$, . The domain of g is 0.0, . Considering the intersection of the domains of f and g, the domains of f + g,

$$f-g$$
, and fg are all $\frac{1}{4}$, . Because $\frac{f}{g}$ for any value of f , the domain of f is also

$$f(x) \xrightarrow{f(x)} 5x \xrightarrow{4} x$$
 re al nu

mbers, so the domains of f+g, f-g, $x^2 3x$ are all, . The domain of f is the set of all real numbers x such that Copyright © 2017 Pearson Education, Inc.

 x^2 3x 2 0. Because and fg

5*x* 4

$x^2 3x 2 (x 1)(x 2)$, the numb	ers which
give this denominator a value	

$$x = 1$$
 and $x = 2$. Therefore, the domain of f is

the set of all real numbers except 1 and 2, which is written in interval notation as

$$(-,1) \ \Box (1,2) \ \Box (2,1).$$

$$g$$
 $g(x)$ $\sqrt{\frac{1}{x}}$ Because $5x 405x 4x$ $\frac{4}{x}$, the domain of

$$f$$
 is $\frac{4}{5}$, . The domain of g is $\sqrt{9}$ 0, . Considering the intersection

of the domains of
$$f$$
 and g , the domains of $f+g$, $f-g$, and fg are all $\frac{4}{5}$, $\frac{1}{x}$ 0 for any

value of x, so the domain of
$$\frac{g}{x}$$
 is also

4

5, .

M 2008 280 and F 2008 470, thus

T 2008 *M* 2008 *F* 2008 280 470 750 (thousand).

M 2012 390 and F 2012 630, thus T 2012 M 2012 F 2012

390 630 1020 (thousand).

Looking at the graphs of the functions, the slopes of the line segments for the period 2008–2012 are much steeper than the slopes of the corresponding line segments for the period 2004–2008. Thus, the number of associate's degrees increased more rapidly during the period 2008–2012.

If 2004
$$k$$
 2012, $T(k)$ r , and $F(k) = s$, then $M(k) = r - s$.

T S 2000 T 2000 S 2000

19136

It represents the dollars in billions spent for general science in 2000.

T G 2010 T 2010 G 2010

29 11 18

It represents the dollars in billions spent on space and other technologies in 2010.

Spending for space and other technologies spending decreased in the years 1995–2000 and 2010–2015.

Total spending increased the most during the years 2005–2010.

(d)
$$f(1) = \frac{f(1)}{1} = \frac{1}{1}$$

(a)
$$(f g)(0) f(0) g(0) 022$$

(b)
$$(f \ g)(1) f(1) g(1)$$
 2 1 3

(c)
$$(fg)(1) f(1) g(1) 2 1 2$$

(d)
$$\frac{f}{}$$
 (2) $\frac{f(2)}{}$ $-\frac{4}{}$ 2

35. (a)
$$(f g)(1) f(1) g(1) 03 3$$

(b)
$$(f g)(2) f(2)g(2)$$

14 5

(c)
$$(fg)(0)$$
 $f(0)g(0)122$

(d)
$$f$$
 (2) $f(2)$ 3 undefined g (2) 0

36. (a)
$$(f \ g)(1) \ f(1) \ g(1) \ 3 \ 1 \ 2$$

 $(f \ g)(0) \ f(0) \ g(0) \ 2 \ 0 \ 2$

(c)
$$(fg)(1)$$
 $f(1)$ $g(1)$ $3(1)$ 3

$$\begin{array}{cccc}
 & f & & \underline{f(1)} & \underline{3} \\
 & & & & 3 \\
 & & & g(1) & 1
\end{array}$$

(d)
$$f(0) \overline{f(0)} \underline{5}$$
 undefined

$$g(0) = 0$$

(d)
$$f$$
 (0) 8 8

39.	x	fx	g x	f	$\int g x$	fg x	f
	-2	0	6	066	066	060	- 0 6 0
	0	5	0	5 0 5	5 0 5	50 0	$\frac{5}{0}$ undefined
	2	7	-2	72 5	729	7 2 14	$\frac{7}{2}$ 3.5
	4	10	5	10515	1055	105 50	$\frac{10}{5}$ 2
40.	х	fx	g x	f g x	f g x	fg x	f_{x}
40.	<i>x</i> –2	f x -4	g x 2	f g x 4 2 2	f gx 426	fg x 4 2 8	g 4 2
40.							g
40.	-2	-4	2	422	4 2 6	428	g ⁴ 2 ⁸ 8

41. Answers may vary. Sample answer: Both the slope formula and the difference quotient

represent the ratio of the vertical change to the horizontal change. The slope formula is stated for a line while the difference quotient is stated for a function f.

- **42.** Answers may vary. Sample answer: As *h* approaches 0, the slope of the secant line *PQ* approaches the slope of the line tangent of the curve at *P*.
- **43.** fx = 2x
 - (a) f(xh) 2(xh) 2xh
 - **(b)** f(xh) f(x) (2xh) (2x)2xh 2xh

f(xh)f(x) h

(c)
$$1$$
 h h

$$f(x h) 1 (x h) 1 x h$$

 $f(x h) f(x) (1 x h) (1 x) 1 x$
 $h 1 x h$

f(xh)f(x) h

(c)
$$h$$
 1 h

- (a) f(xh) 6(xh) 2 6x6h2
- **(b)** f(xh) f(x) (6x6h2)(6x2)6x6h26x26h
- (c) $\frac{f(xh) \cdot f(x)}{h} = 6$
- **46.** *f x* 4 *x* 11
 - (a) f(xh) = 4(xh) 11 4 x 4h 11
 - **(b)** f(xh) f(x) (4 x 4h 11) (4x 11)4 x 4h 11 4x 11 4h

(c)
$$\frac{f(xh)f(x)\overline{4h}}{h} = 4$$

$$f(x h) 2(x h) 5 2x$$

$$2h 5$$

$$f(x h) f(x)$$

$$(2 x 2h 5) (2x 5)$$

$$2x 2h 5 2x 5 2h$$

f(xh)f(x) = 2h

$$f(xh) 4(xh) 2$$

$$4x 4h 2$$

$$f(xh) f(x)$$

(c)
$$\frac{f(xh) f(x)}{h} = \frac{4h}{h} 4$$

49.
$$f(x) x$$

(a)
$$f(xh) = \frac{1}{xh}$$

$$\frac{f(xh) f(x)}{h} \underbrace{\frac{1}{x}}_{x xh}$$

$$\frac{h}{x x h}$$

(c)
$$\frac{f(xh)f(x) xxh}{h} \quad \frac{h}{hx x h} \\
-\frac{1}{x h}$$

(b)
$$f(xh) f(x)$$

 $xh^2 x^2 x^2 xh^2$
 $xh^2 x^2 x^2 xh^2$
 $x^2 x^2 2xh h^2 2xh h^2$
 $x^2 x h^2 x^2 xh^2$

$$\frac{f(x h) f(x)}{x^{2} h} \frac{2xh h^{2}}{2xh h^{2}} - - 2$$

$$f(x) x^2$$

$$f(x h) (x h)^{2} x^{2} 2 x h h^{2}$$

 $f(x h) f(x) x^{2} 2x h h^{2} x^{2}$

(c)
$$\frac{f(xh)f(x)}{h} = \frac{2xh h^2}{h}$$
$$\frac{h(2xh)}{h}$$
$$2xh$$

52.
$$f(x) x^2$$

(b)
$$f(xh) f(x) x$$
 2 $2xh h$ 2 x

$$x^2 2 xh h^2 x^2$$
$$2 xh h^2$$

(c)
$$\frac{f(x h) f(x)}{2xh h^2}$$

$$\begin{array}{c}
h\\
h(2x h)\\
h\\
2x h
\end{array}$$

53.
$$f(x) 1 x$$

$$f(x h) 1 (x h)$$

 $1 (x^2 2xh h^2)$

$$1 x$$
 $^2 2 xh h^2$

$$(1 x^{2} 2 xh h^{2}) (1 x^{2})$$
 $1 x 2 xh h 1 x$
 $2xh h^{2}$

(c)
$$\frac{f(xh)}{h} \cdot \frac{f(x)}{h} = \frac{2xh h^2}{h}$$

$$\frac{h(2xh)}{h}$$

$$2xh$$

(c)
$$h \qquad h \qquad -\frac{1}{2} \qquad 2 \qquad 12x^2$$

$$h^2xh \qquad hx \qquad xh \qquad f(x) \quad 12x^2$$

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(b)
$$f(xh) f(x)$$

 $1 2 x^2 4 xh 2h^2 1 2 x^2$
 $1 2 x^2 4xh 2h^2 1 2x^2$
 $4 xh 2h^2$

(c)
$$\frac{f(xh) f(x)}{h} = \frac{4xh 2h^2}{h}$$
$$\frac{h}{h(4x 2h)}$$
$$h$$
$$4x 2h$$

$$f(x) x^2 3x 1$$

$$f(xh)xh^2 3xh1$$

$$2 xhh^2 3x3h1$$

$$f(x h) f(x)$$

$$2 2xh h^2 3x 3h 1$$

$$xh h^2 3h$$

(c)
$$\frac{f(xh) f(x)}{h} = \frac{2xh h^2 3h}{h}$$

$$\frac{h(2xh3)}{h}$$

$$2xh3$$

56.
$$f(x) x^2 4x2$$

(a)
$$f(xh)xh^2 4xh2$$

 $x^2 2xhh^2 4x4h2$

$$f(x h) f(x)$$

$$^{2} 2xh h^{2} 4x 4h 2$$

$$^{2} 4x 2$$

$$^{2} 2xh h^{2} 4x 4h 2x^{2} 4x 2$$

$$^{2} 2xh h^{2} 4h$$

(c)
$$\frac{f(xh) f(x)}{h} \quad \frac{2xh h^2 4h}{h} \\ \frac{h(2xh 4)}{h}$$

$$f \stackrel{\text{\tiny 0}}{=} g \, 2fg \, 2 \qquad \qquad f5$$

$$g \parallel f3 g \qquad f3 \qquad g3330$$

$$g \, \hat{\mathbb{I}} \, f \, 0 \, g \qquad f \, 0 \qquad g \, 3$$

$$g \ f2 \ gf2 \ g7$$
737310

$$f \stackrel{\parallel}{=} f2 f$$
 $f2 f f1 2 1 3 1$

$$g \circ g \circ 2 \circ g \circ g \circ 2 \qquad \qquad g \circ 5 \circ 3 \circ 2$$

65.
$$(f \circ g)(2) f (g \circ (2)) f(3) 1$$

66.
$$(f^{[]}g)(7) f[g(7)] f(6) 9$$

67.
$$(g \mid f)(3) g[f(3)] g(1) 9$$

68.
$$(g^{\text{d}}f)(6)$$
 $g[f(6)]$ g (9) 12

69.
$$(f^{[]}f)(4)$$
 $f[f(4)]$ f (3) 1

70.
$$(g^{[]}g)(1)g[g(1)]g(9)$$

71.
$$(f^{[]}g)(1)f[g(1)]f(9)$$
 However, $f(9)$ cannot be determined from the table given.

72.
$$(g^{[]}(f g))(7) g(f(g (7)))$$

73. (a)
$$(f g)(x) f(g(x))$$
 $f(5x7)$

f(5x7) © 2017 Pearson Education, Inc.

The domain and range of both f and g are (,), so the domain of fg is (,).

$$(g^{[]}f)(x) \ g(f(x)) \ g(6x9)$$

$$5(6x9) 7$$

$$30x 45 7 \ 30x 52$$

The domain of $g \mid f$ is (,).

74. (a)
$$(f^{\parallel} g)(x)$$
 $f(g(x))$ $f(3x 1)$ 8(3x 1) 12 24x 8 12 24x 4

The domain and range of both f and g are (,), so the domain of f g is

$$(g^{[]}f)(x)g(f(x))g(8x$$

12) 3(8x 12) 1

The domain of $g \mid f$ is (,).

75. (a)
$$(f \ g)(x) \ f(g(x)) \ f(x3)$$
 $\sqrt{x3}$

The domain and range of g are (,), however, the domain and range of f are [0,). So, $x \ 3 \ 0 \ x \ 3$.

Therefore, the domain of $f \mid g$ is

[3,).

(b)
$$(g^{-1}f)(x) g(f(x)) g \sqrt{x} \sqrt{x} 3$$

The domain and range of g are (,), however, the domain and range of f are [0,). Therefore, the domain of $g \, \Box \, f$ is [0,).

76. (a)
$$(f \ g)(x) \ f(g(x)) \ f(x \ 1)$$

The domain and range of g are $(,)$,

however, the domain and range of f are [0,). So, $x \ 1 \ 0 \ x \ 1$. Therefore,

the domain of f is [1,).

(b)
$$(g^{[]}f)(x) \ g \ (f(x)) \ g \ \sqrt{x} \ \sqrt{x} \ 1$$

The domain and range of g are (,),

however, the domain and range of f are

$$(g^{3}f)(x) g(f(x)) g(x^{3})$$

$$x^6 3x^3 1$$

The domain and range of f and g are (,), so the domain of g f is (,).

78. (a)
$$(\int_{a}^{\pi} g(x)f(g(x))f(x^4 x^2 4)$$

$$\begin{array}{cccc} x^4 & x^2 & 4 & 2 \\ x^4 & x^2 & 2 & \end{array}$$

The domain of f and g is (,), while the range of f is (,) and the range of

g is 4, , so the domain of $f \square g$ is (,).

(b)
$$(g^{[]}f)(x) g(f(x)) g(x2)$$

$$(x2)^4 (x2)^2 4$$

The domain of f and g is (,), while

the range of f is (,) and the range of g is 4, , so the domain of g f is (,

79. (a)
$$(f g)(x) f(g(x)) f(3x)$$
 $\sqrt{3x \cdot 1}$

The domain and range of g are (,), however, the domain of f is [1,), while the range of f is [0,). So, $3x \ 1 \ 0 \ x^{\frac{1}{2}}$. Therefore, the

domain of
$$f^{\Box}$$
 g is ¹

(b)
$$(g^{\parallel}f)(x) \ g(f(x)) \ g\sqrt{x \, 1}$$

$$\sqrt[3]{1}$$

The domain and range of g are (,), however, the range of f is [0,). So

$$x ext{ 1 0 } x ext{ 1 . Therefore, the domain}$$
of $g ext{ } f_{ ext{ is } [1,)}$.

[0,). Therefore, the domain Copyrifg ht f@is2017 Pearson Education, Inc.

80. (a) (f g)(x) f(g(x)) f(2x)

2x2

[0,).

77. (a) $(f \circ g)(x)$ f(g(x)) $f(x^2 \circ 3x \circ 1)$

The domain and range of f and g are (,), so the domain of $f \, \Box g$ is (,).

The domain and range of g are (,), however, the domain of f is [2,). So, 2 x 2 0 x 1 . Therefore, the domain of f g is 1, .

Chapter 2 Graphs and Functions

(b)
$$(g^{[]}f)(x) g(f(x)) g = x2$$

The domain and range of g are (,), however, the range of f is [0,). So

x 2 0 x 2. Therefore, the domain

of
$$g^{[]}f$$
 is $[2,)$.

x 1

(a)
$$(f \ g)(x) f(g(x)) f(x 1)^{-2}$$

The domain and range of g are (,), however, the domain of f is $(, 0) \square (0,)$. So, $x \ 1 \ 0 \ x \ 1$.

Therefore, the domain of fg is (,1)(1,).

П

(b)
$$(g^{[]}f)(x) g(f(x)) g^{2}$$

Therefore, the domain of $g \, {}^{[]} f$ is (,0) (0,) .

82. (a)
$$(f \mid g)(x) f(g(x)) f(x4) = 4$$

x 4

The domain and range of g are (,), however, the domain of f is (, 0) (0,). So, $x ext{ 4 } 0 ext{ } x ext{ 4 }$. Therefore, the domain of $f ext{ } g$ is (, 4) (4,).

(b)
$$(g \circ f)(x) g(f(x)) g^{\frac{4}{x}} \stackrel{4}{\xrightarrow{}_{x}} 4$$

(b)
$$(g^{\parallel}f)(x) g(f(x)) g \qquad x2 \qquad \frac{1}{\sqrt{x^2}}$$

The domain of f is [2,) and its range is [0,). The domain and range of g are (0, 0) [0,). So $x \ge 0$ $x \ge 2$.

Therefore, the domain of $g \mid f$ is (2,).

84. (a)
$$(f^{[]}g)(x) f(g(x)) f^{\frac{2}{3}} = \frac{2}{3} 4 = \sqrt{\frac{1}{3}}$$

The domain and range of g are (0,0), however, the domain of f is [4,). So, $\frac{2}{3}$ 40 x

 $x \ 0 \text{ or } x \ 2$ (using test intervals).

Therefore, the domain of $f \mid g$ is

, 0 2, -

(b) $(g^{\Box}f)(x) g(f(x)) g$ x = 4 The domain of f is [4,) and its range is [0,). The domain and range \blacksquare are (, 0) (0,). So $x = 4 \cdot 0 \cdot x = 4 \cdot 0 \cdot 0 \cdot 0 = 4 \cdot 0 \cdot 0 = 4$

Therefore, the domain of $g \ f$ is (4,).

85. (a)
$$(f \ g)(x) f(g(x)) f x 5$$
 $x 5$

The domain of g is $(5, 5)$ $(5, 1)$, and the range of g is $(5, 0)$ $(5, 1)$. The domain of f is $[0, 1)$. Therefore, the domain of $[f]$ $[g]$ is $[f]$.

(b)
$$(g \ f)(x) \ g \ (f(x)) \ g \ x$$
 $\frac{1}{x5}$

The domain and range of f is [0,). The domain of g is (, 5) (5,).

Therefore, the domain of g f is [0,).

domain of $g \mid f$ is (0,0)(0,0).

<u>3</u> <u>3</u>

x x

83. (a)
$$(f \square g)(x) f(g(x)) f^{\perp} = \frac{1}{2} 2$$

The domain and range of
$$g$$
 are $(0,0)$ $\square(0,1)$, however, the domain of f is $[2,1)$. So, $[2,1]$

$$x = 0$$
 or $x = \frac{1}{2}$ (using test intervals).

Therefore, the domain of
$$f \mid g$$
 is

$$,0$$
 $\frac{1}{2}$,.

$$(f^{\square}g)(x) f(g(x)) f x 6 \qquad \sqrt{x 6}$$

The domain of
$$g$$
 is $(, 6) \square (6,)$, and the

range of
$$g$$
 is $(0, 0)$ (0, 1). The domain of f is $[0, 1)$. Therefore, the domain of f (g is g).

(b)
$$(g \ f)(x) \ g(f(x)) \ g \ \frac{\sqrt{x}}{6}$$

The domain and range of f is [0,). The domain of g is $(, 6) \square (6,)$.

Therefore, the domain of $g \ ^{[]} f$ is [0,).

87. (a)
$$(f \parallel g)(x) f(g(x)) f^{\frac{1}{2}} \xrightarrow{x}$$

x = 1/x 21 2x

The domain and range of g are

(,0) (0,) . The domain of f is

 $(, 2) \square (2,)$, and the range of f is

$$(0, 0)$$
 $(0, 0)$ $(0, 0)$ So $(0, 0)$ $(0, 0)$ So $(0, 0)$ or

$$0 \times \frac{1}{2}$$
 or $x \frac{1}{2}$ (using test intervals).

Thus, x = 0 and x = 1. Therefore, the domain of f = 0 g is

$$0, 0^{\square}$$
 $0, 2^{\square}$ $2, .$

(b)
$$(g | f)(x) g (f(x)) g^{-1}$$
.

$$x = 1 (x = 2)$$

2

The domain and range of g are (, 0)(0,). The domain of f is (, 2)(2,), and the range of f is (, 0)(0,). Therefore, the domain of

$$g \, \, \, \, f \, \, \text{is} \, (,2) \, \, \, \, \, \, (2,).$$

88. (a)
$$(f | g)(x) f(g(x)) f^{\frac{1}{2}} - \frac{1}{2}$$

$$-\frac{x}{14x}$$
 $x = 1x4$

The domain and range of g are (0, 0) (0, 1). The domain of f is

$$(4)$$
, and the range of f is

$$(0, 0)^{\square}$$
 (0,). So, $(0, 0)^{\square}$ (0,). So, $(0, 0)^{\square}$

or 0
$$x = \frac{1}{4}$$
 or 1 4 $x = 0$ $x = \frac{1}{4}$

(using test intervals). Thus, $x \neq 0$ and $x \neq \frac{1}{4}$. Therefore, the domain of $f \mid g$ is

$$0, 0 = 0, \frac{1}{4} = \frac{1}{4}, \dots$$

(b)
$$(g | f)(x) g(f(x)) g^{-1}$$

$$f(x)$$
 is odd, so $f(1)$ $f(1)$ (2) 2.

Because g(x) is even, g(1) g(1) 2 and

$$g(2) g(2) 0. (f^{[]} g)(1) 1, so$$

$$fg(1)$$
 1 and $f(2)$ 1. $f(x)$ is odd, so

$$f(2) f(2) 1$$
. Thus,

$$(f^{[]}g)(2) fg(2) f(0)$$
 0 and

$$(f^{[]}g)(1)$$
 $fg(1) f(2) 1$ and

$$(f | g)(2) f g(2) f(0) = 0.$$

x	-2	-1	0	1	2
fx	-1	2	0	-2	1
g x	0	2	1	2	0
$f^{\square} gx$	0	1	-2	1	0

Answers will vary. In general, composition of functions is not commutative. Sample answer:

ñ

Thus, f g x is not equivalent to g fx.

92.
$$f = g x f g x f^3 x 7$$

$$\sqrt[3]{7}$$
 3

$$g^{\parallel}fx \ gfx \ gx^3 \qquad 7$$

93.
$$f g x f g x$$
 4 $\frac{1}{4} x 2 2$

x 4
The domain and range of g are (0,1) (0,). The domain of f is

(,4) (4,) , and the range of f is

 $(,\,0)\,\square\,(0,\,)$. Therefore, the domain of

$$g \, \, \, \, f \, \, \text{is} \, (4, 4) \, \, \, \, \, \, (4, 4) \, \, \, \, \, \, \,$$

gf(2) g(1) 2 and gf(3) g(2) 5 Since gf(1) 7 and f(1) 3, g(3) 7.

х	fx	g x	gf(x)
1	3	2	7
2	1	5	2
3	2	7	5

$$\frac{1}{4}4x22$$
 4x x 4

94.
$$f \circ g x f g x \ 3 \stackrel{1}{=} x$$
 3 $\frac{1}{3} x x$ 3 $\frac{3}{3} x \stackrel{1}{=} x x$

Chapter 2 Graphs and Functions

95.
$$f_{1}gxfgx35^{1}x^{3} + 4f_{5}$$

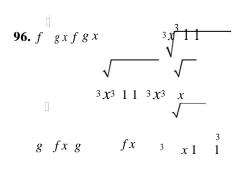
$$g_{1}fxg \qquad fx \qquad 13 \qquad 5x \qquad 4^{34}$$

$$g_{1}fxg \qquad fx \qquad 13 \qquad 5x \qquad 4^{34}$$

$$-5 \qquad -5 \qquad 5$$

$$15x4 + 5x + 4 + 4$$

$$-5 \qquad -5 \qquad 5 \qquad 5$$



x 1 1 x

In Exercises 97–102, we give only one of many possible answers.

$$h(x) (6 x 2)^2$$

Let $g(x) = 6x - 2$ and
$$f(x) x^2.$$

$$(f^{\parallel}g)(x) f(6 x 2) (6 x 2)^2 h(x)$$

$$h(x) (11x^{2} 12 x)^{2}$$
Let $g(x) 11x^{2} 12x$ and $f(x) x^{2}$.
$$(f \mid g)(x) f(11x^{2} 12 x)$$

$$(11x^{2} 12 x)^{2} h(x)$$

$$h(x) \quad x^{2}\sqrt{1}$$
Let $g(x) \quad x^{2} \quad 1$ and $f(x) \quad x.\sqrt{1}$

$$(f \quad g)(x) \qquad \qquad \sqrt{f(x^{2} \quad 1)} \qquad x^{2} \quad 1 \quad h(x) \quad (2x \quad 3)^{3}$$

$$f g x \qquad f g x \qquad f 1760 x$$

g x compute the number of feet in x

miles.
$$\begin{array}{ccc}
& & & & \\
& & & & \\
& & & & \\
(x) & & & & \\
\end{array}$$

(b)
$$(16) \ A(2\sqrt{8}) \ 3(8)^2$$
 $64 \ 3 \text{ square units}$

106. (a)
$$x + 4s = x + s = x + 4$$

(c)
$$y = \frac{6^2}{2.25}$$
 square units

107. (a)
$$r(t) 4t$$
 and $(r) r^2$ $(r) r^2$ $(r) r^2$ $(r) r^2$ $(r) r^2$ $(r) r^2$ $(r) r^2$

Let
$$g(x) 2x 3$$
 and $f(x) x^3$.
 $(f^{\parallel} g)(x)f(2x3)(2x3)^3 h(x)$

(r)(t) defines the area of the leak in terms of the time t, in minutes.

$$(3) 16 (3)^2 144 \text{ ft}^2$$

It defines the area of the circular layer in terms of the time *t*, in hours.

Let
$$g(x)$$
 6 x and $f(x)$ \sqrt{x} 12.

$$(f g)(x) \qquad \sqrt{f(6x)} \qquad 6x \ 12 \ h(x)$$

$$h(x)^{-3} 2 \sqrt{34}$$

The function $f \mid g$ computes the number of inches in x miles.

Let x = the number of people less than 100 people that attend.

x people fewer than 100 attend, so 100 - x people do attend N(x) = 100 - x

The cost per person starts at \$20 and

increases by \$5 for each of the x people that do not attend. The total increase is 55x, and the cost per person increases to 20 + 5x. Thus, G(x) = 20 + 5x.

(d) If 80 people attend, x = 100 - 80 = 20.

110. (a) y₁ 0.02 x

y1 y2 represents the total annual interest.

111. (a) gx = x2

If the area of a square is x^2 square inches, each side must have a length of x inches. If 3 inches is added to one dimension and 1 inch is subtracted from the other, the new dimensions will be x + 3 and x - 1. Thus, the area of the resulting rectangle is $\Box(x) = (x + 3)(x - 1)$.

Chapter 2 Review Exercises

$$P(3,-1), Q(-4,5)$$

$$d(P,Q) = \sqrt{\frac{(43)^2 [5(1)]^2}{\sqrt{7} e^2}} \sqrt{4936} = 85\sqrt{-1}$$

3.
$$A(-6,3)$$
, $B(-6,8)$

$$d(A,B) = \sqrt{\frac{[6\cdot(6)]^2 - (8\cdot3)^2}{\sqrt{05^2}}} = \sqrt{25}\cdot5$$

Midpoint:

2 2 2 2

Label the points A(5, 7), B(3, 9), and C(6, 8).

$$d(A,B) \sqrt{35^{2} 97^{2}} \sqrt{\sqrt{2^{2} 2^{2}}} \sqrt{44} 8$$

$$d(A,C) = \sqrt{(65)^{2} (87)^{2}}$$

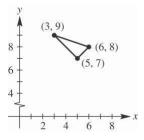
$$1 = 1 = 1 = 1 = 2$$

$$d(B,C) = \sqrt{-63^{2} 89^{2}}$$

$$\sqrt{2 + 1^{2}} = \sqrt{91 + \sqrt{0}}$$

Because 8^2 $\sqrt{2^2}$ 10^2 , triangle

ABC is a right triangle with right angle at (5, 7).



Let B have coordinates (x, y). Using the midpoint formula, we have

$$8, 2 \xrightarrow{6x} , \xrightarrow{10y}$$

$$M(-8, 2), N(3, -7)$$

$$\frac{d(M,N)}{\sqrt{11^{2}(9)^{2}}} \frac{\sqrt{3(8)]^{2}(72)^{2}}}{\sqrt{12181}} \sqrt{12181}$$

Midpoint:
$$\frac{83}{2}, \frac{2(7)}{5}, \frac{5}{5}$$

$$d(Q,R) = \sqrt{\frac{\sqrt{(3 \cdot 1)^2}}{\sqrt{15\sqrt{7}}}} \sqrt{\frac{15\sqrt{7}}{2}} = \sqrt{\frac{2}{8}}$$
2 8 4 64 68217

$$d(P,R) = \sqrt{\frac{(3(2))^2 - (15(5))^2}{\sqrt{(5)^2 + (20)^2} \sqrt{25400}}} = \sqrt{\frac{15(5)^2 + (20)^2}{\sqrt{25400}}} = \sqrt{\frac{15(5)^2 + (20)^2}{\sqrt{2500}}} = \sqrt{\frac{15(5)^2 + (20)^2}{\sqrt{2500}$$

(continued on next page)

Chapter 2 Graphs and Functions (continued)

$$d(P, Q) d(Q, R) 3 1$$
 17 $\sqrt{}$

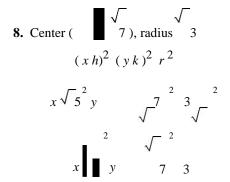
d(P,R), so these three points are collinear.

Center (-2, 3), radius 15

$$(xh)^2 (yk)^2 r^2$$

 $[x(2)]^2 (y3)^2 15^2$

$$(x2)^2 (y3)^2 225$$



Center (-8, 1), passing through (0, 16)

The radius is the distance from the center to

any point on the circle. The distance

between (-8, 1) and (0, 16) is

$$r = (\sqrt{(8))^2 (16 \, 1)^2} \sqrt{8^2 \, 15^2}$$

The equation of the circle is

$$[x(8)]^2 (y1)^2 17^2$$

$$(x8)^2 (y1)^2$$
 289

Center (3, -6), tangent to the x-axis

The point (3, -6) is 6 units directly below the x-axis. Any segment joining a circle's center to a point on the circle must be a radius, so in this case the length of the radius is 6 units.

$$(xh)^2 (yk)^2 r^2$$

 $(x3)^2 [y(6)]^2 6^2$

The center of the circle is (5, 6). Use the distance formula to find the radius:

$$r^2$$
 $(45)^2 (96)^2 1910$

The equation is $(x \, 5)^2 \, (y \, 6)^2 \, 10$.

$$x^2 + 4x + y^2 + 6y + 120$$

Complete the square on *x* and *y* to put the equation in center-radius form.

$$x^2 4x y^2 6y 12$$

$$x^{2}$$
 4 x 4 y^{2} 6 y 9 12 4 9
 x^{2}
 x^{2}
 y 3 1

The circle has center (2, -3) and radius 1.

$$x^2 6x y^2 10 y 30 0$$

Complete the square on x and y to put the equation in center-radius form.

$$(x^2 6 x 9) (y^2 10 y 25) 30 9 25$$

 $(x 3) (y 5) 4$

The circle has center (3, 5) and radius 2.

$$2x^{2} 14x2y^{2} 6y2 0$$

$$27x y^{2} 3y 1 0$$

$$x^{2} 7x y^{2} 3y 1$$

$$y 3y 4 1 4 4$$

$$y 3y 4 1 4 4$$

$$y 3y 4 1 4 4$$

$$\sqrt{\frac{54}{4}} \quad \frac{\sqrt{54}}{\sqrt{1}} \quad \frac{\sqrt{96}}{\sqrt{1}} \quad \frac{3\sqrt{96}}{\sqrt{1}}$$
4 4 4 4 2

$$(x3)^2 (y6)^2 36$$

The center of the circle is (0, 0). Use the distance formula to find the radius:

$$r^2 (30)^2 (50)^2 92534$$

The equation is $x^2 y^2 = 34$.

The center of the circle is (0, 0). Use the distance formula to find the radius:

$$r^{2} (20)^{2} (30)^{2} 4913$$

The equation is $x^{2} y^{2} 13$.

The center of the circle is (0, 3). Use the distance formula to find the radius:

$$r^2 (20)^2 (63)^2 4913$$

The equation is $x^2 (y 3)^2 13$.

The circle has center $\frac{2}{11, \frac{5}{2}}$ and radius

$$\sqrt{146}_{2}$$
.

This is not the graph of a function because a vertical line can intersect it in two points. domain: [-6, 6]; range: [-6, 6]

This is not the graph of a function because a vertical line can intersect it in two points. domain: , ; range: 0,

- This is not the graph of a function because a vertical line can intersect it in two points. domain: , ; range: (, 1] [[],)
- This is the graph of a function. No vertical line will intersect the graph in more than one point. domain: , ; range: 0,
- This is not the graph of a function because a vertical line can intersect it in two points.

domain: 0, ; range: ,

This is the graph of a function. No vertical line will intersect the graph in more than one point. domain: , ; range: ,

 $y 6x^2$

Each value of *x* corresponds to exactly one value of *y*, so this equation defines a function.

- 26. The equation $x = \frac{1}{3}y^2$ does not define y as a function of x. For some values of x, there will be more than one value of y. For example, ordered pairs (3, 3) and (3, -3) satisfy the relation. Thus, the relation would not be a function.
- **27.** The equation $y \times 2$ does not define y as a function of x. For some values of x, there will be more than one value of y. For example, ordered pairs (3, 1) and (3, -1) satisfy the relation.

The equation $\frac{4}{x}$ defines y as a function

of x because for every x in the domain, which is (-, 0) (0,), there will be exactly one value of y.

29. In the function f(x) = 4x, we may use

any real number for x. The domain is , .

30. $f(x) = \frac{8x}{8x}$

x can be any real number except 8 because this will give a denominator of zero. Thus, the domain is (-, 8) (8,).

(a) As x is getting larger on the interval 2, , the value of y is increasing.

As x is getting larger on the interval, 2, the value of y is decreasing.

f(x) is constant on (-2, 2).

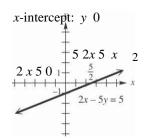
In exercises 33–36, $fx \ 2x^2 \ 3x \ 6$.

2

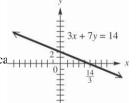
5

The graph is the line with slope $\frac{5}{2}$ and

y-intercept (0, -)1. It may also be graphed using intercepts. To do this, locate the



$$\mathbf{31.} \ fx \qquad \begin{array}{c} \sqrt{} \\ 63x \end{array}$$



38. $3x 7 y 14 7 y 3x 14 y <math>\frac{3}{x} x 2$

The graph is the line with slope of $\frac{3}{7}$ and

y-intercept (0, 2). It may also be graphed using intercepts. To do this, locate the *x*-intercept by setting y=0: 3x 7 0 14 3x 14 $x \frac{14}{}$

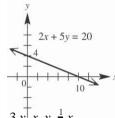
In the function $y = \sqrt{6.3x}$, we must have 6.3x = 0.

 $6 \, 3x \, 0 \, 6 \, 3x \, 2 \, x \, x \, 2$ Thus, the domain is , 2.

39.
$$2x 5 y 20 5 y 2 x 20 y \frac{2}{x} 4$$

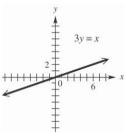
The graph is the line with slope of $\frac{2}{5}$ and

y-intercept (0, 4). It may also be graphed using intercepts. To do this, locate the xintercept: *x*-intercept: *y* 0



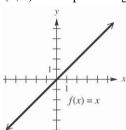
The graph is the line with slope $\frac{1}{3}$ and

y-intercept (0, 0), which means that it passes through the origin. Use another point such as (6, 2) to complete the graph.



f(x) = x

The graph is the line with slope 1 and yintercept (0, 0), which means that it passes through the origin. Use another point such as (1, 1) to complete the graph.



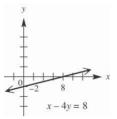
x 4 y 8 4 y x8

 $\overline{1}_{\begin{subarray}{c} x \ 4 \end{subarray}} 2$

The graph is the line with slope $\frac{1}{4}$

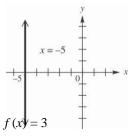
y-intercept (0, -2). It may also be graphed using intercepts. To do this, locate the xintercept:

y 0 x 4 0 8 x 8

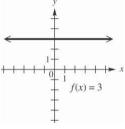


x = -5

The graph is the vertical line through (-5, 0).

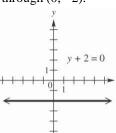


The graph is the horizontal line through (0, 3).



y 2 0 y 2

The graph is the horizontal line through (0, -2).



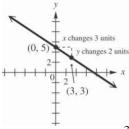
The equation of the line that lies along the *x*-axis is y = 0.

Line through (0, 5), m^2 3 Note that $m = \frac{2}{3} - \frac{1}{3}$.

Begin by locating the point (0, 5). Because the , a change of 3 units horizontally slope is 3

(3 units to the right) produces a change of – 2 units vertically (2 units down). This gives a second point, (3, 3), which can be used to complete the graph.

(continued)

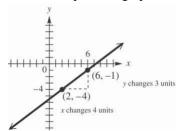


Line through (2, -4), $m = \frac{3}{4}$

First locate the point (2, -4).

Because the slope is $4^{\frac{3}{2}}$, a change of 4 units

horizontally (4 units to the right) produces a change of 3 units vertically (3 units up). This gives a second point, (6, -1), which can be used to complete the graph.



through
$$(2, -2)$$
 and $(3, -4)$
 y y 4 2 2
 x_2 x_1 3 2 1

through (8, 7) and 1 2, 2

$$m \stackrel{y}{=} \stackrel{x}{+} \frac{279}{15}$$

$$\stackrel{x}{=} \frac{x}{15} \stackrel{1}{=} 8$$

$$\stackrel{y}{=} \frac{1}{15} \stackrel{1}{=} 6$$

$$15 \quad 15 \quad 5$$

through (0, -7) and (3, -7)

$$m \quad \frac{77}{30} \quad 0 \quad 3$$

through (5, 6) and (5, -2)

$$m^{\frac{y}{2}} \xrightarrow{\frac{y}{2} - 1} \frac{268}{55}$$

The slope is undefined.

Solve for *y* to put the equation in slope-intercept form. 11*x* 2 *y* 3

$$2 y 11x 3 y 2 x 2$$

Thus, the slope is $\frac{11}{2}$.

9x - 4y = 2.

Solve for *y* to put the equation in slope-intercept form.

$$4y 9x2 y^{\frac{9}{2}}x^{\frac{1}{2}}$$

Thus, the slope is $\frac{9}{4}$.

55. $x = 2 \cdot 0 \cdot x$

The graph is a vertical line, through (2, 0). The slope is undefined.

x - 5y = 0.

Solve for *y* to put the equation in slope-intercept form.

$$5y x y \frac{1}{2}x$$

Thus, the slope is $\frac{1}{2}$.

Initially, the car is at home. After traveling for 30 mph for 1 hr, the car is 30 mi away from home. During the second hour the car travels 20 mph until it is 50 mi away. During the third hour the car travels toward home at 30 mph until it is 20 mi away. During the fourth hour the car travels away from home at 40 mph until it is 60 mi away from home. During the last hour, the car travels 60 mi at 60 mph until it arrived home.

(a) This is the graph of a function because no vertical line intersects the graph in more than one point.

The lowest point on the graph occurs in December, so the most jobs lost occurred in December. The highest point on the graph occurs in January, so the most jobs

gained occurred in January.

The number of jobs lost in December is approximately 6000. The number of jobs gained in January is approximately 2000.

It shows a slight downward trend.

(a) We need to first find the slope of a line that passes between points (0, 30.7) and (12, 82.9)

$$m \frac{y_2y_1}{} 82.930.7 \frac{52.2}{} 4.35$$

Now use the point-intercept form with b = 30.7 and m = 4.35.

120

12

$$y = 4.35x + 30.7$$

The slope 4.35

 x_2 x_1

The slope, 4.35, indicates that the number of e-filing taxpayers increased by 4.35% than year from 2001 to 2013.

For 2009, we evaluate the function for x = 8. y = 4.35(8) + 30.7 = 65.5 65.5% of the tax returns are predicted to have been filed electronically.

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$$m + y_2 + y_1 = 63,80021,000$$

$$\frac{x_2 \ x_1}{42,800} \ 2013 \ 1980$$

$$\frac{42,800}{33} \ \$1297 \ \text{per year}$$

The average rate of change was about \$1297

per year.

(a) through (3, -5) with slope -2

Use the point-slope form.

$$y_1 m(x x_1) y$$

 $2(x 3) y 5 2(x$
 $3)$
 $5 2 x 6$
 $2 x 1$

Standard form: y 2 x 1 2x y 1

(a) through (-2, 4) and (1, 3) First find the slope.

$$m = \frac{34}{1(2)} \frac{1}{3}$$

Now use the point-slope form with

$$(x, y)$$
 (1, 3) and m^{-1} .
 $y y_1 m(xx_1)$
 $y 3 \frac{1}{2}(x 1)$
 $3(y 3) 1(x 1)$
 $3 y 9 x 1$

$$3 y x 10 y \frac{1}{2} x \frac{10}{3}$$

Standard form:

$$3 x^{\frac{1}{2}} 3 3^{\frac{10}{2}} y x 10$$

 $x 3 y 10$

(a) through (2, -1) parallel to 3x - y = 1Find the slope of 3x - y = 1. $3x \ y \ 1 \ y \ 3x \ 1 \ y \ 3x \ 1$

The slope of this line is 3. Because parallel lines have the same slope, 3 is also the slope of the line whose equation is to be found. Now use the point-slope

form with $(x_1, y_1)(2, 1)$ and m 3.

$$y_1 m(x x_1)$$

 $y(1) 3(x 2)$
 $y 1 3x 6 y 3x 7$

(b) Standard form:

(a) x-intercept (-3, 0), y-intercept (0, 5)Two points of the line are (-3, 0)and (0, 5). First, find the slope.

$$m \ 505$$

The slope is $\frac{5}{2}$ and the *y*-intercept is (0, 5). Write the equation in slope-

intercept form:
$$y = x \cdot 5$$

Standard form:

$$y \stackrel{5}{=} x 5 3 y 5x 15$$

5x 3 y 15 5x 3 y 15

(a) through (2, -10), perpendicular to a line with an undefined slope A line with an undefined slope is a vertical line. Any line perpendicular to a vertical line is a horizontal line, with an equation of the form y = b. The line passes through (2, -10), so the equation of the line is y = -10.

Standard form: y = -10

(a) through (0, 5), perpendicular to 8x + 5y = 3Find the slope of 8x + 5y = 3. $8x \ 5 \ y \ 3 \ 5 \ y \ 8x \ 3$ $y \ \frac{8}{5}x \ 5^{\frac{3}{2}} \ 5$

The slope of this line is $\frac{85}{}$. The slope

of any line perpendicular to this line is

$$8^{5}$$
, because 8^{8} 8^{5} 1.

The equation in slope-intercept form with slope $\frac{3}{8}$ and y-intercept (0, 5) is

Standard form:

- (a) through (-7, 4), perpendicular to y = 8The line y = 8 is a horizontal line, so any line perpendicular to it will be a vertical line. Because x has the same value at all points on the line, the equation is x = -7. It is not possible to write this in slope-intercept form.
- **(b)** Standard form: x = -7
- **68.** (a) through (3, -5), parallel to y = 4

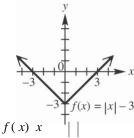
This will be a horizontal line through (3, -5). Because *y* has the same value at all points on the line, the equation is = -5.

Standard form: y = -5

$$f(x) \times 3$$

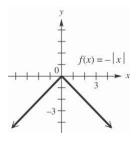
The graph is the same as that of y = x,

except that it is translated 3 units downward.



The graph of f(x) x is the reflection of

the graph of y = x about the x-axis.

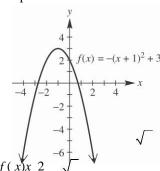


$$f(x) x 1^2 3$$

The graph of $f(x) \times 1^2 = 3$ is a

translation of the graph of $y x^2$ to the left 1

unit, reflected over the x-axis and translated up 3 units.



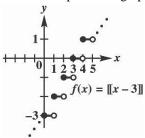
The graph of f(x)

x 2 is the reflection

of the graph of y = x about the x-axis, translated down 2 units.

To get y = 0, we need 0 x 3 1x 4. To get y = 1, we need 1 3 2 4 *x* 5.

Follow this pattern to graph the step function.

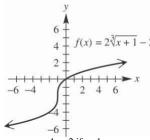


$$f(x) \ 2^{3} x 12$$

The graph of $f(x) 2^3 x 12$ is a

translation of the graph of $y^3 \sqrt{}$ to the left 1 unit, stretched vertically by a factor of 2, and

translated down 2 units.

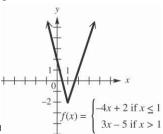


75.
$$f(x)^{4x^2 \text{ if } x \text{ 1}}$$

$$3x 5$$
 if $x 1$

Draw the graph of y = -4x + 2 to the left of x = 1, including the endpoint at x = 1. Draw the graph of y = 3x - 5 to the right of x = 1, but do not include the endpoint at x = 1.

Observe that the endpoints of the two pieces coincide.



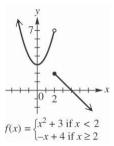
Chapter 2 Graphs and Functions

76.
$$f(x)$$
 x^2 3 if x 2 x 4 if x 2

Graph the curve $y x^2 = 3$ to the left of x = 2,

and graph the line y = -x + 4 to the right of x = 2. The graph has an open circle at (2, 7)

and a closed circle at (2, 2).

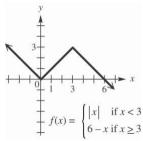


x

77.
$$f(x) = \begin{cases} & \text{if } x \\ & \text{of } x \text{ if } x \end{cases} 3$$

Draw the graph of y x to the left of x = 3,

but do not include the endpoint. Draw the graph of y = 6 - x to the right of x = 3, including the endpoint. Observe that the endpoints of the two pieces coincide.



78. Because *x* represents an integer, $\begin{bmatrix} x \\ x \end{bmatrix} x$. Therefore, $\begin{bmatrix} x \\ x \end{bmatrix} x x x x x 2 x$.

True. The graph of an even function is symmetric with respect to the *y*-axis.

True. The graph of a nonzero function cannot be symmetric with respect to the *x*-axis. Such a graph would fail the vertical line test

81. False. For example, $f(x) x^2$ is even and

(2, 4) is on the graph but (2, -4) is not.

True. The graph of an odd function is symmetric with respect to the origin.

True. The constant function f x = 0 is both

False. For example, $f(x) x^3$ is odd, and

(2, 8) is on the graph but (-2, 8) is not.

$$x y^2 10$$

Replace x with -x to obtain (x) y^2 10.

The result is not the same as the original equation, so the graph is not symmetric with respect to the *y*-axis. Replace y with -y to obtain $x(y)^2$ 10 x y y 10. The result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis. Replace x with -x and y with -y to obtain $(x)(y)^2$ 10 (x) y y 10. The result is not the same as the original equation, so the graph is not symmetric with

respect to the origin. The graph is symmetric with respect to the *x*-axis only.

$$5y^2 5x^2 30$$

Replace x with -x to obtain

$$5 y^2 5(x)^2 30 5 y^2 5x^2 30.$$

The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace *y* with –*y* to obtain

$$5(y)^2 5x^2 305 y^2 5x^2 30.$$

The result is the same as the original equation, so the graph is symmetric with respect to the x-axis. The graph is symmetric with respect to the y-axis and x-axis, so it must also be symmetric with respect to the origin. Note that this equation is the same as $y^2 x^2 6$,

which is a circle centered at the origin.

$$x^2$$
 y^3

Replace x with -x to obtain

 $(x)^2 y^3 x^2 y^3$. The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace y with -y to obtain $x^2 (y)^3 x^2 y^3$. The result is not the same as the original

equation, so the graph is not symmetric with respect to the x-axis. Replace x with -x and y

with -y to obtain $(x)^2 (y)^3 x^2 y^3$. The result is not the same as the original equation, so the graph is not symmetric with

respect to the origin. Therefore, the graph is symmetric with respect to the y-axis only.

even and odd. Because $fx \ 0 \ fx$,

the function is even. Also $fx \ 0 \ 0 \ fx$, so the function is odd.

$$y^3 \times 4$$

Replace x with -x to obtain $y^3 \times 4$.

The result is not the same as the original

equation, so the graph is not symmetric with respect to the *y*-axis. Replace *y* with –*y* to obtain

$$(y)^3 x 4 y^3 x 4$$

$$y^3 \times 4$$

The result is not the same as the original

equation, so the graph is not symmetric with respect to the *x*-axis. Replace x with -x and y with -y to obtain

$$(y)^3 (x) 4 y^3 x 4 y^3 x 4.$$

The result is not the same as the original equation, so the graph is not symmetric with respect to the origin. Therefore, the graph has none of the listed symmetries.

6xy4

Replace *x* with –*x* to obtain 6(*x*) *y* 4 6*x y* 4 . The result is not the same as the original equation, so the graph is not symmetric with respect to the *y*-axis. Replace with –*y* to obtain 6 *x* (*y*) 4 6 *x y* 4 . The result is not the same as the original equation, so the graph is not symmetric with respect to the *x*-axis. Replace *x* with –*x* and *y* with –*y* to obtain 6(*x*) (*y*) 4 6 *x y* 4 . This equation is not equivalent to the original one, so the graph is not symmetric with respect to the origin. Therefore, the graph has none of the listed symmetries.

y * |

Replace x with -x to obtain

$$y \mid (x)$$
 $y \mid x$. The result is not the

same as the original equation, so the graph is not symmetric with respect to the *y*-axis.

Replace y with -y to obtain

$$\begin{vmatrix} y & x \end{vmatrix}$$
 $\begin{vmatrix} y & x \end{vmatrix}$ The result is the same as

the original equation, so the graph is symmetric with respect to the x-axis. Replace x with -x and y with -y to obtain

$$\begin{vmatrix} y \end{vmatrix}$$
 (x) $\begin{vmatrix} y \end{vmatrix}$ x. The result is not the

same as the original equation, so the graph is

not symmetric with respect to the origin. Therefore, the graph is symmetric with respect

Replace
$$k$$
 with $-x$ to obtain $\begin{bmatrix} x & y \\ x & y \end{bmatrix}$, $\begin{bmatrix} y & y \\ y & x \end{bmatrix}$,

The result is the same as the original equation, so the graph is symmetric with respect to the

$$y$$
-axis. Replace y with $-y$ to obtain $\begin{vmatrix} x & y & x \\ & & \end{vmatrix}$. The result is the same as

the original equation, so the graph is symmetric with respect to the *x*-axis. Because the graph is symmetric with respect to the *x*-axis and with respect to the *y*-axis, it must also by symmetric with respect to the origin.

$$x^2 y^2 0$$

Replace x with -x to obtain

 $x^2 y^2 0 x^2 y^2 0$. The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace *y* with -y to obtain $x^2 y^2 0 x^2 y^2 0$. The result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis. Because the graph is symmetric with respect to the *y*-axis, it

must also by symmetric with respect to the

origin.

$$x^2$$
 y 2^2 4
Replace x with $-x$ to obtain
 x^2 y 2^2 4 x^2 y 2^2 4.

The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace *y* with –*y* to obtain

as the original equation, so the graph is not symmetric with respect to the x-axis. Replace x with -x and y with -y to obtain

$$x^2$$
 y 2^2 4 x^2 y 2^2 4,

which is not equivalent to the original equation. Therefore, the graph is not

symmetric with respect to the origin.

95. To obtain the graph of |g(x)| = x, reflect the

graph of
$$f(x)$$
 x across the $|x|$ -axis.

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to the *x*-axis only.

y = 1

This is the graph of a horizontal line through (0, 1). It is symmetric with respect to the *y*-axis, but not symmetric with respect to the *x*-axis and the origin.

96. To obtain the graph of h(x) x 2, translate

the graph of f(x) x down 2 units.

Chapter 2 Graphs and Functions

To obtain the graph of k(x) 2x4, translate the graph of f(x) x to the right 4 units and stretch vertically by a factor of 2.

If the graph of f(x) 3x 4 is reflected about the *x*-axis, we obtain a graph whose equation is y(3x 4) 3x 4.

If the graph of f(x) 3x 4 is reflected about the y-axis, we obtain a graph whose equation is y f(x) 3(x) 4 3x 4.

If the graph of f(x) 3x 4 is reflected about

the origin, every point (x, y) will be replaced by the point (-x, -y). The equation for the

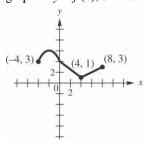
graph will change from y 3x 4 to

$$y 3(x) 4 y 3x 4$$

 $3x 4$.

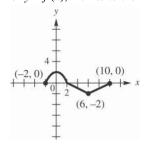
(a) To graph y f(x) 3, translate the

graph of y = f(x), 3 units up.

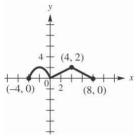


To graph yf(x 2), translate the graph

of y = f(x), 2 units to the right.



(c) To graph y f(x 3) 2, translate the



102. No. For example suppose fx $\sqrt{x \ 2}$ and $gx \ 2x$. Then $\sqrt{(f \ g)(x)} \qquad f(g(x)) \qquad f(2x)$

The domain and range of g are (,), however, the domain of f is [2,). So,

 $2 \times 2 \times 0 \times 1$. Therefore, the domain of

 $f \mid g$ is 1, . The domain of g, (,), is

not a subset of the domain of $f = \begin{bmatrix} g \\ 1 \end{bmatrix}$, 1,

For Exercises 103–110,
$$f(x) = 3x^2 - 4$$
 and $g(x) = x^2 - 3x - 4$.

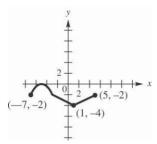
$$(fg)(x) f(x) g(x)$$

 $(3x^2 4)(x^2 3x 4)$
 $3x^4 9x^3 12x^2 4x^2 12x 16$
 $3x^4 9x^3 16x^2 12x 16$

105.
$$(f g)(4)$$
 $f(4) g(4)$ $[3(4)^2 4] [(4)^2 3(4)4]$ $[3(16) 4] [16 3(4) 4]$ $[48 4] [16 12 4]$

44 24 68

graph of y = f(x), 3 units to the left and 2 units down.



$$(f g)(2k) f(2k) g (2k)$$

$$[3(2k)^{2} 4] [(2k)^{2} 3(2k) 4]$$

$$[3(4)k^{2} 4] [4k^{2} 3(2k) 4]$$

$$(12k^{2} 4) (4k^{2} 6k 4)$$

$$16k^{2} 6k 8$$

107.
$$\frac{f}{g}$$
 (3) $\frac{f(3)}{g(3)}$ $\frac{3^2 4}{3^2 334}$ $\frac{394}{9334}$ $\frac{274}{994}$ $\frac{23}{4}$ $\frac{$

108.
$$g^{(1)}$$
 $1^2 \overset{?}{3} 14$ 1314 $\frac{34}{} \overset{1}{} \text{ undefined}$

134

(fg)(x) is,.

109. The domain of (fg)(x) is the intersection of the domain of f(x) and the domain of g(x). Both have domain, , so the domain of

0

$$\frac{f}{3x^2 + 4} = \frac{3x^2 + 4}{3x^2 + 4}$$
110. $g(x) x^2 3x 4 = (x 1)(x 4)$

Because both fx and gx have domain

, , we are concerned about values of x

that make $g \times 0$. Thus, the expression is

undefined if (x + 1)(x - 4) = 0, that is, if x = -1 or x = 4. Thus, the domain is the set of all real numbers except x = -1 and x = 4, or

$$(-,-1)$$
 $(-1,4)$ $(4,)$.

111.
$$fx \ 2x \ 9$$

$$f(x h) \ 2(x h) \ 9 \ 2x \ 2h \ 9$$

$$f(x h) \ f(x) \ (2x \ 2h \ 9) \ (2x \ 9)$$

$$2x \ 2h \ 9 \ 2x \ 9 \ 2h$$
Thus,
$$f(x h) f(x) \ \frac{2h}{2}$$

$$h$$
112. $f(x) \ x^2 \ 5x \ 3$

112.
$$f(x) x^2 5x 3$$

 $f(xh) (xh)^2 5(xh) 3$
 $x^2 2xh h^2 5x 5h 3$
 $f(xh) f(x)$
 $(x^2 2xh h^2 5x 5h 3) (x^2 5x 3)$

For Exercises 113–118,

$$f(x) = \sqrt{\frac{x \ 2 \text{ and } g(x) \ x^2}{x^2}}$$
113. $(g \ f)(x) \ g[f(x)] \ g$

$$x = 2$$
 2×2

115.
$$fx$$
 x 2, so $f3$ 3 2 1 1.

Therefore,

 $g \quad f3 \quad g \quad f3$

116.
$$g \times x^2$$
, so $g \times 66^2$ 36.

Therefore, $f \times g \times 6f \times g \times 6$
 $f \times 36$

117.
$$g$$
 $f^1 g f^1 g$ 128 3

Because 3 is not a real number, g f^1

is not defined.

118. To find the domain of $f\sqrt{g}$, we must consider the domain of g as well as the composed function, f g. Because

f gx fgx
$$x^2$$
 2 we need to determine when x^2 2 0.

Step 1: Find the values of x that satisfy x^2 2 0.

 x^2 2 x 2

 x^2 2xh h^2 5x 5h 3 x^2 5x 3

 x^2 2xh h^2 5h

 x^2 2xh h^2 5h

 x^2 2xh h^2 5h

 x^2 2xh h^2 5h

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St	e two numbers divide a number line into
	three regions.

p
2
:
T
h

$(-\infty, -\sqrt{2})$	$(\sqrt{2},\sqrt{2})$	($(\sqrt{2}, \infty)$	
2 - 1/2	 	+ +	+	-

Step 3 Choose a test value to see if it satisfies the inequality, x^2 2 0.

√ Interval	Test	Is _{x2} 20
	Value	true or false?
, 2 √	2	2 ² 20 ?
		2 0 11ue
2√2	0	02 20? — 20 -False
The domain of	$\int_{-\infty}^{\mathbb{T}} g$ is	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
<u>', √² □</u>	$\sqrt{2}$	

122.
$$f_{(0)} \underline{f(0)} \underline{5}_{\text{undefined}}$$

$$g(0) = 0$$

$$(g^{(1)}f)(2)$$
 $g[f(2)]$ $g(1)$ 2

124.
$$(f \ \ g)(3) f [g(3)] f(2) 1$$

125.
$$(f \ g)(2) \ f[g(2)] \ f(2) \ 1$$

$$(g^{(1)}f)(3)$$
 $g[f(3)]$ $g(4)$ 8

Let x = number of yards.

f(x) = 36x, where f(x) is the number of inches. g(x) = 1760x, where g(x) is the number of yards. Then

$$(g^{[]}f)(x)$$
 $gf(x)$ 1760(36 x) 63, 360 x .

There are 63,360*x* inches in *x* miles Use the definition for the perimeter of a rectangle.

P = length + width + length + width

This is a linear function.

129. If $V(r) \stackrel{4}{-} r^3$ and if the radius is increased

by 3 inches, then the amount of volume gained is given by

$$V_g(r) V(r3) V(r) 3 (r 3)$$
 3⁻r

1 3 1 3

130. (a)
$$V r^2 h$$

If *d* is the diameter of its top, then h = d and r = 2. So,

(b)
$$S 2 r^2 2 rh$$

(b) The range of fx fx

The domain of $fx x^2$ 3 is all real

numbers. In interval notation, this correlates to the interval in C, , .

The range of $fx x^2 3$ is all real

numbers greater than or equal to 3. In interval notation, this correlates to the interval in B, 3, .

The domain of $fx^3 x \sqrt[3]{\text{is all real}}$

numbers. In interval notation, this correlates to the interval in $C, \,$,

$$\sqrt{}$$

The range of fx^3x3 is all real

numbers. In interval notation, this correlates to the interval in C, , .

The domain of $fx \times 3$ is all real

numbers. In interval notation, this correlates to the interval in C, , .

(h) The range of $fx \times 3$ is all real

numbers greater than or equal to 0. In interval notation, this correlates to the

interval in D, 0, .

The domain of x y^2 is x = 0 because

when you square any value of *y*, the outcome will be nonnegative. In interval

notation, this correlates to the interval in

D, 0,.

2

(j) The range of x y is all real numbers. Copyright © 2017 Pearson Education, Inc.

$$S(d) 2 \frac{d^{2}}{2} 2 \frac{d}{2} (d) \frac{d^{2}}{2} \frac{d^{2}}{2}$$

$$- \frac{\frac{2}{2}}{2} \frac{\frac{2}{2}}{2} \frac{\frac{2}{2}}{2} \frac{2}{2}$$
2

Chapter 2 Test

1. (a) The domain of fx \sqrt{x} 3 occurs when x 0. In interval notation, this correlates to the interval in D, 0, .

In interval notation, this correlates to the interval in C, , .

Consider the points 2,1 and 3, 4.

$$m = \frac{41}{3(2)} = \frac{3}{5}$$

We label the points A 2,1 and B 3, 4.

$$d(A, B) \sqrt{\frac{[3(2)]^2 (41)^2}{\sqrt{5^2 3^2 \sqrt{59}}}} \sqrt{34}$$

The midpoint has coordinates

Use the point-slope form with (

$$x_1, y_1$$
) (2,1) and $m^{\frac{3}{2}}$. 5
 $y y_1 m(x x_1)$
 $y 1^{\frac{3}{2}} [x_5 (2)]$
 $y 1^{\frac{3}{2}} (x_2) 5 y 1 3(x_2)$
 $5 y 5 3x^{\frac{5}{6}} 5 y 3x 11$
 $3x 5 y 11 3x 5 y 11$

Solve
$$3x - 5y = -11$$
 for y.
 $3x 5 y 11$
 $5 y 3x 11$
 $\frac{3}{55}$

Therefore, the linear function is

(a) The center is at (0, 0) and the radius is 2, so the equation of the circle is

2
 y^{2} 4.

The center is at (1, 4) and the radius is 1, so the equation of the circle is $(x 1)^2 (y 4)^2 1$

$$(x 1)^2 (y 4)^2$$

 x^2 y^2 4 x 10 y 13 0

Complete the square on *x* and *y* to write the equation in standard form:

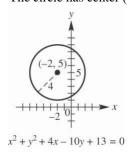
$$x^2$$
 y^2 4x 10 y 13 0

$$x^2 4x$$
 $y^2 10y$ 13

$$x^2$$
 4 x 4 y^2 10 y 25 13 4 25

$$2^2 \text{ v } 5^2 \text{ 16}$$

The circle has center (-2, 5) and radius 4.



This is the graph of a function because no vertical line intersects the graph in more

than one point. The domain of the function is (-,-1) (-1,). The

range is (-, 0) (0,). As x is getting larger on the intervals, 1 and

1, , the value of *y* is decreasing, so the function is decreasing on these intervals. (The function is never increasing or constant.)

Point A has coordinates (5, -3).

The equation of a vertical line through A is x = 5.

The equation of a horizontal line through *A* is y = -3.

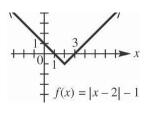
The slope of the graph of y 3x 2 is -3.

A line parallel to the graph of $3x \ 2$ has a slope of -3. Use the point-slope form with $(x_1, y_1) (2, 3)$ and $m \ 3$. $y_1 \ m(x \ x_1)$ $y \ 3 \ 3(x \ 2)$ $y \ 3 \ 3x \ 6 \ y \ 3x \ 9$

A line perpendicular to the graph of

$$3x \ 2$$
 has a slope of $\frac{1}{}$ because 3 $3 \ \frac{1}{} \ 1$. $y \ 3 \ \frac{1}{} \ (x \ 2)$ 3 $3 \ y \ 3 \ x \ 2 \ 3 \ y \ 9 \ x \ 2$

To graph $fx \times 21$, we translate the graph of yx, 2 units to the right and 1 unit down.



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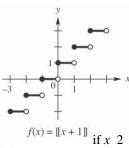
(a) This is not the graph of a function because some vertical lines intersect it in more than one point. The domain of the relation is [0, 4]. The range is [-4, 4].

Chapter 2 Graphs and Functions

$$f(x) x \mathbb{I}$$

To get y = 0, we need $0 \times 1 \times 1$ 1 $x \times 0$. To get y = 1, we need

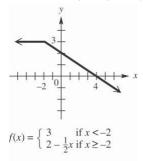
x 1 2 0 x 1. Follow this pattern to graph the step function.



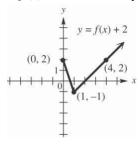
$$f(x) = 2 \cdot x = x \cdot 2$$

For values of x with x < -2, we graph the horizontal line y = 3. For values of x with x = 2, we graph the line with a slope of $\frac{1}{x} = 2$

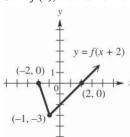
and a y-intercept of (0, 2). Two points on this line are (-2, 3) and (0, 2).



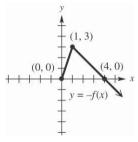
(a) Shift f(x), 2 units vertically upward.



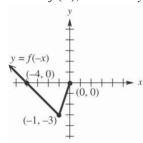
Shift f(x), 2 units horizontally to the left.



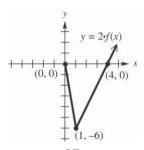
Reflect f(x), across the x-axis.



Reflect f(x), across the y-axis.



Stretch f(x), vertically by a factor of 2.



Starting with y, we shift it to the left 2

units and stretch it vertically by a factor of 2. The graph is then reflected over the *x*-axis and then shifted down 3 units.

$$3x^2 2y^2 3$$

Replace y with –y to obtain

$$3x^2 \ 2(y)^2 \ 3 \ 3x^2 \ 2 \ y^2 \ 3.$$

The result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis.

Replace x with -x to obtain

$$3(x)^2 2y^2 33x^2 2y^23.$$

The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis.

The graph is symmetric with respect to the *x*-axis and with respect to the *y*-axis, so it must also be symmetric with respect to the origin.

$$f(x) 2x^2 3x 2, g(x) 2x 1$$

$$(f g)(x) f(x) g(x) 2 x2 3x 2 2 x 1 2x2 3x 2 2x 1 2x2 x 1$$

(b)
$$-\frac{f}{(x)}$$
 $\frac{f(x)}{g}$ $\frac{2x^2 \ 3x \ 2}{g \ g(x)}$ $2x \ 1$

We must determine which values solve the equation $2 \times 1 = 0$.

domain, 2 and the domain is $, \frac{1}{2} \overline{\big(} \frac{1}{2} , ...$

$$f(x) 2x^2 3x2$$

$$fx h 2x h^2 3x h 2$$

$$2x^2 2xhh^2 3x3h2$$

$$2 x^2 4 xh 2h^2 3x 3h 2$$

$$f(x h) f(x) (2 x2 4 xh 2h2 3x 3h 2) (2 x2 3x 2) 2x2 4 xh 2h2 3x 3h 2 2 x2 3x 2$$

$$\begin{array}{ccc}
4xh 2h^2 & 3h \\
\underline{f(xh)f(x)} & 4xh 2h^2 3h \\
h & & h \\
\underline{h(4x 2h 3)}
\end{array}$$

$$\begin{array}{c}
h \\
4 x 2h 3 \\
1) f(1) g(1)
\end{array}$$

$$(f g)(1) f(1) g(1)$$

 $(21^2 31 2) (211)$
 $(21 31 2) (21 1)$
 $(232)(21)$
 $1(1) 0$

(f)
$$(fg)(2) f(2) g(2)$$

 $(2 2^2 32 2)(221)$
 $(2432 2)(221)$
 $(862)(41)$

0 1 1. Therefore,

$$f \circ g \circ 0 f g \circ 0$$

 $f \circ 1 \circ 2 \circ 1^2 \circ 3 \circ 1 \circ 2$
21312
2321

For exercises 20 and 21, fx x 1 and gx 2 x 7.

20.
$$g fg x f 2x7$$

The domain and range of g are (,), while

the domain of f is [0,). We need to find the values of x which fit the domain of f: 2x 6 0 x 3. So, the domain of f g is [3,).

21.
$$g \not\vdash gfx \not\subseteq x \downarrow 1$$

The domain and range of g are (,), while the domain of f is [0,). We need to find the values of x which fit the domain of f: $x \ 1 \ 0 \ x \ 1$. So, the domain of $g^{\ \ }f$ is [1,).

4(3) 12

(a)
$$C(x) = 3300 + 4.50x$$

 $R(x) = 10.50x$
 $P(x) R(x) C(x)$
 $10.50 x$
 $(3300 4.50 x)$
 $6.00x 3300$
 $P(x) 0$
 $6.00x 3300$
 5
 5
 0
She must produce and sell 551 items before she earns a profit.

Chapter 2

Graphs and Functions

Section 2.1 Rectangular Coordinates and Graphs

Classroom Example 1 (page 184)

(transportation, \$12,153)

(health care, \$4917)

Classroom Example 2 (page 186)

$$d(P,Q) = \begin{cases} \sqrt{2} & \sqrt{2} \\ \sqrt{2} & \sqrt{2} \end{cases} = \begin{cases} \sqrt{2} & \sqrt{2} \\ \sqrt{2} & \sqrt{2} \end{cases}$$

Classroom Example 3 (page 186)

$$d(R,S) \sqrt{50^{2}} \qquad 12 \qquad 2$$

$$\sqrt{259} \qquad \sqrt{34}$$

$$d(R,T) \sqrt{40^{2}} \qquad 32$$

$$\sqrt{1625} \qquad \sqrt{41}$$

$$d(S,T) \sqrt{45^2 31^2} \sqrt{814} = 85$$

The longest side has length√ 85

$$\sqrt{\frac{1}{34^2}}$$
 $\sqrt{\frac{41}{41}}$ 2? $\sqrt{\frac{2}{85}}$ 2

The triangle formed by the three points is not a right triangle.

Classroom Example 4 (page 187)

The distance between P(2, 5) and Q(0, 3) is

$$\sqrt{20^253^2}$$
 $\sqrt{44}$ $\sqrt{82}$ $\sqrt{2}$

The distance between Q(0, 3) and R(8, 5)

$$\sqrt{\frac{1880^253^26464}{1288}}$$

Classroom Example 5 (page 188)

The coordinates of M are

$$\frac{7(2)}{5}$$
, $\frac{5}{13}$, $\frac{9}{2}$, 4

Let (x, y) be the coordinates of Q. Use the midpoint formula to find the coordinates:

The coordinates of Q are (0, 12).

Classroom Example 6 (page 188)

The year 2011 lies halfway between 2009 and 2013, so we must find the coordinates of the midpoint of the segment that has endpoints (2009, 124.0) and (2013, 137.4)

The estimate of \$130.7 billion is \$0.1 billion more than the actual amount.

Classroom Example 7 (page 189)

Choose any real number for x, substitute the value in the equation and then solve for y. Note that additional answers are possible.

(a)
$$y = -2x + 5$$

$$-1 \quad y \quad 2(1) 5 7$$

$$0 \quad y \quad 2(0) 5 5$$

$$3 \quad y \quad 2(3) 5 1$$

Three ordered pairs that are solutions are (-1, 7), (0, 5), and (3, -1). Other answers are possible.

The distance between
$$P(2, 5)$$
 and $R(8, 5)$ is $\sqrt{2.8}^{2}$ $\sqrt{\frac{100 \ 100}{200}}$ $\sqrt{200}$ 10 2/

Because 2 8 $\sqrt[2]{10}$ 2 $\sqrt[4]{\text{the points are collinear.}}$

(b)	у	$x \sqrt[3]{y1}$
	-9	x 3\sqrt{9 1 3 8 2}
	-2	$x = \sqrt[3]{2 \cdot 1^3} \cdot 1 \cdot 1\sqrt{}$
	-1	$\frac{3\sqrt{1} \ 1 \ 30}{\sqrt{1} \ 1 \ 30}$
	0	$\frac{x}{3} \sqrt[3]{1} \sqrt[3]{1} \sqrt[3]{1}$
	7	$x = 3\sqrt{1} + 3 \sqrt{2}$

Ordered pairs that are solutions are (-2, -9), (-1, -2), (0, -1), (1, 0) and (2, 7). Other answers are possible.

(c)	x	y x ² 1
	-2	y (2) ² 13
	-1	y (1) ² 10
	0	y 0 ² 11
	1	y 1 ² 10
	2	y 2 ² 13

Ordered pairs that are solutions are (-2, -3), (-1, 0), (0, 1), (1, 0) and (2, -3). Other answers are possible.

Classroom Example 8 (page 190)

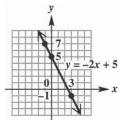
Let y = 0 to find the *x*-intercept, and then let x = 0 to find the *y*-intercept:

$$0\ 2x5x^{\frac{5}{2}}$$

Find a third point on the graph by letting

x = -1 and solving for y: y 2 1 5 7.

The three points are 5 2, 0, (0, 5), and (-1, 7). Note that (3, -1) is also on the graph.

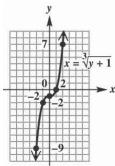


Let y = 0 to the x-intercept, and then let x = 0 to find the y-intercept:

Find a fourth point by letting x = -2 and solving for y:

$$2^{3} \sqrt{12^{3}} y 19 y$$

The points to be plotted are (0, -1), (1, 0), (2, 7), and (-2, -9). Note that (-1, -2) is also on the graph.



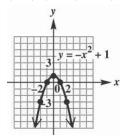
Let y = 0 to find the x-intercept, and then let x = 0 to find the y-intercept:

$$x^2 1 1 x^2 1 x^2 1 x y$$

$$0^2 \, 1 \, 1$$

Find a third point by letting x = 2 and solving for y: $y 2^2 1 3$. Find a fourth point by letting x = -2 and solving for y:

The points to be plotted are (-1, 0), (1, 0), (0, 1), (2, -3), and (-2, -3)



Section 2.2 Circles

Classroom Example 1 (page 195)

$$(h, k) = (1, -2)$$
 and $r = 3$
 $x h^2 y k^2 r^2$

$$x 1^2 y 2 \qquad ^2 3_2$$

Find a third point by letting x = 2 and solving for y: $2^3 y 1 2^3 y 1 7 y$.

$$x 1^{2} y 2^{2} 9$$

$$(h, k) = (0, 0) \text{ and } r = 2$$

$$x h^{2} y k^{2} r^{2}$$

$$0^{2} y 0^{2} 2^{2}$$

$$2 y^{2} 4$$

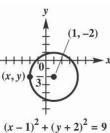
Chapter 2 Graphs and Functions

Classroom Example 2 (page 196)



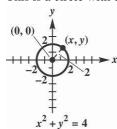
This is a circle with center (1, -2) and radius

3.



$x^2 y^2 4$

This is a circle with center (0, 0) and radius 2.



Classroom Example 3 (page 197)

Complete the square twice, once for x and once for y:

$$x^2 + 4x + y^2 + 8y + 440$$

$$x^2$$
 4 x 4 y^2 8 y 16 44 4 16

$$2^2 v 4^2 64$$

Because c = 64 and 64 > 0, the graph is a circle. The center is (-2, 4) and the radius is 8.

Classroom Example 4 (page 198)

$$2x^2 2y^2 2x6y 45$$

Group the terms, factor out 2, and then complete the square:

$$2x^2x^{\frac{1}{2}}$$
 $2y^23y^{\frac{9}{2}}$

4 4 4 4 4
$$45 2^{-1} 2^{9}$$

4 4

Factor and then divide both sides by 2:

Because c = 25 and 25 > 0, the graph is a circle. The center is $\frac{1}{3}$ and the radius is 5.

2 2

Classroom Example 5 (page 198)

Complete the square twice, once for x and once for y:

$$x^{2} 6x y^{2} 2y 120$$

$$x^{2} 6x 9 y^{2} 2y 1 1291$$

$$x 3^{2} y 1^{2} 2$$

Because c = -2 and -2 < 0, the graph is

nonexistent. Classroom Example 6 (page 199)

Determine the equation for each circle and then substitute x = -3 and y = 4.

Station A:

Station B:

Station C:

$$x 5^2$$
 $y 2^2 10^2$ $x 5$ $y 2 100$

25 25

64 36 100 100 100

Because (-3, 4) satisfies all three equations, we can conclude that the epicenter is (-3, 4).

Section 2.3 Functions

Classroom Example 1 (page 204)

M is a function because each distinct x value has exactly one y value.

N is a function because each distinct x value has exactly one y value.

P is not a function because there are two y-values for x = -4.

Classroom Example 2 (page 205)

Domain: {-4, -1, 1, 3} Range: {-2, 0, 2, 5}

The relation is a function.

Domain: {1, 2, 3} Range: {4, 5, 6, 7}

The relation is not a function because 2

maps to 5 and 6. Domain: $\{-3, 0, 3, 5\}$

Range: {5}

The relation is a function.

Classroom Example 3 (page 206)

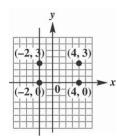
Domain: $\{-2, 4\}$; range: $\{0, 3\}$

Domain: (,); range: (,)

Domain: [-5, 5]; range: [-3, 3]

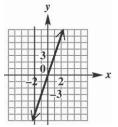
Domain: (,); range: (, 4]

Classroom Example 4 (page 207)



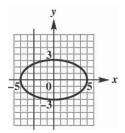
Not a function

(b)



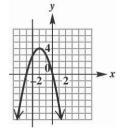
Function

(c)



Not a function

(**d**)

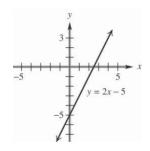


Function

Classroom Example 5 (page 208)

y 2x 5 represents a function because y is always found by multiplying x by 2 and subtracting 5. Each value of x corresponds to just one value of y. x can be any real number, so the domain is all real numbers or (,).

Because y is twice x, less 5, y also may be any real number, and so the range is also all real numbers, (,).

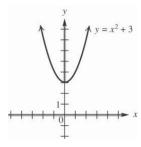


Chapter 2 Graphs and Functions

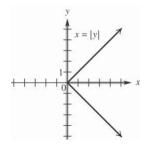
For any choice of x in the domain of

$$x^2$$
 3, there is exactly one corresponding

value for y, so the equation defines a function. The function is defined for all values of x, so the domain is (,). The square of any number is always positive, so the range is [3,).

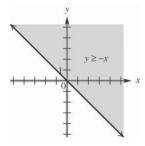


(c) For any choice of x in the domain of $x \ y$, there are two possible values for y. Thus, the equation does not define a function. The domain is [0,) while the range is (,).



By definition, y is a function of x if every value of x leads to exactly one value of y. Substituting a particular value of x, say 1, into y x corresponds to many values of y. The ordered pairs (0, 2) (1, 1) (1, 0) (3, -1) and so on, all satisfy the inequality. This does not represent a function. Any number can be used

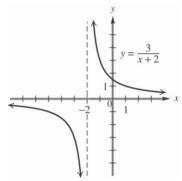
for x or for y, so the domain and range of this relation are both all real numbers, (,).



(e) For
$$y = \frac{3}{x^2}$$
, we see that y can be found by

dividing x + 2 into 3. This process produces one value of y for each value of x in the domain. The domain includes all real numbers except those that make the denominator equal to zero, namely x = -2. Therefore, the domain is (2, 2, 2, 3). Values of y can be

negative or positive, but never zero. Therefore the range is (0, 0) (0, 0).



Classroom Example 6 (page 210)

$$f(3) (3)^2 6(3) 4 13$$

$$f(r) r^2 6r4$$

Classroom Example 7 (page 210)

$$f(1) \ 2(1)^2 \ 9 \ 7$$

0

Classroom Example 8 (page 211)

$$f(x) x^{2} 2x3$$

$$f(5) (5)^{2} 2(5)312$$

$$f(t) t^{2} 2t3$$

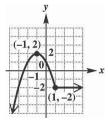
(b)
$$2x3y 6 y \frac{2}{x^2} x^2 = 3$$

$$f(x) \frac{2}{3} x 2$$

$$f(5) \frac{2}{3} (5) 2 \frac{16}{3}$$

$$f(t) \frac{2}{3} t^2$$

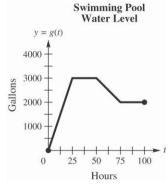
Classroom Example 9 (page 213)



The function is increasing on (, 1), decreasing on (-1, 1) and constant on (1,).

Classroom Example 10 (page 213)

The example refers to the following figure.



The water level is changing most rapidly from 0 to 25 hours.

The water level starts to decrease after 50 hours.

After 75 hours, there are 2000 gallons of water in the pool.

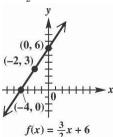
Section 2.4 Linear Functions

Classroom Example 1 (page 220)

 $f(x) = \frac{3}{2}x$ 6; Use the intercepts to graph the

function. $f(0) \stackrel{3}{=} 0 6 6$: y-intercept

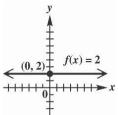
 $0\frac{3}{2} \times 66 = \frac{3}{2} \times \times 4 : x$ -intercept



Domain: (,), range: (,)

Classroom Example 2 (page 220)

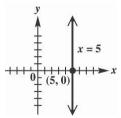
f(x) 2 is a constant function. Its graph is a horizontal line with a *y*-intercept of 2.



Domain: (,), range: {2}

Classroom Example 3 (page 221)

x = 5 is a vertical line intersecting the x-axis at (5, 0).

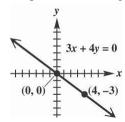


Domain: {5}, range: (,)

Classroom Example 4 (page 221)

 $3x \ 4y \ 0$; Use the intercepts. $3\ 0\ 4y \ 0\ 4y \ 0\ y \ 0$: *y*-intercept $3x \ 4\ 0\ 0\ 3x \ 0x \ 0$: *x*-intercept The graph has just one intercept. Choose an additional value, say 4, for *x*.

Graph the line through (0, 0) and (4, -3).



Domain: (,), range: (,)

Classroom Example 5 (page 223)

(a)
$$m = \frac{4(6)}{22} = \frac{10}{5}$$

$$m \frac{10 \ 10_{20}}{}$$
 the slope is

Classroom Example 6 (page 224)

$$2x - 5y = 10$$
Solve the equation for y.
$$2x 5 y 10$$

$$5 y 2 x 10$$

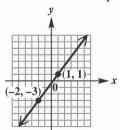
$$\underline{2}$$

$$5 x 2$$

The slope is $\frac{2}{5}$, the coefficient of x.

Classroom Example 7 (page 224)

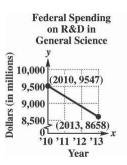
First locate the point (-2, -3). Because the slope is $\frac{4}{3}$, a change of 3 units horizontally (3 units to the right) produces a change of 4 units vertically (4 units up). This gives a second point, (1, 1), which can be used to complete the graph.



Classroom Example 8 (page 225) The

average rate of change per year is

The graph confirms that the line through the ordered pairs fall from left to right, and therefore has negative slope. Thus, the amount spent by the federal government on R&D for general science decreased by an average of \$296.33 million (or \$296,330,000) each year from 2010 to 2013.



Classroom Example 9 (page 226)

- (a) $C(x) 120 \times 2400$
- **(b)** R(x) 150x
- (c) P(x) R(x) C(x) 150 x (120 x 2400)30 x 2400
- (d) $P(x) \ 0 \ 30 \ x \ 2400 \ 0 \ x \ 80$ At least 81 items must be sold to make a profit.

Section 2.5 Equations of Lines and Linear Models

Classroom Example 1 (page 234)

Classroom Example 2 (page 234)

First find the slope: $m \frac{3(1)}{45} \frac{4}{5}$

Now use either point for (x_1, y_1) :

$$y \ 3 \ 4 \ [x(4)]$$

9(y 3) 4(x 4)

Classroom Example 3 (page 235)

Write the equation in slope-intercept form: 3x 4 y 12 4 y 3x 12 y ³ x₂3

The slope is $4^{\underline{3}}$, and the y-intercept is (0, -3).

Classroom Example 4 (page 236)

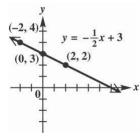
First find the slope: m2 2

Now, substitute $\frac{1}{2}$ for *m* and the coordinates of one

of the points (say, (2, 2)) for x and y into the slope-intercept form y = mx + b, then solve for b:

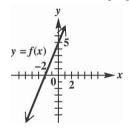
 $2\ 2\ b\ 3\ b$. The equation is

 $y^{\frac{1}{2}}x23$.



Classroom Example 5 (page 236)

The example refers to the following figure:



The line rises 5 units each time the *x*-value increases by 2 units. So the slope is $2^{\frac{5}{2}}$. The *y*-intercept is (0, 5), and the *x*-intercept is (-2, 0).

(b) An equation defining f is $f(x) = \frac{5}{2}x = 5$.

Classroom Example 6 (page 238)

Rewrite the equation $3x \ 2y \ 5$ in slope-intercept form to find the slope:

$$3x 2 y 5 y$$
 $_2x$ $_2$ 3 The slope is $_2$.

The line parallel to the equation also has slope $\frac{3}{2}$. An equation of the line through (2, -4) that is parallel to $3x \ 2y \ 5$ is

$$y(4) \ 2(x^2) \ y4 \ 2x3$$

$$y \ 2^{\frac{3}{2}}x \ 7 \text{ or } 3x - 2y = 14.$$

Section 2.6 Graphs of Basic Functions The line perpendicular to the equation has slope $\frac{2}{3}$. An equation of the line through (2, -4) that is perpendicular to $3x \ 2y \ 5$ is

$$y(4) \stackrel{?}{=} (x\stackrel{3}{2}) y4 \stackrel{?}{=} x\stackrel{4}{=}$$

$$y = \frac{2}{3}x_3 = \frac{8}{3}$$
 or $2x + 3y = -8$.

Classroom Example 7 (page 240)

First find the slope:
$$m \frac{7703\ 6695}{1} 5043$$

Now use either point for (x1, y1): 6695 504(x1) 6695 504 x 504 y 504 x 6191

The year 2015 is represented by x = 6. 504(6) 6191 9215

According to the model, average tuition and fees for 4-year colleges in 2015 will be about \$9215.

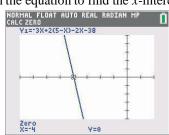
Classroom Example 8 (page 242)

Write the equation as an equivalent equation with 0 on one side.

 $3x \ 2(5 \ x) \ 2 \ x \ 38$

 $3x \ 2(5 \ x) \ 2 \ x \ 38 \ 0$

Now graph the equation to find the *x*-intercept.



The solution set is $\{-4\}$.

Section 2.6 Graphs of Basic Functions

Classroom Example 1 (page 249)

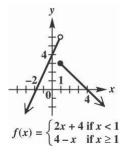
The function is continuous over (, 0) (0,1)

The function is continuous over its entire

domain (,).

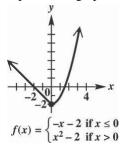
Classroom Example 2 (page 252)

Graph each interval of the domain separately. If x < 1, the graph of f(x) = 2x + 4 has an endpoint at (1, 6), which is not included as part of the graph. To find another point on this part of the graph, choose x = 0, so y = 4. Draw the ray starting at (1, 6) and extending through (0, 4). Graph the function for $x \ge 1$, f(x) = 4 - x similarly. This part of the graph has an endpoint at (1, 3), which is included as part of the graph. Find another point, say (4, 0), and draw the ray starting at (1, 3) which extends through (4, 0).



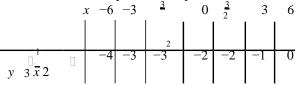
Graph each interval of the domain separately. If $x \le 0$, the graph of f(x) = -x - 2 has an endpoint at (0, -2), which is included as part of the graph. To find another point on this part of the graph, choose x = -2, so y = 0. Draw the ray starting at (0, -2) and extending through (-2, 0). Graph the function for x > 0,

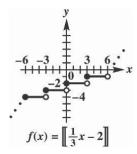
f(x) x^2 2 similarly. This part of the graph has an endpoint at (0, -2), which is not included as part of the graph. Find another point, say (2, 2), and draw the curve starting at (0, -2) which extends through (2, 2). Note that the two endpoints coincide, so (0, -2) is included as part of the graph.



Classroom Example 3 (page 254)

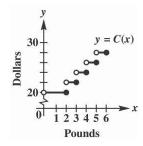
Create a table of sample ordered pairs:





Classroom Example 4 (page 254)

For x in the interval (0, 2], y = 20. For x in (2, 3], y = 20 + 2 = 22. For x in (3, 4], y = 22 + 2 = 24. For x in (4, 5], y = 24 + 2 = 26. For x in (5, 6], y = 26 + 2 = 28.

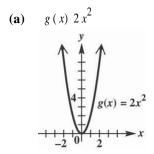


Section 2.7 Graphing Techniques

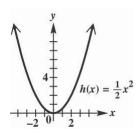
Classroom Example 1 (page 260)

Use this table of values for parts (a)–(c)

x	$g(x) 2x^{-2}$	<u>1</u> 2	1 2
-2	8	h(x) 22 x	k(x) 1 x
-1	2	2	<u>1</u> 4
0	0	0	0
1	2	1 2	<u>1</u> 4
2	8	2	1



(b)
$$h(x) = \frac{1}{2} x^2$$



$$k(x) = \frac{1}{x}$$

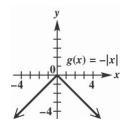
$$k(x) = \frac{1}{x}$$

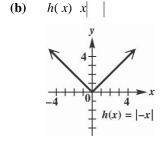
$$k(x) = \left(\frac{1}{2}x\right)^2$$

Classroom Example 2 (page 262)

Use this table of values for parts (a) and (b)

х	g(x) x	h(x) x	
-2	-2	2	
-1	-1	1	
0	0	0	
1	-1	1	
2	-2	2	
g	(x) x		





Classroom Example 3 (page 263)

x yReplace x with -x to obtain x|y|. The result is not the same as the

original equation, so the graph is not symmetric with respect to the y-axis. Replace y with -y to obtain x y x y The

result is the same as the original equation, so the graph is symmetric with respect to the *x*-axis. The graph is symmetric with respect to

the *x*-axis only.

Replace x with -x to obtain $y \mid x \mid 3 \mid$

x 3. The result is the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace y with -y to obtain y x 3. The result is not the same as the original equation, so the graph is not symmetric with respect to the x-axis. Therefore, the graph is symmetric with respect to the y-axis only.

2xy6

Replace x with -x to obtain 2(x) y 6 2x y 6. The result is not the same as the original equation, so the graph is not symmetric with respect to the y-axis. Replace y with -y to obtain 2x(y) 6 2x y 6. The result is not the same as the original equation, so the graph is not symmetric with respect to the x-axis. Therefore, the graph is not symmetric with respect to either axis.

$$x^2$$
 y^2 25

Replace x with -x to obtain

$$(x)^2 y^2 25$$
 $x^2 y^2 25$. The result is

the same as the original equation, so the graph is symmetric with respect to the *y*-axis. Replace *y* with –*y* to obtain

$$x^{2} (y)^{2} 25 x^{2} y^{2} 25$$
. The result is

the same as the original equation, so the graph is symmetric with respect to the *x*-axis. Therefore, the graph is symmetric with respect to both axes. Note that the graph is a circle of radius 5, centered at the origin.

Classroom Example 4 (page 265)

$$y 2 x^{3}$$

Replace x with -x and y with -y to obtain (y) $2(x)^3$ y 2 x^3 y 2 x^3 . The result is the same as the original equation, so the graph is symmetric with respect to the origin.

$$y 2x^2$$

Replace x with -x and y with -y to obtain

 $(y) 2(x)^2 y 2x^2 y 2x^2$. The result is not the same as the original equation, so the graph is not symmetric with respect to the origin.

Classroom Example 5 (page 266)

$$g(x)$$
 x^5 $2x^3$ $3x$
Replace x with $-x$ to obtain
$$g(x) (x)^5 2(x)^3 3(x)$$

$$x^5 2x^3 3x$$

$$(x^5 2x^3 3x)g(x)$$

$$g(x)$$
 is an odd function.

$h(x) 2x^2 3$

Replace x with -x to obtain $h(x) 2(x)^2 3 2 x^2 3 h(x) h(x)$ is an even

$$k(x) x^2 6x9$$

Replace x with -x to obtain

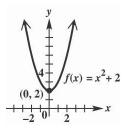
Replace x with
$$-x$$
 to obtain
 $k(x)(x)^2 6(x) 9$
 $x^2 6x 9 k(x)$ and $k(x)$

k(x) is neither even nor odd.

Classroom Example 6 (page 267)

Compare a table of values for g(x) x^2 with $f(x) x^2 2$. The graph of f(x) is the same as the graph of g(x) translated 2 units up.

x	$g(x) x^2$	$f(x) x^2 2$
-2	4	6
-1	1	3
0	0	2
1	1	3
2	4	6

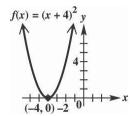


Classroom Example 7 (page 268)

Compare a table of values for g(x)x with

f(x) (x4)². The graph of f(x) is the same as the graph of g(x) translated 4 units left.

x	$g(x) x^2$	$f(x) (x4)^2$
-7	49	9
-6	36	4
-5	25	1
-4	16	0
-3	9	1
-2	4	4
-1	1	9



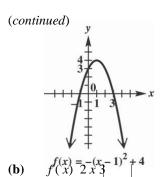
Classroom Example 8 (page 269)

$$f(x) (x 1)^2 4$$

This is the graph of $g(x) x^2$, translated one unit to the right, reflected across the x-axis, and then translated four units up.

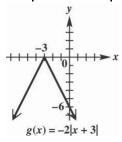
x	$g(x) x^2$	$f(x) (x 1)^2 4$
-2	4	-5
-1	1	0
0	0	3
1	1	4
2	4	3
3	9	0
4	16	-5

(continued on next page)



This is the graph of g(x) x, translated three units to the left, reflected across the x-axis, and then stretched vertically by a factor of two.

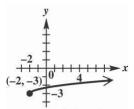
x	g(x) x	f(x) 2x 3
-6	6	-6
-5	5	-4
-4	4_	-2
-3	3_	0
-2	2	-2
-1	1	-4
0	0	-6



(c)
$$h(x) = \sqrt{x \cdot 2 \cdot 3}$$

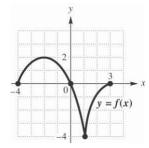
This is the graph of $g(x) = \sqrt{x}$, translated two units to the left, shrunk vertically by a factor of 2, and then translated 3 units down.

	V	
x	g(x) x	$h(x) \stackrel{7}{=} \sqrt[4]{2} \times 23$
-2	undefined	-3
-1	undefined	_ √ -2.5
0	r 0	¹ ₂ 2 3 2.3
2	2 1.4	_√ −2
6	6 2.4	$\frac{1}{2}$ 8 3 1.6
7	√7 2.6	-1.5

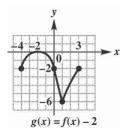


Classroom Example 91 page 270)

The graphs in the exercises are based on the following graph.

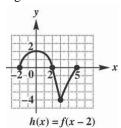


This is the graph of f(x) translated two units down.

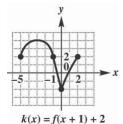


h(x) f(x2)

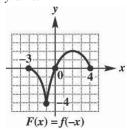
This is the graph of f(x) translated two units right.



This is the graph of f(x) translated one unit left, and then translated two units up.



This is the graph of f(x) reflected across the y-axis.



Section 2.8 Function Operations and Composition

Classroom Example 1 (page 278)

For parts (a)–(d), f(x) 3x 4 and $g(x) 2x^2 1$

$$f(0) 3(0) 4 4$$
 and
 $g(0) 2(0)^2 11$, so
 $(f g)(0) 415$

(b)
$$f(4) 3(4) 4 8$$
 and $g(4) 2(4)^2 1 31$, so $(f g)(4) 83123$
 $f(2) 3(2) 4 10$ and $g(2) 2(2)^2 1 7$, so $(fg)(2) (10)(7) 70$

(d)
$$f(3) 3(3) 45$$
 and $g(3) 2(3)^2 117$, so $f(3) \frac{5}{2}$

Classroom Example 2 (page 279)

For parts (a)–(e),
$$f(x) x^2 3x$$
 and $g(x) 4x5$ (a) (b)

$$(fg)(x) (x^2 3x)(4x 5)$$

 $4 x^3 5x^2 12 x^2 15x$
 $4 x^3 7 x^2 15x$

$$(x) \frac{x_2}{g4x} \frac{3x}{5} \qquad \qquad$$

The domains of f and g are both (,). So, the domains of f+g, f-g, and fg are the intersection of the domains of f and g,

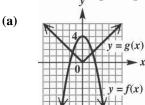
(,) . The domain of $\frac{1}{2}$ includes those

real numbers in the intersection of the domains of f and g for which g(x) 4 x 5 0

$$x = \frac{5}{4}$$
. So the domain of $\frac{f}{g}$ is

$$\frac{5}{4} \quad \boxed{\frac{5}{4}} \; , \; .$$

Classroom Example 3 (page 280)



From the figure, we have f(1) = 3 and g(1) = 1, so (f + g)(1) = 3 + 1 = 4.

$$f(0) = 4$$
 and $g(0) = 0$, so $(f - g)(0) = 4 - 0 = 4$.

2

$$f(-1) = 3$$
 and $g(-1) = 1$, so $(fg)(-1) = (3)(1) = 3$

$$f(-2) = 0$$
 and $g(-2) = 2$, so $\frac{f}{(2)} = 0$.

(b) $\begin{array}{c|cccc} x & f(x) & g(x) \\ \hline -2 & -5 & 0 \\ \hline -1 & -3 & 2 \\ \hline 0 & -1 & 4 \\ \hline \end{array}$

From the table, we have f(1) = 1 and g(1) = 6, so (f + g)(1) = 1 + 6 = 7.

$$f(0) = -1$$
 and $g(0) = 4$, so

$$(f-g)(1) = -1 - 4 = -5.$$

$$f(-1) = -3$$
 and $g(-1) = 2$,
so $(fg)(-1) = (-3)(2) = -6$

$$f(-2) = -5$$
 and $g(-f2) = 0$, so

(f g)(x) (\mathbf{f}

3*x*) (4 *x* 5) 2

5

(f)

 (x^2)

3x)
(4 x
5)
x² 7
x 5

(2) g is

undefined.

(c)
$$f(x) 3x 4, g(x) x$$
 From the formulas, we have $f(1) 3(1) 47$ and $g(1) 11, sop |$ $(f+g)(1) = 7 + (-1) = 6$. $f(0) 3(0) 4 4$ and $g(0) 0 0, sop |$ $(f-g)(1) = 4 - 0 = 4$. $f(1) 3(1) 41$ and $g(1) 11, so (f / 2) (/ 1) = (1)(-1) = -1$. $f(2) 3(2) 4 2$ and $g(2) 2 2 |$, sop $f(2) 2 1$.

Classroom Example 4 (page 281)

Step 1: Find f(xh):

$$f(x h) 3(x h)^{2} 2(x h) 4$$

$$3(x^{2} 2xh h^{2}) 2x 2h 4$$

$$3x^{2} 6xh 3h^{2} 2x 2h 4$$

Step 2: Find f(xh) f(x):

$$f(x h) f(x) (3x2 6 xh 3h2 2 x 2h 4) (3x2 2 x 4) 6 xh 3h2 2h$$

Step 3: Find the difference quotient:

$$\frac{f(xh)f(x)}{h} \quad \frac{6xh 3h^2 - 2h}{h} \quad 6x 3h 2$$

Classroom Example 5 (page 283)

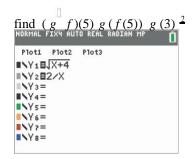
For parts (a) and (b), $f(x) = x\sqrt{4}$ and $g(x) = \frac{2}{x}$

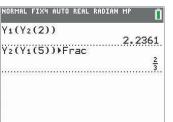
<u>2</u>

First find g(2): g(2) 21. Now find

$$(f \mid g)(2) \ f(g(2)) \ f(1) \qquad \sqrt{14} \quad 5$$

(b) First find f(5): f(5) 5 4 9 3. Now





The screens show how a graphing calculator evaluates the expressions in this classroom example.

Classroom Example 6 (page 283)

For parts (a) and (b), $f(x) = \sqrt{x + 1}$ and g(x) = 2x + 5

(a) (f g)(x) f(g(x)) $\sqrt{(2 x 5) 1}$ $\sqrt{2x 4}$ The domain and range of g are both (,). However, the domain of f is [1,). Therefore,

g(x) must be greater than or equal to 1:

2x 5 1 x 2. So, the domain of f g is [2,).

(b)
$$(g^{[]}f)(x) g(f(x)) 2 x 15$$

The domain of f is [1,), while the range of f is [0,). The domain of g is (,). Therefore, the domain of $(g^{\parallel}f)$ is restricted to that portion of the domain of g that intersects with the domain of f, that is [1,).

Classroom Example 7 (page 284)

For parts (a) and (b), $f(x) = \frac{5}{x4}$ and $g(x) = \frac{2}{x}$

(a)
$$(f | g)(x) f(g(x)) = \frac{5}{2 \cancel{x} 4} = \frac{5x}{2 4 x}$$

The domain and range of g are both all real numbers except 0. The domain of f is all real numbers except -4. Therefore, the expression for g (x) cannot equal -4. So,

$$\frac{2}{x}$$
 4 x . So, $\frac{1}{\text{the domain of } f}$ $\frac{1}{x}$

is the set of all real numbers except for $\frac{1}{2}$, and 0. This is written

$$\frac{1}{22,00}$$
,

(b)
$$(g^{[]}f)(x) g(f(x)) = \frac{2}{5/(x4)} \frac{2x8}{5}$$

The domain of f is all real numbers except -4, while the range of f is all real numbers except The domain and range of g are both all real numbers except 0, which is not in the range of f. So, the domain of $g \, \Box f$ is the set of all real

numbers except for -4. This is written $.4 \square 4$,

Classroom Example 8 (page 285)

$$f(x) \ 2 x 5 \text{ and } g(x) \ 3x_2 \ x$$
 $(g \ f)(x) \ g(2 x 5) \ 3(2 x 5)_2 \ (2 x 5)$
 $3(4 x_2 \ 20 x 25) \ 2 x 5$
 $12 x_2 \ 58x \ 70$
 $(f \ g)(x) \ f(3x_2 \ x) \ 2(3x_2 \ x) 5$
 $6x_2 \ 2 x 5$
In general, $12x_2 \ 58x \ 70 \ 6x_2 \ 2 x 5$, so $(g^{\parallel} f)(x) \ (f^{\parallel} g)(x)$.

Classroom Example 9 (page 286)

$$(f^{[]}g)(x) \ 4(3x \ 2)^2 \ 5(3x \ 2) \ 8$$

Answers may vary. Sample answer: $f(x) \ 4x^2 \ 5x \ 8$ and $g(x) \ 3x \ 2$.