

Solution Manual for Developmental Math 3rd Edition by Lial Hornsby Ginnis Salzman and Hestwood
ISBN 0321854462 9780321854469

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Solution Manual:

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16. Four of the □ coins are pennies: $\frac{\square}{\square}$

Three of the □ coins are nickels: $\frac{\square}{\square}$

Two of the □ coins are dimes: $\frac{\square}{\square}$

17. There are □□ students, and □ are hearing impaired.

$\frac{\square}{\square}$ □ hearing impaired students (numerator)

□□ □ total students (denominator)

18. There are □□□ shopping carts of which □□ are in the parking lot (□□□□□□□□□□ are *not* in the parking lot, but are in the store).

Fraction of carts in store: $\frac{\square\square\square}{\square\square}$

19. There are □□□ rooms. □□□ are for nonsmokers, and

□□□□□□□□□□ are for smokers.

$\frac{\square\square}{\square}$

20. There are □□ employees. □□□□□□□□ are part-time.

$\frac{\square}{\square}$

21. Proper fractions: numerator *smaller* than denominator.

$\frac{\square}{\square}$

Improper fractions: numerator *greater than or equal to* denominator.

$\frac{\square}{\square}$

22. Proper fractions: numerator *smaller* than denominator.

$\frac{\square}{\square}$

24. Proper fractions: numerator *smaller* than denominator.

none

Improper fractions: numerator *greater than or equal to* denominator.

$\frac{\square\square}{\square}$ $\frac{\square\square}{\square}$ $\frac{\square\square}{\square}$ $\frac{\square\square}{\square}$

25. Answers will vary. One possibility is

□ □ Numerator

□ □ Denominator



The denominator shows the number of equal parts in the whole and the numerator shows how many of the parts are being considered.

26. An example is $\frac{\square}{\square}$ as a proper fraction and $\frac{\square}{\square}$ as an

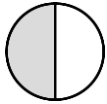
□ □ □

Improper fractions: numerator *greater than or equal to* denominator.

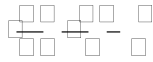
improper fraction.

A proper fraction has a numerator *smaller* than the denominator.

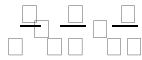
An improper fraction has a numerator that is *greater than or equal to* the denominator.



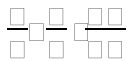
□
□
□
□



23. Proper fractions: numerator *smaller* than denominator.



Improper fractions: numerator *greater than or equal to* denominator.

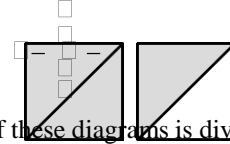


Proper fraction Improper fraction

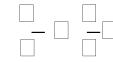
2.2 Mixed Numbers

2.2 Margin Exercises

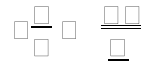
- (a) The figure shows □ whole object with □ equal parts, all shaded, and a second whole with □ parts shaded, so □ parts are shaded in all.



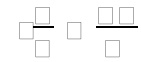
- (b) Since each of these diagrams is divided into □ pieces, the denominator will be □. The number of pieces shaded is □.



- (a) □ · □ □ Multiply □ and □.
Add □.



- (b) □ · □ □ □ □ Multiply □ and □.
Add □.



(c) $\frac{\square}{\square} \cdot \frac{\square}{\square}$ Multiply \square and \square .

$\frac{\square \square \square \square}{\square \square}$ Add \square .

$\frac{\square \square}{\square} + \frac{\square \square}{\square}$

(d) $\frac{\square}{\square} \cdot \frac{\square \square \square \square}{\square \square}$ Multiply \square and \square . Add \square .

$\frac{\square}{\square} + \frac{\square \square}{\square}$

3. (a) $\frac{\square}{\square}$ Divide \square by \square .

\square

\square Whole number part

\square

\square Remainder

\square

5. \square

(b) $\frac{\square}{\square}$ Divide \square by \square .

\square Whole number part

\square Remainder

\square

\square

(c) $\frac{\square \square}{\square}$ Divide $\square \square$ by \square .

\square

\square Whole number part

\square

\square

\square

\square

2. $\frac{\square}{\square}$ is a proper fraction since the numerator is

smaller than the denominator. The statement is *true*.

\square

3. $\frac{\square}{\square} \cdot \frac{\square \square}{\square \square}$ Multiply \square and \square . Add \square .

$\frac{\square \square \square \square}{\square \square}$

$\frac{\square \square}{\square} + \frac{\square \square}{\square}$

\square

The mixed number $\square \frac{\square}{\square}$ can be changed to the improper fraction $\frac{\square \square}{\square}$, not $\frac{\square \square}{\square}$. The statement is

false.

4. The statement "Some mixed number cannot be changed to an improper fraction" is *false* since any mixed number *can* be changed to an improper fraction.

\square

$\frac{\square}{\square} \cdot \frac{\square \square}{\square \square}$ Multiply \square and \square .

$\frac{\square \square \square \square}{\square \square}$ Add \square .

$\frac{\square \square}{\square} + \frac{\square \square}{\square}$

The mixed number $\square \frac{\square}{\square}$ can be changed to the improper fraction $\frac{\square \square}{\square}$, not $\frac{\square \square}{\square}$. The statement is *false*.

6. $\frac{\square}{\square} \cdot \frac{\square \square}{\square \square}$ Multiply \square and \square .

$\frac{\square \square \square \square}{\square \square}$ Add \square .

$\frac{\square \square}{\square} + \frac{\square \square}{\square}$

\square

The statement is *true*.

\square R
 \square e
 \square remainder

$\frac{\square}{\square}$

2.2 Section Exercises

1. $\frac{\square\square}{\square\square}$ is an improper fraction since the numerator is

greater than or equal to the denominator. The statement is *true*.

$\frac{\square}{\square} + \frac{\square\square}{\square}$

10. $\frac{\square}{\square} \cdot \square\square$ Multiply \square and \square .

$\square\square\square\square + \square\square$ Add \square .

$\frac{\square}{\square} + \frac{\square\square}{\square}$

$\square\square$

$$\begin{array}{r} \square \\ \square \square \\ \square \square \\ \square \square \end{array} \begin{array}{r} \square \\ \square \\ \square \end{array}$$

27. $\frac{\square}{\square} \cdot \square$

17. $\frac{\square}{\square} \cdot \square \square$ Multiply \square and \square .

Add \square .

28. $\frac{\square}{\square} \cdot \square$

18. $\frac{\square}{\square} \cdot \square \square$ Multiply \square and \square .

Add \square .

19. $\frac{\square}{\square} \cdot \square$ Multiply \square and \square .

19. $\frac{\square}{\square} \cdot \square \square$ Add \square .

20. $\frac{\square}{\square} \cdot \square$

20. $\frac{\square}{\square} \cdot \square \square$ Multiply \square and \square .

Add \square .

false.

$$\square \square \quad \square \square$$

Multiply $\square \square$ and $\square \square$.

Add $\square \square$.

Multiply \square and $\square \square$. Add \square .

29. $\frac{\square}{\square} \cdot \square \square \square$

Multiply \square and $\square \square$. Add $\square \square$.

30. $\frac{\square}{\square} \cdot \square \square \square$

Multiply \square and $\square \square$. Add \square .

31. $\frac{\square}{\square} \cdot \square \square \square$

The improper fraction $\frac{\square}{\square}$ can be changed to the mixed number $\square \frac{\square}{\square}$, not $\square \frac{\square}{\square}$. The statement is

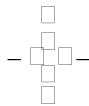
32. The statement "An improper fraction cannot always be written as a whole number or a mixed number" is *false* since a mixed number always has a value equal to or greater than a whole number.

33. The statement "Some improper fractions can be written as a whole number with no fraction part" is *true*. For example, $\frac{\square}{\square}$.

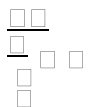
34. The statement "The improper fraction $\frac{\square\square}{\square}$ can be written as the whole number \square " is *true*.

35. $\frac{\square}{\square}$
 \square Whole number part

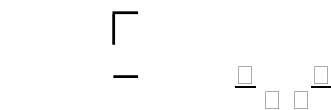
$\frac{\square}{\square}$ Remainder



36. $\frac{\square\square}{\square}$
 \square Whole number part
 $\frac{\square}{\square}$ Remainder



37. $\frac{\square}{\square}$



38. $\frac{\square}{\square}$
 \square Whole number part
 $\frac{\square}{\square}$ Remainder

40. $\frac{\square\square}{\square}$
 \square Whole number part
 $\frac{\square}{\square}$ Remainder

41. $\frac{\square\square}{\square}$
 \square Whole number part
 $\frac{\square}{\square}$ Remainder

42. $\frac{\square\square}{\square}$
 \square Whole number part

$\frac{\square\square}{\square}$ Whole number part
 $\frac{\square}{\square}$ Remainder

43. $\frac{\square\square}{\square}$
 \square Whole number part

Whole number part
 $\frac{\square}{\square}$ Remainder

46.

$$\begin{array}{r} \square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square \square \text{ Whole number part} \\ \square\square \\ \hline \square \\ \square \\ \hline \square \text{ Remainder} \end{array}$$

51.

$$\begin{array}{r} \square\square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square\square \text{ Whole number part} \\ \square\square \\ \hline \square \\ \square \\ \hline \square\square \\ \square\square \\ \hline \square\square \text{ Remainder} \end{array}$$

$$\begin{array}{r} \square\square \\ \square \\ \hline \square\square\square \end{array}$$

$$\begin{array}{r} \square\square \\ \square \\ \hline \square\square \\ \square \end{array}$$

47.

$$\begin{array}{r} \square\square \\ \hline \square \end{array} \quad \square\square \text{ Whole number part}$$

52.

$$\begin{array}{r} \square\square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square\square \text{ Whole number part} \\ \square\square \\ \hline \square \\ \square \\ \hline \square\square \\ \square\square \\ \hline \square \text{ Remainder} \end{array}$$

$$\begin{array}{r} \square\square \\ \square \\ \hline \square \\ \square \\ \hline \square \text{ Remainder} \end{array}$$

$$\begin{array}{r} \square\square \\ \hline \square \end{array}$$

48.

$$\begin{array}{r} \square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square\square \text{ Whole number part} \\ \square\square \\ \hline \square \\ \square \\ \hline \square \text{ Remainder} \end{array}$$

53.

$$\begin{array}{r} \square\square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square\square\square \text{ Whole number part} \\ \square\square\square \\ \hline \square \\ \square \\ \hline \square\square\square \\ \square\square\square \\ \hline \square \text{ Remainder} \end{array}$$

$$\begin{array}{r} \square\square \\ \square \\ \hline \square\square\square \end{array}$$

$$\begin{array}{r} \square\square\square \\ \square \\ \hline \square\square\square \end{array}$$

49.

$$\begin{array}{r} \square\square \\ \hline \square \end{array} \quad \begin{array}{l} \square\square\square \text{ Whole number part} \\ \square\square \\ \hline \square \\ \square \\ \hline \square \end{array}$$

$$\begin{array}{r} \square\square\square \\ \square \\ \hline \square\square\square \\ \square\square\square \\ \hline \square \text{ remainder} \\ \square \\ \square \\ \square\square\square \\ \square\square\square \\ \hline \square \text{ R} \end{array}$$

54.
$$\frac{\square\square\square}{\square\square}$$

Whole
 number
 part

$\overline{\hspace{1cm}}$

$\overline{\hspace{1cm}}$

$\frac{\square\square\square}{\square}$ $\frac{\square}{\square}$

$\frac{\square\square\square}{\square}$

$\frac{\square\square\square}{\square}$

50. $\frac{\square\square}{\square}$

$\overline{\hspace{1cm}}$ Whole number
 part

$\overline{\hspace{1cm}}$

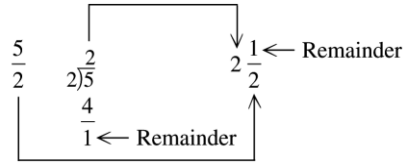
Remainder

$\frac{\square\square}{\square}$

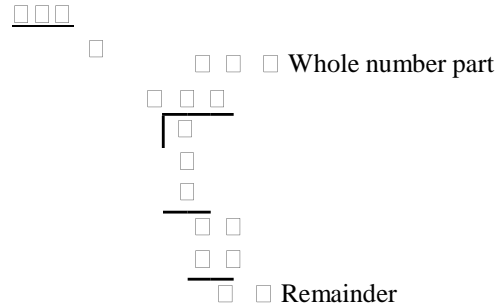
55. Multiply the denominator by the whole number and add the numerator. The result becomes the new numerator, which is placed over the original denominator.

$$2\frac{1}{2} \quad (2 \cdot 2) + 1 = 5 \quad \frac{5}{2}$$

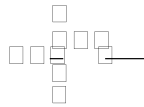
56. Divide the numerator by the denominator. The quotient is the whole number of the mixed number and the remainder is the numerator of the fraction part. The denominator is unchanged.



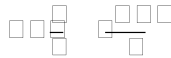
64.



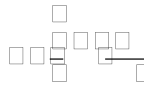
57. $\frac{\square\square\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$



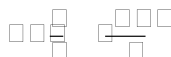
58. $\frac{\square\square\square}{\square} \cdot \frac{\square\square\square\square\square\square}{\square\square\square\square\square\square\square\square}$



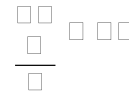
59. $\frac{\square\square\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$



60. $\frac{\square\square\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$

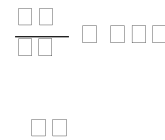


61. $\frac{\square\square\square}{\square} \cdot \frac{\square\square\square\square\square\square}{\square\square\square\square\square\square\square\square}$



65. The commands used will vary. The following is from a TI-83 Plus:

```
int(2565/15) 171
fPart(2565/15) F
rac 0
```



66. The commands used will vary. The following is from a TI-83 Plus:

```
int(2915/16) 182
fPart(2915/16) F
rac 3/16
```



$$\begin{array}{r} \square \quad \square \\ \square \square \end{array}$$

62.
$$\begin{array}{r} \square \square \square \\ \square \square \square \cdot \square \square \\ \square \square \square \square \square \square \square \\ \square \square \square \square \end{array}$$

$$\begin{array}{r} \square \square \square \square \\ \square \square \square \square \\ \square \square \square \square \end{array}$$

63.

$$\begin{array}{r} \square \square \square \\ \square \square \square \square \square \text{ Whole number part} \\ \square \square \square \\ \square \square \square \\ \square \square \square \\ \square \square \square \\ \square \square \square \\ \square \square \square \\ \square \square \square \text{ Remainder} \end{array}$$

$$\begin{array}{r} \square \square \square \\ \square \square \square \square \square \\ \square \square \square \end{array}$$

$$\begin{array}{r} \square \square \square \square \\ \square \square \end{array}$$

67. The commands used will vary. The following is from a TI-83 Plus:

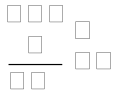
```
int(3917/32) 122
fPart(3917/32) F
rac 13/32
```

$$\begin{array}{r} \square \square \square \square \\ \square \square \square \square \\ \square \square \square \square \end{array}$$

Note: You can use the following procedure on any calculator. Divide $\square\square\square\square$ by $\square\square$ to get $\square\square\square\square\square\square\square\square$. Subtract $\square\square\square$. Multiply by \square to get $\square\square$. The mixed number is $\square\square\square \frac{\square\square}{\square\square}$.

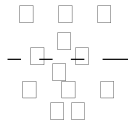
68. The commands used will vary. The following is from a TI-83 Plus:

```
int(5632/64)
fPart(5632/64)
rac
```

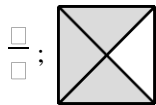
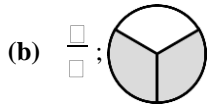


Relating Concepts (Exercises 69–74)

69. The following fractions are proper fractions.

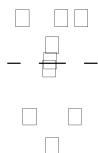


70. (a) The proper fractions in Exercise 69 are the ones where the numerator is less than the denominator.

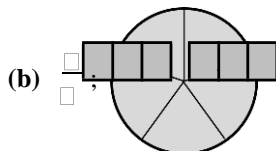


- (c) The proper fractions in Exercise 69 are all less than \square .

71. The following fractions are improper fractions.



72. (a) The improper fractions in Exercise 71 are the ones where the numerator is equal to or greater than the denominator.



- (c) The improper fractions in Exercise 71 are all equal to or greater than \square .

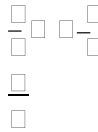
73. The following fractions can be written as whole or mixed numbers.



\square \square Whole number part



\square \square Remainder



\square \square Whole number part



\square \square Remainder



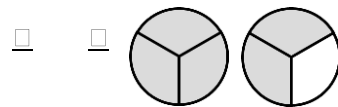
\square \square Whole number part



\square \square Remainder

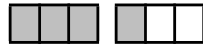
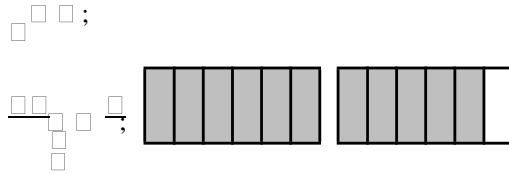
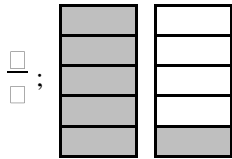


74. (a) The fractions that can be written as whole or mixed numbers in Exercise 73 are improper fractions, and their value is always greater than or equal to \square .



- (b) $\frac{\square}{\square}$; $\frac{\square}{\square}$





2.3 Factors

2.3 Margin Exercises

1. (a) Factorizations of $\square\square$:

$\square \cdot \square \square \square \square$ $\square \cdot \square \square \square \square$ $\square \cdot \square \square \square \square$

The factors of $\square\square$ are \square , \square , $\underline{\square}$, \square , $\underline{\square}$, and $\square\square$.

(b) Factorizations of 100 :

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

The factors of 100 are $1, 2, 4, 5, 10, 20, 25, 50,$ and 100 .

(c) Factorizations of 100 :

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

The factors of 100 are $1, 2, 4, 5, 10, 20, 25, 50,$ and 100 , and

100 .

(d) Factorizations of 100 :

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

The factors of 100 are $1, 2, 4, 5, 10, 20, 25, 50,$ and 100 , and 100 .

2. $1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100$

$1, 11, 13, 17, 19,$ and 23 are prime because they are divisible only by themselves and 1 .

3. $1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100$

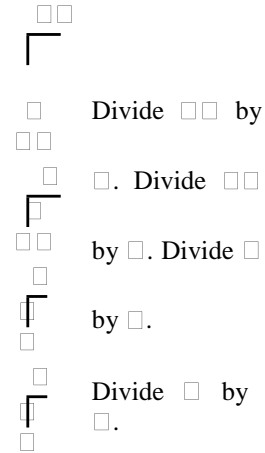
$1, 2, 3, 4, 5,$ and 10 each have no factor other than

themselves or 1 ; $6, 8, 9, 12, 15, 18,$ and 24 each have a factor of 2 ; $3, 6, 9,$ and 18 have a factor of 3 . So $1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100$ are composite.

4. (a) 1000000

$$1000000 = 2^6 \cdot 5^6$$

This division is done from the "top-down."

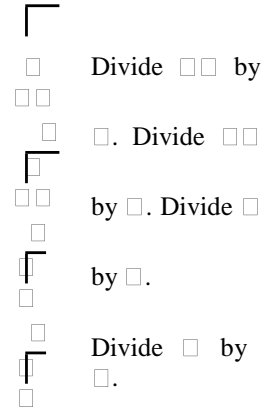


Quotient is 1.

Either method is correct and yields the prime factorization as follows:

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

(b) 100



Quotient is 1.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

(c) 100



(c) $\square\square\square\square\square$ prime
 \square

prime

$\square\square\square\square\square$ prime
 $\square\square\square\square.\square$
 $\cdot\square$

(d) $\square\square\square\square\square$
 $\square\square$
 $\square\square\square\square\square$ prime
 $\square\square$
 $\square\square\square\square\square\square$
 $\square\square\square\square.\square.\square$
 $\cdot\square$

5. (a) This division is done from the "bottom-up."

\square Quotient is 1.
 \square Divide \square by \square .
 \square .
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 \square Divide \square by
 \square .
 \square

Quotient is 1.
 $\square\square\square\square.\square.\square.\square.\square\square\square.\square.\square$

(d) Divide $\square\square$ by \square .
 \square Divide $\square\square$ by \square .
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\square Divide $\square\square$ by \square .
 \square

\square Divide \square by \square .
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 \square Divide \square by \square .
 \square
 Quotient is 1.
 $\square\square\square\square.\square.\square.\square.\square\square\square$

6. (a)
- $\square\square \div \square = \square$ Divide $\square\square$ by \square .
 - $\square \overline{\square \square} \square$ \square . Divide $\square\square$ by \square . Divide \square by \square .
 - $\square \overline{\square \square} \square$ \square by \square . Divide \square by \square .
 - $\square \overline{\square \square} \square$ $\square\square$ by \square .
 - $\square \overline{\square \square} \square$ Divide \square by \square .
 - $\square \overline{\square \square} \square$ Divide \square by \square .

- (e)
- $\square\square \overline{\square \square \square} \square$ Divide $\square\square\square$ by \square .
 - $\square \overline{\square \square \square} \square$ \square . Divide $\square\square$ by \square .
 - $\square \overline{\square \square \square} \square$ \square by \square . Divide \square by \square .
 - $\square \overline{\square \square \square} \square$ $\square\square$ by \square .
 - $\square \overline{\square \square \square} \square$ Divide $\square\square$ by \square .
 - $\square \overline{\square \square \square} \square$ \square . Divide \square by \square .
 - $\square \overline{\square \square \square} \square$ \square .
 - $\square \overline{\square \square \square} \square$
 - $\square \overline{\square \square \square} \square$
 - $\square \overline{\square \square \square} \square$

Quotient is 1.

$$\square\square.\square \div \square = \square.\square.\square.\square.\square$$

Quotient is 1.

$$\square\square\square\square \div \square = \square\square\square\square.\square.\square.\square$$

- (b)
- $\square\square \overline{\square \square} \square$ Divide $\square\square$ by \square .
 - $\square\square \overline{\square \square} \square$ Divide $\square\square$ by \square .
 - $\square\square \overline{\square \square} \square$ Divide $\square\square$ by \square .
 - $\square\square \overline{\square \square} \square$ $\square\square$.

Quotient is 1.

$$\square\square\square\square \div \square = \square.\square.\square.\square$$

- (c)
- $\square\square \overline{\square \square} \square$ $\square\square$
 - $\square\square \overline{\square \square} \square$ \square
 - $\square \overline{\square \square} \square$ $\square\square$
 - \square

7. (a)
- $\square\square \overline{\square \square \square} \square$
 - $\square \overline{\square \square \square} \square$
 - $\square \overline{\square \square \square} \square$
 - $\square \overline{\square \square \square} \square$
 - $\square\square\square\square.\square.\square.\square$

- (b)
- $\square \overline{\square \square} \square$
 - $\square \overline{\square \square} \square$

- (c)
- $\square\square \overline{\square \square} \square$
 - $\square\square \overline{\square \square} \square$

- Divide $\square\square$ by \square . Divide $\square\square$ by \square . Divide $\square\square$ by \square .
- Divide \square by \square .

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$\square \cdot \square \square \square \square \square \square \cdot \square \square \square \square \square \square$

The factors of $\square \square$ are $\square, \square, \square, \square, \square, \square, 1\square, \square \square, \square \square, \square \square,$ and $\square \square$.

13. Factorizations of $\square \square$:

$\square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square$
 $\square \cdot \square \square \square \square \square$

The factors of $\square \square$ are $\square, \square, \square, \square, \square \square, \square \square,$ and $\square \square$.

14. Factorizations of $\square \square$:

$\square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square$
 $\square \cdot \square \square \square \square \square \square \square \cdot \square \square \square \square \square \square \square$

The factors of $\square \square$ are $\square, \square, \square, \square, \square, \square, \square \square, \square \square, \square \square,$ and $\square \square$.

Quotient is 1.

$\square \square \square \square \cdot \square \cdot \square \cdot \square \cdot \square \square \square \square \square \square \cdot \square$

The correct choice is B.

30.

$\square \square$
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$\square \square$
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 $\square \square$
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 $\square \square \square \square \cdot \square \cdot \square \cdot \square \cdot \square \square \square \square \square \square \cdot \square \square$

The correct choice is C.

$\square \square \square$ D
 \square
 $\square \square \square$ i
 \square

b $\sqrt{\quad}$

y $\sqrt{\quad}$

v

i

d

\square

e

.

\square

\square

b

y

\square

.

D

i

v

i

d

e

\square

\square

51.
$$\begin{array}{r} \square\square\square \\ \square\square\square \\ \hline \square \overline{) \square\square\square} \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square$ by \square .

$$\begin{array}{r} \square\square \\ \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

\square . Divide $\square\square$

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

by \square .

Divide \square by \square .

Quotient is 1.

$\square\square\square\square\square\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square$

52.
$$\begin{array}{r} \square\square \\ \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

$$\begin{array}{r} \square\square \\ \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

$\square\square\square\square\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square$

53. Answers will vary. A sample answer follows. A prime number is a whole number that has exactly two *different* factors, itself and \square . Examples

include $\square, \square, \square, \square,$ and \square . A composite number $\square\square\square$

57.
$$\begin{array}{r} \square\square\square \\ \square\square\square \\ \hline \square \overline{) \square\square} \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

Divide \square by \square .

Quotient is 1.

$\square\square\square\square\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square$

58.
$$\begin{array}{r} \square\square\square \\ \square\square\square \\ \hline \square \overline{) \square\square} \end{array}$$

$$\begin{array}{r} \square\square\square \\ \square \overline{) \square\square\square} \\ \square\square\square \\ \hline \square \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square\square} \\ \square\square\square \\ \hline \square \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square\square} \\ \square\square\square \\ \hline \square \end{array}$$

Divide $\square\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

Divide $\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square\square} \\ \square\square \\ \hline \square \end{array}$$

\square . Divide $\square\square$

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

by \square . Divide

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

$\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

Divide $\square\square$ by \square .

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

\square .

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

Divide \square by \square .

$$\begin{array}{r} \square \overline{) \square} \\ \square \\ \hline \square \end{array}$$

\square .

Quotient is 1.

has a factor(s) other than itself or 1. Examples include 4, 6, 8, 9, and 10. The numbers 2 and 3 are neither prime nor composite.

54. No even number other than 2 is prime because all

even numbers have 2 as a factor. Many odd numbers are multiples of prime numbers and are not prime. For example, 3, 5, 7, and 11 are all multiples of 2.

55. All the possible factors of 12 are 1, 2, 3, 4, 6, 12,

3, and 4. This list includes both prime numbers and composite numbers. The prime factors of 12 include only prime numbers. The prime factorization of 12 is

$$12 = 2 \cdot 2 \cdot 3$$

56. Yes, you can divide by 3s before you divide by 2.

No, the order of division does not matter. As long as you use only prime numbers, your answers will be correct. However, it does seem easier to always start with 2 and then use progressively greater prime numbers. The prime factorization of 12 is

$$12 = 2 \cdot 2 \cdot 3$$

$$12 = 2 \cdot 2 \cdot 3$$

59. 12

$$\overline{)12}$$

$$\underline{12}$$

$$0$$

$$\overline{)12}$$

$$\underline{12}$$

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$$\underline{12}$$

$$0$$

Divide 12 by 2.

Divide 12 by 3.

2. Divide 12 by 4.

by 2. Divide

12 by 3.

Divide 12 by

4. Divide 12

by 2. Divide

12 by 3.

Divide 12 by 4.

Quotient is 1.

$$12 = 2 \cdot 2 \cdot 3$$

67. No. Every other even number is divisible by 2 in addition to being divisible by itself and 1.

| | |
|--|--|
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | Divide $\square \square \square \square$ by |
| $\begin{array}{r} \square \square \square \\ \square \square \square \end{array}$ | \square . Divide $\square \square \square \square$ |
| $\begin{array}{r} \square \\ \square \square \square \square \\ \square \square \end{array}$ | by \square . Divide |
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | $\square \square \square$ by \square . |
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | Divide $\square \square \square$ by |
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | \square . Divide $\square \square \square$ |
| $\begin{array}{r} \square \square \\ \square \square \square \end{array}$ | by \square . Divide $\square \square$ |
| $\begin{array}{r} \square \square \square \\ \square \square \square \end{array}$ | by \square . |
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | Divide \square by \square . |
| $\begin{array}{r} \square \\ \square \square \end{array}$ | |

Quotient is 1.
 $\square \square \square \square \square \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square$
 $\square \square \square \cdot \square \square$

68. No. A multiple of a prime number can never be prime because it will always be divisible by the prime number.

| | |
|---|--|
| $\begin{array}{r} \square \square \square \square \\ \square \square \square \square \end{array}$ | 69. Divide $\square \square \square \square$ by |
| $\begin{array}{r} \square \square \square \\ \square \square \square \square \end{array}$ | \square . Divide $\square \square \square \square$ |
| $\begin{array}{r} \square \square \square \\ \square \square \square \square \end{array}$ | by \square . Divide |
| $\begin{array}{r} \square \square \square \square \\ \square \square \square \square \end{array}$ | $\square \square \square$ by \square . |
| $\begin{array}{r} \square \square \square \\ \square \square \square \square \end{array}$ | Divide $\square \square \square$ by |
| $\begin{array}{r} \square \square \square \\ \square \square \square \square \end{array}$ | \square . Divide $\square \square$ by |
| $\begin{array}{r} \square \square \square \square \\ \square \square \square \square \end{array}$ | \square . Divide \square by |
| $\begin{array}{r} \square \\ \square \square \square \square \end{array}$ | \square . |
| $\begin{array}{r} \square \\ \square \square \square \end{array}$ | |

Quotient is 1.
 $\square \square \square \square \square \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square$
70. $\square \square \square \square \square \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square \square \square \square \cdot \square \cdot \square \square \cdot \square$

2.4 Writing a Fraction in Lowest Terms

2.4 Margin Exercises

1. (a) $\frac{12}{18}, \frac{15}{24}$;
 $\frac{3}{3}$

$\frac{12}{18} \cdot \frac{3}{3} = \frac{36}{54}$ $\frac{15}{24} \cdot \frac{3}{3} = \frac{45}{72}$

Yes, 3 is a common factor of 12 and 18.

(b) $\frac{10}{15}, \frac{12}{18}$;
 $\frac{2}{2} \cdot \frac{10}{15} = \frac{20}{30}$ $\frac{2}{2} \cdot \frac{12}{18} = \frac{24}{36}$

Yes, 2 is a common factor of 10 and 12.

(c) $\frac{10}{15}, \frac{12}{18}$; $\frac{5}{5}$
 $\frac{10}{15} \cdot \frac{5}{5} = \frac{50}{75}$, but 5 is not a factor of 15.

No.

(d) $\frac{10}{15}, \frac{12}{18}$;
 $\frac{3}{3}$; $\frac{2}{2}$

$\frac{10}{15} \cdot \frac{3}{3} = \frac{30}{45}$ $\frac{12}{18} \cdot \frac{2}{2} = \frac{24}{36}$

Yes, 3 is a common factor of 10 and 12.

2. (a) $\frac{5}{7}$
 $\frac{5}{7}$

5 and 7 have no common factor other than 1.

Yes, it is in lowest terms.

(b) $\frac{12}{18}$
 $\frac{12}{18}$

12 and 18 have a common factor of 6. No, it is not in lowest terms.

(c) $\frac{10}{15}$
 $\frac{10}{15}$

10 and 15 have a common factor of 5.

No, it is not in lowest terms.

(b) $\frac{12}{18} \cdot \frac{2}{2} = \frac{24}{36}$ $\frac{15}{24} \cdot \frac{2}{2} = \frac{30}{48}$

(c) $\frac{10}{15} \cdot \frac{2}{2} = \frac{20}{30}$ $\frac{12}{18} \cdot \frac{2}{2} = \frac{24}{36}$

(d) $\frac{10}{15} \cdot \frac{3}{3} = \frac{30}{45}$ $\frac{12}{18} \cdot \frac{3}{3} = \frac{36}{54}$

5. (a) $\frac{12}{18}$ and $\frac{15}{24}$
 $\frac{12}{18}$ $\frac{15}{24}$

$\frac{12}{18} \cdot \frac{2}{2} = \frac{24}{36}$ $\frac{15}{24} \cdot \frac{2}{2} = \frac{30}{48}$

The fractions are equivalent $\frac{24}{36} = \frac{30}{48}$

$\frac{24}{36} = \frac{30}{48}$

(b) and $\frac{12}{18}$

$\frac{12}{18} \cdot \frac{2}{2} = \frac{24}{36}$ $\frac{15}{24} \cdot \frac{2}{2} = \frac{30}{48}$

$\frac{24}{36} = \frac{30}{48}$

$$\frac{\square \square}{\square \square} \cdot \frac{\square \square}{\square \square}$$

(d) $\frac{\square \square}{\square \square}$

$\square \square$ and $\square \square$ have no common factor other than \square . Yes, it is in lowest terms.

3. (a) $\frac{\square}{\square} \cdot \frac{\square \square \square}{\square \square \square}$

(b) $\frac{\square}{\square} \cdot \frac{\square \square \square}{\square \square \square}$

(c) $\frac{\square \square}{\square} \cdot \frac{\square \square \square \square \square}{\square \square \square \square \square}$

(d) $\frac{\square \square}{\square} \cdot \frac{\square \square \square \square \square \square}{\square \square \square \square \square \square}$

(e) $\frac{\square \square}{\square} \cdot \frac{\square \square \square \square \square}{\square \square \square \square \square}$

4. (a) $\frac{\square \square}{\square} \cdot \frac{\square \cdot \square \cdot \square}{\square \cdot \square \cdot \square}$

$$\frac{\square \cdot \square \cdot \square}{\square \cdot \square \cdot \square} \cdot \frac{\square \cdot \square \cdot \square}{\square \cdot \square \cdot \square} = \frac{\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square}{\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square}$$

$$\frac{\square \cdot \square \cdot \square}{\square \square} \cdot \frac{\square \square \square}{\square \square \square} = \frac{\square \cdot \square \cdot \square \cdot \square \square \square}{\square \square \square \square \square}$$

The fractions are *not equivalent* $\square \square \square \square \square$

(c) $\frac{\square \square}{\square}$ and $\frac{\square \square \square}{\square \square}$

$$\frac{\square \square}{\square} \cdot \frac{\square \square \square}{\square \square} = \frac{\square \square \square \square \square}{\square \square \square}$$

$$\frac{\square \square \square}{\square \square} \cdot \frac{\square \square \square \square \square}{\square \square \square \square \square} = \frac{\square \square \square \square \square \square \square}{\square \square \square \square \square \square}$$

$$\frac{\square \square \square}{\square \square} \cdot \frac{\square \square \square \square \square \square}{\square \square \square \square \square \square} = \frac{\square \square \square \square \square \square \square \square}{\square \square \square \square \square \square \square \square}$$

The fractions are *equivalent* ($\square \square \square$).

$$\frac{\square \square \square}{\square \square} = \frac{\square \square \square \square}{\square \square \square}$$

(d) and $\frac{\square \square \square}{\square \square \square}$

$$\frac{\square \square \square}{\square \square \square} \cdot \frac{\square \cdot \square \cdot \square}{\square \cdot \square \cdot \square} = \frac{\square \square \square \square \square \square}{\square \square \square \square \square \square}$$

$$\frac{\square\square\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square \cdot \square \cdot \square}{\square \cdot \square}$$

$$\frac{\square\square\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square \cdot \square \cdot \square \cdot \square \cdot \square}{\square \cdot \square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$$

The fractions are *not equivalent* $\frac{\square}{\square} \neq \frac{\square}{\square}$

2.4 Section Exercises

1. A number can be divided by \square if the number is an even number.
2. A number can be divided by \square if the number ends in \square or \square .
3. Any number can be divided by $\square\square$ if the number ends in \square .
4. If the sum of a number's digits is divisible by \square , the

number is divisible by \square .

5. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✓ ✓ ✓
6. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✓ ✓ ✓
7. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✓ ✗ ✗
8. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$
9. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✗ ✓
10. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✗ ✗ ✓
11. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✓ ✗ ✗
12. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ ✓ ✓ ✓ ✓
13. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$, true

24. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

25. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

26. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

27. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

28. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

29. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

30. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

31. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

32. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

33. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

34. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

35. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

14. $\frac{\square}{\square}$ is in lowest terms, so the fractions $\frac{\square}{\square}$ and $\frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$
are not equivalent. *false*

15. $\frac{\square}{\square}$ is in lowest terms, so the fractions $\frac{\square}{\square}$ and $\frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$
are not equivalent. *false*

16. $\frac{\square}{\square} = \frac{\square}{\square}$, *true*

$\frac{\square}{\square}$ $\frac{\square}{\square}$

17. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

18. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

19. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

20. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

21. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

22. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

23. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

36. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

37. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

38. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

39. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

40. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

41. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

42. $\frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square}$ $\frac{\square}{\square}$

53. $\frac{\square\square}{\square\square}$ and $\frac{\square\square}{\square\square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square} = \frac{\square\square \cdot \square}{\square\square \cdot \square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square} = \frac{\square\square \cdot \square}{\square\square \cdot \square}$

The fractions are *equivalent* $\frac{\square\square}{\square\square} = \frac{\square\square}{\square\square}$

54. $\frac{\square\square}{\square\square}$ and $\frac{\square\square}{\square\square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square} = \frac{\square\square \cdot \square}{\square\square \cdot \square}$

$\frac{\square\square}{\square\square} \cdot \frac{\square}{\square} = \frac{\square\square \cdot \square}{\square\square \cdot \square}$

The fractions are *equivalent* $\frac{\square\square}{\square\square} = \frac{\square\square}{\square\square}$

55. A fraction is in lowest terms when the numerator and the denominator have no common factors

other than 1. Some examples are $\frac{\square}{\square}$, $\frac{\square}{\square}$, and $\frac{\square}{\square}$

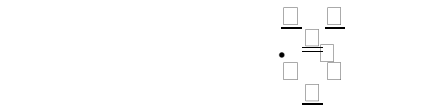
56. Two fractions are equivalent when they represent

the same portion of a whole. For example, the $\frac{\square\square}{\square\square}$ $\frac{\square\square}{\square\square}$

2.5 Multiplying Fractions

2.5 Margin Exercises

1. $\frac{\square}{\square}$ of $\frac{\square}{\square}$ as read from the figure is the darker shaded part of the second figure. One of eight equal parts is shaded, or $\frac{\square}{\square}$



2. (a) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(b) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(c) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(d) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

3. (a) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(b) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(c) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

fractions $\frac{\square}{\square}$ and $\frac{\square}{\square}$ are equivalent.

$$\frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

The fractions are *equivalent* $\frac{\square}{\square} = \frac{\square}{\square}$

57. $\frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

58. $\frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

59. $\frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

60. $\frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

(d) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

4. (a) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

(b) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$ or $\frac{\square}{\square}$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

(c) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(d) $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

5. (a) Area \square length \cdot width

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square} \text{yd}$$

13.

(b) Area \square length \cdot width

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square} \text{mi}$$

(c) Area \square length \cdot width

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square} \text{mi}$$

12. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

13. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

14. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

15. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

16. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

17. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

18. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square} = \frac{\square}{\square}$

2.5 Section Exercises

- To multiply two or more fractions, you multiply the numerators and you multiply the denominators.
- To write a fraction in lowest terms, you must divide both the numerator and denominator by a common factor.

- 3. A shortcut when multiplying fractions is to divide both a numerator and a denominator by the same number.
- 4. Using the shortcut when multiplying fractions

should result in an answer that is in lowest terms.

5. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

6. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

7. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

8. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

9. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

10. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

11. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

19. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

- 20. The statement "When multiplying a fraction by a whole number, the whole number should be rewritten as the number over 1." is *true*.

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

- 21. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$ is *false*.

The correct method is as follows:

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

22. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

23. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

24. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \cdot \square}{\square \cdot \square}$

25. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

26. $\frac{2}{3} \cdot \frac{4}{5} = \frac{8}{15}$

27. $\frac{1}{3} \cdot \frac{2}{5} = \frac{2}{15}$

28. $\frac{3}{4} \cdot \frac{1}{2} = \frac{3}{8}$

29. $\frac{2}{5} \cdot \frac{3}{4} = \frac{6}{20} = \frac{3}{10}$

30. $\frac{1}{4} \cdot \frac{3}{5} = \frac{3}{20}$

31. $\frac{2}{3} \cdot \frac{4}{5} = \frac{8}{15}$

36. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

37. Area = length • width
 $10 \text{ mi} \cdot 3 \text{ mi} = 30 \text{ mi}^2$

38. Area = length • width
 $10 \text{ ft} \cdot 3 \text{ ft} = 30 \text{ ft}^2$

39. Area = length • width
 $10 \text{ meters} \cdot 3 \text{ meters} = 30 \text{ meters}^2$

40. Area = length • width
 $10 \text{ in.} \cdot 3 \text{ in.} = 30 \text{ in.}^2$

41. Area = length • width
 $10 \text{ mi} \cdot 3 \text{ mi} = 30 \text{ mi}^2$

32. $\frac{\square\square}{\square\square\square} \cdot \frac{\square\square\square}{\square\square\square} = \frac{\square\square\square}{\square\square\square}$

33. $\frac{\square\square}{\square\square\square} \cdot \frac{\square\square\square}{\square\square\square} = \frac{\square\square\square}{\square\square\square}$

34. $\frac{\square\square}{\square} \cdot \frac{\square\square\square}{\square\square\square} = \frac{\square\square\square}{\square\square}$

35. $\frac{\square\square\square}{\square\square\square} \cdot \frac{\square\square\square}{\square\square\square} = \frac{\square\square\square}{\square\square\square}$

42. $\frac{\square\square}{\square\square} \cdot \frac{\square\square}{\square\square} = \frac{\square\square}{\square\square}$

43. Area \square length \cdot width
 $\frac{\square}{\square} \cdot \frac{\square\square}{\square} = \frac{\square\square}{\square}$ mi²

43. Multiply the numerators and multiply the denominators. An example is

$\frac{2}{3} \cdot \frac{4}{5} = \frac{2 \cdot 4}{3 \cdot 5} = \frac{8}{15}$

44. You must divide a numerator and a denominator by the same number. If you do all possible divisions, your answer will be in lowest terms. One example is

$\frac{2}{3} \cdot \frac{4}{5} = \frac{2 \cdot 4}{3 \cdot 5} = \frac{8}{15}$

45. Area \square length \cdot width
 $\frac{\square}{\square} \cdot \frac{\square\square}{\square} = \frac{\square\square}{\square}$

$\frac{2}{3} \cdot \frac{4}{5} = \frac{2 \cdot 4}{3 \cdot 5} = \frac{8}{15}$ yd²

46. Area \square width \cdot height
 $\frac{\square\square}{\square} \cdot \frac{\square\square}{\square} = \frac{\square\square\square}{\square}$

$\frac{2}{3} \cdot \frac{4}{5} = \frac{2 \cdot 4}{3 \cdot 5} = \frac{8}{15}$ yd

foreign language, speak Spanish.

Step 3 An estimate is $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$.

Step 4 The exact value is $\frac{1}{4}$, which is the same as the estimate since we didn't round.

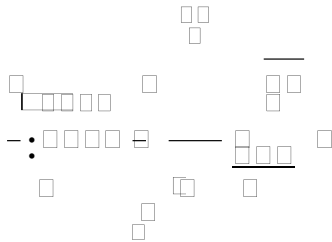
Step 5 The fraction of students who speak Spanish is $\frac{1}{4}$.

Step 6 The answer, $\frac{1}{4}$, matches our estimate.

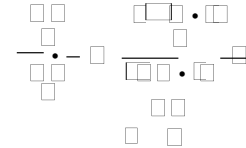
4. (a) From the circle graph, the fraction is $\frac{1}{4}$.

(b) Multiply $\frac{1}{4}$ by the number of people in the survey, 16. Since we can estimate the answer

using the exact values, our estimated answer will be the same as the exact answer.

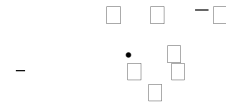


4 children buy food from vending machines.



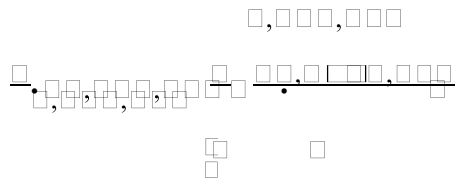
The area of the floor is 120 yd².

7. Multiply the length and the width.



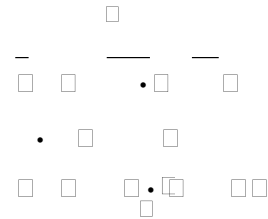
The area of the cookie sheet is 120 ft².

8. Multiply 1/4 by 1,000,000,000.



250,000,000 people who shop at flea markets on a daily basis purchase produce.

9. Multiply the length and the width.

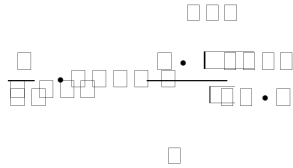


The area of the top of the table is 120 yd².



The daily parking fee in San Francisco is \$□□.

15. (a) □□ of the □□□□ runners are □□ women.

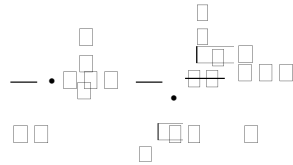


□□□ runners are women.

- (b) The number of runners that are men is

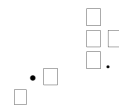


16. (a) Multiply the fraction of nonsmoking rooms by the number of rooms.



There are □□□ nonsmoking rooms.

- (b) The number of smoking rooms is

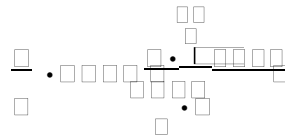


20. The only group that is *not* willing to wait □ hours

or more is the *2 hours or less* group, and the fraction corresponding to that group is □□. Thus, the fraction willing to wait □ hours or more is



The total number of people willing to wait □ hours or more is



21. Because everyone is included and fractions are given for *all* groups, the sum of the fractions must be 1, or *all* of the people.

22. Answers will vary. Some possibilities are

1. You made an addition error.
2. The fractions on the circle graph are incorrect.
3. The fraction errors were caused by rounding.

$$\begin{array}{r} \square\square \\ \square \\ \hline \square\square\square \\ \square \end{array}$$

The Owens family saved \$ $\square\square\square\square$ for the year.

28. Multiply the fraction $\frac{\square}{\square}$ by the total income.

$$\begin{array}{r} \square. \\ \square\square, \square\square\square\square \\ \hline \square\square\square\square \\ \square \\ \hline \square\square\square\square \\ \square \\ \hline \square\square\square\square \\ \square \end{array}$$

They spent \$ $\square\square\square\square$ on clothing.

29. The error was made when dividing $\square\square$ by \square and writing \square instead of \square . The correct solution is

$$\begin{array}{r} \square \quad \square\square \quad \square \quad \square\square\square \\ \square \\ \hline \square\square \quad \square \quad \square \quad \square \quad \square \\ \square\square \quad \square \quad \square\square\square \\ \square\square \quad \square \quad \square \\ \square \end{array}$$

30. Yes, the statements are true. Since whole numbers are \square or greater, when you multiply, the product will always be greater than either of the numbers multiplied. But, when you multiply two proper fractions, you are finding a fractional part of a fraction, and the product will be smaller than either of the two proper fractions.

her votes from senior citizens.

$$\begin{array}{r} \square \\ \square \cdot \square\square, \square\square\square\square - \square\square\square\square \\ \hline \square \end{array}$$

To find the votes needed from voters other than the senior citizens, subtract:

$$\square\square, \square\square\square\square \square\square, \square\square\square\square \square\square\square\square \text{ votes.}$$

She needs $\square\square\square\square$ votes from voters other than the senior citizens.

36. Multiply the fraction $\frac{\square}{\square}$ by the cost (\$ $\square\square, \square\square\square$).

$$\begin{array}{r} \square\square\square\square \\ \square \cdot \square\square, \square\square\square\square \\ \hline \square\square \end{array}$$

To find the amount borrowed in the first years, subtract:

$$\begin{array}{r} \$\square\square, \square\square\square\square \\ \$\square\square, \square\square\square \end{array}$$

\$ $\square\square, \square\square\square$ was borrowed in the first years.

37. Multiply the remaining $\frac{\square}{\square}$ of the estate by the fraction going to the American Cancer Society.

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$\frac{\square}{\square}$ of the estate goes to the American Cancer Society.

38. Multiply the remaining $\frac{\square}{\square}$ of their total investments by the fraction invested in bonds.

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

The couple invested $\frac{\square}{\square}$ of their total investment in bonds.

2.7 Dividing Fractions

2.7 Margin Exercises

1. (a) $\frac{\square}{\square} \div \frac{\square}{\square}$; The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

- (b) $\frac{\square}{\square} \div \frac{\square}{\square}$. The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

- (c) The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

3. (a) $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

- (b) $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

- (c) $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

- (d) $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

4. (a) **Step 1** The problem asks for the number of $\frac{\square}{\square}$

$\frac{\square}{\square}$ -ounce dispensers that can be filled using $\frac{\square}{\square}$ ounces of eye drops.

Step 2 Divide the total number of ounces of eye drops by the fraction of an ounce each dispenser holds.

Step 3 An estimate is $\frac{\square}{\square}$

Step 4 Solving gives us

$$\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

Step 5 $\frac{\square}{\square}$ -ounce dispensers can be filled.

Step 6 The answer is reasonably close to our estimate.

- (b) **Step 1** The problem asks for the number of

(d) The reciprocal of $\frac{a}{b}$ is $\frac{b}{a}$ because

$$\frac{a}{b} \cdot \frac{b}{a} = \frac{ab}{ba} = 1$$

2. (a) $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

(b) $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

(c) $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

(d) $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

2

$$\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$$

$\frac{1}{4}$ -quart bottles that can be filled from a $\frac{3}{4}$ -quart cask.

Step 2 Divide the total number of quarts in the cask by the size of the bottles.

Step 3 An estimate is

$$\frac{3}{4} \div \frac{1}{4} = 3$$

Step 4 Solving gives us

$$\frac{3}{4} \div \frac{1}{4} = \frac{3}{4} \cdot \frac{4}{1} = \frac{12}{4} = 3$$

Step 5 $\frac{12}{4}$ -quart bottles can be filled.

Step 6 The answer is reasonably close to our estimate.

5. (a) **Step 1** The problem asks for the fraction of the bonus money that each employee will receive.

$\frac{1}{2}$

Step 2 Divide the fraction of the bonus money,

$\frac{1}{2}$, by the number of employees, 20 .

Step 3 An estimate is $\frac{1}{2} \div 20 = \frac{1}{40}$

Step 4 Solving gives us

$$\frac{1}{2} \div \frac{3}{4} = \frac{1}{2} \cdot \frac{4}{3} = \frac{4}{6} = \frac{2}{3}$$

Step 5 Each employee will receive $\frac{2}{3}$ of the bonus money.

Step 6 The answer is reasonably close to our estimate.

(b) **Step 1** The problem asks for the fraction of the prize money that each employee will receive.

Step 2 Since they donate $\frac{1}{4}$ of the winnings, they have

$$1 - \frac{1}{4} = \frac{3}{4}$$

of the winnings left to divide. Divide the fraction of the winnings that remain, $\frac{3}{4}$, by the number of employees, 3.

Step 3 An estimate is $\frac{3}{4} \div 3 = \frac{1}{4}$

Step 4 Solving gives us

$$\frac{3}{4} \div 3 = \frac{3}{4} \cdot \frac{1}{3} = \frac{3}{12} = \frac{1}{4}$$

Step 5 Each employee will receive $\frac{1}{4}$ of the prize money.

Step 6 The answer is reasonably close to our estimate.

2.7 Section Exercises

9. The reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$ because

$$\frac{2}{3} \cdot \frac{3}{2} = 1$$

10. The reciprocal of $\frac{5}{6}$ is $\frac{6}{5}$ because

$$\frac{5}{6} \cdot \frac{6}{5} = 1$$

11. The reciprocal of $\frac{7}{8}$ is $\frac{8}{7}$ because

$$\frac{7}{8} \cdot \frac{8}{7} = 1$$

12. The reciprocal of $\frac{9}{10}$ is $\frac{10}{9}$ because

$$\frac{9}{10} \cdot \frac{10}{9} = 1$$

13. $\frac{1}{2} \div \frac{3}{4} = \frac{1}{2} \cdot \frac{4}{3} = \frac{4}{6} = \frac{2}{3}$

14. $\frac{2}{3} \div \frac{4}{5} = \frac{2}{3} \cdot \frac{5}{4} = \frac{10}{12} = \frac{5}{6}$

15. $\frac{3}{4} \div \frac{5}{6} = \frac{3}{4} \cdot \frac{6}{5} = \frac{18}{20} = \frac{9}{10}$

16. $\frac{4}{5} \div \frac{6}{7} = \frac{4}{5} \cdot \frac{7}{6} = \frac{28}{30} = \frac{14}{15}$

17. $\frac{5}{6} \div \frac{7}{8} = \frac{5}{6} \cdot \frac{8}{7} = \frac{40}{42} = \frac{20}{21}$

18. $\frac{6}{7} \div \frac{8}{9} = \frac{6}{7} \cdot \frac{9}{8} = \frac{54}{56} = \frac{27}{28}$

19. $\frac{7}{8} \div \frac{9}{10} = \frac{7}{8} \cdot \frac{10}{9} = \frac{70}{72} = \frac{35}{36}$

- When you invert or flip a fraction, you have the reciprocal of the fraction.
- To find the reciprocal of a whole number, you must first write the whole number over 1, and then invert it.
- To divide by a fraction, you must first invert the divisor and then change division to multiplication.
- After completing a fraction division problem, it is best to write the answer in lowest terms.

5. The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square}$$

6. The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square}$$

7. The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square}$$

8. The reciprocal of $\frac{\square\square}{\square}$ is $\frac{\square}{\square\square}$ because

$$\frac{\square\square}{\square} \cdot \frac{\square}{\square\square} = \frac{\square\square\square}{\square\square\square}$$

20. $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square}$

21. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

22. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

23. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

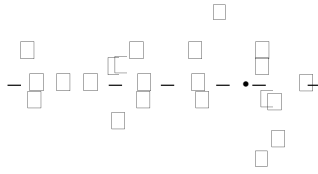
24. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

25. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

26. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

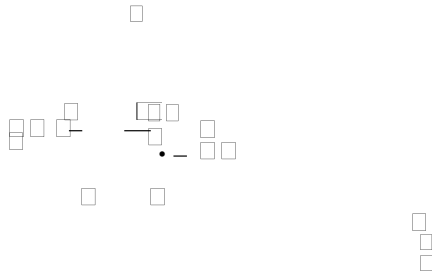
27. $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square}$

33. $\frac{\square}{\square}$ of a quart divided into \square parts:



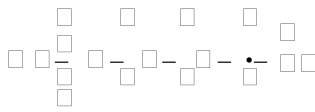
Each horse will get $\frac{\square}{\square}$ of a quart.

34. Divide the number of quarts of shampoo by the fraction of a quart each container holds.



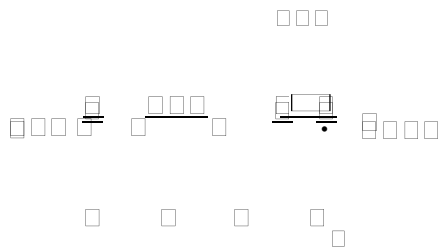
Harold can fill $\square\square$ containers.

35. Divide the total number of cups by the size of the measuring cup.



They need to fill the measuring cup $\square\square$ times.

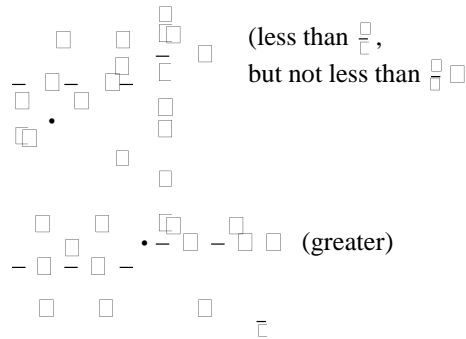
36. Divide the total number of pounds of jelly beans by the size of the bag.



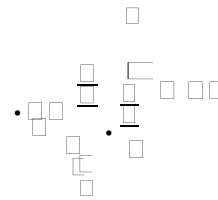
$\square\square\square$ $\frac{\square}{\square}$ -pound bags can be filled.

You can divide two fractions by multiplying the first fraction by the reciprocal of the second fraction (divisor).

42. Sometimes the answer is less and sometimes it is greater.

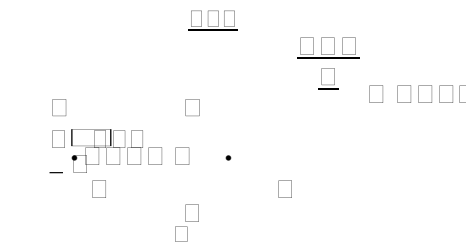


43. Each loafcake requires $\frac{\square}{\square}$ pound of jellybeans, so to make $\square\square$ loafcakes, use multiplication.



$\square\square$ pounds will be needed.

44. We want $\frac{\square}{\square}$ of $\square\square\square$ patients—use multiplication.



$\square\square\square$ patients were still taking their drugs.

45. Divide the $\square\square\square$ cans of compound by the fraction of a can needed for each new home.

$$\begin{array}{r} \square \\ \square\square\square \overline{) \square\square\square\square\square} \\ \underline{\square\square\square} \\ \square\square\square \\ \underline{\square\square\square} \\ \square\square\square \\ \underline{\square\square\square} \\ \square\square\square \end{array}$$

$\square\square\square$ homes can be plumbed.

46. Divide the $\square\square$ gallons of differential fluid by the fraction of a gallon needed for each car serviced.

$$\begin{array}{r} \square \\ \square\square \overline{) \square\square\square\square} \\ \underline{\square\square} \\ \square\square \\ \underline{\square\square} \\ \square\square \\ \underline{\square\square} \\ \square\square \end{array}$$

$\square\square$ cars can be serviced.

47. (a) In \square of the $\square\square\square$ visits, doctors failed to discuss the issues—use multiplication.

$$\begin{array}{r} \square \\ \square \overline{) \square\square\square} \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \end{array}$$

The doctors failed to discuss the issues in $\square\square\square$ visits.

- (b) The doctors *did* discuss the issues in $\square\square\square\square\square\square\square\square$ visits.

48. (a) $\frac{\square}{\square}$ of the $\square\square\square$ miles have been completed—use multiplication.

$$\begin{array}{r} \square \\ \square \overline{) \square\square\square} \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \end{array}$$

52. The indicator words for division are underlined below.

fewer sum of
goes into divide

per quotient
equals double

loss of divided by

53. To divide two fractions, multiply the first fraction by the reciprocal of the second fraction.

54. The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square} = \square\square$

The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square} = \square\square$

The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square} = \square\square$

The reciprocal of $\frac{\square}{\square}$ is $\frac{\square}{\square}$ because

$$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square\square} = \square\square$$

55. (a) To find the perimeter of any flat equal-sided 3-, 4-, 5-, or 6-sided figure, multiply the length of one side by 3, 4, 5, or 6, respectively.

- (b) The stamp has four sides, so multiply $\frac{\square}{\square}$ by \square .

$$\begin{array}{r} \square \\ \square \overline{) \square\square\square} \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \\ \underline{\square} \\ \square\square \end{array}$$

He has gone $\square\square\square$ miles.

(b) The number of miles that remain is $\square\square\square\square\square\square\square\square$ miles.

49. Divide the $\square\square\square$ yards of fabric by the fraction of a yard needed for each dish towel.

$\square\square\square\square$ towels can be made.

50. Multiply the number of applicants by the fraction of jobs available per applicant.

There are \square job openings.

Relating Concepts (Exercises 51–56)

51. The indicator words for multiplication are underlined below.

| | |
|---------------|----------------------|
| more than | per |
| <u>double</u> | <u>twice</u> |
| <u>times</u> | <u>product</u> |
| less than | difference |
| equals | <u>twice as much</u> |

The perimeter of the stamp is \square^{\square} inches.

56. Area \square length \cdot width

$$\square \frac{\square\square}{\square\square} \cdot \frac{\square\square}{\square\square} = \frac{\square\square\square\square}{\square\square\square\square}$$

The area is $\frac{\square\square\square}{\square\square}$ in. $^{\square}$. Multiply the length by the width to find the area of any rectangle.

2.8 Multiplying and Dividing Mixed Numbers

2.8 Margin Exercises

1. (a) $\square \frac{\square}{\square}$

\square is more than $\square\square$
 Half of \square is $\square\square$

$\square \frac{\square}{\square}$ rounds up to \square .

- (b) \square
 \square
 \square

$\square \frac{\square}{\square}$ is less than \square
 Half of \square is $\square\square$
 $\square \frac{\square}{\square}$ rounds down to \square .

(c) $\frac{\square}{\square}$

\square

$\frac{\square}{\square}$ is more than

\square Half of \square is \square

$\frac{\square}{\square}$ rounds up to \square .

(d) $\frac{\square}{\square}$

$\frac{\square}{\square}$ is more than

\square Half of \square is \square

$\frac{\square}{\square}$ rounds up to \square .

(e) $\frac{\square}{\square}$

$\frac{\square}{\square}$ is the same as

\square Half of \square is \square

$\frac{\square}{\square}$ rounds up to \square .

(f) \square

\square

\square is less than \square

\square Half of \square is \square

$\frac{\square}{\square}$ rounds down to \square .

(d) $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\frac{\square}{\square}$ rounds to \square $\frac{\square}{\square}$ rounds to \square .

$\frac{\square}{\square} \cdot \frac{\square}{\square}$

Exact:

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

3. (a) $\frac{\square}{\square}$

Estimate: $\frac{\square}{\square}$ rounds to \square . $\frac{\square}{\square}$ rounds to \square .

$\frac{\square}{\square} \cdot \frac{\square}{\square}$

Exact:

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(b) $\frac{\square}{\square}$

Estimate: $\frac{\square}{\square}$ rounds to \square $\frac{\square}{\square}$ rounds to \square .

$\frac{\square}{\square} \cdot \frac{\square}{\square}$

Exact:

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

(c)

$\frac{a}{b}$ would be $\frac{b}{a}$." is *false*. The reciprocal of $\frac{a}{b}$ is $\frac{b}{a}$.

3. The statement "To round mixed numbers before estimating the answer, decide whether the numerator of the fraction part is less than or more than half of the denominator." is *true*.

4. The statement "When rounding mixed numbers to estimate the answer to a problem, the estimated answer can vary quite a bit from the exact answer. However, it can still show whether the exact

answer is reasonable." is *true*.

5. $\frac{a}{b} \cdot \frac{c}{d}$

$$\frac{a}{b} \cdot \frac{c}{d}$$

Estimate: $\frac{a}{b} \cdot \frac{c}{d}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

6. $\frac{a}{b} \cdot \frac{c}{d}$

$$\frac{a}{b} \cdot \frac{c}{d}$$

Estimate: $\frac{a}{b} \cdot \frac{c}{d}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

12. $\frac{a}{b} \cdot \frac{c}{d}$

Estimate: $\frac{a}{b} \cdot \frac{c}{d}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

13. $\frac{a}{b} \cdot \frac{c}{d}$

Estimate: $\frac{a}{b} \cdot \frac{c}{d}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

14. $\frac{a}{b} \cdot \frac{c}{d}$

$$\frac{a}{b} \cdot \frac{c}{d}$$

Estimate: $\frac{a}{b} \cdot \frac{c}{d}$

Exact: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

15. $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

16. $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

17. $\frac{\square}{\square} \cdot \frac{\square}{\square}$ Estimate: $\square \cdot \square$

The best estimate is choice **D**.

18. $\frac{\square}{\square} \cdot \frac{\square}{\square}$ Estimate: $\square \cdot \square$

The best estimate is choice **A**.

19. $\frac{\square}{\square} \cdot \frac{\square}{\square}$ Estimate: $\square \cdot \square$

The best estimate is choice **B**.

20. $\frac{\square}{\square} \cdot \frac{\square}{\square}$ Estimate: $\square \cdot \square$

The best estimate is choice **C**.

21. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

$\square \cdot \square$

25. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square}$

26. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square}$

27. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square}$

28. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square$

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square}$

29. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

33. Multiply each amount by $\frac{\square}{\square}$
 \square

(a) Applesauce: $\frac{\square}{\square}$ cup

Estimate: $\square \cdot \square \square \square$ cups

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square \square}{\square} \square \square$
 $\frac{\square}{\square}$ cups

$\square \square \square \square \square$
 \square

(b) Salt: $\frac{\square}{\square}$ tsp.

Estimate: $\square \cdot \square \square \square$ tsp.

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \square \square$
 $\frac{\square}{\square}$ tsp.

$\square \square \square \square \square$
 \square

(c) Flour: $\frac{\square}{\square}$ cups

Estimate: $\square \cdot \square \square \square$ cups

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square \square}{\square} \square \square$
 $\frac{\square}{\square}$ cups

$\square \square \square \square \square \square$

34. Multiply each amount by $\frac{\square}{\square}$
 \square

(a) Flour: $\frac{\square}{\square}$ cups

Estimate: $\square \cdot \square \square \square$ cups

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square \square}{\square} \square \square$
 $\frac{\square}{\square}$ cups

$\square \square \square \square \square \square$

(b) Applesauce: $\frac{\square}{\square}$ cup

Estimate: $\square \cdot \square \square \square$ cups

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \square \square \frac{\square}{\square}$
 cups

36. Divide each amount by \square .

(a) Flour: $\frac{\square}{\square}$ cups

Estimate: $\square \square \square \square \frac{\square}{\square}$ cup

Exact: $\frac{\square}{\square} \square \square \square \frac{\square}{\square} \square \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square}$ cup
 $\square \frac{\square}{\square}$

(b) Salt: $\frac{\square}{\square}$ tsp.
 $\square \square \square \square \square \square$

Estimate: $\square \square \square \square \frac{\square}{\square}$ teaspoon

Exact: $\frac{\square}{\square} \square \square \square \frac{\square}{\square} \square \frac{\square}{\square} \square \frac{\square}{\square} \cdot \frac{\square}{\square} \square \frac{\square}{\square}$
 teaspoon

$\square \square \square \square \square \square$

(c) Applesauce: \square cup

Estimate: $\square \square \square \square \frac{\square}{\square}$ cup

Exact: $\frac{\square}{\square} \square \frac{\square}{\square} \frac{\square}{\square} \frac{\square}{\square} \frac{\square}{\square} \cdot \frac{\square}{\square} \frac{\square}{\square}$ cup
 $\square \square \square \square \square \square \square \square \square \square \square$

37. Divide the number of gallons available by the number of gallons needed for each unit.

Estimate: $\square \square \square \square \square \square \square \square \square$ units

Exact: $\frac{\square \square \square \square \square \square \square}{\square} \frac{\square \square \square \square}{\square} \frac{\square \square \square \square \square}{\square} \frac{\square \square \square \square \square \square \square}{\square}$
 $\frac{\square \square \square \square}{\square}$

$\square \square \square \square \square \square \square \square \square \square \square$

$\square \square$ units can be painted with $\square \square \square$ gallons of paint.

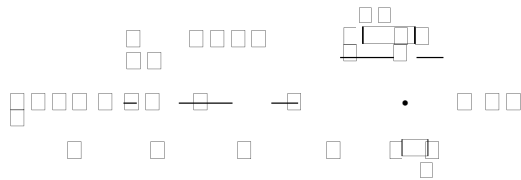
$\square \square \square \square \square$

$\square \square \square$ trips will be needed to deliver $\square \square \square$ cords of firewood.

46. Divide the total amount of roofing material by the amount of roofing material needed for each roof.

Estimate: $\square \square \square \square \square \square \square \square \square \square$ homes

Exact:



$\square \square$ homes can be re-roofed with $\square \square \square \square$ squares of roofing material.

47. (a) The maximum height of the standard jack is

\square

$\square \square \square$ inches. Use multiplication.

Estimate: $\square \square \cdot \square \square \square \square$ in.

$\square \square \square \square$ boxes of tile are needed.

Chapter 2 Review Exercises

1. $\frac{\square}{\square}$ There are \square parts, and \square is shaded.
2. $\frac{\square}{\square}$ There are \square parts, and \square are shaded.
3. $\frac{\square}{\square}$ There are \square parts, and \square are shaded.
4. Proper fractions have numerator (top) smaller than denominator (bottom).

They are: $\frac{\square}{\square} \frac{\square}{\square} \frac{\square}{\square} \frac{\square}{\square}$

Improper fractions have numerator (top) larger than or equal to the denominator (bottom).

They are: $\frac{\square}{\square} \frac{\square}{\square}$

$\square \square$

5. Proper fractions have numerator (top) smaller than denominator (bottom).

They are: $\frac{\square\square}{\square\square} \frac{\square}{\square}$

Improper fractions have numerator (top) larger than or equal to the denominator (bottom).

They are: $\frac{\square}{\square} \frac{\square\square}{\square\square} \frac{\square}{\square}$

6.
$$\frac{\square}{\square} \cdot \frac{\square\square\square\square}{\square\square\square\square}$$

$$\frac{\square}{\square} - \frac{\square\square}{\square}$$

7.
$$\frac{\square}{\square} \cdot \frac{\square\square\square\square}{\square\square\square\square}$$

$$\frac{\square}{\square} - \frac{\square\square\square}{\square}$$

8.
$$\frac{\square\square}{\square}$$

$\square\square$ Whole number part

$$\frac{\square\square\square}{\square}$$

$\square\square$ Remainder

9.
$$\frac{\square\square}{\square}$$

$\square\square\square$ Whole number part

$$\frac{\square\square\square}{\square}$$

$\square\square$ Remainder

$$\frac{\square\square}{\square}$$

14.
$$\frac{\square}{\square} \cdot \frac{\square\square}{\square}$$

15.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

16.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

17.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

18.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

19.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

20.
$$\frac{\square}{\square} \cdot \frac{\square\square\square}{\square\square\square}$$

21. All $\square\square$ parts out of a possible $\square\square$ parts are gold.

$$\frac{\square}{\square}$$

22. 18 of the possible $\square\square\square\square\square\square$ parts are gold.

10. Factorizations of $\frac{1}{2}$:

$$\frac{1}{2} = \frac{1}{2} \cdot \frac{1}{1} = \frac{1}{2} \cdot \frac{1}{1} = \frac{1}{2} \cdot \frac{1}{1}$$

The factors of $\frac{1}{2}$ are $\frac{1}{2}$, 1 , $\frac{1}{2}$, and 1 .

11. Factorizations of $\frac{1}{3}$:

$$\frac{1}{3} = \frac{1}{3} \cdot \frac{1}{1} = \frac{1}{3} \cdot \frac{1}{1} = \frac{1}{3} \cdot \frac{1}{1}$$

The factors of $\frac{1}{3}$ are $\frac{1}{3}$, 1 , $\frac{1}{3}$, 1 , $\frac{1}{3}$, 1 , $\frac{1}{3}$, and 1 .

12. Factorizations of $\frac{1}{4}$:

$$\frac{1}{4} = \frac{1}{4} \cdot \frac{1}{1} = \frac{1}{4} \cdot \frac{1}{1}$$

The factors of $\frac{1}{4}$ are $\frac{1}{4}$, 1 , $\frac{1}{4}$, and 1 .

13. Factorizations of $\frac{1}{5}$:

$$\frac{1}{5} = \frac{1}{5} \cdot \frac{1}{1} = \frac{1}{5} \cdot \frac{1}{1} = \frac{1}{5} \cdot \frac{1}{1}$$

$$\frac{1}{5} = \frac{1}{5} \cdot \frac{1}{1} = \frac{1}{5} \cdot \frac{1}{1}$$

The factors of $\frac{1}{5}$ are $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , $\frac{1}{5}$, 1 , and $\frac{1}{5}$.

$\frac{1}{5}$, and $\frac{1}{5}$.

$$\frac{1}{2} = \frac{1}{2} \cdot \frac{1}{1} = \frac{1}{2} \cdot \frac{1}{1}$$

23. $\frac{1}{2}$ of the possible $\frac{1}{3}$ parts are gold.

$$\frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6}$$

24. $\frac{1}{3}$ of the possible $\frac{1}{4}$ parts are gold.

$$\frac{1}{3} \cdot \frac{1}{4} = \frac{1}{12}$$

$$\frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6}$$

25.

$$\frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6}$$

26.

$$\frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6}$$

27. $\frac{\square}{\square}$ and $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

The fractions are equivalent \square

28. $\frac{\square}{\square}$ and $\frac{\square}{\square}$

$\frac{\square}{\square} \neq \frac{\square}{\square}$

The fractions are not equivalent \square

29. $\frac{\square}{\square}$ and $\frac{\square}{\square}$

$\frac{\square}{\square} = \frac{\square}{\square}$

The fractions are equivalent \square

30. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

31. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

32. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

39. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

40. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

41. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

42. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

43. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

44. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

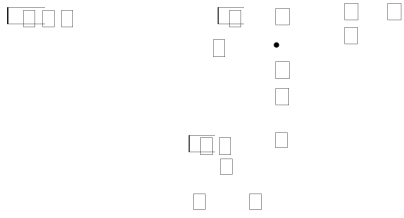
45. To find the area, multiply the length and the width.

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

The area is \square ft².

46. To find the area, multiply the length and the width.

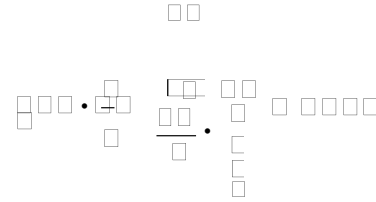
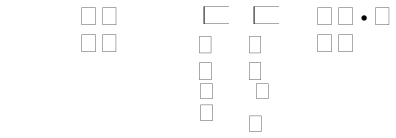
$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$



The area is 12 yd^2 .

47. Multiply the length and width.

33. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

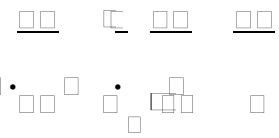


34. $\frac{2}{3} \cdot \frac{4}{5} = \frac{8}{15}$

The area is 24 ft^2 .

48. Multiply the length and width.

35. $\frac{1}{3} \cdot \frac{2}{5} = \frac{2}{15}$



The area is 6 ft^2 .

36. $\frac{3}{4} \cdot \frac{2}{3} = \frac{1}{2}$

49. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

Estimate: 0.375

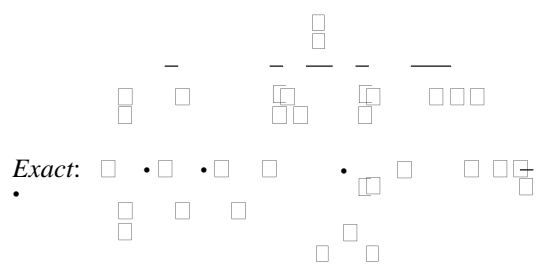
37. $\frac{2}{3} \cdot \frac{3}{4} = \frac{1}{2}$

Exact: $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

38. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

50. $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

Estimate: 0.375



Exact: $\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$

51.
$$\frac{\square\square}{\square} \div \frac{\square}{\square}$$

Estimate: $\square\square \square \square \square \square \square \square$

Exact: $\frac{\square\square}{\square} \div \frac{\square}{\square} = \frac{\square\square}{\square} \cdot \frac{\square}{\square} = \frac{\square\square}{\square}$

52.
$$\frac{\square}{\square} \div \frac{\square}{\square}$$

Estimate: $\square\square \square \square \square \square$

Exact: $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

53. Divide the total tons of almonds by the size of the bins.

Estimate: $\square\square \square \square \square \square \square \square \cdot \square \square$
 $\square\square$ bins

Exact: $\frac{\square\square \square \square \square \square}{\square} \div \frac{\square \square \square \square}{\square} = \frac{\square \square \square \square \square \square}{\square}$

$\square\square$ bins will be needed to store the almonds.

54. The $\frac{\square}{\square}$ other equal partners own

$$\frac{\square}{\square} \div \frac{\square}{\square}$$

of the business. Divide that amount by $\frac{\square}{\square}$.

$$\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

Each of the other partners owns $\frac{\square}{\square}$ of the business.

55. Divide the total yardage by the amount needed for each pull cord.

$$\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

pounds

Ebony gave $\square\square$ pounds to her parents. The amount she has left is $\square\square \square \square \square \square$ pounds.

58. Sheila paid $\frac{\square}{\square}$ of $\$ \square \square \square \square$ for taxes, social security, and a retirement plan.

$$\frac{\square}{\square} \cdot \square \square \square \square = \square \square \square \square$$

She paid $\$ \square \square \square \square$ for taxes, social security, and a retirement plan.

She paid $\frac{\square}{\square}$ of the remainder,

$\$ \square \square \square \square - \$ \square \square \square \square = \$ \square \square \square \square$, for basic living expenses.

$$\frac{\square}{\square} \cdot (\square \square \square \square - \square \square \square \square) = \square \square \square \square$$

She has $\$ \square \square \square \square - \$ \square \square \square \square = \$ \square \square \square$ left.

59. $\frac{\square}{\square}$ must be divided by $\frac{\square}{\square}$.

$$\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$$

Each school will receive $\frac{\square}{\square}$ of the amount raised.

60. $\frac{\square}{\square}$ of the catch must be divided evenly among \square fishermen.

$$\frac{\square}{\square} \div \square = \frac{\square}{\square}$$

Estimate: $\frac{\square\square\square}{\square\square\square} \cdot \frac{\square\square}{\square\square\square}$ pull
cords

Exact:

$$\frac{\square\square\square}{\square\square\square} \cdot \frac{\square\square}{\square\square\square} = \frac{\square\square\square \cdot \square\square}{\square\square\square \cdot \square\square\square}$$

$\square\square$ pull cords can be made.

56. Multiply the weight per gallon times the number of aquariums times the gallons per aquarium.

Estimate: $\square \cdot \square \cdot \square\square\square$
 $\square\square\square$

Exact: $\frac{\square\square}{\square} \cdot \square \cdot \frac{\square\square\square}{\square}$
 \square

The weight of the water is $\frac{\square\square\square\square}{\square}$, or $\square\square\square\square$ pounds.

57. Ebony sold $\frac{\square}{\square}$ of $\square\square\square$ pounds of rice.

$$\square\square\square - \frac{\square}{\square} \cdot \square\square\square = \square\square\square - \frac{\square \cdot \square\square\square}{\square}$$

pounds

$$\square\square\square - \frac{\square \cdot \square\square\square}{\square}$$

Thus, $\square\square\square - \frac{\square \cdot \square\square\square}{\square}$ pounds remain. She gave

of $\square\square$ pounds to her parents.

$$\frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square}$$

Each fisherman receives $\frac{\square}{\square}$ ton.

61. [2.5] $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square \cdot \square}{\square \cdot \square}$

62. [2.5] $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square \cdot \square}{\square \cdot \square}$

63. [2.8] $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

64. [2.8] $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

65. [2.7] $\frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square} \cdot \frac{\square}{\square}$

66. [2.7] $\frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square} - \frac{\square}{\square}$

67. [2.5] $\frac{\square\square}{\square\square} \cdot \frac{\square\square}{\square\square} = \frac{\square\square}{\square\square}$

68. [2.8] $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

69. [2.2] $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

70. [2.2] $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

□ □ Whole number part

□ □ Remainder

71. [2.2] $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

□ □ Whole number part

□ □ Remainder

72. [2.2] $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square}$

79. [2.8] Multiply $\frac{\square}{\square}$ ounces per gallon by the number of gallons.

Estimate: $\square \cdot \square \square \square \square$ ounces

Exact: $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

□ □ □ ounces of the product are needed.

80. [2.8] Multiply the number of tanks by the number of quarts needed for each tank.

Estimate: $\square \cdot \square \square \square \square$ qt

Exact: $\square \cdot \frac{\square}{\square} = \frac{\square}{\square}$

□ □ □ quarts are needed.

81. [2.8] To find the area, multiply the length and the width.

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

The area of the stamp is $\frac{\square}{\square}$ in.².

82. [2.8] To find the area, multiply the length and the width.

$\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square}{\square}$

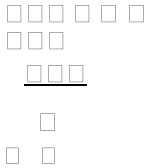
The area of the patio table top is $\frac{\square}{\square}$ yd.².

Chapter 2 Test

□ □



72. [2.2] $\frac{\square}{\square} \cdot \frac{\square}{\square}$



73. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

74. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

75. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

76. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

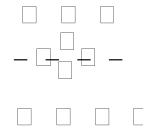
77. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

78. [2.4] $\frac{\square}{\square} \cdot \frac{\square}{\square}$

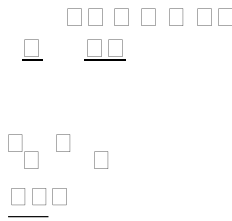
1. $\frac{\square}{\square}$ There are \square parts,
 \square and \square are shaded.

2. $\frac{\square}{\square}$ There are \square parts,
 \square and \square are shaded.

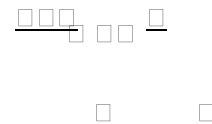
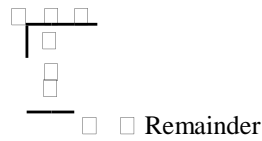
3. Proper fractions have the numerator (top) smaller than the denominator (bottom).



4. $\frac{\square}{\square} \cdot \frac{\square}{\square}$



5. \square Whole number part



6. Factorizations of 100 :

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

The factors of 100 are $1, 2, 4, 5, 10, 20, 25, 50,$ and 100

7.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

8.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

9.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

10.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

11.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

15.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

16. Multiply the length and the width.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

The area of the grill is 100 yd^2 .

17. First, find the number of seedlings that don't survive.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

Next, subtract to find the number that do survive.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

100 seedlings do survive.

18.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

19.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

20. Divide the total length by the length of the pieces.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

100 pieces can be cut.

$$100 = 2 \cdot 2 \cdot 5 \cdot 5 = 4 \cdot 25 = 10 \cdot 10$$

12. Write the prime factorization of both numerator and denominator. Divide the numerator and

denominator by any common factors. Multiply the remaining factors in the numerator and denominator.

$$\frac{\square \square \square \cdot \square \square \square \cdot \square \square \square}{\square \square \square \cdot \square \square \square \cdot \square \square \square} = \frac{\square \square \square \cdot \square \square \square \cdot \square \square \square}{\square \square \square \cdot \square \square \square \cdot \square \square \square}$$

13. Multiply fractions by multiplying the numerators and multiplying the denominators. Divide two fractions by using the reciprocal of the divisor (the

second fraction) and then changing division to multiplication.

14. $\frac{\square}{\square} \cdot \frac{\square}{\square} = \frac{\square \square}{\square \square}$

21. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square \square \square \square$

Exact: $\frac{\square \square}{\square} \cdot \frac{\square \square}{\square} = \frac{\square \square \square \square}{\square \square}$

22. $\frac{\square}{\square} \cdot \frac{\square}{\square}$

Estimate: $\square \cdot \square \square \square \square$

Exact: $\frac{\square \square}{\square} \cdot \frac{\square \square}{\square} = \frac{\square \square \square \square}{\square \square}$

23. $\frac{\square}{\square}$

Estimate: $\square \square \square \square \square \square$

Exact:

$$\frac{\square}{\square} \cdot \frac{\square \square}{\square} = \frac{\square \square \square \square}{\square \square}$$

24.
$$\begin{array}{r} \square \\ \square \\ \hline \square \\ \square \\ \hline \square \end{array}$$

Estimate:
$$\begin{array}{r} \square \\ \square \\ \hline \square \\ \square \\ \hline \square \end{array}$$

Exact:
$$\begin{array}{r} \square \\ \square \\ \hline \square \\ \square \\ \hline \square \end{array}$$

25. If \square grams can be synthesized per day, multiply to find the amount synthesized in \square days.

Estimate: $\square \cdot \square \square \square \square$ grams

Exact:
$$\begin{array}{r} \square \\ \square \\ \hline \square \\ \square \\ \hline \square \end{array}$$