# Solution Manual for Engineering Mechanics Statics in SI Units 14th Edition by Hibbeler ISBN 1292089237 <br> 9781292089232 

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## 2-1.

Determine the magnitude of the resultant force $\mathbf{F}_{R}=\mathbf{F}_{1}+\mathbf{F}_{2}$ and its direction, measured clockwise from the positive $u$ axis.

## Solution

Parallelogram Law. The parallelogram law of addition is shown in Fig. $a$, Trigonometry. Applying Law of cosines by referring to Fig. $b$,

$$
F_{R}=24^{2}+6^{2}-2(4)(6) \cos 105=8.026 \mathrm{kN}=8.03 \mathrm{kN}
$$

Ans.
Using this result to apply Law of sines, Fig. $b$,

$$
\begin{gathered}
\sin u \\
6
\end{gathered}=\begin{gathered}
\sin 105 \\
8.026
\end{gathered} ; \quad u=46.22
$$


(a)

Thus, the direction $\mathbf{f}$ of $\mathbf{F}_{R}$ measured clockwise from the positive $u$ axis is

$$
\mathbf{f}=46.22-45=1.22
$$

Ans.

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Ans:<br>$\mathbf{f}=1.22$

## 2-2.

Resolve the force $\mathbf{F}_{1}$ into components acting along the $u$ and vaxes and determine the magnitudes of the components.


## Solution

Parallelogram Law. The parallelogram law of addition is shown in Fig. $a$, Trigonometry. Applying the sines law by referring to Fig. b.

$$
\begin{aligned}
\begin{array}{l}
\left(F_{1}\right)_{\mathrm{v}} \\
\sin 45
\end{array} & =\begin{array}{c}
4 \\
\frac{\sin 105}{\left(F_{1}\right)_{u}}
\end{array} \\
\frac{\sin 30}{\sin } & =\underline{\sin 105} ;
\end{aligned} \quad\left(F_{1}\right)_{\mathrm{v}}=2.928 \mathrm{kN}=2.93 \mathrm{kN}
$$


(a)

(b)

Ans:
$\left(F_{1}\right)_{\mathrm{v}}=2.93 \mathrm{kN}$
$\left(F_{1}\right)_{u}=2.07 \mathrm{kN}$

## 2-3.

Resolve the force $\mathbf{F}_{2}$ into components acting along the $u$ and $v$ axes and determine the magnitudes of the components.


## Solution

Parallelogram Law. The parallelogram law of addition is shown in Fig. $a$, Trigonometry. Applying the sines law of referring to Fig. b,

$$
\begin{array}{ll}
\frac{\left(F_{2}\right)_{u}}{\sin 75} & =\frac{6}{\left(F_{2}\right)_{\mathrm{v}}}=\frac{\sin 75}{6} ; \\
\sin 30
\end{array}=\quad\left(F_{2}\right)_{u}=6.00 \mathrm{kN}, \quad \text { Ans. }
$$



Ans:
$\left(F_{2}\right)_{u}=6.00 \mathrm{kN}$
$\left(F_{2}\right)_{\mathrm{v}}=3.11 \mathrm{kN}$
*2-4.
If $\theta={ }^{60^{\circ}}$ and $F=450 \mathrm{~N}$, determine the magnitude of the
resultant force and its direction, measured counterclockwise
from the positive $x$ axis.

## SOLUTION

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.


Applying the law of consines to Fig. $b$,

$$
\begin{aligned}
& 700^{2} \quad 450^{2}-2(700)(450) \cos 45^{\circ} \\
& F_{R}=\sqrt{497.01 \mathrm{~N}}+497 \mathrm{~N} \\
&=\quad=
\end{aligned}
$$

Ans.

This yields

$$
\begin{aligned}
& \sin \quad \sin 45^{\circ} \\
& \underline{700 x}=\underline{497.01} \quad \alpha=
\end{aligned}
$$

Thus, the direction of angle $\phi$ of $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis, is

$$
\phi=\alpha+\underset{60^{\circ}}{ }={ }_{95.19^{\circ}}+{ }_{60^{\circ}}=
$$

Ans.

(b)

Ans:
$F_{R}=497 \mathrm{~N}$
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$\mathbf{f}=155$

## 2-5.

If the magnitude of the resultant force is to be 500 N , directed along the positive $y$ axis, determine the magnitude of force $\mathbf{F}$ and its direction u.

## SOLUTION

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.

Applying the law of cosines to Fig. $b$,

$$
\begin{aligned}
\mathrm{F} & =2 \underline{500^{2}+700^{2}-2(500)(700) \cos 105^{\circ}} \\
& =959.78 \mathrm{~N}=960 \mathrm{~N}
\end{aligned}
$$

Ans.
Applying the law of sines to Fig. $b$, and using this result, yields




Ans.

(b)
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$F=960 \mathrm{~N}$
$\mathrm{u}=45.2$

2-6. If $\mathrm{F}_{\mathrm{B}}=2 \mathrm{kN}$ and the resultant force acts along the positive $u$ axis, determine the magnitude of the resultant force and the angle $u$.


## Solution

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.

Applying the law of sines to Fig. $b$, yields

$$
\frac{\sin \mathbf{f}}{3}=\frac{\sin 30}{3} \quad \mathbf{f}=48.59
$$

Thus,

$$
\mathrm{u}=30+\mathbf{f}=30+48.59=78.59=78.6
$$

Ans.

With the result $\mathrm{u}=78.59$, applying the law of sines to Fig. $b$ again, yields

$$
\frac{F_{R}}{\sin (180-78.59)}=\frac{2}{\sin 30} \quad F_{R}=3.92 \mathrm{kN}
$$

Ans.

(a)

(b)

2-7. If the resultant force is required to act along the
positive $u$ axis and have a magnitude of 5 kN , determine the required magnitude of $\mathbf{F}_{B}$ and its direction $u$.


## Solution

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.

Applying the law of cosines to Fig. $b$,

$$
\begin{aligned}
F_{B} & =23^{2}+5^{2}-2(3)(5) \cos 30 \\
& =2.832 \mathrm{kN}=2.83 \mathrm{kN}
\end{aligned}
$$

Ans.

Using this result and realizing that $\sin (180-u)=\sin u$, the application of the sine law to Fig. $b$, yields

$$
\begin{aligned}
& \sin u \\
& \underline{5}
\end{aligned}=\underline{\begin{array}{l}
\sin 30 \\
2.832 \\
\hline
\end{array}}
$$

$$
\mathrm{u}=62.0
$$

Ans.

(a)

(b)

Ans:
2.83 kN
$\mathrm{u}=62.0$
*2-8. Determine the magnitude of the resultant force $\mathbf{F}_{R}=\mathbf{F}_{1}+\mathbf{F}_{2}$ and its direction, measured clockwise from the positive $x$ axis.


## Solution

$F_{R}=2(600)^{2}+(800)^{2}-2(600)(800) \cos 75=866.91=867 \mathrm{~N}$
$\underline{866.91}=\underline{800}$
$u=63.05$
$\mathbf{f}=63.05+45=108$

Ans.


Ans.

## 2-9.

Resolve $\mathbf{F}_{1}$ into components along the $u$ and v axes and determine the magnitudes of these components.

## SOLUTION

Sine law:

$$
\begin{array}{ll}
\frac{\mathrm{F}_{\mathrm{lv}}}{\sin 30^{\circ}}=\frac{250}{\sin 105^{\circ}} & \mathrm{F}_{1 \mathrm{v}}=129 \mathrm{~N} \\
\frac{\mathrm{~F}_{\mathrm{lu}}}{\sin 45^{\circ}}=\frac{250}{\sin 105^{\circ}} & \mathrm{F}_{\mathrm{lu}}=183 \mathrm{~N}
\end{array}
$$



Ans:
$F_{1 v}=129 \mathrm{~N}$
$F_{1 u}=183 \mathrm{~N}$

2-10.
Resolve $\mathbf{F}_{2}$ into components along the $u$ and v axes and determine the magnitudes of these components.

## SOLUTION

Sine law:

$$
\begin{array}{ll}
\frac{\mathrm{F}_{2 \mathrm{v}}}{\sin 30^{\circ}}=\frac{150}{\sin 75^{\circ}} & \mathrm{F}_{2 \mathrm{v}}=77.6 \mathrm{~N} \\
\frac{\mathrm{~F}_{2 \mathrm{u}}}{\sin 75^{\circ}}=\frac{150}{\sin 75^{\circ}} & \mathrm{F}_{2 \mathrm{u}}=150 \mathrm{~N}
\end{array}
$$



Ans:
$F_{2 v}=77.6 \mathrm{~N}$
$F_{2 u}=150 \mathrm{~N}$

2-11. The device is used for surgical replacement of the knee joint. If the force acting along the leg is 360 N , determine its components along the $x$ and $y_{i}$ axes.

## Solution

$$
\begin{gathered}
\frac{-F_{x}}{\sin 20}=\frac{360}{\sin 100} ; \quad F_{x}=-125 \mathrm{~N} \\
F_{y}=360 \\
\sin 60=\sin 100 ; \quad F_{y}=317 \mathrm{~N}
\end{gathered}
$$



Ans.

(a)

(b)

Ans:
$F_{x}=-125 \mathrm{~N}$
$F_{y}=317 \mathrm{~N}$
*2-12. The device is used for surgical replacement of the knee joint. If the force acting along the leg is 360 N , determine its components along the $x_{i}$ and $y$ axes.

## Solution

$$
\begin{gathered}
\frac{-F_{x}}{\sin 30}=\frac{360}{\sin 80} ; \quad F_{x}=-183 \mathrm{~N} \\
F_{y}=360 \\
\sin 70
\end{gathered}=\quad F_{y}=344 \mathrm{~N}
$$



Ans.
(b)

(a)

(b)

Ans:
$F_{x}=-183 \mathrm{~N}$
$F_{y}=344 \mathrm{~N}$

## 2-13.

If the tension in the cable is 400 N , determine the magnitude and direction of the resultant force acting on the pulley. This angle defines the same angle of line $A B$ on the tailboard block.


## Solution



60
Ans.

2-14. The truck is to be towed using two ropes. Determine the magnitude of forces $\mathbf{F}_{A}$ and $\mathbf{F}_{B}$ acting on each rope in order to develop a resultant force of 950 N directed along the positive $x$ axis. Set $\mathrm{u}=50^{\circ}$.

## Solution

Parallelogram Law: The parallelogram law of addition is shown in Fig. (a).

Trigonometry: Using law of sines [Fig. (b)], we have

$$
\begin{gathered}
\underline{F_{A}}=\frac{950}{\sin 110} \\
\sin 50 \\
F_{A}=774 \mathrm{~N} \\
\underline{F_{B}}=\underline{950} \\
\sin 20 \\
\sin 110 \\
F_{B}=346 \mathrm{~N}
\end{gathered}
$$




Ans.

Ans:
$F_{A}=774 \mathrm{~N}$
$F_{B}=346 \mathrm{~N}$

2-15.
The plate is subjected to the two forces at $A$ and $B$ as shown. If $u=60^{\circ}$, determine the magnitude of the resultant of these two forces and its direction measured clockwise from the horizontal.

## SOLUTION

Parallelogram Law: The parallelogram law of addition is shown in Fig. $a$.
Trigonometry: Using law of cosines (Fig. b), we have

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =2 \underline{8^{2}+6^{2}-2(8)(6) \cos 100^{\circ}} \\
& =10.80 \mathrm{kN}=10.8 \mathrm{kN}
\end{aligned}
$$

The angle $u$ can be determined using law of sines (Fig. b).

$$
\begin{aligned}
\frac{\sin u}{6} & =\frac{\sin 100^{\circ}}{10.80} \\
\sin u & =0.5470 \\
u & =33.16^{\circ}
\end{aligned}
$$

Thus, the direction $\mathbf{f}$ of $\mathbf{F}_{R}$ measured from the $x$ axis is

$$
\mathbf{f}=33.16^{\circ}-30^{\circ}=3.16^{\circ}
$$

Ans.


Ans.

(a)

(b)

> Ans: $\begin{gathered}F_{R}=10.8 \mathrm{kN} \\ \mathbf{f}=3.16\end{gathered}$
*2-16.
Determine the angle of u for connecting member $A$ to the plate so that the resultant force of $\mathbf{F}_{A}$ and $\mathbf{F}_{B}$ is directed horizontally to the right. Also, what is the magnitude of the resultant force?

## SOLUTION

Parallelogram Law: The parallelogram law of addition is shown in Fig. a.
Trigonometry: Using law of sines (Fig .b), we have

$$
\frac{\sin \left(90^{\circ}-\mathrm{u}\right)}{6}=\frac{\sin 50^{\circ}}{8}
$$

$$
\begin{aligned}
\sin \left(90^{\circ}-\mathrm{u}\right) & =0.5745 \\
\mathrm{u}=54.93^{\circ} & =54.9^{\circ}
\end{aligned}
$$

Ans.

From the triangle, $\mathbf{f}=180^{\circ}-\left(90^{\circ}-54.93^{\circ}\right)-50^{\circ}=94.93^{\circ}$. Thus, using law of

 cosines, the magnitude of $\mathbf{F}_{R}$ is

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =28^{2}+6^{2}-2(8)(6) \cos 94.93^{\circ} \\
& =10.4 \mathrm{kN}
\end{aligned}
$$

## Ans.


(b)

Ans:

## 2-17.

Two forces act on the screw eye. If $\mathrm{F}_{1}=400 \mathrm{~N}$ and


## SOLUTION

The parallelogram law of addition and triangular rule are shown in Figs. $a$ and $b$, respectively. Applying law of cosines to Fig. $b$,

$$
\begin{gathered}
800=2400^{2}+600^{2}-2(400)(600) \cos \left(180^{\circ}-u^{\circ}\right) \\
800^{2}=400^{2}+600^{2}-480000 \cos \left(180^{\circ}-\mathrm{u}\right) \\
\cos \left(180^{\circ}-\mathrm{u}\right)=-0.25 \\
180^{\circ}-\mathrm{u}=104.48 \\
\mathrm{u}=75.52^{\circ}=75.5^{\circ}
\end{gathered}
$$

between them, so that the resultant force has a magnitude of $\mathrm{F}_{\mathrm{R}}=800 \mathrm{~N}$.

(a)

Ans.

(b)

## Ans:

$\mathrm{u}=75.5$

## 2-18.

Two forces $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ act on the screw eye. If their lines of action are at an angle $u$ apart and the magnitude of each force is $\mathrm{F}_{1}=\mathrm{F}_{2}=\mathrm{F}$, determine the magnitude of the resultant force $\mathbf{F}_{R}$ and the angle between $\mathbf{F}_{R}$ and $\mathbf{F}_{1}$

## SOLUTION

$$
\begin{aligned}
& \underset{F}{\sin \mathbf{f}}=\frac{F}{\sin (u-\mathbf{f})} \\
& \sin (u-\mathbf{f})=\sin \mathbf{f} \\
& u-\mathbf{f}=\mathbf{f} \\
& \mathbf{f}=\frac{u}{2} \\
& F_{R}=2 \overline{(F)^{2}+(F)^{2}-2(F)(F) \cos \left(180^{\circ}-u\right)}
\end{aligned}
$$

Since $\cos \left(180^{\circ}-u\right)=-\cos u$

$$
\mathrm{F}_{\mathrm{R}}=\mathrm{FA} 22 \mathrm{~B} 21+\cos u
$$

Since $\cos \mathrm{a}_{2}^{\mathrm{u}} \mathrm{b}=\mathrm{A}^{\frac{1+\cos \mathrm{u}}{2}}$

Then

$$
\mathrm{F}_{\mathrm{R}}=2 \mathrm{~F} \cos \mathrm{a} \frac{\mathrm{u}}{2} \mathrm{~b}
$$



(a)

(b)

> Ans:
> $\mathbf{f}=\frac{\mathrm{u}}{2}$
> $F_{R}=2 F \cos \mathrm{a} \frac{\mathrm{u}}{2} \mathrm{~b}$

2-19.
Determine the magnitude and direction of the resultant force, $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis. Solve the problem by first finding the resultant $\mathbf{F}=\mathbf{F}_{1}$
$+\mathbf{F}_{2}$ and then forming $\mathbf{F}_{R}=\mathbf{F}+\mathbf{F}_{3}$.

## Solution

Parallelogram Law. The parallelogram law of addition for $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ and then their resultant $\mathbf{F}$ and $\mathbf{F}_{3}$ are shown in Figs. $a$ and $b$, respectively.
Trigonometry. Referring to Fig. $c$,

$$
F=2200^{2}+400^{2}=447.21 \mathrm{~N} \quad \mathrm{u}=\tan ^{-1} \mathrm{a}_{400}^{200} \mathrm{~b}=26.57
$$

Thus $\mathbf{f}=90-30-26.57=33.43$
Using these results to apply the law of cosines by referring to Fig. $d$,

$$
F_{R}=2 \overline{300^{2}+447.21^{2}-2(300)(447.21) \cos 33.43}=257.05 \mathrm{~N}=257 \mathrm{kN} \text { Ans. }
$$

Then, apply the law of sines,

$$
\frac{\sin u}{300}=\frac{\sin 33.43}{257.05} ; \quad u=40.02
$$

Thus, the direction $\mathbf{f}$ of $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis is

$$
\mathbf{f}=90+33.43+40.02=163.45=163
$$

Ans.

(b)

(C)

(d)

## Ans:

$F_{R}=257 \mathrm{~N}$
$\mathbf{f}=163$
*2-20. Determine the magnitude and direction of the resultant force, $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis. Solve the problem by first finding the resultant $\mathbf{F} \square=\mathbf{F}_{2}+\mathbf{F}_{3}$ and then forming $\mathbf{F}_{R}=\mathbf{F} \square+\mathbf{F}_{1}$.

## Solution



Parallelogram Law. The parallelogram law of addition for $\mathbf{F}_{2}$ and $\mathbf{F}_{3}$ and then their resultant $\mathbf{F}$ and $\mathbf{F}_{1}$ are shown in Figs. $a$ and $b$, respectively.
Trigonometry. Applying the law of cosines by referring to Fig. $c$,

$$
F=2200^{2}+300^{2}-2(200)(300) \cos 30=161.48 \mathrm{~N}
$$

Using this result to apply the sines law, Fig. $c$,

$$
\frac{\sin }{200}^{\operatorname{sen}}=\begin{gathered}
\sin 30 \\
161.48 ;
\end{gathered} \quad u=38.26
$$

Using the results of $\mathbf{F}$ and u to apply the law of cosines by referring to Fig. $d$,

$$
F_{R}=2161.48^{2}+400^{2}-2(161.48)(400) \cos 21.74=257.05 \mathrm{~N}=257 \mathrm{~N} \quad \text { Ans. }
$$

Then, apply the sines law,

$$
\frac{\sin u}{161.48}=\frac{\sin 21.74}{257.05} ; \quad u=13.45
$$

Thus, the direction $\mathbf{f}$ of $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis is

$$
\mathbf{f}=90+60+13.45=163.45=163
$$

Ans.

Ans.

(a)

(d)

$$
\begin{aligned}
& \text { Ans: } \\
& \quad \mathbf{f}=163 \\
& F_{R}=257 \mathrm{~N}
\end{aligned}
$$

2-21. The $\log$ is being towed by two tractors $A$ and $B$. Determine the magnitude of the two towing forces $\mathbf{F}_{A}$ and $\mathbf{F}_{B}$ if it is required that the resultant force have a magnitude $F_{R}=10 \mathrm{kN}$ and be directed along the $x$ axis. Set $\mathrm{u}=15^{\circ}$.


## Solution

Parallelogram Law: The parallelogram law of addition is shown in Fig. (a).

Trigonometry: Using law of sines [Fig. (b)], we have
$\frac{F_{A}}{\sin 15}=\frac{10}{\sin 135}$
$F_{A}=3.66 \mathrm{kN}$
$\frac{F_{B}}{\sin 30}=\frac{10}{\sin 135}$
$F_{B}=7.07 \mathrm{kN}$

Ans.

Ans.

(a)


Ans:
$F_{A}=3.66 \mathrm{kN}$
$F_{B}=7.07 \mathrm{kN}$

2-22. If the resultant $\mathbf{F}_{R}$ of the two forces acting on the $\log$ is to be directed along the positive $x$ axis and have a magnitude of 10 kN , determine the angle u of the cable, attached to $B$ such that the force $\mathbf{F}_{B}$ in this cable is minimum. What is the magnitude of the force in each cable for this situation?


## Solution

Parallelogram Law: In order to produce a minimum force, $\mathbf{F}_{B}, \mathbf{F}_{B}$ has to act perpendicular to $\mathbf{F}_{A}$. The parallelogram law of addition is shown in Fig. (a).

Trigonometry: Fig.(b).
$F_{B}=10 \sin 30=5.00 \mathrm{kN}$
$F_{A}=10 \cos 30=8.66 \mathrm{kN}$

The angle $u$ is
$\mathrm{u}=90-30=60.0$

Ans.
Ans.

Ans.

(a)

(b)

Ans:
$F_{B}=5.00 \mathrm{kN}$
$F_{A}=8.66 \mathrm{kN}$
$\mathrm{u}=60.0$

## 2-23.

Determine the magnitude and direction of the resultant $\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3}$ of the three forces by first finding the resultant $\mathbf{F}_{i}=\mathbf{F}_{1}+\mathbf{F}_{2}$ and then forming $\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{i}+\mathbf{F}_{3}$.

$$
\mathrm{F}^{i}=2(20)^{2}+(30)^{2}-2(20)(30) \cos 73.13^{\circ}=30.85 \mathrm{~N}
$$

$30.85 \quad 30$

$$
\overline{\sin 73.13^{\circ}}=\overline{\sin \left(70^{\circ}-u^{i}\right)} ; \quad u=1.47^{\circ}
$$

$\mathrm{F}_{\mathrm{R}}=2 \overline{(30.85)^{2}+(50)^{2}-2(30.85)(50) \cos 1.47^{\circ}}=19.18=19.2 \mathrm{~N}$
$\frac{19.18}{\sin 1.47^{\circ}}=\frac{30.85}{\sin u} ; \quad u=2.37^{\circ} \sigma$


Ans.


Ans.

Ans:
$F_{R}=19.2 \mathrm{~N}$ $\mathrm{u}=2.37 \mathrm{C}$

## *2-24.

Determine the magnitude and direction of the resultant $\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3}$ of the three forces by first finding the resultant $\mathbf{F}_{i}=\mathbf{F}_{2}+\mathbf{F}_{3}$ and then forming $\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{i}+\mathbf{F}_{1}$.

$$
\begin{aligned}
& \mathrm{F}^{i}=\frac{2(20)^{2}+(50)^{2}-2(20)(50) \cos 70^{\circ}}{}=47.07 \mathrm{~N} \\
& 20=\begin{array}{c}
47.07 \\
\sin 70^{\circ} ; \quad u^{i}=23.53^{\circ}
\end{array}
\end{aligned}
$$

$$
\mathrm{F}_{\mathrm{R}}=2 \overline{(47.07)^{2}+(30)^{2}-2(47.07)(30) \cos 13.34^{\circ}}=19.18=19.2 \mathrm{~N}
$$

$\overline{19.18}=\overline{30}$
$\sin 13.34^{\circ}$
$u=23.53^{\circ}-21.15^{\circ}=2.37^{\circ}$ 文


Ans.

Ans.


## Ans:

$F_{R}=19.2 \mathrm{~N}$

## 2-25.

If the resultant force of the two tugboats is 3 kN , directed along the positive x axis, determine the required magnitude of force $\mathbf{F}_{\mathrm{B}}$ and its direction $u$.

## SOLUTION

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.

Applying the law of cosines to Fig. b,

$$
\begin{aligned}
\mathrm{F}_{\mathrm{B}} & =2 \underline{2^{2}+3^{2}-2(2)(3) \cos 30^{\circ}} \\
& =1.615 \mathrm{kN}=1.61 \mathrm{kN}
\end{aligned}
$$

Ans.

Using this result and applying the law of sines to Fig. b, yields

$$
\begin{array}{ll}
\sin \mathrm{u} \\
2
\end{array}=\begin{aligned}
& \sin 30^{\circ} \\
& 1.615
\end{aligned} \quad \mathrm{u}=38.3^{\circ}
$$


(b)

[^0]
## 2-26.

If $\mathrm{F}_{\mathrm{B}}=3 \mathrm{kN}$ and $\mathrm{u}=45^{\circ}$, determine the magnitude of the resultant force of the two tugboats and its direction measured clockwise from the positive x axis.

## SOLUTION

C

The parallelogram law of addition and the triangular rule are shown in Figs. $a$ and $b$, respectively.

Applying the law of cosines to Hig. $b$,

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =2 \overline{2^{2}+3^{2}-2(2)(3) \cos 105^{\circ}} \\
& =4.013 \mathrm{kN}=4.01 \mathrm{kN}
\end{aligned}
$$

Ans.
Using this result and applying the law of sines to Fig. $b$, yields

$$
\frac{\sin \mathrm{a}}{3}=\frac{\sin 105^{\circ}}{4.013} \quad \mathrm{a}=46.22^{\circ}
$$

Thus, the direction angle $\mathbf{f}$ of $\mathbf{F}_{\mathrm{R}}$, measured clockwise from the positive x axis, is

$$
\mathbf{f}=\mathbf{a}-30^{\circ}=46.22^{\circ}-30^{\circ}=16.2^{\circ}
$$

Ans.

(b)

> Ans:
> $F_{R}=4.01 \mathrm{kN}$
> $\mathbf{f}=16.2$

2-27.
If the resultant force of the two tugboats is required to be directed towards the positive x axis, and $\mathrm{F}_{\mathrm{B}}$ is to be a minimum, determine the magnitude of $\mathbf{F}_{R}$ and $\mathbf{F}_{\mathrm{B}}$ and the angle $u$.

## SOLUTION

For $\mathbf{F}_{\mathrm{B}}$ to be minimum, it has to be directed perpendicular to $\mathbf{F}_{\mathrm{R}}$. Thus,

$$
\mathrm{u}=90^{\circ}
$$

Ans.


The parallelogram law of addition and triangular rule are shown in Figs. $a$ and $b$, respectively.

By applying simple trigonometry to Fig. $b$,

$$
\begin{aligned}
& \mathrm{F}_{\mathrm{B}}=2 \sin 30^{\circ}=1 \mathrm{kN} \\
& \mathrm{~F}_{\mathrm{R}}=2 \cos 30^{\circ}=1.73 \mathrm{kN}
\end{aligned}
$$

Ans.
Ans.


Ans:
$\mathrm{u}=90$
$F_{B}=1 \mathrm{kN}$
$F_{R}=1.73 \mathrm{kN}$
*2-28.
Determine the magnitude of force $\mathbf{F}$ so that the resultant $\mathbf{F}_{R}$ of the three forces is as small as possible. What is the minimum magnitude of $\mathbf{F}_{R}$ ?.


Parallelogram Law. The parallelogram laws of addition for 6 kN and 8 kN and then their resultant $F$ and $F$ are shown in Figs. $a$ and $b$, respectively. In order for $F_{R}$ to be minimum, it must act perpendicular to $\mathbf{F}$.
Trigonometry. Referring to Fig. $b$,

$$
F=2 \underline{6^{2}+8^{2}}=10.0 \mathrm{kN} \quad \mathrm{u}=\tan ^{-1} \mathrm{a}_{\underline{6}}^{8} \mathrm{~b}=53.13 .
$$

Referring to Figs. $c$ and $d$,

$$
\begin{array}{rl}
F_{R} & =10.0 \sin 83.13 \\
F & =9.928 \mathrm{kN}=9.93 \mathrm{kN} \\
F & 0.0 \cos 83.13
\end{array}=1.196 \mathrm{kN}=1.20 \mathrm{kN} \text { }
$$


(a)

(b)


Ans:
$F_{R}=9.93 \mathrm{kN}$
$F=1.20 \mathrm{kN}$

## 2-29.

Determine the magnitude and direction u of $\mathbf{F}_{A}$ so that the resultant force is directed along the positive $x$ axis and has a magnitude of 1250 N .

## SOLUTION

$$
\begin{array}{ll}
\$ F_{R_{x}}=\Sigma F_{x} ; & F_{R_{x}}=F_{A} \sin \mathrm{u}+800 \cos 30^{\circ}=1250 \\
+\mathrm{c} F_{R_{y}}=\Sigma F_{y} ; & F_{R_{y}}=F_{A} \cos \mathrm{u}-800 \sin 30^{\circ}=0 \\
\mathrm{u} & =54.3^{\circ} \\
& F_{A}=686 \mathrm{~N}
\end{array}
$$



Ans.

Ans.

Ans:
$\mathrm{u}=54.3$
$F_{A}=686 \mathrm{~N}$

## 2-30.

Determine the magnitude and direction, measured counterclockwise from the positive $x$ axis, of the resultant force acting on the ring at $O$, if $F_{A}=750 \mathrm{~N}$ and $\mathrm{u}=45^{\circ}$.

## SOLUTION

Scalar Notation: Suming the force components algebraically, we have

$$
\begin{aligned}
\$ F_{R_{x}}=\Sigma F_{x} ; \quad F_{R_{x}} & =750 \sin 45^{\circ}+800 \cos 30^{\circ} \\
& =1223.15 \mathrm{~N} \mathrm{~S}
\end{aligned}
$$

$$
+\mathrm{c} F_{R_{y}}=\Sigma F_{y} ; \quad F_{R_{y}}=750 \cos 45^{\circ}-800 \sin 30^{\circ}
$$

$$
=130.33 \mathrm{~N} \mathrm{c}
$$

The magnitude of the resultant force $\mathbf{F}_{R}$ is

$$
\begin{aligned}
F_{R} & =3 \overline{F_{R_{x}}^{2}+F_{R_{y}}^{2}} \\
& =2 \overline{1223.15^{2}+130.33^{2}}=1230 \mathrm{~N}=1.23 \mathrm{kN}
\end{aligned}
$$

The directional angle u measured counterclockwise from positive $x$ axis is

$$
\mathrm{u}=\tan ^{-1} \frac{F_{R_{y}}}{F_{R_{x}}}=\tan ^{-1} \mathrm{a}_{1223.15}^{130.33 \mathrm{~b}=6.08^{\circ} .}
$$



Ans.


Ans.


## Ans:

$F_{R}=1.23 \mathrm{kN}$
$\mathrm{u}=6.08$

## 2-31.

Two forces act on the screw eye. If $\mathrm{F}=600 \mathrm{~N}$, determine the magnitude of the resultant force and the angle $u$ if the resultant force is directed vertically upward.
F
$500 \mathrm{~N} \quad \mathrm{u}$

## SOLUTION

The parallelogram law of addition and triangular rule are shown in Figs. $a$ and $b$ respectively. Applying law of sines to Fig. $b$,

$$
\begin{gathered}
\sin u \\
600
\end{gathered}=\begin{gathered}
\sin 30^{\circ} \\
500
\end{gathered} ; \quad \sin u=0.6 \quad u=36.87^{\circ}=36.9^{\circ}
$$

Ans.


Using the result of $u$,

$$
\mathbf{f}=180^{\circ}-30^{\circ}-36.87^{\circ}=113.13^{\circ}
$$

Again, applying law of sines using the result of $\mathbf{f}$,

$$
\frac{\mathrm{F}_{\mathrm{R}}}{\sin 113.13^{\circ}}=\frac{500}{\sin 30^{\circ}} ; \quad \mathrm{F}_{\mathrm{R}}=919.61 \mathrm{~N}=920 \mathrm{~N}
$$

Ans.


Ans:
$\mathrm{u}=36.9$
$\mathrm{u}=920 \mathrm{~N}$
*2-32.
Resolve each force acting on the gusset plate into its x and y components, and express each force as a Cartesian vector.

## SOLUTION

$\mathbf{F}_{1}=\{900(+\mathbf{i})\}=\{900 \mathbf{i}\} \mathrm{N}$
$\mathbf{F}_{2}=\left\{750 \cos 45^{\circ}(+\mathbf{i})+750 \sin 45^{\circ}(+\mathbf{j})\right\} \mathrm{N}$
$=\{530 \mathbf{i}+530 \mathbf{j}\} \mathrm{N}$
$\mathbf{F}_{3}=$ e $650 \mathrm{a} \frac{4}{5} \mathrm{~b}(+\mathbf{i})+650 \mathrm{a} \frac{3}{5} \mathrm{~b}(-\mathbf{j}) \mathrm{f} \mathbf{N}$
$=\{520 \mathbf{i}-390 \mathbf{j})\} \mathrm{N}$


## Ans.

## Ans.

## Ans.





Ans:
$\mathbf{F}_{1}=5900 \mathbf{i} 6 \mathrm{~N}$
$\mathbf{F}_{2}=5530 \mathbf{i}+530 \mathbf{j} 6 \mathrm{~N}$
$\mathbf{F}_{3}=5520 \mathbf{i}-390 \mathbf{j} 6 \mathrm{~N}$

## 2-33.

Determine the magnitude of the resultant force acting on the plate and its direction, measured counterclockwise from the positive $x$ axis.


## SOLUTION

Rectangular Components: By referring to Fig. $a$, the $x$ and $y$ components of $\mathbf{F}_{1}, \mathbf{F}_{2}$, and $\mathbf{F}_{3}$ can be written as

$$
\begin{array}{lr}
\left(\mathrm{F}_{1}\right)_{\mathrm{x}}=900 \mathrm{~N} & \left(\mathrm{~F}_{1}\right)_{\mathrm{y}}=0 \\
\left(\mathrm{~F}_{2}\right)_{\mathrm{x}}=750 \cos 45^{\circ}=530.33 \mathrm{~N} & \left(\mathrm{~F}_{2}\right)_{\mathrm{y}}=750 \sin 45^{\circ}=530.33 \mathrm{~N} \\
\left(\mathrm{~F}_{3}\right)_{\mathrm{x}}=650 \mathrm{a}{ }_{5}^{4} \mathrm{~b}=520 \mathrm{~N} & \left(\mathrm{~F}_{3}\right)_{\mathrm{y}}=650 \mathrm{a}{ }_{5}^{3} \mathrm{~b}=390 \mathrm{~N}
\end{array}
$$

Resultant Force: Summing the force components algebraically along the x and y axes, we have

$$
\begin{array}{ll} 
\pm \odot\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=\odot \mathrm{F}_{\mathrm{x}} ; & \left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=900+530.33+520=1950.33 \mathrm{~N}= \\
+\mathrm{c} \odot\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y}}=\odot \mathrm{F}_{\mathrm{y}} ; & \left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}=530.33-390=140.33 \mathrm{~N} \mathrm{c}
\end{array}
$$

The magnitude of the resultant force $\mathbf{F}_{\mathrm{R}}$ is

$$
\mathrm{F}_{\mathrm{R}}=2\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{x}}^{2}+\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}^{2}=21950.33^{2}+140.33^{2}=1955 \mathrm{~N}=1.96 \mathrm{kN} \text { Ans. }
$$

The direction angle u of $\mathbf{F}_{\mathrm{R}}$, measured clockwise from the positive x axis, is
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$$
\begin{gathered}
F_{R}=1.96 \mathrm{kN} \\
\mathrm{u}=4.12
\end{gathered}
$$

2-34.

Resolve $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ into their x and y components.

## SOLUTION

$$
\begin{aligned}
\mathbf{F}_{1} & =\left\{400 \sin 30^{\circ}(+\mathbf{i})+400 \cos 30^{\circ}(+\mathbf{j})\right\} \mathrm{N} \\
& =\{200 \mathbf{i}+346 \mathbf{j}\} \mathrm{N} \\
\mathbf{F}_{2} & =\left\{250 \cos 45^{\circ}(+\mathbf{i})+250 \sin 45^{\circ}(-\mathbf{j})\right\} \mathrm{N} \\
& =\{177 \mathbf{i}-177 \mathbf{j}\} \mathrm{N}
\end{aligned}
$$



Ans.

Ans.


Ans:
$\mathbf{F}_{1}=5200 \mathbf{i}+346 \mathbf{j} 6 \mathrm{~N}$ $\mathbf{F}_{2}=5177 \mathbf{i}-177 \mathbf{j} 6 \mathrm{~N}$

## 2-35.

Determine the magnitude of the resultant force and its
direction measured counterclockwise from the positive $x$ axis.
$y$
60
30
$F_{1} \quad 400 \mathrm{~N}$

## SOLUTION

Rectangular Components: By referring to Fig. $a$, the $x$ and $y$ components of $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be written as

$$
\begin{array}{ll}
\left(\mathrm{F}_{1}\right)_{\mathrm{x}}=400 \sin 30^{\circ}=200 \mathrm{~N} & \left(\mathrm{~F}_{1}\right)_{\mathrm{y}}=400 \cos 30^{\circ}=346.41 \mathrm{~N} \\
\left(\mathrm{~F}_{2}\right)_{\mathrm{x}}=250 \cos 45^{\circ}=176.78 \mathrm{~N} & \left(\mathrm{~F}_{2}\right)_{\mathrm{y}}=250 \sin 45^{\circ}=176.78 \mathrm{~N}
\end{array}
$$

Resultant Force: Summing the force components algebraically along the x and y axes, we have

$$
\begin{array}{ll} 
\pm \odot\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=\odot \mathrm{F}_{\mathrm{x}} ; & \left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=200+176.78=376.78 \mathrm{~N} \\
+\mathrm{c} \odot\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y}}=\odot \mathrm{F}_{\mathrm{y}} ; & \left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}=346.41-176.78=169.63 \mathrm{~N} \mathrm{c}
\end{array}
$$

The magnitude of the resultant force $\mathbf{F}_{\mathrm{R}}$ is

The direction angle u of $\mathbf{F}_{\mathrm{R}}$, Fig. $b$, measured counterclockwise from the positive axis, is

$$
\mathrm{u}=\tan ^{-1}{ }_{\mathrm{c}}^{\left.\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}\right)_{\mathrm{x}}} \mathrm{~d}=\tan ^{-1} \mathrm{a} \frac{169.63}{376.78} \mathrm{~b}=24.2^{\circ}
$$

Ans.

Ans:
$F_{R}=413 \mathrm{~N}$
$\mathrm{u}=24.2$
*2-36.
Determine the magnitude of the resultant force and its direction, measured counterclockwise from the positive $x$ axis.

## SOLUTION

$+\mathrm{R} \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; \quad \mathrm{F}_{\mathrm{Rx}}=-150 \cos 30^{\circ}+200 \sin 45^{\circ}=11.518 \mathrm{~N}$
$\mathrm{Q}+\mathrm{F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad \mathrm{F}_{\mathrm{Ry}}=150 \sin 30^{\circ}+200 \cos 45^{\circ}=216.421 \mathrm{~N}$
$\mathrm{F}_{\mathrm{R}}=2(11.518)^{2}+(216.421)^{2}=217 \mathrm{~N}$
$u=\tan ^{-1} \phi \frac{216.421}{11.518} \leq=87.0^{\circ}$


Ans.

Ans.

Ans:
$F_{R}=217 \mathrm{~N}$ $\mathrm{u}=87.0$

2-37.
Determine the magnitude of the resultant force and its direction, measured clockwise from the positive $x$ axis.

## Solution

Scalar Notation. Summing the force components along $x$ and $y$ axes by referring to Fig. $a$,

$$
\begin{aligned}
& \mathbf{S}\left(F_{R}\right)_{x}=F_{x} ; \quad\left(F_{R}\right)_{x}=400 \cos 30+800 \sin 45=912.10 \mathrm{~N} \mathrm{~S} \\
& +\mathrm{c}\left(F_{R}\right)_{y}=F_{y} ; \quad\left(F_{R}\right)_{y}=400 \sin 30-800 \cos 45=-365.69 \mathrm{~N}=365.69 \mathrm{NT}
\end{aligned}
$$

Referring to Fig. $b$, the magnitude of the resultant force is

$$
F_{R}=2 \underline{\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}=2 \underline{912.10^{2}+365.69^{2}}=982.67 \mathrm{~N}=983 \mathrm{~N} \quad \text { Ans. }}
$$

And its directional angle $u$ measured clockwise from the positive $x$ axis is

$$
\mathrm{u}=\tan ^{-1}{ }_{\mathrm{c}}^{\left(F_{R}\right)_{y}}{ }_{\left(F_{R}\right) \bar{x}}=\tan ^{-1} \mathrm{a} \frac{365.69}{912.10} \mathrm{~b}=21.84=21.8
$$

Ans.


## Ans:

$$
F_{R}=983 \mathrm{~N}
$$

$$
\mathrm{u}=21.8
$$

2-38.

Determine the magnitude of the resultant force and its direction, measured clockwise from the positive $x$ axis.

## Solution

Given:
$F_{1} \quad 70 \mathrm{~N}$
$F_{2} \quad 50 \mathrm{~N}$
$F_{3} \quad 65 \mathrm{~N}$
30
45

$$
F_{R x}=F_{x} ; \quad F_{R X} \quad F_{1} \quad F_{2} \cos \quad F_{3} \cos
$$

$$
F_{R y}=F_{y} ; \quad F_{R Y} \quad F_{2} \sin \quad F_{3} \sin
$$

$F_{R} \sqrt{F_{R X}{ }^{2} F_{R Y}{ }^{2}}$
$\operatorname{atan} \frac{\left|F_{R Y}\right|}{\left|F_{R X}\right|}$
$F_{R} \quad 97.8 \mathrm{~N}$
46.5

Ans.

Ans.

Ans:
$F_{R}=97.8 \mathrm{~N}$

## 2-39.

Express $\mathbf{F}_{1}, \mathbf{F}_{2}$, and $\mathbf{F}_{3}$ as Cartesian vectors.

## SOLUTION

## 43


$=\{680 \mathbf{i}-510 \mathbf{j}\} \mathrm{N}$
$\mathbf{F}_{2}=-625 \sin 30^{\circ} \mathbf{i}-625 \cos 30^{\circ} \mathbf{j}$
$=\{-312 \mathbf{i}-541 \mathbf{j}\} \mathrm{N}$
$\mathbf{F}_{3}=-750 \sin 45^{\circ} \mathbf{i}+750 \cos 45^{\circ} \mathbf{j}$
$\{-530 \mathbf{i}+530 \mathbf{j}\} \mathrm{N}$
$=$


Ans.

Ans.

Ans.

Ans:
$\mathbf{F}_{1}=\{680 \mathbf{i}-510 \mathbf{j}\} \mathrm{N}$
$\mathbf{F}_{2}=\{-312 \mathbf{i}-541 \mathbf{j}\} \mathrm{N}$
$\mathbf{F}_{3}=\{-530 \mathbf{i}+530 \mathbf{j}\} \mathrm{N}$
*2-40.
Determine the magnitude of the resultant force and its direction measured counterclockwise from the positive $x$ axis.

## SOLUTION

$$
\begin{array}{ll} 
\pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; & \mathrm{F}_{\mathrm{Rx}}={ }_{5}^{4}(850)-625 \sin 30^{\circ}-750 \sin 45^{\circ}=-162.83 \mathrm{~N} \\
+\mathrm{cF}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; & \mathrm{F}_{\mathrm{Ry}}=-\frac{-}{3}(850)-625 \cos 30^{\circ}+750 \cos 45^{\circ}=-520.94 \mathrm{~N} \\
& \mathrm{~F}_{\mathrm{R}}=2 \underline{(-162.83)^{2}+(-520.94)^{2}}=546 \mathrm{~N} \\
& \mathbf{f}=\tan ^{-1} \mathrm{a} \frac{520.94}{162.83} \mathrm{~b}=72.64^{\circ} \\
& \mathrm{u}=180^{\circ}+72.64^{\circ}=253^{\circ} \quad \text { Ans. }
\end{array}
$$



Ans:
$F_{R}=546 \mathrm{~N}$
$\mathrm{u}=253$

## 2-41.

Determine the magnitude and direction $u$ of the resultant force $\mathbf{F}_{\mathrm{R}}$. Express the result in terms of the magnitudes of the components $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ and the angle $\mathbf{f}$.

## SOLUTION

$$
\mathrm{F}_{\mathrm{R}}^{2}=\mathrm{F}_{1}^{2}+\mathrm{F}_{2}^{2}-2 \mathrm{~F}_{1} \mathrm{~F}_{2} \cos \left(180^{\circ}-\mathbf{f}\right)
$$

Since $\cos \left(180^{\circ}-\mathbf{f}\right)=-\cos \mathbf{f}$,

$$
\mathrm{F}_{\mathrm{R}}=\frac{2 \mathrm{~F}^{2}+\mathrm{F}^{2}+2 \mathrm{FF} \cos \mathbf{f}}{122}
$$

From the figure,

$$
\begin{gathered}
\tan \mathrm{u}=\begin{array}{c}
\mathrm{F}_{1} \sin \mathbf{f} \\
\underline{\mathrm{~F}_{2}+\mathrm{F}_{1} \cos \mathbf{f}} \\
\mathrm{u}=\tan ^{-1} \phi \frac{\mathrm{~F}_{1} \underline{\sin \mathbf{f}}}{\mathrm{~F}_{2}+\mathrm{F}_{1} \cos \mathbf{f}} \leq
\end{array}
\end{gathered}
$$

Ans.


Ans.


Ans:
$F_{R}=2 \overline{F_{1}^{2}+F_{2}^{2}+2 F_{1} F_{2} \cos \mathbf{f}}$
$\mathrm{u}=\tan ^{-1} \mathrm{a} \frac{F_{1} \underline{\sin \mathbf{f}}}{F_{2}+F_{1} \cos \mathbf{f}} \mathrm{~b}$

2-42.
Determine the magnitude of the resultant force and its direction, measured counterclockwise from the positive $x$ axis.

## Solution

Scalar Notation. Summing the force components along $x$ and $y$ axes algebraically by referring to Fig. $a$,


$$
\begin{array}{ll}
\mathbf{S}\left(F_{R}\right)_{x}=F_{x} ; & \left(F_{R}\right)_{x}=4+5 \cos 45-8 \sin 15=5.465 \mathrm{kN} \mathrm{~S} \\
+\mathrm{c}\left(F_{R}\right)_{y}=F_{y} ; & \left(F_{R}\right)_{y}=5 \sin 45+8 \cos 15=11.263 \mathrm{kN} \mathrm{c}
\end{array}
$$

By referring to Fig. $b$, the magnitude of the resultant force $\mathbf{F}_{R}$ is

$$
F_{R}=2\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}=25.465^{2}+11.263^{2}=12.52 \mathrm{kN}=12.5 \mathrm{kN}
$$

Ans.

And the directional angle u of $\mathbf{F}_{R}$ measured counterclockwise from the positive $x$ axis is

$$
\mathrm{u}=\tan ^{-1}{ }^{c}{ }^{\left(F_{R}\right)_{y}}{ }_{\left(F_{R}\right)_{x}}{ }^{d}=\tan ^{-1} \mathrm{a}_{5.465}^{11.263} \mathrm{~b}=64.12=64.1
$$

Ans.

(a)

(b)

Ans:
$F_{R}=12.5 \mathrm{kN}$
$\mathrm{u}=64.1$

## 2-43.

Determine the $x$ and $y$ components of $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$.

## SOLUTION

$$
\begin{aligned}
& \mathrm{F}_{1 \mathrm{x}}=200 \sin 45^{\circ}=141 \mathrm{~N} \\
& \mathrm{~F}_{1 \mathrm{y}}=200 \cos 45^{\circ}=141 \mathrm{~N} \\
& \mathrm{~F}_{2 \mathrm{x}}=-150 \cos 30^{\circ}=-130 \mathrm{~N} \\
& \mathrm{~F}_{2 \mathrm{y}}=150 \sin 30^{\circ}=75 \mathrm{~N}
\end{aligned}
$$

Ans.

Ans.
Ans.
Ans.

Ans:
$F_{1 x}=141 \mathrm{~N}$
$F_{1 y}=141 \mathrm{~N}$
$F_{2 x}=-130 \mathrm{~N}$
$F_{2 y}=75 \mathrm{~N}$

## *2-44.

Determine the magnitude of the resultant force and its direction, measured counterclockwise from the positive $x$ axis.

## SOLUTION

$+\mathrm{R} \mathrm{F}_{\mathrm{Rx}}=$ © $\mathrm{F}_{\mathrm{x}} ; \quad \mathrm{F}_{\mathrm{Rx}}=-150 \cos 30^{\circ}+200 \sin 45^{\circ}=11.518 \mathrm{~N}$
$\mathrm{Q}+\mathrm{F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad \mathrm{F}_{\mathrm{Ry}}=150 \sin 30^{\circ}+200 \cos 45^{\circ}=216.421 \mathrm{~N}$
$\mathrm{F}_{\mathrm{R}}=2(11.518)^{2}+(216.421)^{2}=217 \mathrm{~N}$
$u=\tan ^{-1} 中_{\frac{216.421}{11.518}} \leq=87.0^{\circ}$


Ans.

Ans.

Ans:
$\mathrm{F}_{\mathrm{R}}=217 \mathrm{~N}$
u $=87.0^{\circ}$

2-45.
Express each of the three forces acting on the support in Cartesian vector form and determine the magnitude of the resultant force and its direction, measured clockwise from positive $x$ axis.

## Solution

Cartesian Notation. Referring to Fig. $a$,

$$
\begin{aligned}
& \mathbf{F}_{1}=\left(F_{1}\right)_{x} \mathbf{i}+\left(F_{1}\right)_{y} \mathbf{j}=50 \mathrm{a}_{5} \mathrm{~b}_{\mathbf{i}}+50 \mathrm{a}_{5}{ }^{\mathrm{b}} \mathbf{j}=\{30 \mathbf{i}+40 \mathbf{j}\} \mathrm{N} \\
& \mathbf{F}_{2}=-\left(F_{2}\right)_{x} \mathbf{i}-\left(F_{2}\right)_{y} \mathbf{j}=-80 \sin 15 \mathbf{i}-80 \cos 15 \mathbf{j} \\
& =\{-20.71 \mathbf{i}-77.27 \mathbf{j}\} \mathrm{N} \\
& =\{-20.7 \mathbf{i}-77.3 \mathbf{j}\} \mathrm{N} \\
& F_{3}=\left(F_{3}\right)_{x} \mathbf{i}=\{30 \mathbf{i}\}
\end{aligned}
$$

Thus, the resultant force is

$$
\begin{aligned}
\mathbf{F}_{R}=\mathbf{F} ; \quad \mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3} \\
& =(30 \mathbf{i}+40 \mathbf{j})+(-20.71 \mathbf{i}-77.27 \mathbf{j})+30 \mathbf{i} \\
& =\{39.29 \mathbf{i}-37.27 \mathbf{j}\} \mathbf{N}
\end{aligned}
$$

Referring to Fig. $b$, the magnitude of $\mathbf{F}_{R}$ is

$$
F_{R}=239.29^{2}+37.27^{2}=54.16 \mathrm{~N}=54.2 \mathrm{~N}
$$

And its directional angle $u$ measured clockwise from the positive $x$ axis is

$$
\mathrm{u}=\tan ^{-1} \mathrm{a} \frac{37.27}{39.29} \mathrm{~b}=43.49=43.5
$$



Ans.

Ans.
Ans.

Ans.

Ans.

(b) Ans:
$\mathbf{F}_{1}=\{30 \mathbf{i}+40 \mathbf{j}\} \mathbf{N}$
$\mathbf{F}_{2}=\{-20.7 \mathbf{i}-77.3 \mathbf{j}\} \mathbf{N}$
$\mathbf{F}_{3}=\{30 \mathbf{i}\}$
$F_{R}=54.2 \mathrm{~N}$
$u=43.5$

## 2-46.

Determine the $x$ and $y$ components of each force acting on the gusset plate of a bridge truss. Show that the resultant force is zero.

## Solution



Scalar Notation. Referring to Fig. $a$, the $x$ and $y$ components of each forces are

$$
\begin{aligned}
& \left(F_{1}\right)_{x}=8 \mathrm{a}_{5}^{4} \mathrm{~b}=6.40 \mathrm{kN} \mathrm{~S} \\
& \left(F_{1}\right)_{y}=8 \mathrm{a}_{5}^{3} \mathrm{~b}=4.80 \mathrm{kN} \mathrm{~T} \\
& \left(F_{2}\right)_{x}=6 \mathrm{a}_{5}^{\frac{3}{5}} \mathrm{~b}=3.60 \mathrm{kN} \mathrm{~S} \\
& \left(F_{2}\right)_{y}=6 \mathrm{a}_{5}^{4} \mathrm{~b}=4.80 \mathrm{kN} \mathrm{c} \\
& \left(F_{3}\right)_{x}=4 \mathrm{kN} \mathrm{~d} \\
& \left(F_{3}\right)_{y}=0 \\
& \left(F_{4}\right)_{x}=6 \mathrm{kN} \mathrm{~d} \\
& \left(F_{4}\right)_{y}=0
\end{aligned}
$$

Ans.

Ans.

Ans.

Ans.

Ans.
Ans.
Ans.
Ans.

Summing these force components along $x$ and $y$ axes algebraically,

$$
\begin{array}{ll}
\mathbf{S}\left(F_{R}\right)_{x}=F_{x} ; & \left(F_{R}\right)_{x}=6.40+3.60-4-6=0 \\
+\mathrm{c}\left(F_{R}\right)_{y}=F_{y} ; & \left(F_{R}\right)_{y}=4.80-4.80=0
\end{array}
$$

Thus,

$$
\begin{equation*}
F_{R}=2\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}=20^{2}+0^{2}=0 \tag{Q.E.D}
\end{equation*}
$$


(a)

$$
\begin{aligned}
& \text { Ans: } \\
& \begin{array}{l}
\left(F_{1}\right)_{x}=6.40 \mathrm{kN} \mathrm{~S} \\
\left(F_{1}\right)_{y}=4.80 \mathrm{kN} \mathrm{~T} \\
\left(F_{2}\right)_{x}=3.60 \mathrm{kN} \mathrm{~S} \\
\left(F_{2}\right)_{y}=4.80 \mathrm{kN} \mathrm{c} \\
\left(F_{3}\right)_{x}=4 \mathrm{kN} \mathrm{~d} \\
\left(F_{3}\right)_{y}=0 \\
\left(F_{4}\right)_{x}=6 \mathrm{kN} \mathrm{~d} \\
\left(F_{4}\right)_{y}=0
\end{array}
\end{aligned}
$$

2-47.
Express $\mathbf{F}_{1}, \mathbf{F}_{2}$, and $\mathbf{F}_{3}$ as Cartesian vectors.

## Solution

$$
\begin{aligned}
\mathbf{F}_{1} & =\{15 \sin 40 \mathbf{i}+15 \cos 40 \mathbf{j}\} \mathrm{kN} \\
& =\{9.6 \mathbf{i}+11.49 \mathbf{j}\} \mathrm{kN} \\
\mathbf{F}_{2} & =-26(12>13) \mathbf{i}+26(5>13) \mathbf{j} \\
& =\{-24 \mathbf{i}+10 \mathbf{j}\} \mathrm{kN} \\
\mathbf{F}_{3} & =36 \cos 30 \mathbf{i}-36 \sin 30 \mathbf{j} \\
& =\{31.2 \mathbf{i}+18 \mathbf{j}\} \mathrm{kN}
\end{aligned}
$$

Ans.

Ans.

Ans:
$\mathbf{F}_{1}=\{9.64 \mathbf{i}+11.5 \mathbf{j}\} \mathrm{kN}$
$\mathbf{F}_{2}=\{-24 \mathbf{i}+10 \mathbf{j}\} \mathrm{kN}$
$\mathbf{F}_{3}=\{31.2 \mathbf{i}-18 \mathbf{j}\} \mathrm{kN}$

## *2-48.

Determine the magnitude of the resultant force and its direction measured counterclockwise from the positive $x$ axis.

## SOLUTION

$$
\left.\begin{array}{cc} 
\pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; & \mathrm{F}_{\mathrm{Rx}}=15 \sin 40^{\circ}-\frac{12}{13}(26)+36 \cos 30^{\circ}=16.82 \mathrm{kN} \\
+\mathrm{c} \mathrm{~F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; & \mathrm{F}_{\mathrm{Ry}}=15 \cos 40^{\circ}+\frac{-5}{13}(26)-36 \sin 30^{\circ}=3.491 \mathrm{kN} \\
& \mathrm{~F}_{\mathrm{R}}=2(16.82)^{2}+(3.491)^{2}
\end{array}\right) 17.2 \mathrm{kN} .
$$

Ans.

Ans.



$$
\begin{aligned}
\mathbf{F}_{1} & =\left\{15 \sin 40^{\circ} \mathbf{i}+15 \cos 40^{\circ} \mathbf{j}\right\} \mathrm{kN}=\{9.64 \mathbf{i}+11.5 \mathbf{j}\} \mathrm{kN} \\
\mathbf{F}_{2} & =\mathrm{b}-\frac{12}{13}(26) \mathbf{i}+\frac{5}{13}(26) \mathbf{j} \mathrm{rkN}=\{-24 \mathbf{i}+10 \mathbf{j}\} \mathrm{kN} \\
\mathbf{F}_{3} & =\left\{36 \cos 30^{\circ} \mathbf{i}-36 \sin 30^{\circ} \mathbf{j}\right\} \mathrm{kN}=\{31.2 \mathbf{i}-18 \mathbf{j}\} \mathrm{kN} \\
\mathbf{F}_{\mathrm{R}} & =\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3} \\
& =\{9.64 \mathbf{i}+11.5 \mathbf{j}\}+\{-24 \mathbf{i}+10 \mathbf{j}\}+\{31.2 \mathbf{i}-18 \mathbf{j}\} \\
& =\{16.8 \mathbf{i}+3.49 \mathbf{j}\} \mathrm{kN}
\end{aligned}
$$

## Also,

Ans:
$F_{R}=17.2 \mathrm{kN}, \mathrm{u}=11.7$

2-49.
If $\mathrm{F}_{1}=300 \mathrm{~N}$ and $\mathrm{u}=10^{\circ}$, determine the magnitude and direction, measured counterclockwise from the positive $x i$ axis, of the resultant force acting on the bracket.

## SOLUTION

$$
\begin{array}{ll} 
\pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{Fx} ; & \mathrm{F}_{\mathrm{Rx}}=300 \sin 70^{\circ}-\frac{12}{\underline{13}}(180)=115.8 \mathrm{~N} \\
+\mathrm{c} \mathrm{~F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; & \mathrm{F}_{\mathrm{Ry}}=300 \cos 70^{\circ}+200+\frac{5}{\underline{13}}(180)=371.8 \mathrm{~N} \\
& \mathrm{~F}_{\mathrm{R}}=2 \underline{(115.8)^{2}+(371.8)^{2}}=389 \mathrm{~N} \\
& \mathbf{f}=\tan ^{-1} \mathrm{~B} \frac{371.8}{115.8^{2}} \mathrm{~K}=72.71^{\circ} \quad \mathbf{a u} \\
& \mathbf{f i} i=72.71^{\circ}-30^{\circ}=42.7^{\circ}
\end{array}
$$

Ans:
$F_{R}=389 \mathrm{~N}$
$\mathbf{f}=42.7$

## 2-50.

Three forces act on the bracket. Determine the magnitude and direction $u$ of $\mathbf{F}_{1}$ so that the resultant force is directed along the positive $\mathrm{x}_{6}$ axis and has a magnitude of 800 N .

## SOLUTION

$$
\begin{array}{cl} 
\pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; & 800 \sin 60^{\circ}=\mathrm{F}_{1} \sin \left(60^{\circ}+\mathrm{u}\right)-\frac{12}{13}(180) \\
+\mathrm{cF}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; & 800 \cos 60^{\circ}=\mathrm{F}_{1} \cos \left(60^{\circ}+\mathrm{u}\right)+200+\frac{5}{13}(180) \\
& 60^{\circ}+\mathrm{u}=81.34^{\circ} \\
\mathrm{u}=21.3^{\circ} \\
& \mathrm{F}_{1}=869 \mathrm{~N}
\end{array}
$$



Ans.
Ans.

Ans:
$\mathrm{u}=21.3$
$F_{1}=869 \mathrm{~N}$

2-51.

Determine the magnitude and orientation u of $\mathbf{F}_{B}$ so that the resultant force is directed along the positive $y$ axis and has a magnitude of 1500 N .

## SOLUTION

Scalar Notation: Suming the force components algebraically, we have

$$
\begin{array}{cc}
\$ F_{R_{z}}=\Sigma F_{x} ; & 0=700 \sin 30^{\circ}-F_{B} \cos \mathrm{u} \\
F_{B} \cos \mathrm{u}=350 \\
+\mathrm{c} F_{R_{y}}=\Sigma F_{y} ; & 1500=700 \cos 30^{\circ}+F_{B} \sin \mathrm{u} \\
F_{B} \sin \mathrm{u}=893.8 \tag{2}
\end{array}
$$

Solving Eq. (1) and (2) yields

$$
\mathrm{u}=68.6^{\circ} \quad F_{B}=960 \mathrm{~N}
$$

(1)

Ans.



Ans:
$\mathrm{u}=68.6$
$F_{B}=960 \mathrm{~N}$
*2-52.

Determine the magnitude and orientation, measured counterclockwise from the positive $y$ axis, of the resultant force acting on the bracket, if $F_{B}=600 \mathrm{~N}$ and $\mathrm{u}=20^{\circ}$.

## SOLUTION

Scalar Notation: Suming the force components algebraically, we have

$$
\begin{aligned}
\mathrm{S} F_{R_{x}}=\Sigma F_{x} ; \quad F_{R_{x}} & =700 \sin 30^{\circ}-600 \cos 20^{\circ} \\
& =-213.8 \mathrm{~N}=213.8 \mathrm{~N} \mathrm{~d} \\
+\mathrm{c} F_{R_{y}}=\Sigma F_{y} ; \quad F_{R_{y}} & =700 \cos 30^{\circ}+600 \sin 20^{\circ} \\
& =811.4 \mathrm{~N} \mathrm{c}
\end{aligned}
$$

The magnitude of the resultant force $\mathbf{F}_{R}$ is

$$
F_{R}=2 F_{R_{x}}^{2}+F_{R_{y}}^{2}=2213.8^{2}+811.4^{2}=839 \mathrm{~N}
$$

Ans.

The directional angle u measured counterclockwise from positive $y$ axis is

$$
\mathrm{u}=\tan ^{-1} \frac{F_{R_{x}}}{F_{R_{y}}}=\tan ^{-1} \mathrm{a}_{811.4}^{213.8 \mathrm{~b}}=14.8^{\circ}
$$

$y$


$$
\begin{aligned}
& \text { Ans: } \\
& F_{R}=839 \mathrm{~N} \\
& \mathrm{u}=14.8
\end{aligned}
$$

2-53.
Three forces act on the bracket. Determine the magnitude and direction u of $\mathbf{F}$ so that the resultant force is directed along the positive $x$ axis and has a magnitude of 8 kN .

## Solution

Scalar Notation. Equating the force components along the $x$ and $y$ axes algebraically by referring to Fig. $a$,


$$
\begin{align*}
\mathbf{S}\left(F_{R}\right)_{x}=\quad F_{x} ; \quad 8 \cos 30 & =F \sin \mathrm{u}+6-4 \sin 15 \\
F \sin \mathrm{u} & =1.9635  \tag{1}\\
+\mathrm{c}\left(F_{R}\right)_{y}=\quad F_{y} ; \quad 8 \sin 30 & =F \cos \mathrm{u}+4 \cos 15 \\
F \cos \mathrm{u} & =0.1363 \tag{2}
\end{align*}
$$

Divide Eq (1) by (2)

$$
\tan \mathrm{u}=14.406 \quad \mathrm{u}=86.03=86.0
$$

Ans.
Substitute this result into Eq (1)

$$
\begin{aligned}
F \sin 86.03 & =1.9635 \\
F=1.968 \mathrm{kN} & =1.97 \mathrm{kN}
\end{aligned}
$$

Ans.


Ans:
$\mathrm{u}=86.0$
$F=1.97 \mathrm{kN}$

2-54.
If $F=5 \mathrm{kN}$ and $\mathrm{u}=30^{\circ}$, determine the magnitude of the resultant force and its direction, measured counterclockwise from the positive $x$ axis.

## Solution

Scalar Notation. Summing the force components along $x$ and $y$ axes algebraically
 by referring to Fig. $a$,

$$
\begin{aligned}
& \mathbf{S}\left(F_{R}\right)_{x}=F_{x} ; \quad\left(F_{R}\right)_{x}=5 \sin 30+6-4 \sin 15=7.465 \mathrm{kN} \mathrm{~S} \\
& +\mathrm{c}\left(F_{R}\right)_{y}=F_{y} ; \quad\left(F_{R}\right)_{y}=4 \cos 15+5 \cos 30=8.194 \mathrm{kN} \mathrm{c}
\end{aligned}
$$

By referring to Fig. $b$, the magnitude of the resultant force is

$$
F_{R}=\frac{2\left(F_{R}\right)^{2}+(F)^{2}}{x y}=2 \underline{7.465^{2}+8.194^{2}}=11.08 \mathrm{kN}=11.1 \mathrm{kN} \text { Ans. }
$$

And its directional angle u measured counterclockwise from the positive $x$ axis is

$$
\mathrm{u}=\tan ^{-1}{ }_{\mathrm{c}}^{\left(F_{R}\right)_{y}}{ }_{\left(F_{R}\right)_{x}}^{\mathrm{d}} \mathrm{~d}=\tan ^{-1} \mathrm{a}_{7.465}^{8.194} \mathrm{~b}=47.67=47.7
$$

Ans.

(a)

(b)

Ans:
$F_{R}=11.1 \mathrm{kN}$
$\mathrm{u}=47.7$

2-55.
If the magnitude of the resultant force acting on the bracket is to be 450 N directed along the positive $u$ axis, determine the magnitude of $\mathbf{F}_{1}$ and its direction $\mathbf{f}$.

## SOLUTION

Rectangular Components: By referring to Fig. $a$, the $x$ and $y$ components of $\mathbf{F}_{1}, \mathbf{F}_{2}$,
$\mathbf{F}_{3}$, and $\mathbf{F}_{R}$ can be written as
$\left(\mathrm{F}_{1}\right)_{\mathrm{x}}=\mathrm{F}_{1} \sin \mathbf{f}$
$\left(\mathrm{F}_{1}\right)_{\mathrm{y}}=\mathrm{F}_{1} \cos \mathbf{f}$
$\left(\mathrm{F}_{2}\right)_{\mathrm{x}}=200 \mathrm{~N}$
$\left(\mathrm{F}_{2}\right)_{\mathrm{y}}=0$
$\left(\mathrm{F}_{3}\right)_{\mathrm{x}}=260 \not{ }_{13}^{5} \leq=100 \mathrm{~N}$
$\left(\mathrm{F}_{3}\right)_{\mathrm{y}}=260 ¢_{13}^{12} \leq=240 \mathrm{~N}$
$\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=450 \cos 30^{\circ}=389.71 \mathrm{~N}$
$\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}=450 \sin 30^{\circ}=225 \mathrm{~N}$
Resultant Force: Summing the force components algebraically along the $x$ and $y$ axes,

$$
\pm \odot\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=\odot \mathrm{F}_{\mathrm{x}} ; \quad 389.71=\mathrm{F}_{1} \sin \mathbf{f}+200+100
$$

$$
\begin{equation*}
\mathrm{F}_{1} \sin \mathbf{f}=89.71 \tag{1}
\end{equation*}
$$

$$
\begin{equation*}
\mathrm{F}_{1} \cos \mathbf{f}=465 \tag{2}
\end{equation*}
$$

$$
+\mathrm{c} \odot\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad 225=\mathrm{F}_{1} \cos \mathbf{f}-240
$$



Solving Eqs. (1) and (2), yields

$$
\mathbf{f}=10.9^{\circ}
$$

$$
\mathrm{F}_{1}=474 \mathrm{~N}
$$

Ans.
(a)

(b)
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$$
F_{1}=474 \mathrm{~N}
$$

## *2-56.

If the resultant force acting on the bracket is required to be a minimum, determine the magnitudes of $\mathbf{F}_{1}$ and the resultant force. Set $\mathbf{f}=30^{\circ}$.

## SOLUTION

Rectangular Components: By referring to Fig. $a$, the $x$ and $y$ components of $\mathbf{F}_{1}, \mathbf{F}_{2}$, and $\mathbf{F}_{3}$ can be written as

$$
\begin{aligned}
\left(\mathrm{F}_{1}\right)_{\mathrm{x}}=\mathrm{F}_{1} \sin 30^{\circ}=0.5 \mathrm{~F}_{1} & \left(\mathrm{~F}_{1}\right)_{\mathrm{y}}=\mathrm{F}_{1} \cos 30^{\circ}=0.8660 \mathrm{~F}_{1} \\
\left(\mathrm{~F}_{2}\right)_{\mathrm{x}}=200 \mathrm{~N} & \left(\mathrm{~F}_{2}\right)_{\mathrm{y}}=0 \\
- & \left(\mathrm{F}_{3}\right)_{\mathrm{y}}=260 \mathrm{a}{ }^{12} \mathrm{~b}=240 \mathrm{~N} \\
\left(\mathrm{~F}_{3}\right)_{\mathrm{x}}=260 \mathrm{a}{ }_{13}^{5} \mathrm{~b}=100 \mathrm{~N} &
\end{aligned}
$$

Resultant Force: Summing the force components algebraically along the $x$ and $y$ axes,

$$
\begin{aligned}
& \pm \odot\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=\odot \mathrm{F}_{\mathrm{x}} ;\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}}=0.5 \mathrm{~F}_{1}+200+100=0.5 \mathrm{~F}_{1}+300 \\
&+\mathrm{c} \odot\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}=0.8660 \mathrm{~F}_{1}-240
\end{aligned}
$$

The magnitude of the resultant force $\mathbf{F}_{R}$ is

$$
\begin{align*}
\mathrm{F}_{\mathrm{R}} & =2 \overline{\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{x}}^{2}+\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}^{2}} \\
& =2 \overline{\left(0.5 \mathrm{~F}_{1}+300\right)^{2}+\left(0.8660 \mathrm{~F}_{1}-240\right)^{2}} \\
& =2 \mathrm{~F}^{2}-115.69 \mathrm{~F}+147600 \tag{1}
\end{align*}
$$

Thus,

$$
\begin{equation*}
\mathrm{F}_{\mathrm{R}}^{2}=\mathrm{F}_{1}^{2}-115.69 \mathrm{~F}_{1}+147600 \tag{2}
\end{equation*}
$$

The first derivative of Eq. (2) is

$$
2 \mathrm{~F}_{\mathrm{R}} \frac{\mathrm{dF}_{\underline{\mathrm{R}}}}{\mathrm{dF}_{1}}=2 \mathrm{~F}_{1}-115.69
$$

For $\mathbf{F}_{R}$ to be minimum, $\frac{\mathrm{dF}_{\mathrm{R}}}{\mathrm{dF}}=0$. Thus, from Eq. (3)

$$
\begin{aligned}
& 2 \mathrm{~F}_{\mathrm{R}} \frac{\mathrm{dF}_{\mathrm{R}}}{\mathrm{dF}_{1}}=2 \mathrm{~F}_{1}-115.69=0 \\
& \mathrm{~F}_{1}=57.846 \mathrm{~N}=57.8 \mathrm{~N}
\end{aligned}
$$

from Eq. (1),
Ans.
(3)

$$
\mathrm{F}_{\mathrm{R}}=2(57.846)^{2}-115.69(57.846)+147600=380 \mathrm{~N}
$$


(a)

(b)

## Ans: <br> $\mathrm{F}_{1}=57.8 \mathrm{~N}$ <br> $\mathrm{F}_{\mathrm{R}}=380 \mathrm{~N}$

2-57.
Determine the magnitude of force $\mathbf{F}$ so that the resultant force of the three forces is as small as possible. What is the magnitude of the resultant force?

## SOLUTION

$$
\begin{align*}
\pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; \quad \mathrm{F}_{\mathrm{Rz}} & =8-\mathrm{F} \cos 45^{\circ}-14 \cos 30^{\circ} \\
& =-4.1244-\mathrm{F} \cos 45^{\circ} \\
+\mathrm{c} \mathrm{~F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad & \mathrm{F}_{\mathrm{Ry}}  \tag{1}\\
= & -\mathrm{F} \sin 45^{\circ}+14 \sin 30^{\circ} \\
& =7-\mathrm{F} \sin 45^{\circ} \\
\mathrm{F}_{\mathrm{R}}^{2} & =\left(-4.1244-\mathrm{F} \cos 45^{\circ}\right)^{2}+\left(7-\mathrm{F} \sin 45^{\circ}\right)^{2}
\end{align*}
$$



$$
\underline{\mathrm{dF}}_{\underline{\mathrm{R}}}
$$

$$
2 \mathrm{~F}_{\mathrm{R}} \mathrm{dF}=2\left(-4.1244-\mathrm{F} \cos 45^{\circ}\right)\left(-\cos 45^{\circ}\right)+2\left(7-\mathrm{F} \sin 45^{\circ}\right)\left(-\sin 45^{\circ}\right)=0
$$

$$
\mathrm{F}=2.03 \mathrm{kN}
$$

From Eq. (1);

$$
\mathrm{F}_{\mathrm{R}}=7.87 \mathrm{kN}
$$

Also, from the figure require

$$
\begin{array}{ll}
\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{x}_{i}}=0=\odot \mathrm{F}_{\mathrm{x} i} ; & \mathrm{F}+14 \sin 15^{\circ}-8 \cos 45^{\circ}=0 \\
& \mathrm{~F}=2.03 \mathrm{kN} \\
\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y} i}=\odot \mathrm{F}_{\mathrm{y} i} ; & \mathrm{F}_{\mathrm{R}}=14 \cos 15^{\circ}-8 \sin 45^{\circ} \\
& \mathrm{F}_{\mathrm{R}}=7.87 \mathrm{kN}
\end{array}
$$

Ans.
Ans.

Ans.

Ans.

Ans:
$F=2.03 \mathrm{kN}$
$F_{R}=7.87 \mathrm{kN}$

2-58.
Express $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ as Cartesian vectors.

## SOLUTION

$$
\begin{aligned}
\mathbf{F}_{1} & =-30 \sin 30^{\circ} \mathbf{i}-30 \cos 30^{\circ} \mathbf{j} \\
& =5-15.0 \mathbf{i}-26.0 \mathbf{j} 6 \mathrm{kN}
\end{aligned}
$$

$\mathbf{F}_{2}=-\frac{5}{13} 1262 \mathbf{i}+\frac{12}{13} 1262 \mathbf{j}$
$=\{-10.0 \mathbf{i}+24.0 \mathbf{j}\} \mathrm{kN}$


Ans.

Ans:
$\mathbf{F}_{1}=\{-15.0 \mathbf{i}-26.0 \mathbf{j}\} \mathrm{kN}$
$\mathbf{F}_{2}=\{-10.0 \mathrm{i}+24.0 \mathrm{j}\} \mathrm{kN}$

## 2-59.

Determine the magnitude of the resultant force and its direction measured counterclockwise from the positive $x$ axis.

## SOLUTION

$$
\begin{aligned}
& \pm \mathrm{F}_{\mathrm{Rx}}=\odot \mathrm{F}_{\mathrm{x}} ; \quad \mathrm{F}_{\mathrm{Rx}}=-30 \sin 30^{\circ}-{ }_{\underline{13}}^{5} 1262=-25 \mathrm{kN} \\
& +c \mathrm{~F}_{\mathrm{Ry}}=\odot \mathrm{F}_{\mathrm{y}} ; \quad \mathrm{F}_{\mathrm{Ry}}=-30 \cos 30^{\circ}+\frac{12}{13} 1262=-1.981 \mathrm{kN} \\
& \mathrm{~F}_{\mathrm{R}}=21-252^{2}+1-1.9812^{2}=25.1 \mathrm{kN} \\
& \mathbf{f}=\tan ^{-1} \mathrm{a} \frac{1.981}{25} \mathrm{~b}=4.53^{\circ} \\
& \mathrm{u}=180^{\circ}+4.53^{\circ}=185^{\circ}
\end{aligned}
$$



Ans.


[^1]*2-60. Determine the coordinate angleg for $\mathbf{F}_{2}$ and then express each force acting on the bracket as a Cartesian vector.


## Solution

Rectangular Components: Since $\cos ^{2} \mathrm{a}_{2}+\cos ^{2} \mathrm{~b}_{2}+\cos ^{2} \mathrm{~g}_{2}=1$, then $\cos g_{2 z}=\left\{21-\cos ^{2} 45-\cos ^{2} 60=\left\{0.5\right.\right.$. However, it is required $g_{2} 790$, thus, $\mathrm{g}_{2}=\cos ^{-1} 1-0.52-120$. By resolving $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ into their $x, y$, and $z$ components, as shown in Figs. $a$ and $b$, respectively $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be expressed in Cartesian vector form as
$\mathbf{F}_{1}=450 \cos 45 \sin 30(-\mathbf{i})+450 \cos 45 \cos 30(+\mathbf{j})+450 \sin 45(+\mathbf{k})$
$=5-159 \mathbf{i}+276 \mathbf{j}+318 \mathbf{k} 6 \mathrm{~N}$
Ans.
$\mathbf{F}_{2}=600 \cos 45 \mathbf{i}+600 \cos 60 \mathbf{j}+600 \cos 120 \mathbf{k}$
$=5424 \mathbf{i}+300 \mathbf{j}-300 \mathbf{k} 6 \mathrm{~N}$
Ans.

(a)

(b)

Ans:
$\mathbf{F}_{1}=5-159 \mathbf{i}+276 \mathbf{j}+318 \mathbf{k} 6 \mathrm{~N}$
$\mathbf{F}_{2}=5424 \mathbf{i}+300 \mathbf{j}-300 \mathbf{k} 6 \mathrm{~N}$

2-61. Determine the magnitude and coordinate direction angles of the resultant force acting on the bracket.

## Solution



Rectangular Components: Since $\cos ^{2} \mathrm{a}_{2}+\cos ^{2} \mathrm{~b}_{2}+\cos ^{2} \mathrm{~g}_{2}=1$, then $\cos g_{2 z}=\left\{21-\cos ^{2} 45-\cos ^{2} 60=\left\{0.5\right.\right.$. However, it is required $\mathrm{a}_{2} 790$, thus, $\mathrm{g}_{2}=\cos ^{-1} 1-0.52=120$. By resolving $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ into their $x, y$, and $z$ components, as shown in Figs. $a$ and $b$, respectively $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be expressed in Cartesian vector form, as
$\mathbf{F}_{1}=450 \cos 45 \sin 30(-\mathbf{i})+450 \cos 45 \cos 30(+\mathbf{j})+450 \sin 45(+\mathbf{k})$
$=\{-159.10 \mathbf{i}+275.57 \mathbf{j}+318.20 \mathbf{k} 6 \mathrm{~N}$
Ans.
$\mathbf{F}_{2}=600 \cos 45 \mathbf{i}+600 \cos 60 \mathbf{j}+600 \cos 120 \mathbf{k}$
$=5424 \mathbf{i}+300 \mathbf{j}-300 \mathbf{k}\} \mathrm{N}$
Ans.
Resultant Force: By adding $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ vectorally, we obtain $\mathbf{F}_{R}$.
$\mathbf{F}_{R}=\mathbf{F}_{1}+\mathbf{F}_{2}$

$$
=(-159.10 \mathbf{i}+275.57 \mathbf{j}+318.20 \mathbf{k})+(424.26 \mathbf{i}+300 \mathbf{j}-30 \mathbf{O O} \mathbf{k})
$$

$$
=5265.16 \mathbf{i}+575.57 \mathbf{j}+18.20 \mathbf{k} 6 \mathrm{~N}
$$

The magnitude of $\mathbf{F}_{R}$ is

$$
\begin{aligned}
F_{R} & =2 \underline{\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2}} \\
& =2265.16^{2}+575.57^{2}+18.20^{2}=633.97 \mathrm{~N}=634 \mathrm{~N}
\end{aligned}
$$

Ans.
The coordinate direction angles of $\mathbf{F}_{R}$ are
$\left.\mathrm{a}=\cos ^{-1}{ }_{\mathrm{c}}{ }_{F_{R}}^{F_{R}}\right)_{\mathrm{d}}{ }_{\mathrm{d}}=\cos ^{-1} \mathrm{a} \frac{265.16}{633.97} \mathrm{~b}=65.3$
Ans.
$\mathrm{b}=\cos ^{-1} \mathrm{c} \frac{\left(F_{R}\right)_{\mathrm{y}}}{F_{R}}{ }_{\mathrm{d}}=\cos ^{-1} \mathrm{a} \frac{575.57}{633.97} \mathrm{~b}=24.8$
Ans.
$\mathrm{g}=\cos ^{-1} \mathrm{c}{ }_{\mathrm{c}}^{\left(F_{R}\right)_{z_{\mathrm{d}}}} F_{R}=\cos ^{-1} \mathrm{a} \frac{18.20}{633.97} \mathrm{~b}=88.4$
Ans.

Ans:
$\mathbf{F}_{1}=\{-159.10 \mathbf{i}+275.57 \mathbf{j}+318.20 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{2}=\{424 \mathbf{i}+300 \mathbf{j}-300 \mathbf{k}\} \mathrm{N}$
$F_{R}=634 \mathrm{~N}$
$\mathrm{a}=65.3$
$\mathrm{b}=24.8$
$\mathrm{g}=88.4$

## 2-62.

Determine the magnitude and coordinate direction angles of the force $\mathbf{F}$ acting on the support. The component of $\mathbf{F}$ in the $x 9 y$ plane is 7 kN .

## Solution

Coordinate Direction Angles. The unit vector of $\mathbf{F}$ is

Thus,

$$
\begin{aligned}
\mathbf{u}_{F} & =\cos 30 \cos 40 \mathbf{i}-\cos 30 \sin 40 \mathbf{j}+\sin 30 \mathbf{k} \\
& =\{0.6634 \mathbf{i}-0.5567 \mathbf{j}+0.5 \mathbf{k}\}
\end{aligned}
$$

$$
\begin{array}{ll}
\cos \mathrm{a}=0.6634 ; & \mathrm{a}=48.44=48.4 \\
\cos \mathrm{~b}=-0.5567 ; & \mathrm{b}=123.83=124 \\
\cos \mathrm{~g}=0.5 ; & \mathrm{g}=60
\end{array}
$$

Ans.
Ans.
Ans.
The magnitude of $\mathbf{F}$ can be determined from

$$
F \cos 30=7 ; \quad F=8.083 \mathrm{kN}=8.08 \mathrm{kN}
$$

Ans.


Ans:
a $=48.4$
b $=124 \mathrm{~g}$
$=60$
$F=8.08 \mathrm{kN}$

## 2-63.

The bolt is subjected to the force $\mathbf{F}$, which has components acting along the $x, y, z$ axes as shown. If the magnitude of $\mathbf{F}$ is 80 N , and $\mathrm{a}=60^{\circ}$ and $\mathrm{g}=45^{\circ}$, determine the magnitudes of its components.

## SOLUTION

$$
\begin{aligned}
\cos \mathrm{b} & =21-\cos ^{2} \mathrm{a}-\cos ^{2} \mathrm{~g} \\
& =2 \overline{1-\cos ^{2} 60^{\circ}-\cos ^{2} 45^{\circ}} \\
\mathrm{b} & =120^{\circ} \\
\mathrm{F}_{\mathrm{x}} & =\left|80 \cos 60^{\circ}\right|=40 \mathrm{~N} \\
\mathrm{~F}_{\mathrm{y}} & =\left|80 \cos 120^{\circ}\right|=40 \mathrm{~N} \\
\mathrm{~F}_{\mathrm{z}} & =\left|80 \cos 45^{\circ}\right|=56.6 \mathrm{~N}
\end{aligned}
$$



Ans.
Ans.
Ans.

## Ans:

$F_{x}=40 \mathrm{~N}$
$F_{y}=40 \mathrm{~N}$
$F_{z}=56.6 \mathrm{~N}$
*2-64.
The stock mounted on the lathe is subjected to a force of 60 N . Determine the coordinate direction angle b and express the force as a Cartesian vector.

## SOLUTION

$$
\begin{aligned}
& 1=2 \cos ^{2} \mathrm{a}+\cos ^{2} \mathrm{~b}+\cos ^{2} \mathrm{~g} \\
& 1=\cos ^{2} 60^{\circ}+\cos ^{2} \mathrm{~b}+\cos ^{2} 45^{\circ} \\
& \cos \mathrm{b}=; 0.5 \\
& \quad \mathrm{~b}=60^{\circ}, 120^{\circ}
\end{aligned}
$$

Use

$$
\mathrm{b}=120^{\circ}
$$

$$
\begin{aligned}
\mathrm{F} & =60 \mathrm{~N}\left(\cos 60^{\circ} \mathbf{i}+\cos 120^{\circ} \mathbf{j}+\cos 45^{\circ} \mathbf{k}\right) \\
& =\{30 \mathbf{i}-30 \mathbf{j}+42.4 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$



Ans.

## Ans.

## Ans:

b $=120^{\circ}$

2-65. Specify the magnitude $F_{3}$ and directions $\mathrm{a}_{3}, \mathrm{~b}_{3}$, and $\mathrm{g}_{3}$ of $\mathbf{F}_{3}$ so that the resultant force of the three forces is $\mathbf{F}_{R}=\{9 \mathbf{j}\} \mathrm{kN}$.

## SOLUTION

Initial Guesses:

$$
F_{3 x} \quad 1
$$

$$
F_{3 y} \quad 1 \mathrm{kN}
$$


kN



Ans.
$\qquad$
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$$
\begin{aligned}
\mathrm{F}_{3} & =9.6 \mathrm{kN} \\
\mathrm{a}_{3} & =15.5 \\
\mathrm{~b}_{3} & =98.4 \\
\mathrm{~g}_{3} & =77.0
\end{aligned}
$$

## 2-66.

Determine the magnitude and coordinate direction angles of the resultant force, and sketch this vector on the coordinate system.

## Solution



Cartesian Vector Notation. For $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$,
$\mathbf{F}_{1}=400(\cos 45 \mathbf{i}+\cos 60 \mathbf{j}-\cos 60 \mathbf{k})=\{282.84 \mathbf{i}+200 \mathbf{j}-200 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{2}=125 \mathrm{c} \frac{4}{5}(\cos 20) \mathbf{i}-\frac{4}{5}(\sin 20) \mathbf{j}+\frac{3}{5} \mathbf{k} d=\{93.97 \mathbf{i}-34.20 \mathbf{j}+75.0 \mathbf{k}\}$

## Resultant Force.

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2} \\
& =\{282.84 \mathbf{i}+200 \mathbf{j}-200 \mathbf{k}\}+\{93.97 \mathbf{i}-34.20 \mathbf{j}+75.0 \mathbf{k}\} \\
& =\{376.81 \mathbf{i}+165.80 \mathbf{j}-125.00 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
F_{R}=2\left(F_{R}\right)^{2},\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2} & =2376.81^{2}+165.80^{2}+(125.00)^{2} \\
& =430.23 \mathrm{~N}=430 \mathrm{~N}
\end{aligned}
$$



The coordinate direction angles are

$$
\begin{aligned}
& \cos \mathrm{a}=\begin{array}{l}
\left(F_{R}\right)_{x}=376.81 \\
F_{R}=430.23
\end{array}, \quad \mathrm{a}=28.86=28.9 \\
& \cos \mathrm{~b}=\begin{array}{l}
\left(F_{R}\right)_{y}=165.80 \\
-F_{R}=\underline{430.23} ;
\end{array} \quad \mathrm{b}=67.33=67.3 \\
& \cos \mathrm{~g}=\begin{array}{l}
\left(F_{\underline{R}}\right)_{\underline{z}}=\underline{-125.00} \\
F_{R}=430.23 ;
\end{array} \quad \mathrm{g}=106.89=107
\end{aligned}
$$

Ans.

Ans.

Ans.

Ans:
$F_{R}=430 \mathrm{~N}$
$\mathrm{a}=28.9$
$\mathrm{b}=67.3$
$\mathrm{g}=107$

## 2-67.

Determine the magnitude and coordinate direction angles of the resultant force, and sketch this vector on the coordinate system.


## Solution

Cartesian Vector Notation. For $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$,

$$
\begin{aligned}
& \mathbf{F}_{1}=450 a_{5}^{3} \mathbf{j}-{ }_{5}^{4} \mathbf{k} b=\{270 \mathbf{j}-360 \mathbf{k}\} \mathbf{N} \\
& \mathbf{F}_{2}=525(\cos 45 \mathbf{i}+\cos 120 \mathbf{j}+\cos 60 \mathbf{k})=\{371.23 \mathbf{i}-262.5 \mathbf{j}+262.5 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

## Resultant Force.

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2} \\
& =\{270 \mathbf{j}-360 \mathbf{k}\}+\{371.23 \mathbf{i}-262.5 \mathbf{j}+262.5 \mathbf{k}\} \\
& =\{371.23 \mathbf{i}+7.50 \mathbf{j}-97.5 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
F_{R}=2 \underline{\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2}} & =2 \underline{371.23^{2}+7.50^{2}+(-97.5)^{2}} \\
& =383.89 \mathrm{~N}=384 \mathrm{~N}
\end{aligned}
$$



The coordinate direction angles are

$$
\begin{array}{ll}
\cos \mathrm{a}= & \left(F_{R}\right)_{x}=\frac{371.23}{F_{R}} ; \frac{383.89}{\left(F_{R}\right)_{y}}=3.50 \\
\cos \mathrm{~b}= & \mathrm{a}=14.76=14.8 \\
\frac{F_{R}}{383.89} ; & \mathrm{b}=88.88=88.9 \\
\cos \mathrm{~g}=\frac{\left(F_{R}\right)^{2}}{F_{R}}=\frac{-97.5}{383.89} ; & \mathrm{g}=104.71=105
\end{array}
$$

Ans.

Ans.

Ans.

Ans:

$$
\begin{aligned}
F_{R} & =384 \mathrm{~N} \\
\cos \mathrm{a} & =\frac{371.23}{383.89} ; \mathrm{a}=14.8 \\
\cos \mathrm{~b} & =\begin{array}{l}
7.50 \\
383.89
\end{array} \mathrm{~b}=88.9 \\
\cos \mathrm{~g} & =\frac{-97.5}{383.89} ; \mathrm{g}=105
\end{aligned}
$$

*2-68. Determine the magnitude and coordinate direction angles of $\mathbf{F}_{3}$ so that the resultant of the three forces acts along the positive $y$ axis and has a magnitude of 600 N .

## SOLUTION

## Given:

| $F$ | 600 N |
| :--- | :--- |
| $F_{1}$ | 180 N |
| $F_{2}$ | 300 N |
| 1 | 30 |
| 2 | 40 |

Initial guesses:

| 40 |  | 50 |
| :---: | :---: | :---: |
| 50 | $F_{3}$ | 45 N |

Given

$$
\begin{array}{lllllllll}
F_{R x}= & F_{x} ; & 0 & F_{1} & F_{2} \cos & 1 & \sin & 2 & F_{3} \cos \\
F_{R y}= & F_{y} ; & F & F_{2} \cos & 1 & \cos & 2 & F_{3} \cos \\
F_{R z} & = & F_{z} ; & 0 & F_{2} \sin & 1 & F_{3} \cos & \\
& & \cos & 2 & \cos & 2 & \cos & 2 & 1
\end{array}
$$

Find $F_{3} \quad F_{3} \quad 428 \mathrm{~N} \quad 20.6 \mathrm{deg}$

## Ans:

$F_{3}=428 \mathrm{~N}$
$\mathrm{a}=88.3$
$\mathrm{b}=20.6$
$\mathrm{g}=69.5$

2-69. Determine the magnitude and coordinate direction angles of $\mathbf{F}_{3}$ so that the resultant of the three forces is zero.

## SOLUTION

Given:

| $F_{1}$ | 180 N | 1 | 30 |
| :--- | :--- | :--- | :--- |
| $F_{2}$ | 300 N | 2 | 40 |

Initial
guesses: $40 \quad 50$ $50 \quad F_{3} \quad 45 \mathrm{~N}$

Given

$$
F_{R x}=F_{x} ; \quad 0 \quad F_{1} \quad F_{2} \cos \quad 1 \sin \quad 2 \quad F_{3} \cos
$$

$$
F_{R y}=F_{y} ; \quad 0 \quad F_{2} \cos \quad 1 \cos \quad 2 \quad F_{3} \cos
$$

$F_{R z}=F_{z} ; \quad 0 \quad F_{2} \sin \quad 1 \quad F_{3} \cos$

$$
\cos \quad 2 \quad \cos \quad 2 \quad \cos \quad 2 \quad 1
$$

$F_{3}$
Find $F_{3} \quad F_{3} \quad 250 \mathrm{~N} \quad 142.9 \mathrm{deg}$ Ans.
53.1

Ans:
$\mathrm{F}_{3}=250 \mathrm{~N}$
$\mathrm{a}=87.0$
b $=142.9$
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$$
\mathrm{g}=53.1
$$

2-70.
The screw eye is subjected to the two forces shown. Express each force in Cartesian vector form and then determine the resultant force. Find the magnitude and coordinate direction angles of the resultant force.

## SOLUTION

$$
\begin{aligned}
\mathbf{F}_{1} & =300\left(-\cos 60^{\circ} \sin 45^{\circ} \mathbf{i}+\cos 60^{\circ} \cos 45^{\circ} \mathbf{j}+\sin 60^{\circ} \mathbf{k}\right) \\
& =\{-106.07 \mathbf{i}+106.07 \mathbf{j}+259.81 \mathbf{k}\} \mathrm{N} \\
& =\{-106 \mathbf{i}+106 \mathbf{j}+260 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

$\mathbf{F}_{2}=500\left(\cos 60^{\circ} \mathbf{i}+\cos 45^{\circ} \mathbf{j}+\cos 120^{\circ} \mathbf{k}\right)$
$=\{250.0 \mathbf{i}+353.55 \mathbf{j}-250.0 \mathbf{k}\} \mathrm{N}$
$=\{250 \mathbf{i}+354 \mathbf{j}-250 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{1}+\mathbf{F}_{2}$
$=-106.07 \mathbf{i}+106.07 \mathbf{j}+259.81 \mathbf{k}+250.0 \mathbf{i}+353.55 \mathbf{j}-250.0 \mathbf{k}$
$=143.93 \mathbf{i}+459.62 \mathbf{j}+9.81 \mathbf{k}$
$=\{144 \mathbf{i}+460 \mathbf{j}+9.81 \mathbf{k}\} \mathrm{N}$
$\mathrm{F}_{\mathrm{R}}=2143.93^{2}+459.62^{2}+9.81^{2}=481.73 \mathrm{~N}=482 \mathrm{~N}$
$\mathbf{u}_{\mathrm{F}_{\mathrm{R}}}=\frac{\mathbf{F}_{\mathrm{R}}}{\mathrm{F}_{\mathrm{R}}}=\frac{143.93 \mathbf{i}+459.62 \mathbf{j}+9.81 \mathbf{k}}{481.73}=0.2988 \mathbf{i}+0.9541 \mathbf{j}+0.02036 \mathbf{k}$
$\cos \mathrm{a}=0.2988$
$\mathrm{a}=72.6^{\circ}$
$\cos \mathrm{b}=0.9541$
$\mathrm{b}=17.4^{\circ}$
$\cos g=0.02036$
$\mathrm{g}=88.8^{\circ}$


Ans.

Ans.

Ans.
Ans.

Ans.
Ans.
Ans.

Ans:
$\mathbf{F}_{1}=\{-106 \mathbf{i}+106 \mathbf{j}+260 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{2}=\{250 \mathbf{i}+354 \mathbf{j}-250 \mathbf{k}\} \mathbf{N}$
$\mathbf{F}_{R}=\{144 \mathbf{i}+460 \mathbf{j}+9.81 \mathbf{k}\} \mathbf{N}$
$F_{R}=482 \mathrm{~N}$
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$\mathrm{a}=72.6$
$b=17.4$
$\mathrm{g}=88.8$

2-71.
Determine the coordinate direction angles of $\mathbf{F}_{1}$.

## SOLUTION

$$
\begin{aligned}
\mathbf{F}_{1} & =300\left(-\cos 60^{\circ} \sin 45^{\circ} \mathbf{i}+\cos 60^{\circ} \cos 45^{\circ} \mathbf{j}+\sin 60^{\circ} \mathbf{k}\right) \\
& =\{-106.07 \mathbf{i}+106.07 \mathbf{j}+259.81 \mathbf{k}\} \mathrm{N} \\
& =\{-106 \mathbf{i}+106 \mathbf{j}+260 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

$\mathbf{u}_{1}=\frac{\mathbf{F}_{1}}{300}=-0.3536 \mathbf{i}+0.3536 \mathbf{j}+0.8660 \mathbf{k}$
$\mathrm{a}_{1}=\cos ^{-1}(-0.3536)=111^{\circ}$
$\mathrm{b}_{1}=\cos ^{-1}(0.3536)=69.3^{\circ}$
$\mathrm{g}_{1}=\cos ^{-1}(0.8660)=30.0^{\circ}$


Ans.
Ans.
Ans.

Ans:
$\mathrm{a}_{1}=111$
$\mathrm{b}_{1}=69.3$
$g_{1}=30.0$
*2-72.
Determine the magnitude and coordinate direction angles of the resultant force, and sketch this vector on the coordinate system.

## Solution



Cartesian Vector Notation. For $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$,
$\mathbf{F}_{1}=400(\sin 60 \cos 20 \mathbf{i}-\sin 60 \sin 20 \mathbf{j}+\cos 60 \mathbf{k})$

$$
=\{325.52 \mathbf{i}-118.48 \mathbf{j}+200 \mathbf{k}\} \mathbf{N}
$$

$\mathbf{F}_{2}=500(\cos 60 \mathbf{i}+\cos 60 \mathbf{j}+\cos 135 \mathbf{k})$

$$
=\{250 \mathbf{i}+250 \mathbf{j}-353.55 \mathbf{k}\} \mathbf{N}
$$

## Resultant Force.

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2} \\
& =(325.52 \mathbf{i}-118.48 \mathbf{j}+200 \mathbf{k})+(250 \mathbf{i}+250 \mathbf{j}-353.55 \mathbf{k}) \\
& =\{575.52 \mathbf{i}+131.52 \mathbf{j}-153.55 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
F_{R}=2\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2} & =2575.52^{2}+131.52^{2}+(-153.55)^{2} \\
& =610.00 \mathrm{~N}=610 \mathrm{~N}
\end{aligned}
$$



$$
\text { Ans. } \quad F_{R}=610 \mathrm{~N}
$$

The coordinate direction angles are

$$
\begin{array}{ll}
\left.\cos \mathrm{a}=\begin{array}{l}
\left(F_{R}\right)_{x}=575.52 \\
F_{R}
\end{array}\right) & \mathrm{a}=19.36=19.4 \\
\cos \mathrm{~b}=\begin{array}{c}
\left(F_{R}\right)_{y} \\
F_{R}=131.52 \\
610.00
\end{array} & \mathrm{~b}=77.549=77.5 \\
\cos \mathrm{~g}=\begin{array}{c}
\left(F_{R}\right) \bar{z} \\
F_{R}
\end{array}=\begin{array}{l}
-153.55 \\
610.00
\end{array} & \mathrm{~g}=104.58=105
\end{array}
$$

Ans.

Ans.

Ans.

## Ans:

$F_{R}=610 \mathrm{~N}$
$\mathrm{a}=19.4$
$\mathrm{b}=77.5$
$\mathrm{g}=105$

2-73.
Determine the coordinate direction angles of force $\mathbf{F}_{1}$.

## SOLUTION

Rectangular Components: By referring to Figs. $a$, the $x, y$, and $z$ components of $\mathbf{F}_{1}$ can be written as
$\left(F_{1}\right)_{x}=600 a_{5}^{4} b \cos 30^{\circ} N$
$\left(F_{1}\right)_{y}=600 a_{5}^{4} b \sin 30^{\circ} N$
$\left(F_{1}\right)_{z}=600 a_{5}^{3} b N$

Thus, $\mathbf{F}_{1}$ expressed in Cartesian vector form can be written as

$$
\begin{aligned}
\mathbf{F}_{1} & =600 e^{\frac{4}{5}} \cos 30^{\circ}(+\mathbf{i})+\frac{4}{5} \sin 30^{\circ}(-\mathbf{j})+\frac{3}{5}(+\mathbf{k}) f \mathrm{~N} \\
& =600[0.6928 \mathbf{i}-0.4 \mathbf{j}+0.6 \mathbf{k}] \mathrm{N}
\end{aligned}
$$

Therefore, the unit vector for $\mathbf{F}_{1}$ is given by

$$
\mathbf{u}_{\mathrm{F}_{1}}=\frac{\mathbf{F}_{1}}{\mathrm{~F}_{1}}=\frac{600(0.6928 \mathbf{i}-0.4 \mathbf{j}+0.6 \mathbf{k}}{600}=0.6928 \mathbf{i}-0.4 \mathbf{j}+0.6 \mathbf{k}
$$

The coordinate direction angles of $\mathbf{F}_{1}$ are


$$
\begin{aligned}
& \mathrm{a}=\cos ^{-1}\left(\mathrm{u}_{\mathrm{F}_{1}}\right)_{\mathrm{x}}=\cos ^{-1}(0.6928)=46.1^{\circ} \\
& \mathrm{b}=\cos ^{-1}\left(\mathrm{u}_{\mathrm{F}_{1}}\right)_{\mathrm{y}}=\cos ^{-1}(-0.4)=114^{\circ} \\
& \mathrm{g}=\cos ^{-1}\left(\mathrm{u}_{\mathrm{F}_{1}}\right)_{\mathrm{z}}=\cos ^{-1}(0.6)=53.1^{\circ}
\end{aligned}
$$

Ans.
(a)

Ans.
Ans.

Ans:
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$$
\begin{aligned}
& a=46.1 \\
& b=114 g \\
& =53.1
\end{aligned}
$$

## 2-74.

Determine the magnitude and coordinate direction angles of the resultant force acting on the eyebolt.

## SOLUTION

Force Vectors: By resolving $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ into their $x, y$, and $z$ components, as shown in Figs. $a$ and $b$, respectively, they are expressed in Cartesian vector form as
$\mathbf{F}_{1}=600 \mathrm{a}_{5}^{4} \mathrm{~b} \cos 30^{\circ}(+\mathbf{i})+600 \mathrm{a} \frac{4}{5} \mathrm{~b} \sin 30^{\circ}(-\mathbf{j})+600 \mathrm{a}{ }_{5}^{3} \mathrm{~b}(+\mathbf{k})$

$$
=5415.69 \mathbf{i}-240 \mathbf{j}+360 \mathbf{k} 6 \mathrm{~N}
$$

$\mathbf{F}_{2}=0 \mathbf{i}+450 \cos 45^{\circ}(+\mathbf{j})+450 \sin 45^{\circ}(+\mathbf{k})$

$$
=5318.20 \mathbf{j}+318.20 \mathbf{k} 6 \mathrm{~N}
$$

Resultant Force: The resultant force acting on the eyebolt can be obtained by vectorally adding $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$. Thus,

$$
\begin{aligned}
\mathbf{F}_{\mathrm{R}} & =\mathbf{F}_{1}+\mathbf{F}_{2} \\
& =(415.69 \mathbf{i}-240 \mathbf{j}+360 \mathbf{k})+(318.20 \mathbf{j}+318.20 \mathbf{k}) \\
& =5415.69 \mathbf{i}+78.20 \mathbf{j}+678.20 \mathbf{k} 6 \mathbf{N}
\end{aligned}
$$


(a)

The magnitude of $\mathbf{F}_{\mathrm{R}}$ is given by

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =3\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{x}}^{2}+\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}^{2}+\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{z}}^{2} \\
& =3(415.69)^{2}+(78.20)^{2}+(678.20)^{2}=799.29 \mathrm{~N}=799 \mathrm{~N}
\end{aligned}
$$

The coordinate direction angles of $\mathbf{F}_{\mathrm{R}}$ are

$$
\begin{gathered}
\underline{\left(\mathrm{F}_{\underline{R}}\right)_{\underline{\mathrm{x}}}} \underline{\underline{415.69}} \\
\mathrm{a}=\cos ^{-1} \mathrm{c} \mathrm{~F}_{\mathrm{R}} \mathrm{~d}=\cos ^{-1} \mathrm{a}{ }_{799.29} \mathrm{~b}=58.7^{\circ} \\
\mathrm{b}=\cos ^{-1} \mathrm{c} \frac{\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{y}}}{\mathrm{~F}_{\mathrm{R}}} \mathrm{~d}=\cos ^{-1} \mathrm{a} \frac{78.20}{799.29} \mathrm{~b}=84.4^{\circ} \\
\underline{\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{z}}} \quad \underline{\underline{678.20}}
\end{gathered}
$$

Ans.

Ans.

$$
g=\cos ^{-1} c F_{R}^{d=\cos ^{-1} a_{799.29} b=32.0^{\circ}}
$$

Ans.

(b)

Ans:
$F_{R}=799 \mathrm{~N}$
$\mathrm{a}=58.7$
b -844
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$\mathrm{g}=32.0$

## 2-75.

Express each force in Cartesian vector form.

## Solution

Cartesian Vector Notation. For $\mathbf{F}_{1}, \mathbf{F}_{2}$ and $\mathbf{F}_{3}$,

$$
\begin{aligned}
\mathbf{F}_{1} & =90 \mathrm{a}_{5}^{4} \mathbf{i}+\frac{3}{5} \mathbf{k} b=\{72.0 \mathbf{i}+54.0 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{2} & =150(\cos 60 \sin 45 \mathbf{i}+\cos 60 \cos 45 \mathbf{j}+\sin 60 \mathbf{k}) \\
& =\{53.03 \mathbf{i}+53.03 \mathbf{j}+129.90 \mathbf{k}\} \mathbf{N} \\
& =\{53.0 \mathbf{i}+53.0 \mathbf{j}+130 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{3} & =\{200 \mathbf{k}\}
\end{aligned}
$$



Ans.

Ans.
Ans.

Ans:
$\mathbf{F}_{1}=\{72.0 \mathbf{i}+54.0 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{2}=\{53.0 \mathbf{i}+53.0 \mathbf{j}+130 \mathbf{k}\} \mathbf{N}$
$\mathbf{F}_{3}=\{200 \mathbf{k}\}$
*2-76.
Determine the magnitude and coordinate direction angles of the resultant force, and sketch this vector on the coordinate system.

## Solution

Cartesian Vector Notation. For $\mathbf{F}_{1}, \mathbf{F}_{2}$ and $\mathbf{F}_{3}$,
$\mathbf{F}_{1}=90 \mathrm{a}_{5}^{4} \mathbf{i}+{ }_{5}^{3} \mathbf{k b}=\{72.0 \mathbf{i}+54.0 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{2}=150(\cos 60 \sin 45 \mathbf{i}+\cos 60 \cos 45 \mathbf{j}+\sin 60 \mathbf{k})$

$$
=\{53.03 \mathbf{i}+53.03 \mathbf{j}+129.90 \mathbf{k}\} \mathrm{N}
$$

$\mathbf{F}_{3}=\{200 \mathrm{k}\} \mathrm{N}$

## Resultant Force.

$$
\begin{aligned}
\mathbf{F} & =\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3} \\
& =(72.0 \mathbf{i}+54.0 \mathbf{k})+(53.03 \mathbf{i}+53.03 \mathbf{j}+129.90 \mathbf{k})+(200 \mathbf{k}) \\
& =\{125.03 \mathbf{i}+53.03 \mathbf{j}+383.90\} \mathbf{N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
F_{R}=2 \underline{\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2}} & =2 \underline{125.03^{2}+53.03^{2}+383.90^{2}} \\
& =407.22 \mathrm{~N}=407 \mathrm{~N}
\end{aligned}
$$

And the coordinate direction angles are

$$
\begin{array}{ll}
\cos \mathrm{a}= & \left(F_{R}\right)_{x}=125.03 \\
\frac{F_{R}}{\left(F_{R}\right)_{y}}=\underline{407.22} ; & \mathrm{a}=72.12=72.1 \\
\cos \mathrm{~b}= & \begin{array}{l}
\frac{53.03}{F_{R}} ; \\
\frac{407.22}{\left(F_{R}\right)_{z}}=\frac{383.90}{38}
\end{array} \\
\cos \mathrm{~g}=82.52=82.5 \\
F_{R}=\underline{407.22} ; & \mathrm{g}=19.48=19.5
\end{array}
$$



Ans.

Ans.

Ans.

## Ans:

$F_{R}=407 \mathrm{~N}$
$\mathrm{a}=72.1$
$\mathrm{b}=82.5$
$\mathrm{g}=19.5$

2-77.
The cables attached to the screw eye are subjected to the three forces shown. Express each force in Cartesian vector form and determine the magnitude and coordinate direction angles of the resultant force.

## SOLUTION

## Cartesian Vector Notation:

$$
\begin{aligned}
\mathbf{F}_{1} & =3505 \sin 40^{\circ} \mathbf{j}+\cos 40^{\circ} \mathbf{k} 6 \mathrm{~N} \\
& =5224.98 \mathbf{j}+268.12 \mathbf{k} 6 \mathrm{~N} \\
& =5225 \mathbf{j}+268 \mathbf{k} 6 \mathrm{~N}
\end{aligned}
$$

Ans.
$\mathbf{F}_{2}=1005 \cos 45^{\circ} \mathbf{i}+\cos 60^{\circ} \mathbf{j}+\cos 120^{\circ} \mathbf{k} 6 \mathrm{~N}$
$=570.71 \mathbf{i}+50.0 \mathbf{j}-50.0 \mathbf{k} 6 \mathrm{~N}$
$=570.7 \mathbf{i}+50.0 \mathbf{j}-50.0 \mathbf{k} 6 \mathrm{~N}$
$\mathbf{F}_{3}=2505 \cos 60^{\circ} \mathbf{i}+\cos 135^{\circ} \mathbf{j}+\cos 60^{\circ} \mathbf{k} 6 \mathrm{~N}$
$=5125.0 \mathbf{i}-176.78 \mathbf{j}+125.0 \mathbf{k} 6 \mathrm{~N}$
$=5125 \mathbf{i}-177 \mathbf{j}+125 \mathbf{k} 6 \mathrm{~N}$
Ans.

Ans.


## Resultant Force:

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3} \\
& =5170.71+125.02 \mathbf{i}+1224.98+50.0-176.782 \mathbf{j}+1268.12-50.0+125.02 \mathbf{k} 6 \mathrm{~N} \\
& =5195.71 \mathbf{i}+98.20 \mathbf{j}+343.12 \mathbf{k} 6 \mathrm{~N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =2 \overline{\mathrm{~F}_{\mathrm{R}_{\mathrm{x}}}^{2}+\mathrm{F}_{\mathrm{R}_{\mathrm{y}}}^{2}+\mathrm{F}_{\mathrm{R}_{z}}^{2}} \\
& =2 \overline{195.71^{2}+98.20^{2}+343.12^{2}} \\
& =407.03 \mathrm{~N}=407 \mathrm{~N}
\end{aligned}
$$

Ans.

The coordinate direction angles are

$$
\begin{array}{lll}
\cos \mathrm{a}=\frac{\mathrm{F}_{\mathrm{R}_{\mathrm{x}}}}{\mathrm{~F}_{\mathrm{R}}}=\frac{195.71}{407.03} & \mathrm{a}=61.3^{\circ} & \text { Ans. } \\
\cos \mathrm{b}=\frac{\mathrm{F}_{\mathrm{R}_{\mathrm{y}}}}{\mathrm{~F}_{\mathrm{R}}}=\frac{98.20}{407.03} & \mathrm{~b}=76.0^{\circ} & \text { Ans. } \\
\underline{\mathrm{F}_{\underline{\mathrm{R}}}} \underline{ } \underline{343.12} & & \\
\cos \mathrm{~g}= & & \\
\mathrm{F}_{\mathrm{R}}=407.03 & \mathrm{~g}=32.5^{\circ} & \text { Ans. } \\
& & \mathbf{F}_{1}=\{225 \mathbf{j}+268 \mathbf{k}\} \mathrm{N} \\
& & \mathbf{F}_{2}=\{70.7 \mathbf{i}+50.0 \mathbf{j}-50.0 \mathbf{k}\} \mathrm{N} \\
& & \mathbf{F}_{3}=\{125 \mathbf{i}-177 \mathbf{j}+125 \mathbf{k}\} \mathrm{N} \\
& & F_{R}=407 \mathrm{~N} \\
& \mathrm{a}=61.3 \\
& & \mathrm{~b}=76.0
\end{array}
$$

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$$
\mathrm{g}=32.5
$$

2-78. The mast is subjected to the three forces shown. Determine the coordinate direction angles $\mathrm{a}_{1}, \mathrm{~b}_{1}, \mathrm{~g}_{1}$ of $\mathbf{F}_{1}$ so that the resultant force acting on the mast is $\mathbf{F}_{\mathrm{R}}=5350 \mathrm{i} 6 \mathrm{~N}$.

## Solution

$\mathbf{F}_{1}=500 \cos \mathrm{a}_{1} \mathbf{i}+500 \cos \mathrm{~b}_{1} \mathbf{j}+500 \cos \mathrm{~g}_{1} \mathbf{k}$
$\mathbf{F}_{R}=\mathbf{F}_{1}+(-300 \mathbf{j})+(-200 \mathbf{k})$
$350 \mathbf{i}=500 \operatorname{cosa}_{1} \mathbf{i}+\left(500 \operatorname{cosb}_{1}-300\right) \mathbf{j}+\left(500 \operatorname{cosg}_{1}-2 \mathrm{OO}\right) \mathbf{k}$
$350=500 \cos \mathrm{a}_{1} ;$
$\mathrm{a}_{1}=45.6$
$0=500 \cos \mathrm{~b}_{1}-300$;
$\mathrm{b}_{1}=53.1$
$0=500 \cos \mathrm{~g}_{1}-200 ;$
$g_{1}=66.4$

Ans.
Ans.
Ans.

ns.

Ans:
$\mathrm{a}_{1}=45.6$
$\mathrm{b}_{1}=53.1$
$\mathrm{g}_{1}=66.4$

## 2-79. The mast is subjected to the three forces shown.

Determine the coordinate direction angles $\mathrm{a}_{1}, \mathrm{~b}_{1}, \mathrm{~g}_{1}$ of $\mathbf{F}_{1}$ so that the resultant force acting on the mast is zero.

## Solution

$\mathbf{F}_{1}=5500 \cos \mathrm{a}_{1} \mathbf{i}+500 \cos \mathrm{~b}_{1} \mathbf{j}+500 \cos \mathrm{~g}_{1} \mathbf{k} 6 \mathrm{~N}$
$\mathbf{F}_{2}=5-200 \mathrm{k} 6 \mathrm{~N}$
$\mathbf{F}_{3}=5-300 \mathbf{j} 6 \mathrm{~N}$
$\mathbf{F}_{R}=\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3}=0$
$500 \cos \mathrm{a}_{1}=0 ; \quad \mathrm{a}_{1}=90$
$500 \cos \mathrm{~b}_{1}=300 ; \quad \mathrm{b}_{1}=53.1$
$500 \cos g_{1}=200 ; \quad g_{1}=66.4$


Ans.
Ans.
Ans.

Ans:
$\mathrm{a}_{1}=90$
$\mathrm{b}_{1}=53.1$
$\mathrm{g}_{1}=66.4$

## *2-80.

Express each force as a Cartesian vector.

## SOLUTION

Rectangular Components: By referring to Figs. $a$ and $b$, the $x, y$, and $z$ components of $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be written as

$$
\begin{array}{ll}
\left(\mathrm{F}_{1}\right)_{\mathrm{x}}=300 \cos 30^{\circ}=259.8 \mathrm{~N} & \left(\mathrm{~F}_{2}\right)_{\mathrm{x}}=500 \cos 45^{\circ} \sin 30^{\circ}=176.78 \mathrm{~N} \\
\left(\mathrm{~F}_{1}\right)_{\mathrm{y}}=0 & \left(\mathrm{~F}_{2}\right)_{\mathrm{y}}=500 \cos 45^{\circ} \cos 30^{\circ}=306.19 \mathrm{~N} \\
\left(\mathrm{~F}_{1}\right)_{\mathrm{t}}=300 \sin 30^{\circ}=150 \mathrm{~N} & \left(\mathrm{~F}_{2}\right)_{\mathrm{z}}=500 \sin 45^{\circ}=353.55 \mathrm{~N}
\end{array}
$$

Thus, $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be written in Cartesian vector form as

$$
\begin{aligned}
\mathbf{F}_{1} & =259.81(+\mathbf{i})+0 \mathbf{j}+150(-\mathbf{k}) \\
& =\{260 \mathbf{i}-150 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{2} & =176.78(+\mathbf{i})+306.19(+\mathbf{j})+353.55(-\mathbf{k}) \\
& =2\{177 \mathbf{i}+306 \mathbf{j}-354 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

Ans.

Ans.

(b)

$$
\begin{aligned}
& \text { Ans: } \\
& \mathbf{F}_{1}=\{260 \mathbf{i}-150 \mathbf{k}\} \mathbf{N} \\
& \mathbf{F}_{2}=2\{177 \mathbf{i}+306 \mathbf{j}-354 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

## 2-81.

Determine the magnitude and coordinate direction angles of the resultant force acting on the hook.

## SOLUTION

Force Vectors: By resolving $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ into their $x, y$, and $z$ components, as shown in Figs. $a$ and $b$, respectively, $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ can be expessed in Cartesian vector form as

$$
\begin{aligned}
\mathbf{F}_{1} & =300 \cos 30^{\circ}(+\mathbf{i})+0 \mathbf{j}+300 \sin 30^{\circ}(-\mathbf{k}) \\
& =\{259.81 \mathbf{i}-150 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

$\mathbf{F}_{2}=500 \cos 45^{\circ} \sin 30^{\circ}(+\mathbf{i})+500 \cos 45^{\circ} \cos 30^{\circ}(+\mathbf{j})+500 \sin 45^{\circ}(-\mathbf{k})$

$$
=\{176.78 \mathbf{i}-306.19 \mathbf{j}-353.55 \mathbf{k}\} \mathbf{N}
$$

Resultant Force: The resultant force acting on the hook can be obtained by vectorally adding $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$. Thus,

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{1}+\mathbf{F}_{2} \\
& =(259.81 \mathbf{i}-150 \mathbf{k})+(176.78 \mathbf{i}+306.19 \mathbf{j}-353.55 \mathbf{k}) \\
& =\{436.58 \mathbf{i})+306.19 \mathbf{j}-503.55 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

The magnitude of $\mathbf{F}_{\mathrm{R}}$ is

$$
\begin{aligned}
\mathrm{F}_{\mathrm{R}} & =2 \overline{\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{x}}^{2}+\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}^{2}\left(\mathrm{~F}_{\mathrm{R}}\right)_{\mathrm{z}}^{2}} \\
& =2(436.58)^{2}+(306.19)^{2}+(-503.55)^{2}
\end{aligned}=733.43 \mathrm{~N}=733 \mathrm{~N} \quad \text { Ans. }
$$

The coordinate direction angles of $\mathbf{F}_{\mathrm{R}}$ are

$$
\begin{aligned}
& u_{x}=\cos ^{-1} \frac{\left(\mathrm{~F}_{\mathrm{R}} \underline{\underline{x}}^{\mathrm{F}_{\mathrm{R}}}\right.}{\mathrm{F}_{\mathrm{d}}}=\cos ^{-1} \mathrm{a} \frac{436.58}{733.43} \mathrm{~b}=53.5^{\circ}
\end{aligned}
$$

$$
\begin{aligned}
& \left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{z}} \\
& u_{z}=\cos ^{-1} c F_{R}^{d}=\cos ^{-1} a^{\frac{-503.55}{733.43}} \mathrm{~b}=133^{\circ}
\end{aligned}
$$

Ans.

Ans.

Ans.

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$$
\begin{aligned}
F_{R} & =733 \mathrm{~N} \\
\mathrm{u}_{x} & =53.5 \\
\mathrm{u}_{y} & =65.3 \\
\mathrm{u}_{z} & =133
\end{aligned}
$$

## 2-82.

Three forces act on the ring. If the resultant force $\mathbf{F}_{R}$ has a magnitude and direction as shown, determine the magnitude and the coordinate direction angles of force $\mathbf{F}_{3}$.

## SOLUTION

## Cartesian Vector Notation:

$$
\begin{aligned}
\mathbf{F}_{R} & =120\left\{\cos 45^{\circ} \sin 30^{\circ} \mathbf{i}+\cos 45^{\circ} \cos 30^{\circ} \mathbf{j}+\sin 45^{\circ} \mathbf{k}\right\} \mathrm{N} \\
& =\{42.43 \mathbf{i}+73.48 \mathbf{j}+84.85 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{1} & =80 \mathrm{~b} \frac{4}{5} \mathbf{i}+\frac{3}{5} \mathbf{k r N}=\{64.0 \mathbf{i}+48.0 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{2} & =\{-110 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{3} & =\left\{\mathrm{F}_{3_{\mathrm{x}}} \mathbf{i}+\mathrm{F}_{3_{\mathrm{y}}} \mathbf{j}+\mathrm{F}_{3_{\mathbf{z}}} \mathbf{k}\right\} \mathrm{N}
\end{aligned}
$$

## Resultant Force:

$\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{1}+\mathbf{F}_{2}+\mathbf{F}_{3}$
$\{42.43 \mathbf{i}+73.48 \mathbf{j}+84.85 \mathbf{k}\}=\mathrm{EA} 64.0+\mathrm{F}_{3_{\mathrm{x}}} \mathrm{B} \mathbf{i}+\mathrm{F}_{3_{\mathrm{y}}} \mathbf{j}+A 48.0-110+\mathrm{F}_{3_{z}} \mathrm{~B} \mathrm{BF}$
Equating $\mathbf{i}, \mathbf{j}$ and $\mathbf{k}$ components, we have

$$
\begin{array}{ll}
64.0+\mathrm{F}_{3_{\mathrm{x}}}=42.43 & \mathrm{~F}_{3_{\mathrm{x}}}=-21.57 \mathrm{~N} \\
& \mathrm{~F}_{3_{\mathrm{y}}}=73.48 \mathrm{~N} \\
48.0-110+\mathrm{F}_{3_{z}}=84.85 & \mathrm{~F}_{3_{z}}=146.85 \mathrm{~N}
\end{array}
$$

The magnitude of force $\mathbf{F}_{3}$ is

$$
\begin{aligned}
\mathrm{F}_{3} & =2 \overline{\mathrm{~F}_{3_{x}}^{2}+\mathrm{F}_{3_{y}}^{2}+\mathrm{F}_{3_{z}}^{2}} \\
& =2(-21.57)^{2}+73.48^{2}+146.85^{2} \\
& =165.62 \mathrm{~N}=166 \mathrm{~N}
\end{aligned}
$$

Ans.

The coordinate direction angles for $\mathbf{F}_{3}$ are

$$
\cos \mathrm{a}=\frac{\underline{\mathrm{F}}_{3_{3}}}{\mathrm{~F}_{3}}=\frac{-21.57}{165.62} \quad \mathrm{a}=97.5^{\circ}
$$

$$
\cos \mathrm{b}=\mathrm{F}=165.62
$$

$\mathrm{b}=63.7^{\circ}$
Ans.

$$
\cos g==\frac{F_{3_{z}}}{F_{3}}=\begin{aligned}
& 146.85 \\
& 165.62
\end{aligned} \quad \mathrm{~g}=27.5^{\circ}
$$

Ans.
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$$
\begin{aligned}
& \mathrm{b}=63.7 \\
& \mathrm{~g}=27.5
\end{aligned}
$$

2-83.
Determine the coordinate direction angles of $\mathbf{F}_{1}$ and $\mathbf{F}_{R}$.

## SOLUTION

Unit Vector of $\mathrm{F}_{1}$ and $\mathrm{F}_{\boldsymbol{R}}$ :

$$
\begin{aligned}
\mathbf{u}_{\mathrm{F}_{1}} & =\frac{4}{5} \mathbf{i}+\frac{3}{5} \mathbf{k}=0.8 \mathbf{i}+0.6 \mathbf{k} \\
\mathbf{u}_{\mathrm{R}} & =\cos 45^{\circ} \sin 30^{\circ} \mathbf{i}+\cos 45^{\circ} \cos 30^{\circ} \mathbf{j}+\sin 45^{\circ} \mathbf{k} \\
& =0.3536 \mathbf{i}+0.6124 \mathbf{j}+0.7071 \mathbf{k}
\end{aligned}
$$

Thus, the coordinate direction angles $\mathbf{F}_{1}$ and $\mathbf{F}_{R}$ are

$$
\begin{array}{ll}
\cos \mathrm{a}_{\mathrm{F}_{1}}=0.8 & \mathrm{a}_{\mathrm{F}_{1}}=36.9^{\circ} \\
\cos \mathrm{b}_{\mathrm{F}_{1}}=0 & \mathrm{~b}_{\mathrm{F}_{1}}=90.0^{\circ} \\
\cos \mathrm{g}_{\mathrm{F}_{1}}=0.6 & \mathrm{~g}_{\mathrm{F}_{1}}=53.1^{\circ} \\
\cos \mathrm{a}_{\mathrm{R}}=0.3536 & \mathrm{a}_{\mathrm{R}}=69.3^{\circ} \\
\cos \mathrm{b}_{\mathrm{R}}=0.6124 & \mathrm{~b}_{\mathrm{R}}=52.2^{\circ} \\
\cos \mathrm{g}_{\mathrm{R}}=0.7071 & \mathrm{~g}_{\mathrm{R}}=45.0^{\circ}
\end{array}
$$



Ans.
Ans.
Ans.

Ans.
Ans.
Ans.

Ans:
$\mathrm{a}_{F_{1}}=36.9$
$\mathrm{b}_{F_{1}}=90.0$
$\mathrm{g}_{F_{1}}=53.1$
$\mathrm{a}_{R}=69.3$
$\mathrm{b}_{R}=52.2$
$\mathrm{g}_{R}=45.0$

## *2-84.

The pole is subjected to the force $\mathbf{F}$, which has components acting along the $x, y, z$ axes as shown. If the magnitude of $\mathbf{F}$ is $3 \mathrm{kN}, \mathrm{b}=30^{\circ}$, and $\mathrm{g}=75^{\circ}$, determine the magnitudes of its three components.

## SOLUTION

$$
\begin{aligned}
& \cos ^{2} \mathrm{a}+\cos ^{2} \mathrm{~b}+\cos ^{2} \mathrm{~g}=1 \\
& \cos ^{2} \mathrm{a}+\cos ^{2} 30^{\circ}+\cos ^{2} 75^{\circ}=1 \\
& \mathrm{a}=64.67^{\circ} \\
& \mathrm{F}_{\mathrm{x}}=3 \cos 64.67^{\circ}=1.28 \mathrm{kN} \\
& \mathrm{~F}_{\mathrm{y}}=3 \cos 30^{\circ}=2.60 \mathrm{kN} \\
& \mathrm{~F}_{\mathrm{z}}=3 \cos 75^{\circ}=0.776 \mathrm{kN}
\end{aligned}
$$



Ans.
Ans.
Ans.

## Ans:

$\mathrm{F}_{\mathrm{x}}=1.28 \mathrm{kN}$
$\mathrm{F}_{\mathrm{y}}=2.60 \mathrm{kN}$
$\mathrm{F}_{\mathrm{z}}=0.776 \mathrm{kN}$

2-85.
The pole is subjected to the force $\mathbf{F}$ which has components $\mathrm{F}_{\mathrm{x}}=1.5 \mathrm{kN}$ and $\mathrm{F}_{\mathrm{z}}=1.25 \mathrm{kN}$. If $\mathrm{b}=75^{\circ}$, determine the magnitudes of $\mathbf{F}$ and $\mathbf{F}_{y}$.

## SOLUTION

$$
\begin{aligned}
& \cos ^{2} a+\cos ^{2} b+\cos ^{2} g=1 \\
& a \frac{1.5}{\mathrm{~F}} \mathrm{~b}^{2}+\cos ^{2} 75^{\circ}+\mathrm{a} \frac{1.25}{\mathrm{~F}} b^{2}=1
\end{aligned}
$$

$\mathrm{F}=2.02 \mathrm{kN}$
$\mathrm{F}_{\mathrm{y}}=2.02 \cos 75^{\circ}=0.523 \mathrm{kN}$


## Ans:

$F=2.02 \mathrm{kN}, F_{y}=0.523 \mathrm{kN}$

## 2-86.

Determine the lengths of wires $A D, B D$, and $C D$. The ring at $D$ is midway between $A$ and $B$.

## SOLUTION

$\mathrm{Da} \frac{2+0}{2}, \frac{0+2}{2}, \frac{1.5+0.5}{2} \mathrm{~b} \mathrm{~m}=D(1,1,1) \mathrm{m}$
$\mathbf{r}_{\mathrm{AD}}=(1-2) \mathbf{i}+(1-0) \mathbf{j}+(1-1.5) \mathbf{k}$
$=-1 \mathbf{i}+1 \mathbf{j}-0.5 \mathbf{k}$

$\mathbf{r}_{\mathrm{BD}}=(1-0) \mathbf{i}+(1-2) \mathbf{j}+(1-0.5) \mathbf{k}$
$=1 \mathbf{i}-1 \mathbf{j}+0.5 \mathbf{k}$
$\mathbf{r}_{\mathrm{CD}}=(1-0) \mathbf{i}+(1-0) \mathbf{j}+(1-2) \mathbf{k}$
$=1 \mathbf{i}+1 \mathbf{j}-1 \mathbf{k}$
$\mathrm{r}_{\mathrm{AD}}=2(-1)^{2}+1^{2}+(-0.5)^{2}=1.50 \mathrm{~m}$
$r_{B D}=21^{2}+(-1)^{2}+0.5^{2}=1.50 \mathrm{~m}$
$r_{C D}=21^{2}+1^{2}+(-1)^{2}=1.73 \mathrm{~m}$

Ans.
Ans.
Ans.
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$$
\begin{aligned}
& r_{A D}=1.50 \mathrm{~m} \\
& r_{B D}=1.50 \mathrm{~m} \\
& r_{C D}=1.73 \mathrm{~m}
\end{aligned}
$$

## 2-87.

Determine the length of the connecting rod $A B$ by first formulating a Cartesian position vector from $A$ to $B$ and then determining its magnitude.

## Solution

Position Vector. The coordinates of points $A$ and $B$ are $A(-150 \cos 30$, - $150 \sin 30) \mathrm{mm}$ and $B(0,300) \mathrm{mm}$ respectively. Then
$\mathbf{r}_{A B}=[0-(-150 \cos 30)] \mathbf{i}+[300-(-150 \sin 30)] \mathbf{j}$

$$
=\{129.90 \mathbf{i}+375 \mathbf{j}\} \mathrm{mm}
$$



Thus, the magnitude of $\mathbf{r}_{A B}$ is

$$
\mathbf{r}_{A B}=2 \overline{129.90^{2}+375^{2}}=396.86 \mathrm{~mm}=397 \mathrm{~mm}
$$

Ans:
$r_{A B}=397 \mathrm{~mm}$
*2-88.
If $\mathbf{F}=5350 \mathbf{i}-250 \mathbf{j}-450 \mathbf{k} 6 \mathrm{~N}$ and cable AB is 9 m long,
determine the $\mathrm{x}, \mathrm{y}, \mathrm{z}$ coordinates of point A .

## SOLUTION

Position Vector: The position vector $\mathbf{r}_{\mathrm{AB}}$, directed from point A to point B , is given by
$\mathbf{r}_{\mathrm{AB}}=[0-(-\mathrm{x})] \mathbf{i}+(0-\mathrm{y}) \mathbf{j}+(0-\mathrm{z}) \mathbf{k}$

$=\mathrm{xi}-\mathrm{y} \mathbf{j}-\mathrm{zk}$
Unit Vector: Knowing the magnitude of $\mathbf{r}_{\mathrm{AB}}$ is 9 m , the unit vector for $\mathbf{r}_{\mathrm{AB}}$ is given by
$\mathbf{u}_{\mathrm{AB}}=\frac{\mathbf{r}_{\mathrm{AB}}}{\mathrm{r}_{\mathrm{AB}}}=\frac{\mathrm{x} \mathbf{i}-\mathrm{y} \mathbf{j}-\mathbf{z} \mathbf{k}}{9}$

The unit vector for force $\mathbf{F}$ is
$\mathbf{u}_{\mathrm{F}}=\frac{\mathbf{F}}{\mathrm{F}}=\frac{350 \mathbf{i}-250 \mathbf{j}-450 \mathbf{k}}{350^{2}+(-250)^{2}+(-450)^{2}}=0.5623 \mathbf{i}-0.4016 \mathbf{j}-0.7229 \mathbf{k}$
Since force $\mathbf{F}_{\mathbf{F}}$ is also directed from point A to point B, then
$\mathbf{u}_{\mathrm{AB}}=\mathbf{u}_{\mathrm{F}}$
$\frac{\mathrm{xi}-\mathrm{yj}-\mathrm{zk}}{9}=0.5623 \mathbf{i}-0.4016 \mathbf{j}-0.7229 \mathbf{k}$
Equating the $\mathbf{i}, \mathbf{j}$, and $\mathbf{k}$ components,

| $x$ |  |
| :--- | :--- |
| 9 | $=0.5623$ |
| $-y=-0.4016$ | $x=5.06 m$ |
| 9 | $y=3.61 \mathrm{~m}$ |
| $\frac{-z}{9}=0.7229$ | $z=6.51 \mathrm{~m}$ |

Ans.

Ans.

Ans.

## Ans:

$x=5.06 \mathrm{~m}$
$y=3.61 \mathrm{~m}$
$z=6.51 \mathrm{~m}$

## 2-89.

Determine the magnitude and coordinate direction angles of the resultant force acting at A .

## SOLUTION

Force Vectors: The unit vectors $\mathbf{u}_{\mathrm{B}}$ and $\mathbf{u}_{\mathrm{C}}$ of $\mathbf{F}_{\mathrm{B}}$ and $\mathbf{F}_{\mathrm{C}}$ must be determined first. From Fig. $a$
$\mathbf{u}_{\mathrm{B}}=\frac{\underline{\mathbf{r}}_{\mathrm{B}}}{\mathrm{r}_{\mathrm{B}}}=\frac{(-1.5-0.5) \mathbf{i}+[-2.5-(-1.5)] \mathbf{j}+(2-0) \mathbf{k}}{3 \overline{(-1.5-0.5)^{2}+[-2.5-(-1.5)]^{2}+(2-0)^{2}}}$

$$
=-\frac{2}{3} \mathbf{i}-\frac{1}{3} \mathbf{j}+\frac{2}{3} \mathbf{k}
$$

$\mathbf{u}_{\mathrm{C}}=\frac{\mathbf{r}_{\mathrm{C}}}{\mathrm{r}_{\mathrm{C}}}=\frac{(-1.5-0.5) \mathbf{i}+[0.5-(-1.5)] \mathbf{j}+(3.5-0) \mathbf{k}}{3 \overline{(-1.5-0.5)^{2}+[0.5-(-1.5)]^{2}+(3.5-0)^{2}}}$

$$
=-{ }_{9}^{4} \mathbf{i}+{ }_{9}^{4} \mathbf{j}+{ }_{9}^{7} \mathbf{k}
$$

Thus, the force vectors $\mathbf{F}_{\mathrm{B}}$ and $\mathbf{F}_{\mathrm{C}}$ are given by
$\mathbf{F}_{\mathrm{B}}=\mathrm{F}_{\mathrm{B}} \mathbf{u}_{\mathrm{B}}=600 \mathrm{a}-\frac{\overline{2}}{3} \mathbf{i}-{ }_{3}^{1} \mathbf{j}+{ }_{3}^{2} \mathbf{k} \mathbf{b}=5-400 \mathbf{i}-200 \mathbf{j}+400 \mathbf{k} 6 \mathrm{~N}$
$\mathbf{F}_{\mathrm{C}}=\mathrm{F}_{\mathrm{C}} \mathbf{u}_{\mathrm{C}}=450 \mathrm{a}-{ }_{9}^{\overline{4}} \mathbf{i}+{ }_{9}^{\overline{4}} \mathbf{j}+{ }_{9}^{\overline{7}} \mathbf{k} \mathbf{b}=5-200 \mathbf{i}+200 \mathbf{j}+350 \mathbf{k} 6 \mathrm{~N}$

## Resultant Force:

$\mathbf{F}_{\mathrm{R}}=\mathbf{F}_{\mathrm{B}}+\mathbf{F}_{\mathrm{C}}=(-400 \mathbf{i}-200 \mathbf{j}+400 \mathbf{k})+(-200 \mathbf{i}+200 \mathbf{j}+350 \mathbf{k})$

$$
=5-600 \mathbf{i}+750 \mathbf{k} 6 \mathrm{~N}
$$

The magnitude of $\mathbf{F}_{\mathrm{R}}$ is
$F_{R}=\mathbf{3}\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2}$

$$
=3(-600)^{2}+0^{2}+750^{2}=960.47 \mathrm{~N}=960 \mathrm{~N}
$$

The coordinate direction angles of $\mathbf{F}_{\mathrm{R}}$ are
$\mathrm{a}=\cos ^{-1} \frac{\left(\mathrm{~F}_{\underline{\mathrm{R}}}\right)_{\underline{x}_{\mathrm{x}}}}{\mathrm{F}_{\mathrm{R}}}=\cos ^{-1} \mathrm{a} \frac{-600}{960.47} \mathrm{~b}=129^{\circ}$
$\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{y}}$
$b=\cos ^{-1} c_{\underline{F_{R}}} d=\cos ^{-1} \underline{\underline{0} \underline{060.47}} b=90^{\circ}$
$\left(\mathrm{F}_{\mathrm{R}}\right)_{\mathrm{z}} \quad 760$
$g=\cos ^{-1} c F_{R}^{d=\cos ^{-1} a_{960.47} b=38.7^{\circ}}$

Ans.

Ans.

Ans.
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$$
\begin{aligned}
& \mathrm{a}=129 \\
& \mathrm{~b}=90 \\
& \mathrm{~g}=38.7
\end{aligned}
$$

2-90. The door is held opened by means of two chains. If the tension in $A B$ and $C D$ is $\mathbf{F}_{A}=300 \mathrm{~N}$ and $\mathbf{F}_{C}=250 \mathrm{~N}$, respectively, express each of these forces in Cartesian vector form.


## Solution

Unit Vector: First determine the position vector $\mathbf{r}_{A B}$ and $\mathbf{r}_{C D}$. The coordinates of points $A$ and $C$ are

$$
\begin{aligned}
A 30,-(1+1.5 \cos 30), 1.5 \sin 304 \mathrm{~m} & =A(0,-2.299,0.750) \mathrm{m} \\
C[-2.50,-(1+1.5 \cos 30), 1.5 \sin 304 \mathrm{~m} & =C(-2.50,-2.299,0.750) \mathrm{m}
\end{aligned}
$$

Then

$$
\begin{aligned}
\mathbf{r}_{A B} & =5(0-0) \mathbf{i}+30-(-2.299) 4 \mathbf{j}+(0-\mathbf{O} .75 \mathrm{O} \mathbf{k} 6 \mathrm{~m} \\
& =52.299 \mathbf{j}-\mathbf{O} .750 \mathbf{k} 6 \mathrm{~m} \\
r_{A B} & =2 \overline{2.299^{2}+(-0.750)^{2}}=2.418 \mathrm{~m} \\
\mathbf{u}_{A B} & =\frac{\mathbf{r}_{A B}}{r_{A B}}=\frac{2.299 \mathbf{j}-0.750 \mathbf{k}}{2.418}=0.9507 \mathbf{j}-0.3101 \mathbf{k} \\
\mathbf{r}_{C D} & =5[-0.5-(-2.5) 4 \mathbf{i}+30-(-2.299) 4 \mathbf{j}+(0-0.750) \mathbf{k} 6 \mathrm{~m} \\
& =52.00 \mathbf{i}+2.299 \mathbf{j}-\mathbf{O . 7 5 0 \mathbf { k }} 6 \mathrm{~m} \\
r_{C D} & =2 \overline{22.00^{2}+2.299^{2}+(-0.750)^{2}}=3.318 \mathrm{~m} \\
\mathbf{u}_{C D} & =\frac{\mathbf{r}_{C D}}{r_{C D}}=\frac{2.00 \mathbf{i}+2.299 \mathbf{j}-0.750 \mathbf{k}}{3.318}=0.6373 \mathbf{i}+0.7326 \mathbf{j}-0.2390 \mathbf{k}
\end{aligned}
$$

## Force Vector:

$$
\begin{aligned}
\mathbf{F}_{A}=F_{A} \mathbf{u}_{A B} & =30050.9507 \mathbf{j}-0.3101 \mathbf{k}\} \mathrm{N} \\
& =5285.21 \mathbf{j}-93.04 \mathbf{k} 6 \mathrm{~N} \\
& =5285 \mathbf{j}-93.0 \mathbf{k} 6 \mathrm{~N} \\
\mathbf{F}_{C}=F_{C} \mathbf{u}_{C D} & =25050.6373 \mathbf{i}+0.7326 \mathbf{j}-0.2390 \mathbf{k} 6 \mathrm{~N} \\
& =5159.33 \mathbf{i}+183.15 \mathbf{j}-59.75 \mathbf{k} 6 \mathrm{~N} \\
& =5159 \mathbf{i}+183 \mathbf{j}-59.7 \mathbf{k} 6 \mathrm{~N}
\end{aligned}
$$

Ans.

Ans.

Ans:
$\mathbf{F}_{A}=\{285 \mathbf{j}-93.0 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{C}=\{159 \mathbf{i}+183 \mathbf{j}-59.7 \mathbf{k}\} \mathrm{N}$

## 2-91.

If $F_{B}=560 \mathrm{~N}$ and $F_{C}=700 \mathrm{~N}$, determine the magnitude
and coordinate direction angles of the resultant force acting on the flag pole.

## SOLUTION

Force Vectors: The unit vectors $\mathbf{u}$ and $\mathbf{u}$ of $\mathbf{F}$ and $\mathbf{F}$ must be determined first. From Fig. $a$
$\mathbf{u}_{B}=\frac{\mathbf{r}}{r_{B}}=\frac{(2-0) \mathbf{i}+(3-0) \mathbf{i}_{+}(0-6) \mathbf{k}}{\sqrt{(2-0)^{2}+(-3-0)^{2}+(0-6)^{2}}}=\frac{2}{7}{ }_{7} \quad-\frac{3}{7} \mathbf{j}-\frac{6}{7} \mathbf{k}$
$\mathbf{u}_{C}=\frac{\mathbf{r}_{C}}{r_{C}}=\frac{(3-0) \mathbf{i}+(2-0) \mathbf{j}+(0-6) \mathbf{k}}{\sqrt{(3-0)^{2}+(2-0)^{2}+(0-6)^{2}}}=\frac{3}{7} \mathbf{i}+\frac{2}{7} \mathbf{j}-\frac{6}{7} \mathbf{k}$
Thus, the force vectors $\mathbf{F}^{B}$ and $\mathbf{F}^{C}$ are given by

Rgsteltapt+Foree-
$\mathbf{F}=\begin{array}{lllllll}\mathbf{F} & \overline{\mathbf{F}} & \stackrel{+}{(160 \mathbf{i}} \quad 2{ }^{2} 40 \mathbf{j} & 480 \mathbf{k}) & (300 \mathbf{i} & 200 \mathbf{j} & 600 \mathbf{k})\end{array}$


$$
\begin{array}{rl}
=\sqrt{()^{2+}()^{2+}()^{2}}= & = \\
(460)^{2}(40)^{2}(1080)^{2} & 1174.56 \mathrm{~N} \quad 1.17 \mathrm{kN}
\end{array}
$$



Ans.

Ans.

$$
\begin{aligned}
& \gamma=-\left[\begin{array}{c}
F_{R z} \\
F_{R}
\end{array}\right]= \\
& \cos ^{1} \underline{\left({ }^{2}\right)} \\
& \cos ^{1} \frac{-40}{1174.56}
\end{aligned}
$$

Ans.

$$
\cos ^{1} \underline{(\quad)} \quad \cos ^{1} \frac{1080}{1174.56} \quad 157^{\circ}
$$

Ans.

$$
\begin{aligned}
& { }_{C}=F_{C} C=(-+---)=\{+\quad+\quad\} \\
& \begin{array}{llllllllll}
\mathbf{F} & \mathbf{u} & 700 & { }_{7}^{3} \mathbf{i} & { }_{7}^{2} \mathbf{j} & { }_{7}^{6} \mathbf{k} & 300 \mathbf{i} & 200 \mathbf{j} & 600 k & \mathrm{~N}
\end{array}
\end{aligned}
$$

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> Ans:
> $F_{R}=1.17 \mathrm{kN}$
> $\mathrm{a}=66.9$
> $\mathrm{~b}=92.0$
> $\mathrm{~g}=157$

## *2-92.

If $F=700 \mathrm{~N}$, and $F_{C}=560 \mathrm{~N}$, determine the magnitude and coordinate direction angles of the resultant force acting on the flag pole.


## SOLUTION

Force Vectors: The unit vectors $\mathbf{u}$ and $\mathbf{u}_{C}$ of $\mathbf{F}$ and $\mathbf{F}_{C}$ must be determined first. From Fig. $a$
$\mathbf{u}=\frac{\mathbf{r}}{r}=\frac{(2-0) \mathbf{i}+(-3-0) \mathbf{j}+(0-6) \mathbf{k}}{\sqrt{(2-0)^{2}+\left({ }^{3}-0\right)^{2}+(0-6)^{2}}}={ }_{7}^{2} \mathbf{i}-{ }_{7}^{3} \mathbf{j}-{ }_{7}^{6} \mathbf{k}$
$\mathbf{u}_{C}=\frac{\mathbf{r}_{C}}{r_{C}}=\frac{\left.\left.(3-0) \mathbf{i}+{ }^{(2}-0\right) \mathbf{j}+{ }^{(0}-6\right) \mathbf{k}}{\sqrt{(3-0)^{2}+(2-0)^{2}+(0-6)^{2}}}=\frac{{ }_{7}^{3}}{} \mathbf{i}^{2}+\frac{2}{7} \mathbf{j}-\frac{6}{7} \mathbf{k}$
Thus, the force vectors $\mathbf{F}$ and $\mathbf{F}_{C}$ are given by
$\mathbf{F}=F^{\mathbf{u}}=700\left({ }_{7}^{2} \mathbf{i}-{ }_{7}^{3} \mathbf{j}-{ }_{7}^{6} \mathbf{k}\right)=\left\{200 \mathbf{i}-300 \mathbf{j}-600 \mathbf{k}_{\}} \mathrm{N}\right.$
$\mathbf{F}_{C}=F_{C}{ }^{\mathbf{u}}{ }_{C}={ }^{560}\left({ }_{7}^{3} \mathbf{i}+{ }_{7}^{2} \mathbf{j}-{ }_{7}^{6} \mathbf{k}\right)=\left\{{ }^{240 \mathbf{i}}+{ }^{160 \mathbf{j}}-480 \mathbf{k}_{\}}\right\}^{\mathrm{N}}$

## Resultant Force:

${ }_{R}={ }^{\mathbf{F}}+{ }_{C}={ }^{(200 \mathbf{i}}{ }_{-}{ }^{300 \mathbf{j}}{ }_{-}^{600 \mathbf{k})}+{ }^{(240 \mathbf{i}}+{ }^{160 \mathbf{j}}{ }_{-}^{480 \mathbf{k})}$

$$
=\left\{{ }^{440 \mathbf{i}}-{ }^{140 \mathbf{j}}-{ }^{1080 \mathbf{k}}\right\}^{\mathrm{N}}
$$

The magnitude of $\mathbf{F}$ is
$F_{R}=\sqrt{\left.\left({ }_{F_{R}}\right)^{2}+\left({ }_{F}\right)^{2}\right)^{2}+\left({ }_{F}\right)^{2}}$
$={\sqrt{(440)^{2}+(140)^{2}+\left({ }_{-}^{(1080)^{2}}\right.}=1174.56 \mathrm{~N}}_{=}=1.17 \mathrm{kN}$
The coordinate direction angles of $\mathbf{F}$ are

$$
=\cos ^{1}-\left[\begin{array}{c}
\left(\frac{)}{F_{R}}\right. \\
F_{R}
\end{array}\right]=\cos _{-}^{1}\left(\begin{array}{c}
440{ }^{R} \\
1174.56 \\
-140
\end{array}\right)=68.0^{\circ}
$$

Ans.

(a)

Ans.

Ans.

Ans.

## Ans:

$F_{R}=1.17 \mathrm{kN}$
$\mathrm{a}=68.0$
$\mathrm{b}=96.8$
$\mathrm{g}=157$

## 2-93.

Express each of the forces in Cartesian vector form and determine the magnitude and coordinate direction angles of the resultant force.

## Solution

Unit Vectors. The coordinates for points $A, B$ and $C$ are $(0,-0.75,3) \mathrm{m}$, $B(2 \cos 40,2 \sin 40,0) \mathrm{m}$ and $C(2,-1,0) \mathrm{m}$ respectively.

$$
\mathbf{u}_{A B}=\frac{\mathbf{r}_{A B}}{\mathbf{r}_{A B}}=\frac{(2 \cos 40-0) \mathbf{i}+[2 \sin 40-(-0.75)] \mathbf{j}+(0-3) \mathbf{k}}{2 \overline{(2 \cos 40-0)^{2}+[2 \sin 40-(-0.75)]^{2}+(0-3)^{2}}}
$$

$$
=0.3893 \mathbf{i}+0.5172 \mathbf{j}-0.7622 \mathbf{k}
$$

$$
\mathbf{u}_{A C}=\frac{\mathbf{r}_{A C}}{\mathbf{r}_{A C}}=\frac{(2-0) \mathbf{i}+[-1-(-0.75)] \mathbf{j}+(0-3) \mathbf{k}}{2 \overline{(2-0)^{2}+[-1-(-0.75)]^{2}+(0-3)^{2}}}
$$

$$
=0.5534 \mathbf{i}-0.0692 \mathbf{j}-0.8301 \mathbf{k}
$$

## Force Vectors

$\mathbf{F}_{A B}=\mathbf{F}_{A B} \mathbf{u}_{A B}=250(0.3893 \mathbf{i}+0.5172 \mathbf{j}-0.7622 \mathbf{k})$

$$
=\{97.32 \mathbf{i}+129.30 \mathbf{j}-190.56 \mathbf{k}\} \mathrm{N}
$$

$$
=\{97.3 \mathbf{i}+129 \mathbf{j}-191 \mathbf{k}\} \mathrm{N}
$$

Ans.

$$
\begin{aligned}
\mathbf{F}_{A C}=\mathbf{F}_{A C} \mathbf{u}_{A C} & =400(0.5534 \mathbf{i}-0.06917 \mathbf{j}-0.8301 \mathbf{k}) \\
& =\{221.35 \mathbf{i}-27.67 \mathbf{j}-332.02 \mathbf{k}\} \mathrm{N} \\
& =\{221 \mathbf{i}-27.7 \mathbf{j}-332 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

Ans.

## Resultant Force

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{A B}+\mathbf{F}_{A C} \\
& =\{97.32 \mathbf{i}+129.30 \mathbf{j}-190.56 \mathbf{k}\}+\{221.35 \mathbf{i}-27.67 \mathbf{j}-332.02 \mathbf{k}\} \\
& =\{318.67 \mathbf{i}+101.63 \mathbf{j}-522.58 \mathbf{k}\} \mathbf{N}
\end{aligned}
$$

The magnitude of $\mathbf{F}_{R}$ is

$$
\begin{aligned}
\mathbf{F}_{R}=2\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2} & =2318.67^{2}+101.63^{2}+(-522.58)^{2} \\
& =620.46 \mathrm{~N}=620 \mathrm{~N}
\end{aligned}
$$

And its coordinate direction angles are
Ans.

$$
\mathbf{F}_{A B}=\{97.3 \mathbf{i}-129 \mathbf{j}-191 \mathbf{k}\} \mathbf{N}
$$

Ans.

$$
\mathbf{F}_{A C}=\{221 \mathbf{i}-27.7 \mathbf{j}-332 \mathbf{k}\} \mathrm{N}
$$

Ans.
$\cos \mathrm{a}=59.1$
$\cos \mathrm{b}=80.6$
$\cos \mathrm{g}=147$

$$
\begin{aligned}
& \cos \mathrm{a}=\begin{array}{l}
\left(F_{R}\right)_{x}=\begin{array}{l}
318.67 \\
\underline{F_{R}}
\end{array} \underline{\underline{620.46}} ; \quad \mathrm{a}=59.10=59.1
\end{array} \\
& \underline{\left(F_{\underline{R}}\right)_{v}} \quad \underline{101.63} \\
& \cos \mathrm{~b}={ }_{F}^{R}={ }_{620.46} ; \quad \mathrm{b}=80.57=80.6 \\
& \cos \mathrm{~g}=\frac{\left(F_{R}\right)_{z}}{F_{R}}=\frac{-522.58}{620.46} ; \quad \mathrm{g}=147.38=147
\end{aligned}
$$

## 2-94.

The 8 -m-long cable is anchored to the ground at $A$. If $x=4 \mathrm{~m}$ and $y=2 \mathrm{~m}$, determine the coordinate $z$ to the highest point of attachment along the column.

## Solution

$\mathbf{r}=\{4 \mathbf{i}+2 \mathbf{j}+z \mathbf{k}\} \mathrm{m}$
$r=2(4)^{2}+(2)^{2}+(z)^{2}=8$
$z=6.63 \mathrm{~m}$

Ans.


## 2-95.

The 8 -m-long cable is anchored to the ground at $A$. If $z=5 \mathrm{~m}$, determine the location $+x,+y$ of point $A$. Choose a value such that $x=y$.

## Solution

$\mathbf{r}=\{x \mathbf{i}+y \mathbf{j}+5 \mathbf{k}\} \mathrm{m}$
$r=2 \overline{(x)^{2}+(y)^{2}+(5)^{2}}=8$
$x=y$, thus
$2 x^{2}=8^{2}-5^{2}$
$x=y=4.42 \mathrm{~m}$


Ans.
*2-96.
Determine the magnitude and coordinate direction angles of the resultant force acting at point $A$ on the post.

$$
F_{A C} \quad 150 \mathrm{~N} \quad A \begin{array}{ll} 
& F_{A B}
\end{array} 200 \mathrm{~N}
$$



Unit Vector. The coordinates for points $A, B$ and $C$ are $A(0,0,3) \mathrm{m}, B(2,4,0) \mathrm{m}$ and $C(-3,-4,0) \mathrm{m}$ respectively
$\mathbf{r}_{A B}=(2-0) \mathbf{i}+(4-0) \mathbf{j}+(0-3) \mathbf{k}=\{2 \mathbf{i}+4 \mathbf{j}-3 \mathbf{k}\} \mathbf{m}$

$\mathbf{r}_{A C}=(-3-0) \mathbf{i}+(-4-0) \mathbf{j}+(0-3) \mathbf{k}=\{-3 \mathbf{i}-4 \mathbf{j}-3 \mathbf{k}\} \mathrm{m}$


## Force Vectors

$\mathbf{F}_{A B}=\mathbf{F}_{A B} \mathbf{u}_{A B}=200 \mathrm{a}_{22 \overline{9}}^{2} \mathbf{i}+\frac{4}{2 \overline{29}} \mathbf{j}-\frac{3}{2 \overline{29}} \mathbf{k b}$
$=\{74.28 \mathbf{i}+148.56 \mathbf{j}-111.42 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{A C}=\mathbf{F}_{A C} \mathbf{u}_{A C}=150 \mathrm{a}-\frac{3}{2 \overline{34}} \mathbf{i}-\frac{4}{2 \overline{34}} \mathbf{j}-\frac{3}{2 \overline{34}} \mathbf{k b}$
$=\{-77.17 \mathbf{i}-102.90 \mathbf{j}-77.17 \mathbf{k}\} \mathrm{N}$

## Resultant Force

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{A B}+\mathbf{F}_{A C} \\
& =\{74.28 \mathbf{i}+148.56 \mathbf{j}-111.42 \mathbf{k}\}+\{-77.17 \mathbf{i}-102.90 \mathbf{j}-77.17 \mathbf{k}\} \\
& =\{-2.896 \mathbf{i}+45.66 \mathbf{j}-188.59 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

The magnitude of the resultant force is

$$
\begin{aligned}
F_{R}=2\left(F_{R}\right)_{x}^{2}+\left(F_{R}\right)_{y}^{2}+\left(F_{R}\right)_{z}^{2} & =2(-2.896)^{2}+45.66^{2}+(-188.59)^{2} \\
& =194.06 \mathrm{~N}=194 \mathrm{~N}
\end{aligned}
$$

Ans.
And its coordinate direction angles are

$$
\begin{array}{ll}
\cos \mathrm{a}=\frac{\left(F_{R}\right)_{\underline{x}}}{F_{R}}=\frac{-2.896}{194.06} ; & \mathrm{a}=90.86=90.9 \\
\cos \mathrm{~b}={ }_{\left.F_{R}\right)_{y}}=\frac{45.66}{194.06} ; & \mathrm{b}=76.39=76.4
\end{array}
$$

Ans.

Ans.

$$
\left(F_{\underline{R}}\right) \underline{z} \quad-188.59
$$

Ans:
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$\cos \mathrm{g}={ }_{F_{R}}={ }_{194.06} ; \mathrm{g}=166.36=166$
Ans.
$F_{R}=194 \mathrm{~N}$
$\mathrm{a}=90.9$
b $=76.4$


2-97. The cylindrical plate is subjected to the three cable forces which are concurrent at point $D$. Express each force which the cables exert on the plate as a Cartesian vector, and determine the magnitude and coordinate direction angles of the resultant force.

## Solution

$$
\begin{aligned}
& \mathbf{r}_{A}=(0-0.75) \mathbf{i}+(0-0) \mathbf{j}+(3-0) \mathbf{k}=5-0.75 \mathbf{i}+0 \mathbf{j}+3 \mathbf{k} 6 \mathrm{~m} \\
& r_{A}=2(-0.75)^{2}+0^{2}+3^{2}=3.0923 \mathrm{~m}
\end{aligned}
$$

$\mathbf{F}_{A}=F_{A} \mathrm{a}^{\underline{\underline{\underline{r}}}}{ }_{r_{A}} \mathrm{~b}=6 \mathrm{a} \frac{-0.75 \mathbf{i}+3 \mathbf{k}}{3.0923} \mathrm{~b}$
$=5-1.4552 \mathbf{i}+5.8209 \mathbf{k} 6 \mathrm{kN}$
$=5-1.46 \mathbf{i}+5.82 \mathbf{k} 6 \mathrm{kN}$
$\mathbf{r}_{C}=30-(0.75 \sin 45) 4 \mathbf{i}+30-(-0.75 \cos 45) 4 \mathbf{j}+(3-0) \mathbf{k}$
$=50.5303 \mathbf{i}+0.5303 \mathbf{j}+3 \mathbf{k} 6 \mathrm{~m}$
$r_{C}=2 \overline{(0.5303)^{2}+(0.5303)^{2}+3^{2}}=3.0923 \mathrm{~m}$
$\mathbf{F}_{C}=F_{C}{ }^{2} \stackrel{\underline{\mathrm{r}}}{C}^{r_{C}} \mathrm{~b}=5 \mathrm{a} \frac{0.5303 \mathbf{i}+0.5303 \mathbf{j}+3 \mathbf{k}}{3.0923} \mathrm{~b}$
$=50.8575 \mathbf{i}+0.8575 \mathbf{j}+4.8507 \mathbf{k} 6 \mathrm{kN}$
$=50.857 \mathbf{i}+0.857 \mathbf{j}+4.85 \mathbf{k} 6 \mathbf{k N}$
$\mathbf{r}_{B}=30-(0.75 \sin 30) 4 \mathbf{i}+(0-0.75 \cos 30) \mathbf{j}+(3-0) \mathbf{k}$
$=50.375 \mathbf{i}-0.6495 \mathbf{j}+3 \mathbf{k} 6 \mathrm{~m}$
$\mathbf{r}_{B}=2(0.375)^{2}+(-0.6495)^{2}+3^{2}=3.0923 \mathrm{~m}$
$\mathbf{F}_{B}=F_{B^{2}}{ }_{r B}^{\underline{\mathrm{r}_{B}}} \mathrm{~b}=8 \mathrm{a} \frac{0.375 \mathbf{i}-0.6495 \mathbf{j}+3 \mathbf{k}}{3.0923} \mathrm{~b}$
$=50.9701 \mathbf{i}-1.6803 \mathbf{j}+7.7611 \mathbf{k} 6 \mathrm{kN}$
$=50.970 \mathbf{i}-1.68 \mathbf{j}+7.76 \mathbf{k} 6 \mathrm{kN}$


Ans.

Ans.

## 2-97 (Continued)

$$
\begin{aligned}
\mathbf{F}_{R} & =\mathbf{F}_{A}+\mathbf{F}_{B}+\mathbf{F}_{C} \\
& =5-1.4552 \mathbf{i}+5.8209 \mathbf{k} 6+50.9701 \mathbf{i}-1.6803 \mathbf{j}+7.7611 \mathbf{k} 6+50.8575 \mathbf{i}+0.8575 \mathbf{j}+4.8507 \mathbf{k} 6 \\
& =50.3724 \mathbf{i}-0.8228 \mathbf{j}+18.4327 \mathbf{k} 6 \mathrm{kN} \\
F_{R} & =2(0.3724)^{2}+(-0.8228)^{2}+(18.4327)^{2}
\end{aligned}
$$

$$
=18.4548 \mathrm{kN}=18.5 \mathrm{kN}
$$

$$
\mathrm{u}_{R}=\frac{\mathrm{F}_{R}}{F_{R}}=\frac{0.3724 \mathbf{i}-0.8228 \mathbf{j}+18.4327 \mathbf{k}}{18.4548}
$$

$$
=0.02018 \mathbf{i}-0.04459 \mathbf{j}+0.9988 \mathbf{k}
$$

$\cos \mathrm{a}=0.02018 \quad \mathrm{a}=88.8$
$\cos \mathrm{b}=-0.04458 \quad \mathrm{~b}=92.6$
$\cos \mathrm{g}=0.9988 \quad \mathrm{~g}=2.81$

Ans.

Ans.
Ans.
Ans.

> Ans:
> $\mathbf{F}_{A}=\{-1.46 \mathbf{i}+5.82 \mathbf{k}\} \mathrm{kN}$
> $\mathbf{F}_{C}=\{0.857 \mathbf{i}+0.857 \mathbf{j}+4.85 \mathbf{k}\} \mathrm{kN}$
> $\mathbf{F}_{B}=\{0.970 \mathbf{i}-1.68 \mathbf{j}+7.76 \mathbf{k}\} \mathrm{kN}$
> $F_{R}=18.5 \mathrm{kN}$
> $\mathrm{a}=88.8$
> $\mathrm{~b}=92.6$
> $\mathrm{~g}=2.81$
$\mathbf{2 - 9 8}$. The cord exerts a force $\mathbf{F}=\{12 \mathbf{i}+9 \mathbf{j}-8 \mathbf{k}\} \mathrm{kN}$ on the hook. If the cord is 4 m long, determine the location $x, y$ of the point of attachment $B$, and the height $z$ of the hook.

## Solution



## Given:

12
$\mathrm{F}=9 \mathrm{~N}$
8
$\mathrm{L}=4 \mathrm{~m}$
$\mathrm{a}=1 \mathrm{~m}$

Initial guesses $\quad=1 \mathrm{~m} \quad \mathrm{y}=1 \mathrm{~m} \quad \mathrm{z}=1 \mathrm{~m}$
x
X a
X
X
3.82


Given

[^2]2-99.
The three supporting cables exert the forces shown on the sign. Represent each force as a Cartesian vector.

## Solution

$\mathbf{r}_{C}=(0-5) \mathbf{i}+(-2-0) \mathbf{j}+(3-0) \mathbf{k}=\{-5 \mathbf{i}-2 \mathbf{j}+3 \mathbf{k}\} \mathrm{m}$
$r_{C}=2(-5)^{2}+(-2)^{2}+3^{2}=238 \mathrm{~m}$
$\mathbf{r}_{B}=(0-5) \mathbf{i}+(2-0) \mathbf{j}+(3-\overline{0}) \mathbf{k}=\{-5 \mathbf{i}+2 \mathbf{j}+3 \mathbf{k}\} \mathrm{m}$
$r_{B}=2(-5)^{2}+2^{2}+3^{2}=238 m$
$\mathbf{r}_{E}=(0-2) \mathbf{i}+(0-0) \mathbf{j}+(3-0) \mathbf{k}=\{-2 \mathbf{i}+0 \mathbf{j}+3 \mathbf{k}\} \mathrm{m}$
$r_{E}=2(-2)^{2}+0^{2}+3^{2}=213 \mathrm{~m}$
$\mathbf{F}=F_{\mathbf{u}}=F \mathrm{a}_{r} \mathbf{r}_{\mathrm{b}}$
$\mathbf{F}_{C}=400 \mathrm{a}^{-5 \mathbf{i}-2 \mathbf{j}+3 \mathbf{k}}{ }_{\mathrm{b}}=\{-324 \mathbf{i}-130 \mathbf{j}+195 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{B}=400 \mathrm{a}^{\overline{-5 \mathbf{i}+2 \bar{j}+3 \mathbf{k}}} \mathrm{~b}=\{-324 \mathbf{i}+130 \mathbf{j}+195 \mathbf{k}\} \mathrm{N}$
$\mathbf{F}_{E}=350 \mathrm{a}^{-2 \mathbf{i}+0 \dot{\mathbf{j}}+3 \mathbf{k}} \mathrm{~b}=\{-194 \mathbf{i}+291 \mathbf{k}\} \mathrm{N}$
113


Ans.

Ans.

Ans.

Ans:
$\mathbf{F}_{C}=\{-324 \mathbf{i}-130 \mathbf{j}+195 \mathbf{k}\} \mathbf{N}$
$\mathbf{F}_{B}=\{-324 \mathbf{i}+130 \mathbf{j}+195 \mathbf{k}\} \mathbf{N}$
$\mathbf{F}_{E}=\{-194 \mathbf{i}+291 \mathbf{k}\} \mathbf{N}$

## *2-100.

Determine the magnitude and coordinate direction angles of the resultant force of the two forces acting on the sign at point $A$.

## Solution

$\mathbf{r}_{C}=(0-5) \mathbf{i}+(-2-0) \mathbf{j}+(3-0) \mathbf{k}=\{-5 \mathbf{i}-2 \mathbf{j}+3 \mathbf{k}\}$ $r_{C}=2(-5)^{2}+(-2)^{2}+(3)^{2}=238 \mathrm{~m}$
$\mathbf{F}_{C}=400 \mathrm{a}_{r_{C} \mathbf{r}_{C}}^{r_{\mathrm{b}}}=400 \mathrm{a} \frac{(-5 \mathbf{i}-2 \mathbf{j}+\overline{3} \mathbf{k})}{\mathbf{1} 38} \mathrm{~b}$
$\mathbf{F}_{C}=(-324.4428 \mathbf{i}-129.777 \mathbf{j}+194.666 \mathbf{k})$
$\mathbf{r}_{B}=(0-5) \mathbf{i}+(2-0) \mathbf{j}+(3-0) \mathbf{k}=\{-5 \mathbf{i}+2 \mathbf{j}+3 \mathbf{k}\}$
$r_{B}=2(-5)^{2}+2^{2}+3^{2}=238 \mathrm{~m}$
$\mathbf{F}_{B}=400 \mathrm{a}_{r_{B}}^{\underline{\mathbf{r}_{B}}} \mathrm{r}_{\mathrm{b}}=400 \mathrm{a} \frac{(-5 \mathbf{i}+2 \mathbf{j}+3 \mathbf{k})}{\mathbf{1} 38} \mathrm{~b}$
$\mathbf{F}_{B}=(-324.443 \mathbf{i}+129.777 \mathbf{j}+194.666 \mathbf{k})$
$\mathbf{F}_{R}=\mathbf{F}_{C}+\mathbf{F}_{B}=(-648.89 \mathbf{i}+389.33 \mathbf{k})$
$F_{R}=2(-648.89)^{2}+(389.33)^{2}+0^{2}=756.7242$
$F_{R}=757 \mathrm{~N}$
$\mathrm{a}=\cos ^{-1} \mathrm{a} \frac{-648.89}{756.7242} \mathrm{~b}=149.03=149$
$\mathrm{b}=\cos ^{-1} \mathrm{a}_{\underline{756.7242}} \mathrm{O}=90.0$
$g=\cos ^{-1} a \frac{389.33}{756.7242} \mathrm{~b}=59.036=59.0$

Z


Ans.

Ans.

Ans.

Ans.

Ans:
$F_{R}=757 \mathrm{~N}$
$\mathrm{a}=149$
b $=90.0$
$\mathrm{g}=59.0$
$\mathbf{2 - 1 0 1}$. The tower is held in place by three cables. If the force of each cable acting on the tower is shown, determine the magnitude and coordinate direction angles $\mathrm{a}, \mathrm{b}, \mathrm{g}$, of the resultant force. Take $x=20 \mathrm{~m}, y=15 \mathrm{~m}$.

## Solution

$\mathbf{F}_{D A}=400 \mathrm{a}_{\underline{34.66}}{ }^{2} \mathbf{i}+{ }_{\underline{34.66}}^{15} \mathbf{j}-{ }_{34.66}^{24} \mathbf{k b ~ N}$
$\mathbf{F}_{D B}=800 \mathrm{a} \frac{-6}{25.06} \mathbf{i}+\frac{4}{25.06} \mathbf{j}-\frac{24}{25.06} \mathrm{~kb} \mathrm{~N}$
$\mathbf{F}_{D C}=600 \mathrm{a}_{34}^{16} \mathbf{i}+\frac{18}{34} \mathbf{j}-{ }_{34}^{24} \mathrm{~kb} \mathrm{~N}$
$\mathbf{F}_{R}=\mathbf{F}_{D A}+\mathbf{F}_{D B}+\mathbf{F}_{D C}$
$=5321.66 \mathbf{i}-16.82 \mathbf{j}-1466.71 \mathbf{k} 6 \mathrm{~N}$
$F_{R}=2(321.66)^{2}+(-16.82)^{2}+(-1466.71)^{2}$

$$
=1501.66 \mathrm{~N}=1.50 \mathrm{kN}
$$

$a=\cos ^{-1} \frac{321.66}{}{ }_{1501.66} b=77.6$
$b=\cos ^{-1} \frac{-16.82}{}{ }_{1501.66} b=90.6$
$g=\cos ^{-1} \frac{-1466.71}{}$
${ }^{a}{ }_{1501.66} \mathrm{~b}=168$


Ans.

Ans.

Ans.

Ans.

Ans:
$F_{R}=1.50 \mathrm{kN}$
$\mathrm{a}=77.6$
$\mathrm{b}=90.6$

## 2-102.

The guy wires are used to support the telephone pole. Represent the force in each wire in Cartesian vector form. Neglect the diameter of the pole.

## SOLUTION

## Unit Vector:

$$
\begin{aligned}
& \mathbf{r}_{\mathrm{AC}}=\{(-1-0) \mathbf{i}+(4-0) \mathbf{j}+(0-4) \mathbf{k}\} \mathrm{m}=\{-1 \mathbf{i}+4 \mathbf{j}-4 \mathbf{k}\} \mathrm{m} \\
& \\
& \mathrm{r}_{\mathrm{AC}}=2(-1)^{2}+4^{2}+(-4)^{2}=5.745 \mathrm{~m} \\
& \mathbf{u}_{\mathrm{AC}}=\frac{\mathbf{r}_{\mathrm{AC}}}{\mathrm{r}_{\mathrm{AC}}}=\frac{-1 \mathbf{i}+4 \mathbf{j}-4 \mathbf{k}}{5.745}=-0.1741 \mathbf{i}+0.6963 \mathbf{j}-0.6963 \mathbf{k} \\
& \mathbf{r}_{\mathrm{BD}}=\{(2-0) \mathbf{i}+(-3-0) \mathbf{j}+(0-5.5) \mathbf{k}\} \mathrm{m}=\{2 \mathbf{i}-3 \mathbf{j}-5.5 \mathbf{k}\} \mathrm{m} \\
& \mathrm{r}_{\mathrm{BD}}=22^{2}+(-3)^{2}+(-5.5)^{2}=6.576 \mathrm{~m} \\
& \mathbf{u}_{\mathrm{BD}}=\frac{\mathbf{r}_{\mathrm{BD}}}{\mathrm{r}_{\mathrm{BD}}}=\frac{2 \mathbf{i}-3 \mathbf{j}-5.5 \mathbf{k}}{6.576}=0.3041 \mathbf{i}-0.4562 \mathbf{j}-0.8363 \mathbf{k}
\end{aligned}
$$

## Force Vector:

$$
\begin{aligned}
\mathbf{F}_{\mathrm{A}}=\mathrm{F}_{\mathrm{A}} \mathbf{u}_{\mathrm{AC}} & =250\{-0.1741 \mathbf{i}+0.6963 \mathbf{j}-0.6963 \mathbf{k}\} \mathrm{N} \\
& =\{-43.52 \mathbf{i}+174.08 \mathbf{j}-174.08 \mathbf{k}\} \mathrm{N} \\
& =\{-43.5 \mathbf{i}+174 \mathbf{j}-174 \mathbf{k}\} \mathrm{N} \\
\mathbf{F}_{\mathrm{B}}=\mathrm{F}_{\mathrm{B}} \mathbf{u}_{\mathrm{BD}} & =175\{0.3041 \mathbf{i}+0.4562 \mathbf{j}-0.8363 \mathbf{k}\} \mathrm{N} \\
& =\{53.22 \mathbf{i}-79.83 \mathbf{j}-146.36 \mathbf{k}\} \mathrm{N} \\
& =\{53.2 \mathbf{i}-79.8 \mathbf{j}-146 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$


$x$

Ans.

Ans.
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$$
\mathbf{F}_{B}=\{53.2 \mathbf{i}-79.8 \mathbf{j}-146 \mathbf{k}\} \mathrm{N}
$$

## 2-103.

Determine the magnitude and coordinate direction angles of the resultant force acting at point $A$.

## SOLUTION

$$
\mathrm{a}=\cos ^{-1} \mathrm{a} \frac{157.4124}{315.7786} \mathrm{~b}=60.100^{\circ}=60.1^{\circ}
$$

$$
\mathrm{b}=\cos ^{-1} \mathrm{a} \frac{83.9389}{315.7786} \mathrm{~b}=74.585^{\circ}=74.6^{\circ}
$$

$$
g=\cos ^{-1} a \frac{-260.5607}{315.7786} b=145.60^{\circ}=146^{\circ}
$$

$$
\begin{aligned}
& \mathbf{r}_{\mathrm{AC}}=\{3 \mathbf{i}-0.5 \mathbf{j}-4 \mathbf{k}\} \mathrm{m} \\
& \left|\mathbf{r}_{\mathrm{AC}}\right|=23^{2}+(-0.5)^{2}+(-4)^{2}=225.25=5.02494 \\
& 3 \mathbf{i}-0.5 \mathbf{j}-4 \mathbf{k} \\
& \mathbf{F}_{2}=200 \mathrm{a} \quad 5.02494 \mathrm{~b}=(119.4044 \mathbf{i}-19.9007 \mathbf{j}-159.2059 \mathbf{k}) \\
& \mathbf{r}_{\mathrm{AB}}=\left(3 \cos 60^{\circ} \mathbf{i}+\left(1.5+3 \sin 60^{\circ}\right) \mathbf{j}-4 \mathbf{k}\right) \\
& \mathbf{r}_{\mathrm{AB}}=(1.5 \mathbf{i}+4.0981 \mathbf{j}+4 \mathbf{k}) \\
& \left|\mathbf{r}_{\mathrm{AB}}\right|=2(1.5)^{2}+(4.0981)^{2}+(-4)^{2}=5.9198 \\
& \mathbf{F}_{1}=150 \mathrm{a}^{1.5 \mathbf{i}+4.0981 \mathbf{j}-4 \mathbf{k}} \underset{5.9198}{ } \mathrm{~b}=(38.0079 \mathbf{i}+103.8396 \mathbf{j}-101.3545 \mathbf{k}) \\
& \mathbf{F}_{\mathrm{R}}=\mathbf{F}_{1}+\mathbf{F}_{2}=(157.4124 \mathbf{i}+83.9389 \mathbf{j}-260.5607 \mathbf{k}) \\
& \mathrm{F}_{\mathrm{R}}=2 \overline{(157.4124)^{2}+(83.9389)^{2}+(-260.5604)^{2}}=315.7786=316 \mathrm{~N}
\end{aligned}
$$



Ans.

Ans.

Ans.

Ans.

Ans:
$F_{R}=316 \mathrm{~N}$
$\mathrm{a}=60.1$
$\mathrm{b}=74.6$
$g=146$
*2-104. Two cables are used to secure the overhang boom in position and support the $1500-\mathrm{N}$ load. If the resultant force is directed along the boom from point $A$ towards $O$, determine the magnitudes of the resultant force and forces $\mathbf{F}_{B}$ and $\mathbf{F}_{C}$. Set $\mathrm{x}=3 \mathrm{~m}$ and $\mathrm{z}=2 \mathrm{~m}$.

## Solution

Force Vectors: The unit vectors $\mathrm{u}_{B}$ and $\mathrm{u}_{C}$ must be determined first. From Fig. $a$,

$\mathbf{u}_{B}=\underline{r}_{r_{B}}^{\underline{\mathbf{r}}_{\underline{B}}}=\frac{(-2-0) \mathbf{i}+(0-6) \mathbf{j}+(3-0) \mathbf{k}}{2(-2-0)^{2}+(0-6)^{2}+(3-0)^{2}}=-\frac{\underline{2}}{7} \mathbf{i}-\frac{6}{7} \mathbf{j}+\frac{\underline{3}}{7} \mathbf{k}$
$\mathbf{u}_{C}=\frac{\mathbf{r}_{C}}{r_{C}}=\frac{(3-0) \mathbf{i}+(0-6) \mathbf{j}+(2-0) \mathbf{k}}{2\left(\overline{(3-0)^{2}+(0-6)^{2}+(2-0)^{2}}\right.}=\frac{3}{7} \mathbf{i}-\frac{6}{7} \mathbf{j}+\frac{2}{7} \mathbf{k}$
Thus, the force vectors $\mathrm{F}_{B}$ and $\mathrm{F}_{C}$ are given by
$\mathbf{F}_{B}=F_{B} \mathbf{u}_{B}=-{ }_{7}^{2} F_{B} \mathbf{i}-{ }_{-}^{6} F_{B} \mathbf{j}+{ }_{-}^{3} F_{B} \mathbf{k}$
$\mathbf{F}_{\mathbf{C}}=F_{C} \mathbf{u}_{C}={ }_{7}^{3} F_{C} \mathbf{i}-{ }_{7}^{6} F_{C} \mathbf{j}+{ }_{7}^{2} F_{C} \mathbf{k}$
Since the resultant force $\mathrm{F}_{R}$ is directed along the negative $y$ axis, and the load $\mathbf{W}$ is directed along the $z$ axis, these two forces can be written as
$\mathbf{F}_{R}=-F_{R} \mathbf{j} \quad$ and $\quad \mathbf{W}=[-1500 \mathbf{k}] \mathrm{N}$
Resultant Force: The vector addition of $\mathrm{F}_{B}, \mathrm{~F}_{C}$, and $\mathbf{W}$ is equal to $\mathrm{F}_{R}$. Thus,
$\mathbf{F}_{R}=\mathbf{F}_{B}+\mathbf{F}_{C}+\underline{\mathbf{W}}$
$-F_{R} \mathbf{j}={ }^{2}{ }_{7}{ }_{7} F_{B} \mathbf{i}-{ }_{7}^{6} F_{B} \mathbf{j}+{ }_{7}{ }_{7} F_{-} \mathbf{k} \mathrm{b}+{ }_{-}^{\mathrm{a}_{7}} F_{C} \mathbf{i}-{ }_{7}{ }_{7} F_{C} \mathbf{j}+{ }_{7}{ }_{C}{ }_{C} \mathbf{k} \mathrm{~b}+(-1500 \mathbf{k})$
$-F_{R} \mathbf{j}=\mathrm{a}-{ }_{7}^{2} F_{B}+{ }_{7}^{3} F_{C} \mathrm{~b} \mathbf{i}+\mathrm{a}-{ }_{7}^{6} F_{B}-{ }_{7}^{6} F_{C} \mathrm{~b} \mathbf{j}+\mathrm{a}_{7}^{3} F_{B}+{ }_{7}^{2} F_{C}-1500 \mathrm{~b} \mathbf{k}$
Equating the $\mathbf{i}, \mathbf{j}$, and $\mathbf{k}$ components,
$0=-{ }_{7}^{2} F_{B}+{ }_{7}^{3} F_{C}$
$-F_{R}=-{ }_{7}^{6} F_{B}-{ }_{7}^{6} F_{C}$
$0={ }_{7}^{3} F_{B}+{ }_{7}^{2} F_{C}-1500$
Solving Eqs. (1), (2), and (3) yields
$F_{C}=1615.38 \mathrm{~N}=1.62 \mathrm{kN}$
Ans.
$F_{B}=2423.08 \mathrm{~N}=2.42 \mathrm{kN}$
Ans.

$F_{R}=3461.53 \mathrm{~N}=3.46 \mathrm{kN}$
Ans.

Ans:
$F_{C}=1.62 \mathrm{kN}$
$F_{B}=2.42 \mathrm{kN}$
$F_{R}-3.46 \mathrm{kN}$
$\mathbf{2 - 1 0 5}$. Two cables are used to secure the overhang boom in position and support the $1500-\mathrm{N}$ load. If the resultant force is directed along the boom from point $A$ towards $O$, determine the values of $x$ and $z$ for the coordinates of point $C$ and the magnitude of the resultant force. Set $\mathbf{F}_{B}=1610 \mathrm{~N}$ and $\mathbf{F}_{C}=2400 \mathrm{~N}$.

## Solution



$\mathbf{u}_{C}={\underset{C}{r}}_{\underline{\mathbf{r}}_{C}}^{{ }_{C}}=\frac{(x-0) \mathbf{i}+(0-6) \mathbf{j}+(z-0) \mathbf{k}}{2(x-0)^{2}+(0-6)^{2}+(z-}=\frac{x}{2 \overline{x^{2}+z^{2}+36}} \mathbf{i}-\frac{6}{2 x^{2}+z^{2}+36} \mathbf{j}+\frac{z}{2 x^{2}+z^{2}+36} \mathbf{k}$
Thus,
O) ${ }^{2}$
$\mathbf{F}_{B}=F_{B} \mathbf{u}_{B}=1610 \mathbf{a}-\frac{2}{7} \mathbf{i}-\frac{6}{7} \mathbf{j}+{ }^{3} \mathbf{k} \mathbf{k b}=3-460 \mathbf{i}-1380 \mathbf{j}+690 \mathbf{k} 4 \mathbf{N}$ $\qquad$

$$
\begin{aligned}
& \mathbf{F}_{C}=F_{C} \mathbf{u}_{C}=2400 \mathbf{a} \underset{2 x^{2}+z^{2}+36}{ } \mathbf{i}-\frac{6}{2 x^{2}+z^{2}+36}{ }^{\mathbf{j}}+\underset{x^{2}+z^{2}+36}{ }{ }^{\mathbf{b}} \\
& 2400 x 14400 \quad 2400 z \\
& =2{\overrightarrow{x^{2}}+z^{2}+36}_{\mathbf{i}}{ }^{-} \mathbf{2} \vec{x}^{2}+z^{2}+36 \mathbf{j}+2 \vec{x}^{2}+z^{2}+36
\end{aligned}
$$



Since the resultant force $\mathrm{F}_{R}$ is directed along the negative $y$ axis, and the load is directed along the $z$ axis, these two forces can be written as
$\mathbf{F}_{R}=-F_{R} \mathbf{j} \quad$ and $\quad \mathbf{W}=[-1500 \mathrm{k}] \mathrm{N}$

## Resultant Force:

$\mathbf{F}_{R}=\mathbf{F}_{B}+\mathbf{F}_{C}+\mathbf{W}$
$-F_{R \mathbf{j}}=(-460 \mathbf{i}-1380 \mathbf{j}+690 \mathbf{k})+\mathbf{a} \overline{2400 x} \overline{2 x^{2}+z^{2}+36} \mathbf{i}-\overline{2400} \overline{2 x^{2}+z^{2}+36} \mathbf{j}+\overline{2 x^{2}+z^{2}+36} \mathbf{k b}+(-1500 \mathbf{k})$
$2400 x$
$\qquad$ -460 bi - a
$-14400$
2400z
$-F_{B j}=\mathrm{a}$
a 690 $\qquad$ $+1380 \mathrm{~b} \mathbf{j}+$

- 1500 bk $2 \overline{x^{2}+z^{2}+36}$

$$
2 x^{2}+z^{2}+36
$$

$$
2 x^{2}+z^{2}+36
$$

Equating the $\mathbf{i}, \mathbf{j}$, and $\mathbf{k}$ components, $\qquad$
$2400 x \quad 2400 x$
$0={\frac{x^{2}+z^{2}+36}{}}^{-460} 2{\vec{x}^{2}+z^{2}+36}^{2}=460$
1440014400
$-F_{R}=-\mathrm{a} 2 \vec{x}^{2}+z^{2}+36+1380 \mathrm{~b} F_{R}=\mathrm{a} 2{\overrightarrow{x^{2}}+z^{2}+36}+1380 \mathrm{~b}$
$2400 z 2400 z$
$0=690+2 \vec{x}^{2}+\vec{z}^{2}+36-15002{\overrightarrow{x^{2}}+z^{2}+36}^{-1510}$

## 2-105 (Continued)

Dividing Eq. (1) by Eq. (3), yields
$x=0.5679$
Substituting Eq. (4) into Eq. (1), and solving
$z=2.197 \mathrm{~m}=2.20 \mathrm{~m}$
Ans.
Substituting $z=2.197 \mathrm{~m}$ into Eq. (4), yields,
$x=1.248 \mathrm{~m}=1.25 \mathrm{~m}$
Substituting $x=1.248 \mathrm{~m}$ and $z=2.197 \mathrm{~m}$ into Eq. (2), yields
$F_{R}=3591.85 \mathrm{~N}=3.59 \mathrm{kN}$
Ans.

Ans.

Ans:
$Z=2.20 \mathrm{~m} X$
$=1.25 \mathrm{~m} F_{R}$
$=3.59 \mathrm{kN}$

2-106.

Giyen the three vectors $\mathbf{A}, \mathbf{B}$, and $\mathbf{D}$, show that $\mathbf{A}^{\dagger}(\mathbf{B}+\mathbf{D})=\left(\mathbf{A}^{\dagger} \mathbf{B}\right)+\left(\mathbf{A}^{i} \mathbf{D}\right)$.

## SOLUTION

Since the component of $(\mathbf{B}+\mathbf{D})$ is equal to the sum of the components of $\mathbf{B}$ and D, then

$$
\mathbf{A}^{\ddagger}(\mathbf{B}+\mathbf{D})=\mathbf{A}^{\ddagger} \mathbf{B}+\mathbf{A}^{\ddagger} \mathbf{D}
$$

(QED)

Also,

$$
\begin{aligned}
\mathbf{A}^{\ddagger}(\mathbf{B}+\mathbf{D}) & =\left(\mathrm{A}_{\mathrm{x}} \mathbf{i}+\mathrm{A}_{\mathrm{y}} \mathbf{j}+\mathrm{A}_{\mathrm{z}} \mathbf{k}\right)^{\dagger}\left[\left(\mathrm{B}_{\mathrm{x}}+\mathrm{D}_{\mathrm{x}}\right) \mathbf{i}+\left(\mathrm{B}_{\mathrm{y}}+\mathrm{D}_{\mathrm{y}}\right) \mathbf{j}+\left(\mathrm{B}_{\mathrm{z}}+\mathrm{D}_{\mathrm{z}}\right) \mathbf{k}\right] \\
& =\mathrm{A}_{\mathrm{x}}\left(\mathrm{~B}_{\mathrm{x}}+\mathrm{D}_{\mathrm{x}}\right)+\mathrm{A}_{\mathrm{y}}\left(\mathrm{~B}_{\mathrm{y}}+\mathrm{D}_{\mathrm{y}}\right)+\mathrm{A}_{\mathrm{z}}\left(\mathrm{~B}_{\mathrm{z}}+\mathrm{D}_{\mathrm{z}}\right) \\
& =\left(\mathrm{A}_{\mathrm{x}} \mathrm{~B}_{\mathrm{x}}+\mathrm{A}_{\mathrm{y}} \mathrm{~B}_{\mathrm{y}}+\mathrm{A}_{\mathrm{z}} \mathrm{~B}_{\mathrm{z}}\right)+\left(\mathrm{A}_{\mathrm{x}} \mathrm{D}_{\mathrm{x}}+\mathrm{A}_{\mathrm{y}} \mathrm{D}_{\mathrm{y}}+\mathrm{A}_{\mathrm{z}} \mathrm{D}_{\mathrm{z}}\right) \\
& =\left(\mathbf{A}^{\dagger} \mathbf{B}\right)+\left(\mathbf{A}^{\dagger} \mathbf{D}\right)
\end{aligned} \text { (QED)}
$$



2-107. Determine the design angle $u\left(0^{\circ} \ldots \mathrm{u} \ldots 90^{\circ}\right)$ for
strut $A B$ so that the $400-\mathrm{N}$ horizontal force has a component of 500 N directed from $A$ towards $C$. What is the component of force acting along member $A B$ ? Take $\mathbf{f}=40^{\circ}$.


## Solution

Parallelogram Law: The parallelogram law of addition is shown in Fig. (a).
Trigonometry: Using law of sines [Fig. (b)], we have

$$
\begin{aligned}
\sin u & =\sin 40 \\
500 & =-400- \\
\sin u & =0.8035 \\
u & =53.46=53.5
\end{aligned}
$$

Thus, $\mathbf{f}=180-40-53.46=86.54$
Using law of sines [Fig. (b)]

$$
\begin{aligned}
\frac{F_{A B}}{\sin 86.54} & =\frac{400}{\sin 40} \\
F_{A B} & =621 \mathrm{~N}
\end{aligned}
$$

Ans.

(b)

## Ans:

$\mathrm{u}=53.5$
$F_{A B}=621 \mathrm{~N}$
*2-108.
Determine the projection of the force $\mathbf{F}$ along the pole.

## SOLUTION

$\operatorname{Proj} F=\mathbf{F}^{\ddagger} \mathbf{u}_{\mathrm{a}}=12 \mathbf{i}+4 \mathbf{j}+10 \mathbf{k} 2^{\ddagger} \mathrm{a}_{\underline{3}}^{2} \mathbf{i}+{ }_{\underline{3}}^{2} \mathbf{j}-{ }_{-}^{1} \mathbf{k} \mathrm{~b}$
Proj $\mathrm{F}=0.667 \mathrm{kN}$


Ans:
Proj $\mathrm{F}=0.667 \mathrm{kN}$

## 2-109.

Determine the angle $u$ between the sides of the triangular plate.

## SOLUTION

A
$\mathbf{r}_{\mathrm{AC}}=53 \mathbf{i}+4 \mathbf{j}-1 \mathbf{k} 6 \mathrm{~m}$
$\mathbf{r}_{\mathrm{AB}}=52 \mathbf{j}+3 \mathbf{k} 6 \mathrm{~m}$
$r_{A B}=2 \overline{122^{2}+132^{2}}=3.6056 \mathrm{~m}$
$\mathbf{r}_{\mathrm{AC}}{ }^{\dagger} \mathbf{r}_{\mathrm{AB}}=0+4122+1-12132=5$
$u=\cos ^{-1}\binom{\underline{\mathbf{r}_{A C}}-\underline{\mathbf{r}_{A B}} \underline{r^{\prime}}}{\mathrm{r}_{\mathrm{AC}} \mathrm{r}_{\mathrm{AB}}}=\cos ^{-1} \frac{15.0990213 .60562}{5}$
$u=74.219^{\circ}=74.2^{\circ}$


Ans.
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Ans:
$\mathrm{u}=74.2$

## 2-110.

Determine the length of side $B C$ of the triangular plate. Solve the problem by finding the magnitude of $\mathbf{r}_{B C}$; then check the result by first finding $\theta, r_{A B}$, and $r_{A C}$ and then using the cosine law.

## SOLUTION

$$
\begin{aligned}
& \mathbf{r}_{\mathrm{BC}}=\{3 \mathbf{i}+2 \mathbf{j}-4 \mathbf{k}\} \mathrm{m} \\
& \mathrm{r}_{\mathrm{BC}}=2(3)^{2}+(2)^{2}+(-4)^{2}=5.39 \mathrm{~m}
\end{aligned}
$$

Also,

$$
\mathbf{r}_{\mathrm{AC}}=\{3 \mathbf{i}+4 \mathbf{j}-1 \mathbf{k}\} \mathrm{m}
$$

$r_{A C}=2(3)^{2}+(4)^{2}+(-1)^{2}=5.0990 \mathrm{~m}$
$\mathbf{r}_{\mathrm{AB}}=\{2 \mathbf{j}+3 \mathbf{k}\} \mathrm{m}$
$r_{A B}=2(2)^{2}+(3)^{2}=3.6056 \mathrm{~m}$
$\mathbf{r}_{\mathrm{AC}}{ }^{\dagger} \mathbf{r}_{\mathrm{AB}}=0+4(2)+(-1)(3)=5$
$\mathrm{u}=\cos ^{-1} \mathrm{a} \frac{\mathbf{r}_{\mathrm{AC}}}{\mathrm{r}_{\mathrm{AC}}}-\frac{\mathrm{r}_{\mathrm{AB}}}{\mathrm{r}_{\mathrm{AB}}} \mathrm{b}=\cos ^{-1} \frac{5}{(5.0990)(3.6056)}$
$\mathrm{u}=74.219^{\circ}$
$r_{B C}=2(5.0990)^{2}+(3.6056)^{2}-2(5.0990)(3.6056) \cos 74.219^{\circ}$
$r_{B C}=5.39 \mathrm{~m}$


Ans.
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$$
r_{B C}=5.39 \mathrm{~m}
$$

2-111. Determine the magnitude of the projected component of $\mathbf{r}_{1}$ along $\mathbf{r}_{2}$, and the projection of $\mathbf{r}_{2}$ along $\mathbf{r}_{1}$.

## SOLUTION

Given:

| $r_{1}$ | 9 m |
| :--- | :--- |
| $r_{2}$ | 6 m |

$60^{\circ}$
$45^{\circ}$
$120^{\circ}$
$30^{\circ}$
$40^{\circ}$

Write the vectors and unit vectors


| The magnitude of the projection of $\mathbf{r}_{1}$ along $\mathbf{r}_{\mathbf{2}}$. | $\mathbf{r}_{\mathbf{1} \mathbf{v}}$ | 2.99 m |
| :--- | :--- | :--- | Ans. $\mathbf{u}_{2}$

Ans.
The magnitude of the projection of $\mathbf{r}_{2}$ along $\mathbf{r}_{1}$
$\mathbf{r}_{2 v}$
$\mathbf{u}_{1}$

## Ans:

$\left|r_{1}{ }_{\mathrm{l}_{2}}=2.99 \mathrm{~m},\right| r_{2}{ }^{\dagger}{ }_{\mathrm{l}_{1}}=1.99 \mathrm{~m}$
*2-112.

Determine the angle between the two cords.

## SOLUTION

## Given:

a 3 m
b $\quad 2 \mathrm{~m}$
c 6 m
d 3 m
e 4 m

|  | $b$ |  | 0 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{r}_{\mathbf{A C}}$ | $a \mathrm{~m}$ | $\mathbf{r}_{\mathbf{A B}} \quad d \mathrm{~m}$ |  |

c
$\mathbf{r}_{\mathrm{AB}}$

$64.6^{\circ}$
Ans.

## 2-113.

Determine the magnitudes of the components of $\mathrm{F}=600 \mathrm{~N}$ acting along and perpendicular to segment $D E$ of the pipe assembly.

## SOLUTION

Unit Vectors: The unit vectors $\mathbf{u}_{E B}$ and $\mathbf{u}_{E D}$ must be determined first. From Fig. $a$,
$\mathbf{u}_{\mathrm{EB}}=\frac{\mathbf{r}_{\mathrm{EB}}}{\mathrm{r}_{\mathrm{EB}}}=\frac{(0-4) \mathbf{i}+(2-5) \mathbf{j}+[0-(-2)] \mathbf{k}}{2(0-4)^{2}+(2-5)^{2}+[0-(-2)]^{2}}=-0.7428 \mathbf{i}-0.5571 \mathbf{j}+0.3714 \mathbf{k}$

$\mathbf{u}_{\mathrm{ED}}=-\mathbf{j}$

Thus, the force vector $\mathbf{F}$ is given by
$\left.\mathbf{F}=F \mathbf{u}_{\mathrm{EB}}=600 \mathrm{~A}-0.7428 \mathbf{i}-0.5571 \mathbf{j}+0.3714 \mathbf{k}\right)=[-445.66 \mathbf{i}-334.25 \mathbf{j}+222.83 \mathbf{k}] \mathrm{N}$
Vector Dot Product: The magnitude of the component of $\mathbf{F}$ parallel to segment $D E$ of the pipe assembly is

$$
\begin{aligned}
\left(\mathrm{F}_{\mathrm{ED}}\right)_{\text {paral }}=\mathbf{F}^{\ddagger} \mathbf{u}_{\mathrm{ED}} & =A-445.66 \mathbf{i}-334.25 \mathbf{j}+222.83 \mathbf{k} \mathbb{B}^{\ddagger} A-\mathbf{j} B \\
& =(-445.66)(0)+(-334.25)(-1)+(222.83)(0) \\
& =334.25=334 \mathrm{~N}
\end{aligned}
$$

Ans.

The component of $\mathbf{F}$ perpendicular to segment $D E$ of the pipe assembly is

$$
\left(\mathrm{F}_{\mathrm{ED}}\right)_{\text {per }}=2 \mathrm{~F}^{2}-\left(\mathrm{F}_{\mathrm{ED}}\right)_{\text {parall }^{2}}=2600^{2}-334.25^{2}=498
$$

Ans.

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$\left(F_{E D}\right)=334 \mathrm{~N}$
$\left(F_{E D}\right)_{\#}=498 \mathrm{~N}$

## 2-114.

Determine the angle $u$ between the two cables.
 $B(0,3,0)$ and $C(-2,3,4) \mathrm{m}$ respectively. Thus, the unit vectors along $A B$ and $A C$ are
$\mathbf{u}_{A B}=\frac{(0-2) \mathbf{i}+[3-(-3)] \mathbf{j}+(0-3) \mathbf{k}}{2(0-2)^{2}+[3-(-3)]^{2}+(0-3)^{2}}=-{ }_{7}^{2} \mathbf{i}+{ }_{7}^{6} \mathbf{j}-{ }_{7}^{3} \mathbf{k}$
$\mathbf{u}_{A C}=\frac{(-2-2) \mathbf{i}+[3-(-3)] \mathbf{j}+(4-3) \mathbf{k}}{\frac{2(-2-2)^{2}+[3-(-3)]^{2}+(4-}{3)^{2}}}=-\frac{4}{25 \overline{5}} \mathbf{i}+\frac{6}{2 \overline{53}} \mathbf{j}+\frac{1}{253} \mathbf{k}$
The Angle U Between $A B$ and $A C$.

$$
\begin{aligned}
& =\begin{array}{c}
41 \\
72 \overline{53}
\end{array}
\end{aligned}
$$

Then

$$
\mathrm{u}=\cos ^{-1}\left(\mathbf{u}_{A B}{ }^{\dagger} \mathbf{u}_{A C}\right)=\cos ^{-1} \frac{41}{7253} \mathrm{~b}=36.43=36.4
$$

Ans.

## Ans: <br> $u=36.4$

## 2-115.

Determine the magnitude of the projection of the force $\mathbf{F}_{\mathbf{1}}$ along cable $A C$.

## Solution



$$
\mathbf{u}_{A B}=\frac{(0-2) \mathbf{i}+[3-(-3)] \mathbf{j}+(0-3) \mathbf{k}}{2(0-2)^{2}+[3-(-3)]^{2}+(0-3)^{2}}=-\frac{2}{7} \mathbf{i}+{ }_{7}^{6} \mathbf{j}-{ }_{7}^{3} \mathbf{k}
$$

$$
\mathbf{u}_{A C}=\frac{(-2-2) \mathbf{i}+[3-(-3)] \mathbf{j}+(4-3) \mathbf{k}}{\frac{2 \overline{(-2-2)^{2}+[3-(-3)]^{2}+(4-}}{3)^{2}}}=-\frac{4}{2 \overline{53}} \mathbf{i}+\frac{6}{2 \overline{53}} \mathbf{j}+\frac{1}{2 \overline{53}} \mathbf{k}
$$

Force Vector, For $\mathbf{F}_{1}$,

$$
\mathbf{F}_{1}=\mathbf{F}_{1} \mathbf{u}_{A B}=70 \mathrm{a}-\frac{2}{7} \mathbf{i}+{ }_{7}^{6} \mathbf{j}-\frac{3}{7} \mathbf{k} \mathrm{~b}=\{-20 \mathbf{i}+60 \mathbf{j}-3 \mathrm{O} \mathbf{k}\} \mathrm{N}
$$

Projected Component of $\mathbf{F}_{\mathbf{1}}$. Along $A C$, it is

$$
\begin{aligned}
& 4 \\
& 6 \\
& 1 \\
& =(-20) a-2 \overline{53}^{b+60 a} 2 \overline{53}^{b+(-30) a} 2 \overline{53}^{b} \\
& =56.32 \mathrm{~N}=56.3 \mathrm{~N}
\end{aligned}
$$

Ans.
The positive sign indicates that this component points in the same direction as $\mathbf{u}_{A C}$.
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Ans:
$\left(F_{1}\right)_{A C}=56.3 \mathrm{~N}$
*2-116. A force of $F=80 \mathrm{~N}$ is applied to the handle of the wrench. Determine the angle u between the tail of the force and the handle $A B$.

## Solution

## Given:



| $a$ | 300 mm |
| :--- | :--- |
| $b$ | 500 mm |
| $F$ | 80 N |
| 1 | $30^{\circ}$ |
| 2 | $45^{\circ}$ |



[^3]Ans.
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## 2-117.

Determine the angle u between the cables $A B$ and $A C$.
Z

## Solution

Unit Vectors. Here, the coordinates of points $A, B$ and $C$ are $A(6,0,0) \mathrm{m}$, $B(0,-1,2) \mathrm{m}$ and $C(0,1,3)$ respectively. Thus, the unit vectors along $A B$ and $A C$ are


The Angle u Between $A B$ and $A C$. $\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
\begin{aligned}
& \mathbf{u}_{A B}^{\dagger} \mathbf{u}_{A C}=\mathrm{a}-\frac{6}{2 \overline{41}} \mathbf{i}-\frac{1}{2 \overline{41}} \mathbf{j}+\frac{2}{2 \overline{41}} \mathbf{k b}^{\ddagger} \mathrm{a}-\frac{6}{2 \overline{46}} \mathbf{i}+\frac{1}{2 \overline{46}} \mathbf{j}+\frac{3}{2 \overline{46}} \mathbf{k b}
\end{aligned}
$$

$$
\begin{aligned}
& =\frac{41}{2 \overline{1886}}
\end{aligned}
$$

Then

$$
\mathrm{u}=\cos ^{-1}\left(U_{A B}^{\dagger} U_{A C}\right)=\cos ^{-1} \mathrm{a} \frac{41}{21886} \mathrm{~b}=19.24998=19.2
$$

Ans.

Ans:
$u=19.2$

2-118.

Determine the magnitude of the projected component of the
z
force $\mathbf{F}=\{400 \mathbf{i}-200 \mathbf{j}+500 \mathbf{k}\} \mathrm{N}$ acting along the cable $B A$.
F
$\qquad$

Unit Vector. Here, the coordinates of points $A$ and $B$ are $A(6,0,0) \mathrm{m}$ and $B(0,-1,2) \mathrm{m}$ respectively. Thus the unit vector along $B A$ is $\underline{\underline{r}}_{\underline{B A}} \quad \underline{(6-0) \mathbf{i}+[0-(-1)] \mathbf{j}+(0-}$ $\qquad$
6 $\qquad$

## Solution



$$
=\quad-\mathbf{i}
$$

$\mathbf{u}_{B A}=\underset{B A}{\mathbf{r}}=\overline{2(6-0)^{2}+[0-(-1)]^{2}+(0-2)^{2}}$

$$
{ }_{241}^{-\mathbf{j}}
$$

$$
\mathbf{k}
$$

$$
-\quad-k
$$

$\qquad$ -
Projected component of $\mathbf{F}$. Along $B A$, it is
$=400 a \overline{41}^{b}+(-200) a \overline{211}^{b}+500 a-2 \overline{41}^{b}$
$=187.41 \mathrm{~N}=187 \mathrm{~N}$
Ans.
The positive sign indicates that this component points in the same direction as $\mathbf{u}_{B A}$.

> 6
> 1
> 2
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> Ans:
> $F_{B A}=187 \mathrm{~N}$

## 2-119.

Determine the magnitude of the projected component of the Z force $\mathbf{F}=\{400 \mathbf{i}-200 \mathbf{j}+500 \mathbf{k}\} \mathrm{N}$ acting along the cable $C A$.

## Solution

Unit Vector. Here, the coordinates of points $A$ and $C$ are $A(6,0,0) \mathrm{m}$ and $C(0,1,3) \mathrm{m}$ respectively. Thus, the unit vector along $C A$ is


Projected component of $\mathbf{F}$. Along $C A$, it is

$$
\begin{aligned}
& =400 \mathrm{a} 2 \overline{46}^{b}+(-200) a-2 \overline{46}^{b}+500 a-2 \overline{46}^{b} \\
& =162.19 \mathrm{~N}=162 \mathrm{~N}
\end{aligned}
$$

Ans.
The positive sign indicates that this component points in the same direction as $\mathbf{u}_{C A}$.
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> Ans:
> $F_{C A}=162 \mathrm{~N}$
*2-120. Determine the magnitude of the projected component of force $\mathbf{F}_{A B}$ acting along the $z$ axis.

## Solution

Unit Vector: The unit vector $\mathbf{u}_{A B}$ must be determined first. From Fig. $a$,

$$
\mathbf{u}_{A B}=\frac{\mathbf{r}_{A B}}{r_{A B}}=\frac{(4.5-0) \mathbf{i}+(-3-0) \mathbf{j}+(0-9) \mathbf{k}}{\sqrt{(4.5-0)^{2}+(-3-0)^{2}+(0-9)^{2}}}=\frac{3}{7} \mathbf{i}-\frac{2}{7} \mathbf{j}-\frac{6}{7} \mathbf{k}
$$



$$
\begin{aligned}
& \text { Thus, the force vector } \mathbf{F}_{A B} \text { is given by } \\
& \qquad \mathbf{F}_{A B}=\mathbf{F}_{A B} \mathbf{u}_{A B}=3.5\left(\begin{array}{l}
\overline{3}{ }_{7} \mathbf{i}-{ }_{7}^{\overline{2}} \mathbf{j}-{ }_{7}^{\overline{6}} \mathbf{k}
\end{array}\right)=\{1.5 \mathbf{i}-1 \mathbf{j}-3 \mathbf{k}\} \mathrm{kN}
\end{aligned}
$$

Vector Dot Product: The projected component of $\mathbf{F}_{A B}$ along the $z$ axis is

$$
\begin{aligned}
\left(F_{A B}\right)_{z} & =\mathbf{F}_{A B} \cdot \mathbf{k}=(1.5 \mathbf{i}-1 \mathbf{j}-3 \mathbf{k}) \cdot \mathbf{k} \\
& =-3 \mathrm{kN}
\end{aligned}
$$

The negative sign indicates that $\left(F_{A B}\right)_{z}$ is directed towards the negative $z$ axis. Thus

$$
\left(F_{A B}\right)_{z}=3 \mathrm{kN}
$$



2-121. Determine the magnitude of the projected component of force $\mathbf{F}_{A C}$ acting along the $z$ axis.

## Solution



Unit Vector: The unit vector $\mathbf{u}_{A C}$ must be determined first. From Fig. $a$,

$$
\mathbf{u}_{A C}=\frac{\mathbf{r}_{A C}}{r_{A C}}=\frac{\left(3 \sin 30^{\circ}-0\right) \mathbf{i}+\left(3 \cos 30^{\circ}-0\right) \mathbf{j}+(0-9) \mathbf{k}}{\sqrt{\left(3 \sin 30^{\circ}-0\right)^{2}+\left(3 \cos 30^{\circ}-0\right)^{2}+(0-9)^{2}}}=0.1581 \mathbf{i}+0.2739 \mathbf{j}-0.9487 \mathbf{k}
$$

Thus, the force vector $\mathbf{F}_{A C}$ is given by

$$
\mathbf{F}_{A C}=\mathbf{F}_{A C} \mathbf{u}_{A C}=3(0.1581 \mathbf{i}+0.2739 \mathbf{j}-0.9487 \mathbf{k})=\{0.4743 \mathbf{i}+0.8217 \mathbf{j}-2.8461 \mathbf{k}\} \mathrm{kN}
$$

Vector Dot Product: The projected component of $\mathbf{F}_{A C}$ along the $z$ axis is

$$
\begin{aligned}
\left(F_{A C}\right)_{z} & =\mathbf{F}_{A C} \cdot \mathbf{k}=(0.4743 \mathbf{i}+0.8217 \mathbf{j}-2.8461 \mathbf{k}) \cdot \mathbf{k} \\
& =-2.8461 \mathrm{kN}
\end{aligned}
$$

The negative sign indicates that $\left(F_{A C}\right)_{z}$ is directed towards the negative $z$ axis. Thus

$$
\left(F_{A C}\right)_{z}=2.846 \mathrm{kN} \quad \text { Ans. }
$$



Ans:
$1 F_{A C} 2_{z}=2.846 \mathrm{kN}$

2-122.
Determine the components of $\mathbf{F}$ that act along rod $A C$ and perpendicular to it. Point $B$ is located at the midpoint of the rod.

## SOLUTION

$\mathbf{r}_{\mathrm{AC}}=(-3 \mathbf{i}+4 \mathbf{j}-4 \mathbf{k}), \quad \mathrm{r}_{\mathrm{AC}}=2 \underline{(-3)^{2}+4^{2}+(-4)^{2}=2 \underline{41} \mathrm{~m}}$
$\mathbf{r}_{\mathrm{AB}}=\frac{\mathbf{r}_{\mathrm{AC}}}{2}=\frac{-3 \mathbf{i}+4 \mathbf{j}+4 \mathbf{k}}{2}=-1.5 \mathbf{i}+2 \mathbf{j}-2 \mathbf{k}$
$\mathbf{r}_{\mathrm{AD}}=\mathbf{r}_{\mathrm{AB}}+\mathbf{r}_{\mathrm{BD}}$
$\mathbf{r}_{\mathrm{BD}}=\mathbf{r}_{\mathrm{AD}}-\mathbf{r}_{\mathrm{AB}}$
$=(4 \mathbf{i}+6 \mathbf{j}-4 \mathbf{k})-(-1.5 \mathbf{i}+2 \mathbf{j}-2 \mathbf{k})$
$=\{5.5 \mathbf{i}+4 \mathbf{j}-2 \mathbf{k}\} \mathrm{m}$
$r_{B D}=2(5.5)^{2}+(4)^{2}+(-2)^{2}=7.0887 m$
$\mathbf{F}=600 \mathrm{a} \mathrm{a}_{\mathrm{r}_{\mathrm{BD}}}^{\mathrm{r}_{\mathrm{BD}}} \mathrm{b}=465.528 \mathbf{i}+338.5659 \mathbf{j}-169.2829 \mathbf{k}$

Component of $\mathbf{F}$ along $\mathbf{r}_{\mathrm{AC}}$ is $\mathbf{F}_{| |}$
$\mathrm{F}_{| |}=\frac{\mathbf{F}^{\dagger} \underline{r}_{\mathrm{AC}}}{\mathrm{r}_{\mathrm{AC}}}=\frac{(465.528 \mathbf{i}+338.5659 \mathbf{j}-169.2829 \mathbf{k})^{\ddagger}(-3 \mathbf{i}+4 \mathbf{j}-}{\frac{4 \mathbf{k})}{241}}$
$\mathrm{F}_{| |}=99.1408=99.1 \mathrm{~N}$
$\perp$

## Ans.

Ans.
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$$
\begin{aligned}
& F_{\| \mid}=99.1 \mathrm{~N} \\
& F_{\#}=592 \mathrm{~N}
\end{aligned}
$$

## 2-123.

Determine the components of $\mathbf{F}$ that act along rod $A C$ and perpendicular to it. Point $B$ is located 3 m along the rod from end $C$.

## SOLUTION

$$
\begin{aligned}
\mathbf{r}_{\mathrm{CA}} & =3 \mathbf{i}-4 \mathbf{j}+4 \mathbf{k} \\
\mathrm{r}_{\mathrm{CA}} & =6.403124 \\
\mathbf{r}_{\mathrm{CB}} & =\begin{array}{c}
3.403124
\end{array}\left(\mathbf{r}_{\mathrm{CA}}\right)=1.40556 \mathbf{i}-1.874085 \mathbf{j}+1.874085 \mathbf{k} \\
\mathbf{r}_{\mathrm{OB}} & =\mathbf{r}_{\mathrm{OC}}+\mathbf{r}_{\mathrm{CB}} \\
& =-3 \mathbf{i}+4 \mathbf{j}+\mathbf{r}_{\mathrm{CB}} \\
& =-1.59444 \mathbf{i}+2.1259 \mathbf{j}+1.874085 \mathbf{k} \\
\mathbf{r}_{\mathrm{OD}} & =\mathbf{r}_{\mathrm{OB}}+\mathbf{r}_{\mathrm{BD}} \\
\mathbf{r}_{\mathrm{BD}} & =\mathbf{r}_{\mathrm{OD}}-\mathbf{r}_{\mathrm{OB}}=(4 \mathbf{i}+6 \mathbf{j})-\mathbf{r}_{\mathrm{OB}} \\
& =5.5944 \mathbf{i}+3.8741 \mathbf{j}-1.874085 \mathbf{k} \\
\mathbf{r}_{\mathrm{BD}} & =2(5.5944)^{2}+(3.8741)^{2}+(-1.874085)^{2}=7.0582 \\
\mathbf{F} & =600\left(\frac{\mathbf{r}_{\mathrm{BD}}}{\mathrm{r}_{\mathrm{BD}}}\right)=475.568 \mathbf{i}+329.326 \mathbf{j}-159.311 \mathbf{k} \\
\mathbf{r}_{\mathrm{AC}} & =(-3 \mathbf{i}+4 \mathbf{j}-4 \mathbf{k}), \quad \mathrm{r}_{\mathrm{AC}}=2 \overline{41}
\end{aligned}
$$

Component of $\mathbf{F}$ along $\mathbf{r}_{\mathrm{AC}}$ is $\mathbf{F}_{| |}$
$\mathrm{F}_{\|}=\frac{\mathbf{F}^{\dagger} \mathbf{r}_{\mathrm{AC}}}{\mathrm{r}_{\mathrm{AC}}}=\frac{(475.568 \mathbf{i}+329.326 \mathbf{j}-159.311 \mathbf{k})^{\frac{1}{2}}(-3 \mathbf{i}+4 \mathbf{j}-}{\frac{4 \mathbf{k})}{241}}$
$\mathrm{F}_{| |}=82.4351=82.4 \mathrm{~N}$

Component of $\mathbf{F}$ perpendicular to $\mathbf{r}_{\mathrm{AC}}$ is $\mathbf{F}$
$\mathrm{F}^{2}+\mathrm{F}_{\dagger}^{2}=\mathrm{F}^{2}=600^{2}$
$F^{2}=600^{2}-82.4351^{2}$
$\mathrm{F}^{\perp}=594 \mathrm{~N}$


Ans.

Ans.

Ans:
$F_{\}}=82.4 \mathrm{~N}$
$F_{\#}-592 \mathrm{~N}$
*2-124.
Determine the magnitudes of the projected components of the force $\mathbf{F}=[60 \mathbf{i}+12 \mathbf{j}-40 \mathbf{k}] \mathbf{N}$ along the cables $A B$ and $A C$.

## Solution

$$
\begin{aligned}
\mathbf{F}= & \{60 \mathbf{i}+12 \mathbf{j}-40 \mathbf{k}\} \mathbf{N} \\
\mathbf{u}_{A B} & =\begin{array}{c}
-3 \mathbf{i}-0.75 \mathbf{j}+1 \mathbf{k} \\
\mathbf{1}(-3)^{2}+(-0.75)^{2}+(1)^{2}
\end{array} \\
= & -0.9231 \mathbf{i}-0.2308 \mathbf{j}+0.3077 \mathbf{k} \\
\mathbf{u}_{A C} & =\begin{array}{c}
-3 \mathbf{i}+1 \mathbf{j}+1.5 \mathbf{k} \\
\mathbf{1}(-3)^{2}+(1)^{2}+(1.5)^{2}
\end{array} \\
& =-0.8571 \mathbf{i}+0.2857 \mathbf{j}+0.4286 \mathbf{k}
\end{aligned}
$$

Proj $F_{A B}=\mathbf{F}^{\dagger} \mathbf{u}_{A B}=(60)(-0.9231)+(12)(-0.2308)+(-40)(0.3077)$

$$
=-70.46 \mathrm{~N}
$$

$\left|\operatorname{Proj} F_{A B}\right|=70.5 \mathrm{~N}$
Proj $F_{A C}=\mathbf{F}^{\ddagger} \mathbf{u}_{A C}=(60)(-0.8571)+(12)(0.2857)+(-40)(0.4286)$

$$
=-65.14 \mathrm{~N}
$$

$\left|\operatorname{Proj} F_{A C}\right|=65.1 \mathrm{~N}$


Ans.

Ans.

## Ans:

$\left|\operatorname{Proj} F_{A B}\right|=70.5 \mathrm{~N}$
$\left|\operatorname{Proj} F_{A C}\right|=65.1 \mathrm{~N}$

## 2-125.

Determine the angle u between cables $A B$ and $A C$.

## Solution

$\mathbf{r}_{A B}=\{-3 \mathbf{i}-0.75 \mathbf{j}+1 \mathbf{k}\} \mathrm{m}$
$r_{A B}=2(-3)^{2}+(-0.75)^{2}+(1)^{2}=3.25 \mathrm{~m}$
$\mathbf{r}_{A C}=\{-3 \mathbf{i}+1 \mathbf{j}+1.5 \mathbf{k}\} \mathrm{m}$
$r_{A C}=2(-3)^{2}+(1)^{2}+(1.5)^{2}=3.50 \mathrm{~m}$
$\mathbf{r}_{A B}{ }^{\dagger} \mathbf{r}_{A C}=(-3)(-3)+(-0.75)(1)+(1)(1.5)=9.75$
$\mathrm{u}=\cos ^{-1} \mathrm{a} \frac{\mathbf{r}_{A B}}{r_{A B}} \underline{\underline{\mathbf{r}}_{A C}} \underline{\mathrm{~b}}=\cos ^{-1} \mathrm{a} \frac{9.75}{(3.25)(3.50)} \mathrm{b}$
$r_{A C}$
$\mathrm{u}=31.0$


Ans.

## 2-126.

Determine the angles $u$ and $\mathbf{f}$ made between the axes $O A$ of the flag pole and $A B$ and $A C$, respectively, of each cable.

## SOLUTION

| $\mathbf{r}_{\mathrm{AC}}=\{-2 \mathbf{i}-4 \mathbf{j}+1 \mathbf{k}\} \mathrm{m} ;$ | $\mathrm{r}_{\mathrm{AC}}=4.58 \mathrm{~m}$ |
| :--- | :--- |
| $\mathbf{r}_{\mathrm{AB}}=\{1.5 \mathbf{i}-4 \mathbf{j}+3 \mathbf{k}\} \mathrm{m} ;$ | $\mathrm{r}_{\mathrm{AB}}=5.22 \mathrm{~m}$ |
| $\mathbf{r}_{\mathrm{AO}}=\{-4 \mathbf{j}-3 \mathbf{k}\} \mathrm{m} ;$ | $\mathrm{r}_{\mathrm{AO}}=5.00$ |

m
$\mathbf{r}_{\mathrm{AB}}{ }^{\dagger} \mathbf{r}_{\mathrm{AO}}=(1.5)(0)+(-4)(-4)+(3)(-3)=7$
$u=\cos ^{-1} \phi \frac{\mathbf{r}_{\mathrm{AB}}{ }^{\dagger} \mathbf{r}_{\mathrm{AO}}}{\mathrm{r}_{\mathrm{AB}} \mathrm{r}_{\mathrm{AO}}} \leq$

$$
=\cos ^{-1} \phi \frac{7}{5.22(5.00)} \leq=74.4^{\circ}
$$

$\mathbf{r}_{\mathrm{AC}}{ }^{\dagger} \mathbf{r}_{\mathrm{AO}}=(-2)(0)+(-4)(-4)+(1)(-3)=13$

$$
\underline{\mathbf{r}}_{\mathrm{AC}} \underline{\mathbf{r}_{\mathrm{AO}}}
$$

$\mathbf{f}=\cos ^{-1} \mathrm{a}_{\mathrm{r}_{\mathrm{AC}} \mathrm{r}_{\mathrm{AO}}} \mathrm{b}$

$$
=\cos ^{-1} \mathrm{a} \frac{13}{4.58(5.00)} \mathrm{b}=55.4^{\circ}
$$



Ans.
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$$
\mathbf{f}=55.4
$$

## 2-127.

Determine the angle u between $B A$ and $B C$.
Z


## Solution

Unit Vectors. Here, the coordinates of points $A, B$ and $C$ are $A(0,-2,0) \mathrm{m}$, $B(0,0,0) \mathrm{m}$ and $C(3,4,-1) \mathrm{m}$ respectively. Thus, the unit vectors along $B A$ and $B C$ are
$\mathbf{u}_{B A}=-\mathbf{j} \quad \mathbf{u}_{B E}=\frac{(3-0) \mathbf{i}+(4-0) \mathbf{j}+(-1-0) \mathbf{k}}{2\left(\overline{3-0)^{2}+(4-0)^{2}+(-1-0)^{2}}\right.}=\frac{3}{2 \overline{26}} \mathbf{i}+\frac{4}{2 \overline{26}} \mathbf{j}-\frac{1}{2 \overline{26}} \mathbf{k}$
The Angle U Between BA and BC.

$$
\begin{aligned}
\mathbf{u}_{B A} \mathbf{u}_{B C} & =(-\mathbf{j}) \mathrm{a}^{\frac{3}{-}-\mathbf{i}}+\frac{4}{-} \mathbf{j}-\frac{1}{-} \mathbf{k} \mathbf{b} \\
& \frac{226}{\frac{226}{4}} 226 \\
& =(-1) \mathrm{a} 2_{26}^{\mathrm{b}}=-2 \overline{26}
\end{aligned}
$$

Then

$$
\mathrm{u}=\cos ^{-1}\left(\mathbf{u}_{B A}{ }^{\dagger} \mathbf{u}_{B C}\right)=\cos ^{-1} \mathrm{a}-\frac{4}{2 \overline{26}} \mathrm{~b}=141.67=142
$$

Ans.

Ans:
$u=142$
*2-128.
Determine the magnitude of the projected component of the

## Solution

Unit Vectors. Here, the coordinates of points $B, C$ and $D$ are $B(0,0,0) \mathrm{m}$, $C(3,4,-1) \mathrm{m}$ and $D(8,0,0)$. Thus the unit vectors along $B C$ and $C D$ are

$$
\begin{aligned}
& \mathbf{u}_{C D}=\frac{}{2(8-3)^{2}+(0-4)^{2}+[0-(-1)]^{2}}=\overline{2 \overline{42}} \mathbf{i}-\overline{2 \overline{42}} \mathbf{j}+\overline{2 \overline{42}}^{k}
\end{aligned}
$$

Force Vector. For F,

$$
\begin{aligned}
& \mathbf{F}=F \mathbf{u}_{C D}=3 \overline{a^{5} \overline{42}} \mathbf{i}-\overline{2^{4}} \overline{42} \mathbf{j}+\overline{{ }^{\frac{1}{42}}} \mathbf{k b} \\
& =a_{2 \overline{42}}^{15} \mathbf{i}-\frac{12}{2 \overline{42}} \mathbf{j}+\frac{3}{2 \overline{42}} \mathbf{k b ~ k N}
\end{aligned}
$$

Projected Component of $\mathbf{F}$. Along $B C$, it is $\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
\begin{aligned}
& ={ }^{\mathrm{a}} 2 \overline{42}^{\mathrm{b} a} 2 \overline{26}^{\mathrm{b}}+\mathrm{a}-2 \overline{42}^{\mathrm{b} a} 22_{26}^{\mathrm{b}}+2 \overline{242}^{\mathrm{a}-} 226^{\mathrm{b}} \\
& 6 \\
& =-2 \overline{1092}=-0.1816 \mathrm{kN}=0.182 \mathrm{kN} \quad \text { Ans. }
\end{aligned}
$$

The negative signs indicate that this component points in the direction opposite to that of $\mathbf{u}_{B C}$.

## 2-129.

Determine the angles and between the axis $O A$ of the pole and each cable, $A B$ and $A C$.

## Solution

## Given:



$$
\begin{array}{ll}
F_{1} & 50 \mathrm{~N} \\
F_{2} & 35 \mathrm{~N}
\end{array}
$$

$a \quad 1 \mathrm{~m}$
b $\quad 3 \mathrm{~m}$
c. 2 m
d 5 m
e 4 m
$f \quad 6 \mathrm{~m}$
g 4 m

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$$
\begin{aligned}
& u=52.4 \\
& \mathbf{f}=68.2
\end{aligned}
$$

## 2-130.

The two cables exert the forces shown on the pole. Determine the magnitude of the projected component of each force acting along the axis $O A$ of the pole.

## Solution

Given:
$F_{1} \quad 50 \mathrm{~N}$
$F_{2} \quad 35 \mathrm{~N}$
a 1 m
b 3 m
c 2 m
d 5 m
e 4 m
$f \quad 6 \mathrm{~m}$
g 4 m

| $\mathrm{raB}_{\text {A }}$ | $e$ | c |  |  | 0 |  |  | $\mathrm{r}_{\mathrm{AO}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a$ | $\mathbf{r a C}_{\text {AC }}$ | $a$ | $b$ | $\mathbf{r a O}_{\mathrm{A}}$ |  | $\mathbf{u}_{\text {AO }}$ |  |
|  | $f$ |  |  | $f$ |  | $f$ |  | $\mathrm{raO}^{\text {a }}$ |
| $\mathrm{F}_{1 \mathrm{v}}$ | $F_{1} \overline{\left\lvert\, \begin{array}{c}\mathbf{r}_{\mathrm{AC}} \mid \\ \mathbf{r}_{\mathrm{AC}}\end{array}\right.}$ |  | $F_{1 A O}$ | $\mathrm{F}_{1 \mathrm{l}} \mathbf{u}_{\text {AO }}$ | $F_{1 A O}$ | 18.5 N |  |  |
| $\mathrm{F}_{2 \mathrm{v}}$ | $F_{2} \overline{\mid c} \begin{gathered}\left\|\mathbf{r}_{\mathbf{A B}}\right\| \\ \mathbf{r}_{\mathrm{AB}}\end{gathered}$ |  | $F_{2 A O}$ | $\mathrm{F}_{2 \mathrm{v}} \mathbf{u}_{\text {AO }}$ | $F_{2 A O}$ | 21.3 N |  |  |

Ans.

Ans.
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$$
F_{2 A O}=21.3 \mathrm{~N}
$$

## 2-131.

Determine the magnitude of the projection of force $\mathrm{F}=600 \mathrm{~N}$ along the u axis.

## SOLUTION

Unit Vectors: The unit vectors $\mathbf{u}_{\mathrm{OA}}$ and $\mathbf{u}_{\mathrm{u}}$ must be determined first. From Fig. $a$,

$$
\begin{aligned}
& \mathbf{u}_{\mathrm{OA}}=\frac{\mathbf{r}_{\mathrm{OA}}}{\mathrm{r}_{\mathrm{OA}}}=\frac{(-2-0) \mathbf{i}+(4-0) \mathbf{j}+(4-0) \mathbf{k}}{3(-2-0)^{2}+(4-0)^{2}+(4-0)^{2}}=-\frac{1}{3} \mathbf{i}+\frac{2}{3} \mathbf{j}+\frac{2}{3} \mathbf{k} \\
& \mathbf{u}_{\mathrm{u}}=\sin 30^{\circ} \mathbf{i}+\cos 30^{\circ} \mathbf{j}
\end{aligned}
$$



Thus, the force vectors $\mathbf{F}$ is given by

$$
\mathbf{F}=\mathrm{F} \mathbf{u}_{\mathrm{OA}}=600 \mathrm{a}-\frac{1}{3} \mathbf{i}-\frac{2}{3} \mathbf{j}+\frac{2}{3} \mathbf{k} b=5-200 \mathbf{i}+400 \mathbf{j}+400 \mathbf{k} 6 \mathrm{~N}
$$

Vector Dot Product: The magnitude of the projected component of $\mathbf{F}$ along the u axis is

$$
\begin{aligned}
\mathbf{F}_{\mathrm{u}}=\mathrm{F}^{\ddagger} \mathbf{u}_{\mathrm{u}} & =(-200 \mathbf{i}+400 \mathbf{j}+400 \mathbf{k})^{\dagger}\left(\sin 30^{\circ} \mathbf{i}+\cos 30^{\circ} \mathbf{j}\right) \\
& =(-200)\left(\sin 30^{\circ}\right)+400\left(\cos 30^{\circ}\right)+400(0) \\
& =246 \mathrm{~N}
\end{aligned}
$$

Ans.


Ans:
$F_{u}=246 \mathrm{~N}$
*2-132.

Determine the projected component of the force $\mathbf{F}$ acting along the axis $A B$ of the pipe.

## Solution

Given:
$F \quad 80 \mathrm{~N}$
a 4 mb
$3 \mathrm{~m} c$
$12 \mathrm{~m} d$
2 m
e 6 m

Find the force and the unit vector
$e$
$\mathbf{r}_{\mathbf{A}} \quad a \quad b \quad \mathbf{r}_{\mathbf{A}} \quad \begin{array}{lllll} & a & \mathrm{~m}\end{array}$
$\begin{array}{ll}d & 10\end{array}$

6 $\left.\mathbf{r a B}_{\mathrm{AB}} \quad \begin{array}{ll}3 & \mathrm{~m} \\ & 2\end{array}\right]$
$d$
6
$\mathbf{r}_{\mathrm{A}}$


$\mathbf{u}_{\mathrm{AB}} \quad$| $\mathrm{r}_{\mathrm{AB}}$ |
| :---: |

$\mathbf{F}_{\mathbf{v}} \quad 41.2 \mathrm{~N}$
58.8
0.9
35.3
$\mathbf{u}_{\mathbf{A B}} \quad 0.4$
0.3

Now find the projection using the Dot product.
$\begin{array}{lllll}F_{A B} & \mathbf{F}_{\mathbf{v}} \mathbf{u}_{\mathbf{A B}} \quad F_{A B} \quad 31.1 \mathrm{~N} \quad \text { Ans. }\end{array}$
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Ans:
$F_{A B} \quad 31.1 \mathrm{~N}$

## 2-133.

The cables each exert a force of 400 N on the post. Determine the magnitude of the projected component of $\mathbf{F}_{1}$ along the line of action of $\mathbf{F}_{2}$.

## SOLUTION

## Force Vector:

$$
\begin{aligned}
\mathbf{u}_{\mathrm{F}_{1}} & =\sin 35^{\circ} \cos 20^{\circ} \mathbf{i}-\sin 35^{\circ} \sin 20^{\circ} \mathbf{j}+\cos 35^{\circ} \mathbf{k} \\
& =0.5390 \mathbf{i}-0.1962 \mathbf{j}+0.8192 \mathbf{k} \\
\mathbf{F}_{1}=\mathrm{F}_{1} \mathbf{u}_{\mathrm{F}_{1}} & =400(0.5390 \mathbf{i}-0.1962 \mathbf{j}+0.8192 \mathbf{k}) \mathrm{N} \\
& =\{215.59 \mathbf{i}-78.47 \mathbf{j}+327.66 \mathbf{k}\} \mathrm{N}
\end{aligned}
$$

Unit Vector: The unit vector along the line of action of $\mathbf{F}_{2}$ is

$$
\begin{aligned}
\mathbf{u}_{\mathrm{F}_{2}} & =\cos 45^{\circ} \mathbf{i}+\cos 60^{\circ} \mathbf{j}+\cos 120^{\circ} \mathbf{k} \\
& =0.7071 \mathbf{i}+0.5 \mathbf{j}-0.5 \mathbf{k}
\end{aligned}
$$

Projected Component of $\mathrm{F}_{1}$ Along Line of Action of $\mathrm{F}_{2}$ :

$$
\begin{aligned}
\left(\mathrm{F}_{1}\right)_{\mathrm{F}_{2}}=\mathbf{F}_{1}^{\dagger} \mathbf{u}_{\mathrm{F}_{2}} & =(215.59 \mathbf{i}-78.47 \mathbf{j}+327.66 \mathbf{k})^{\ddagger}(0.7071 \mathbf{i}+0.5 \mathbf{j}-\mathbf{O} .5 \mathbf{k}) \\
& =(215.59)(0.7071)+(-78.47)(0.5)+(327.66)(-0.5) \\
& =-50.6 \mathrm{~N}
\end{aligned}
$$

Negative sign indicates that the force component $\left(\mathbf{F}_{1}\right) F_{2}$ acts in the opposite sense of direction to that of $\mathbf{u}_{F 2}$. thus the magnitude is $\left(F_{1}\right)_{\mathrm{F}_{2}}=50.6 \mathrm{~N}$

Ans.

Ans:
$1 F_{1} 2_{F_{2}}=50.6 \mathrm{~N}$

## 2-134.

Determine the angle $u$ between the two cables attached to the post.

## SOLUTION

## Unit Vector:

$$
\begin{aligned}
\mathbf{u}_{\mathrm{F}_{1}} & =\sin 35^{\circ} \cos 20^{\circ} \mathbf{i}-\sin 35^{\circ} \sin 20^{\circ} \mathbf{j}+\cos 35^{\circ} \mathbf{k} \\
& =0.5390 \mathbf{i}-0.1962 \mathbf{j}+0.8192 \mathbf{k} \\
\mathbf{u}_{\mathrm{F}_{2}} & =\cos 45^{\circ} \mathbf{i}+\cos 60^{\circ} \mathbf{j}+\cos 120^{\circ} \mathbf{k} \\
& =0.7071 \mathbf{i}+0.5 \mathbf{j}-0.5 \mathbf{k}
\end{aligned}
$$

The Angle Between Two Vectors u: The dot product of two unit vectors must be determined first.

$$
\begin{aligned}
& \mathbf{u}_{\mathrm{F}_{1}}{ }^{\ddagger} \mathbf{u}_{\mathrm{F}_{2}}=(0.5390 \mathbf{i}-0.1962 \mathbf{j}+0.8192 \mathbf{k})^{\ddagger}(0.7071 \mathbf{i}+0.5 \mathbf{j}- \\
& \quad \mathbf{O . 5 \mathbf { k } )} \\
& =0.5390(0.7071)+(-0.1962)(0.5)+0.8192(-0.5) \\
& =-0.1265
\end{aligned}
$$

Then,

$$
\mathrm{u}=\cos ^{-1} A \mathbf{u}_{\mathrm{F}}{ }^{\dagger} \mathbf{u}_{\mathrm{F}} \mathrm{~B}=\cos ^{-1}(-0.1265)=97.3^{\circ}
$$

Ans.

2-135.
If the force $F=100 \mathrm{~N}$ lies in the plane $D B E C$, which is parallel to the $x-z$ plane, and makes an angle of 10 with the extended line $D B$ as shown, determine the angle that F makes with the diagonal $A B$ of the crate.

## Solution

Use the $x, y, z$ axes.

$$
-0.5 \mathbf{i}+0.2 \mathbf{j}+0.2 \mathbf{k}
$$

$\mathbf{u}_{A B}=\mathrm{a}$ $\qquad$

$$
=-0.8704 \mathbf{i}+0.3482 \mathbf{j}+0.3482 \mathbf{k}
$$

$$
\mathbf{F}=-100 \cos 10 \mathbf{i}+100 \sin 10 \mathbf{k}
$$

$$
\mathrm{u}=\cos ^{-1} \mathrm{a} \frac{\mathbf{F}^{\dagger}-\frac{A B}{}}{u_{A B}} \mathrm{~b}
$$

$$
=\cos ^{-1} \mathrm{a}^{-100(\cos 10)(-0.8704)+0+100 \sin 10(0.3482)}{ }_{\mathrm{b}}
$$ 100(1)

$$
=\cos ^{-1}(0.9176)=23.4
$$



Ans.

Ans:
u $=23.4$

## *2-136.

Determine the magnitudes of the projected components of the force $\mathrm{F}=300 \mathrm{~N}$ acting along the $x$ and $y$ axes.


## SOLUTION

Force Vector: The force vector $\mathbf{F}$ must be determined first. From Fig. $a$,

$$
\begin{aligned}
\mathbf{F} & =-300 \sin 30^{\circ} \sin 30^{\circ} \mathbf{i}+300 \cos 30^{\circ} \mathbf{j}+300 \sin 30^{\circ} \cos 30^{\circ} \mathbf{k} \\
& =[-75 \mathbf{i}+259.81 \mathbf{j}+129.90 \mathbf{k}] \mathrm{N}
\end{aligned}
$$

Vector Dot Product: The magnitudes of the projected component of $\mathbf{F}$ along the $x$ and $y$ axes are

$$
\begin{aligned}
\mathrm{F}_{\mathrm{x}} & =\mathbf{F}^{\ddagger} \mathbf{i}=A-75 \mathbf{i}+259.81 \mathbf{j}+129.90 \mathbf{k} B^{\ddagger} \mathbf{i} \\
& =-75(1)+259.81(0)+129.90(0) \\
& =-75 \mathrm{~N} \\
\mathrm{~F}_{\mathrm{y}} & =\mathbf{F}^{\ddagger} \mathbf{j}=A-75 \mathbf{i}+259.81 \mathbf{j}+129.90 \mathbf{k}^{\ddagger} \mathbf{j} \\
& =-75(0)+259.81(1)+129.90(0) \\
& =260 \mathrm{~N}
\end{aligned}
$$

The negative sign indicates that $\mathbf{F}_{x}$ is directed towards the negative $x$ axis. Thus

$$
\mathrm{F}_{\mathrm{x}}=75 \mathrm{~N}, \quad \mathrm{~F}_{\mathrm{y}}=260 \mathrm{~N}
$$

Ans.

Ans:
$F_{x}=75 \mathrm{~N}$
$F_{y}=260 \mathrm{~N}$

## 2-137.

Determine the magnitude of the projected component of the force $\mathrm{F}=300 \mathrm{~N}$ acting along line $O A$.

## SOLUTION



Force and Unit Vector: The force vector $\mathbf{F}$ and unit vector $\mathbf{u}_{O A}$ must be determined first. From Fig. a
$\mathbf{F}=\left(-300 \sin 30^{\circ} \sin 30^{\circ} \mathbf{i}+300 \cos 30^{\circ} \mathbf{j}+300 \sin 30^{\circ} \cos 30^{\circ} \mathbf{k}\right)$
$=\{-75 \mathbf{i}+259.81 \mathbf{j}+129.90 \mathbf{k}\} \mathrm{N}$
$\mathbf{u}_{\mathrm{OA}}=\frac{\mathbf{r}_{\mathrm{OA}}}{\mathrm{r}_{\mathrm{OA}}}=\frac{(-0.45-0) \mathbf{i}+(0.3-0) \mathbf{j}+(0.2598-0) \mathbf{k}}{2(-0.45-0)^{2}+(0.3-0)^{2}+(0.2598-0)^{2}}=-0.75 \mathbf{i}+0.5 \mathbf{j}+0.4330 \mathbf{k}$

Vector Dot Product: The magnitude of the projected component of $\mathbf{F}$ along line $O A$ is
$\mathrm{F}_{\mathrm{OA}}=\mathbf{F}^{\ddagger} \mathbf{u}_{\mathrm{OA}}=A-75 \mathbf{i}+259.81 \mathbf{j}+129.90 \mathbf{k}^{\sharp}{ }^{\sharp}-0.75 \mathbf{i}+0.5 \mathbf{j}+0.4330 \mathbf{k} B$

$$
=(-75)(-0.75)+259.81(0.5)+129.90(0.4330)
$$

$$
=242 \mathrm{~N}
$$

Ans.


Ans:
$F_{O A}=242 \mathrm{~N}$

2-138. Cable $O A$ is used to support column $O B$. Determine the angle u it makes with beam $O C$.

## Solution

## Unit Vector:



$$
\begin{aligned}
\mathbf{u}_{O C} & =1 \mathbf{i} \\
\mathbf{u}_{O A} & =\frac{(4-0) \mathbf{i}+(8-0) \mathbf{j}+(-8-\mathbf{O}) \mathbf{k}}{2(4-0)^{2}+(8-0)^{2}+(-8-\mathbf{O})^{2}} \\
& =\frac{1}{3} \mathbf{i}+{ }_{3}^{2} \mathbf{j}-\frac{2}{3} \mathbf{k}
\end{aligned}
$$

The Angles Between Two Vectors U: -

$$
\mathbf{u}_{O C}{ }^{\dagger} \mathbf{u}_{O A}=(1 \mathbf{i})^{\dagger}{ }_{3}^{1} \mathbf{i}+{ }_{3}^{2} \mathbf{j}-{ }_{3}^{2} \mathbf{k} \mathbf{b}=1 \mathrm{a}_{3}^{1} \mathrm{~b}+0 \mathrm{a}_{3}^{2} \mathrm{~b}+(0) \mathrm{a}-\frac{2}{2} \mathrm{~b}=\frac{1}{3}
$$

Then,

$$
1
$$

$$
\mathrm{U}=\cos ^{-1}\left(\mathbf{u}_{O C}{ }^{\ddagger} \mathbf{u}_{O A}\right)=\cos ^{-1} \frac{-}{3}=70.5
$$

Ans.

2-139. Cable $O A$ is used to support column $O B$. Determine the angle $\mathbf{f}$ it makes with beam $O D$

## Solution

## Unit Vector:

$$
\begin{aligned}
& \mathbf{u}_{O D}=-\sin 30 \mathbf{i}+\cos 30 \mathbf{j}=-0.5 \mathbf{i}+0.8660 \mathbf{j} \\
& \mathbf{u}_{O A}=(4-0) \mathbf{i}+(8-0) \mathbf{j}+(-8-\mathbf{O}) \mathbf{k} \\
& 2(4-0)^{2}+(8-0)^{2}+(-8-\mathbf{O})^{2}
\end{aligned}
$$

The Angles Between Two Vectors F: _

$$
\begin{aligned}
\mathbf{u}_{O D}{ }^{\dagger} \mathbf{u}_{O A} & =(-0.5 \mathbf{i}+0.8660 \mathbf{j}){ }_{3}^{i}{ }_{3}^{1} \mathbf{i}+{ }_{3}^{2} \mathbf{j}-{ }_{3}^{2} \mathbf{k b} \\
& 1 \\
& =(-0.5) \mathrm{a}_{3} \mathrm{~b}+(0.8660) \mathrm{a}_{3} \mathrm{~b}+0 \mathrm{a}-{ }_{3} \mathrm{~b} \\
& =0.4107-
\end{aligned}
$$

Then,

$$
\mathbf{F}=\cos ^{-1}\left(\mathbf{u}_{O D}^{\dagger} \mathbf{u}_{O A}\right)=\cos ^{-1} 0.4107=65.8
$$

Ans.

Ans:
$\mathbf{f}=65.8$


[^0]:    Ans:
    $F_{B}=1.61 \mathrm{kN}$
    $\mathrm{u}=38.3$

[^1]:    Ans:
    $F_{R}=25.1 \mathrm{kN}$
    $\mathrm{u}=185$

[^2]:    Ans:
    $x=3.82 \mathrm{~m}$
    $y=2.12 \mathrm{~m}$
    $z=1.88 \mathrm{~m}$

[^3]:    
    $127.8^{\circ}$

