# Solution Manual for Intermediate Algebra for College Students 7th 

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## Solution <br> Manual:

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## Chapter 2

Functions and Linear Functions

### 2.1 Check Points

1. The domain is the set of all first components. The domain is $\{0,10,20,30,40\}$.
The range is the set of all second components. The range is $\{9.1,6.7,10.7,13.2,21.2\}$.
2. a. The relation is not a function because an element, 5 , in the domain corresponds to two elements in the range.
b. The relation is a function.
3. a.b.c.
4. $f, x$
5. $r,-2$
2.1 Exercise Set
6. The relation is a function.

The domain is $\{1,3,5\}$.
The range is $\{2,4,5\}$.
2. The relation is a function.

| $f(x)=4 x$ | T |
| :---: | :---: |
| $+5$ | h |
| $f(6)=$ | e |
| $4(6)+5$ | d |
| $f(6)=29$ | O m |
|  | a |
| $g(x)=$ | i |
| $3 x^{2}-10$ | n |
| $g(-5)=$ | i |
| $3(-5)^{2}-$ | \{ |
| 10 | 4 |
| $g(-5)=$ | , |
| 65 | 6 |
|  | , |
| $h($ | 8 |
| $r$ ) | \} |
| $=$ | . |
| $r^{2}$ | T |
| - | h |
| $7 r$ | e |
| + | r |
| 2 | a |
|  | n |
| $h(-4)=$ | g |
| $(-4)^{2}-$ | e |
| 7(-4) + 2 | i |
| $h(-4)=$ | S |
| 46 | \{ |
|  | 5 |
| $F$ | , |
| ( | 7 |
| $x$ | , |
| ) | 8 |
| $=$ | \} |
| 6 | . |
| $x$ | 3. The relation is not a |
| + | function. |
| 9 | T |
| $F(a+h)$ | h |
| $=6(a+h)$ | e |
| +9 | d |
| $F(a+h)$ | o |
| $=6 a+6 h$ | m |
| +9 | a |
|  | i |
|  | n |
|  | i |
|  | S |
|  | \{ |
|  | 3 |
|  | , |
|  | 4 |
|  | \} |

. The range is $\{4,5\}$.
4. The relation is not a function.

The domain is $\{5,6\}$.
The range is $\{6,7\}$.
5. The relation is a function. The domain is $\{-3,-2,-1,0\}$. The range is $\{-3,-2,-1,0\}$.
6. The relation is a function. The domain is $\{-7,-5,-3,0\}$. The range is $\{-7,-5,-3,0\}$.
7. The relation is not a function.
4. a. Every element in the domain corresponds to exactly one element in the range.
b. The domain is $\{0,1,2,3,4\}$. The range is $\{3,0,1,2\}$.
c. $g(1)=0$
d. $g(3)=2$
e. $x=0$ and $x=4$.

### 2.1 Concept and Vocabulary Check

1. relation; domain; range
2. function

The domain is $\{1\}$.
The range is $\{4,5,6\}$.
8. The relation is a function.

The domain is $\{4,5,6\}$.
The range is $\{1\}$.
9. a. $f(0)=0+1=1$
b. $f(5)=5+1=6$
c. $f(-8)=-8+1=-7$
d. $f(2 a)=2 a+1$
e. $f(a+2)=(a+2)+1$

$$
=a+2+1=a+3
$$

10. $f(x)=x+3$
a. $f(0)=0+3=3$
b. $f(5)=5+3=8$
c. $f(-8)=-8+3=-5$
d. $f(2 a)=2 a+3$
e. $f(a+2)=(a+2)+3$

$$
=a+2+3=a+5
$$

11. a. $g(0)=3(0)-2=0-2=-2$
b. $g(-5)=3(-5)-2$

$$
=-15-2=-17
$$

c. $g^{(\underline{2})}=3^{(\underline{2})}-2=2-2=0$

33
d. $g(4 b)=3(4 b)-2=12 b-2$
e. $g(b+4)=3(b+4)-2$

$$
=3 b+12-2=3 b+10
$$

12. $g(x)=4 x-3$
a. $g(0)=4(0)-3=0-3=-3$
b. $g(-5)=4(-5)-3=-20-3=-23$
c. $g^{(\underline{3})}=4^{(\underline{3})}-3=3-3=0$
d. $g(5 b)=4(5 b)-3=20 b-3$
e. $g(b+5)=4(b+5)-3$

$$
=4 b+20-3=4 b+17
$$

13. a. $h(0)=3(0)^{2}+5=3(0)+5$

$$
=0+5=5
$$

d. $h(-3)=3(-3)^{2}+5=3(9)+5$

$$
=27+5=32
$$

e. $h(4 b)=3(4 b)^{2}+5=3\left(16 b^{2}\right)+5$

$$
=48 b^{2}+5
$$

14. $h(x)=2 x^{2}-4$
a. $h(0)=2(0)^{2}-4=2(0)-4$

$$
=0-4=-4
$$

b. $h(-1)=2(-1)^{2}-4=2(1)-4$

$$
=2-4=-2
$$

c. $h(5)=2(5)^{2}-4=2(25)-4$

$$
=50-4=46
$$

d. $h(-3)=2(-3)^{2}-4=2(9)-4$

$$
=18-4=14
$$

e. $h(5 b)=2(5 b)^{2}-4=2\left(25 b^{2}\right)-4$

$$
=50 b^{2}-4
$$

15. a. $f(0)=2(0)^{2}+3(0)-1$

$$
=0+0-1=-1
$$

b. $f(3)=2(3)^{2}+3(3)-1$

$$
\begin{aligned}
& =2(9)+9-1 \\
& =18+9-1=26
\end{aligned}
$$

c. $f(-4)=2(-4)^{2}+3(-4)-1$

$$
\begin{aligned}
& =2(16)-12-1 \\
& =32-12-1=19
\end{aligned}
$$

d. $f(b)=2(b)^{2}+3(b)-1$

$$
=2 b^{2}+3 b-1
$$

b. $h(-1)=3(-1)^{2}+5=3(1)+5$

$$
=3+5=8
$$

c. $h(4)=3(4)^{2}+5=3(16)+5$

$$
=48+5=53
$$

16. $f(x)=3 x^{2}+4 x-2$
a. $f(0)=3(0)^{2}+4(0)-2$

$$
=3(0)+0-2
$$

$$
=0+0-2=-2
$$

b. $f(3)=3(3)^{2}+4(3)-2$

$$
\begin{aligned}
& =3(9)+12-2 \\
& =27+12-2=37
\end{aligned}
$$

c. $f(-5)=3(-5)^{2}+4(-5)-2$

$$
\begin{aligned}
& =3(25)-20-2 \\
& =75-20-2=53
\end{aligned}
$$

d. $f(b)=3(b)^{2}+4(b)-2$

$$
=3 b^{2}+4 b-2
$$

e. $f(5 a)=3(5 a)^{2}+4(5 a)-2$

$$
\begin{aligned}
& =3\left(25 a^{2}\right)+20 a-2 \\
& =75 a^{2}+20 a-2
\end{aligned}
$$

17. a. $f(0)=(-0)^{3}-(0)^{2}-(0)+7$

$$
=7
$$

b. $\quad f(2)=(-2)^{3}-(2)^{2}-(2)+7$

$$
=-7
$$

c. $\quad f(-2)=(-(-2))^{3}-(-2)^{2}-(-2)+7$

$$
=13
$$

d. $f(1)+f(-1)=\left[(-1)^{3}-(1)^{2}-(1)+7\right]+\left[(-(-1))^{3}-(-1)^{2}-(-1)+7\right]$

$$
\begin{aligned}
& =4+8 \\
& =12
\end{aligned}
$$

18. a. $f(0)=(-0)^{3}-(0)^{2}-(0)+10$

$$
=10
$$

b. $f(2)=(-2)^{3}-(2)^{2}-(2)+10$

$$
=-4
$$

c. $\quad f(-2)=(-(-2))^{3}-(-2)^{2}-(-2)+10$

$$
=16
$$

d. $f(1)+f(-1)=\left[(-1)^{3}-(1)^{2}-(1)+10\right]+\left[(-(-1))^{3}-(-1)^{2}-(-1)+10\right]$

$$
\begin{aligned}
& =7+11 \\
& =18
\end{aligned}
$$

19. a. $f(0)=\frac{2(0)-3}{(0)-4}=\frac{0-3}{0-4}$

$$
=\frac{-3}{-4}=\frac{3}{4}
$$

b. $f(3)=\frac{2(3)-3}{(3)-4}=\frac{6-3}{3-4}$

$$
=\frac{3}{-1}=-3
$$

c. $f(-4)=\frac{2(-4)-3}{(-4)-4}=\frac{-8-3}{-8}$

$$
=\frac{-11}{-8}=\frac{11}{8}
$$

d. $f(-5)=\frac{2(-5)-3}{(-5)-4}=\frac{-10-3}{-9}$

$$
=\frac{-13}{-9}=\frac{13}{9}
$$

e. $f(a+h)=\frac{2(a+h)-3}{(a+h)-4}$

$$
=\frac{2 a+2 h-3}{a+h-4}
$$

f. Four must be excluded from the domain, because four would make the denominator zero. Division by zero is undefined.
20. $f(x)=\frac{3 x-1}{x-5}$
a. $f(0)=\frac{3(\underline{0})-1}{(0)-5}=\frac{0-1}{-5}=\frac{-1}{-5}=\frac{1}{5}$
b. $\left.f(3)=\frac{3}{3}-\frac{3}{3} \underline{2}-1\right]=\frac{9-1}{-2}=\frac{8}{-2}=-4$
c. $f(-3)=\frac{3(-3)}{-3-5}=\frac{-1}{-8}$

$$
=\frac{-10}{-8}=\frac{5}{4}
$$

d. $f(10)=\underline{3}\left(\underline{10} \underline{-1}=\frac{30-1}{=} \underline{29}\right.$
e. $f(a+h)=\frac{\underline{3}\left(\frac{a+h}{}\right) \frac{-1}{a+h-5}}{3 a+3 h}$

$$
=\frac{3 a+3 h-1}{a+h-5}
$$

f. Five must be excluded from the domain, because 5 would make the denominator zero. Division by zero is undefined.
21. a. $f(-2)=6$
b. $f(2)=12$
c. $x=0$
22. a. $f(-3)=8$
b. $f(3)=16$
c. $x=0$
23. a. $h(-2)=2$
b. $h(1)=1$
c. $x=-1$ and $x=1$
24. a. $h(-2)=-2$
b. $h(1)=-1$
c. $x=-1$ and $x=1$
25. $g(1)=3(1)-5=3-5=-2$

$$
\begin{aligned}
f(g(1)) & =f(-2)=(-2)^{2}-(-2)+4 \\
& =4+2+4=10
\end{aligned}
$$

26. $g(-1)=3(-1)-5=-3-5=-8$

$$
\begin{aligned}
f(g(-1)) & =f(-8)=(-8)^{2}-(-8)+4 \\
& =64+8+4=76
\end{aligned}
$$

27. $\sqrt{3-(-1)}-(-6)^{2}+6 \div-6 \cdot 4$
$=\sqrt{3+1}-36+-1 \cdot 4$
$=\sqrt{4}-36+-4=2-36-4=-38$
28. $f(-x)-f(x)$
$=(-x)^{3}+(-x)-5-\left[x^{3}+x-5\right]$
$=-x^{3}-x-5-x^{3}-x+5$
$=-2 x^{3}-2 x$
29. $f(-x)-f(x)$
$=(-x)^{2}-3(-x)+7-\left(x^{2}-3 x+7\right)$
$=x^{2}+3 x+7-x^{2}+3 x-7$
$=6 x$
30. a. $f(-2)=3(-2)+5=-6+5=-1$
b. $f(0)=4(0)+7=0+7=7$
c. $f(3)=4(3)+7=12+7=19$
d. $f(-100)+f(100)$
$=3(-100)+5+4(100)+7$
$=-300+5+400+7=112$
31. a. $f(-3)=6(-3)-1=-18-1=-19$
b. $f(0)=7(0)+3=0+3=3$
c. $f(4)=7(4)+3=28+3=31$
d. $f(-100)+f(100)$
$=6(-100)-1+7(100)+3$
$=-600-1+700+3$
$=100+2=102$
32. a. $\{($ Iceland, 9.7), (Finland, 9.6), (New Zealand, 9.6), (Denmark, 9.5) \}
b. Yes, the relation is a function because each country in the domain corresponds to exactly one corruption rating in the range.
c. $\{(9.7$, Iceland $),(9.6$, Finland $),(9.6$, New Zealand $)$, (9.5, Denmark) \}
d. No, the relation is not a function because 9.6 in the domain corresponds to two countries in the
33. $-4-(-1)-(-3)^{2}+-3 \div 3 \cdot-6$
range, Finland and New Zealand.
$=|-4+1|-9+-3 \div 3 \cdot-6$
$=|-3|-9+-1 \cdot-6$
$=3-9+6=-6+6=0$
34. a. $\{($ Bangladesh, 1.7), (Chad, 1.7), (Haiti, 1.8), (Myanmar, 1.8)\}
b. Yes, the relation is a function because each country in the domain corresponds to exactly one corruption rating in the range.
c. $\{(1.7$, Bangladesh $),(1.7$, Chad $),(1.8$, Haiti), (1.8, Myanmar) $\}$
d. No, the relation is not a function because 1.7 in the domain corresponds to two countries in the range, Bangladesh and Chad.
35.     - 38. Answers will vary.
1. makes sense
2. makes sense
3. makes sense
4. does not make sense; Explanations will vary. Sample explanation: The range is the chance of divorce.
5. false; Changes to make the statement true will vary.

A sample change is: All functions are relations.
44. false; Changes to make the statement true will vary. A sample change is: Functions can have ordered pairs with the same second component. It is the first component that cannot be duplicated.
45. true
46. true
47. true
48. false; $g(-4)+f(-4)$

$$
\begin{aligned}
& =(-1)+(-1) \\
& =-2
\end{aligned}
$$

49. $f(a+h)=3(a+h)+7=3 a+3 h+7$
$f(a)=3 a+7$
50. It is given that $f(x+y)=f(x)+f(y)$ and $f(1)=3$.

To find $f(2)$, rewrite 2 as $1+1$.

$$
\begin{aligned}
f(2) & =f(1+1)=f(1)+f(1) \\
& =3+3=6
\end{aligned}
$$

Similarly:

$$
\begin{aligned}
f(3) & =f(2+1)=f(2)+f(1) \\
& =6+3=9 \\
f(4) & =f(3+1)=f(3)+f(1) \\
& =9+3=12
\end{aligned}
$$

While $f(x+y)=f(x)+f(y)$ is true for this
function, it is not true for all functions. It is not true for $f(x)=x^{2}$, for example.
52. $24 \div 4[2-(5-2)]^{2}-6$
$=24 \div 4[2-(3)]^{2}-6$
$=24 \div 4(-1)^{2}-6$
$=24 \div 4(1)-6$
$=6(1)-6=6-6=0$
53. $\left(\frac{\left(3 x^{2} y^{-2}\right)_{-2}\left(3 x^{2}\right)^{-2}}{y^{3}}\right)^{\left(y^{5}\right)^{2}}=\left(\begin{array}{l}y^{5}\end{array}\right)=\binom{y^{10}}{3 x^{2}}=\begin{aligned} & 9 x^{4}\end{aligned}$
x $\quad 3 x$
54. $3=5^{+4}$

$$
\left.15^{(\underline{x})}=15^{(\underline{3 x}}+4\right)
$$

35

$$
15^{(\underline{x})}=15^{(\underline{3 x})}+15(4)
$$

35
$5 x=3(3 x)+60$
$5 x=9 x+60$
$5 x-9 x=9 x-9 x+60$
$-4 x=60$
$\frac{-4 x}{-4}=\frac{60}{-4}$

```
\(\frac{f(a+h)-f(a)}{h}\)
\(=\frac{(3 a+3 h+7)}{h}=\left(\frac{3 a+7)}{h}\right.\)
\(=\frac{3 a+3 h+7-3 a-7}{h}=\frac{3 h}{h}=3\)
```

50. Answers will vary. An example is $\{(1,1),(2,1)\}$.
51. 

| $x$ | $f(x)=2 x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=2(-2)=-4$ | $(-2,-4)$ |
| -1 | $f(-1)=2(-1)=-2$ | $(-1,-2)$ |
| 0 | $f(0)=2(0)=0$ | $(0,0)$ |
| 1 | $f(1)=2(1)=2$ | $(1,2)$ |
| 2 | $f(2)=2(2)=4$ | $(2,4)$ |


56.

| $x$ | $f(x)=2 x+4$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=2(-2)+4=0$ | $(-2,0)$ |
| -1 | $f(-1)=2(-1)+4=2$ | $(-1,2)$ |
| 0 | $f(0)=2(0)+4=4$ | $(0,4)$ |
| 1 | $f(1)=2(1)+4=6$ | $(1,6)$ |
| 2 | $f(2)=2(2)+4=8$ | $(2,8)$ |

57. a. When the $x$-coordinate is 2 , the $y$-coordinate is 3.
b. When the $y$-coordinate is 4 , the $x$-coordinates are -3 and 3 .
c. $(-\infty, \infty)$

### 2.2 Check Points

1. $f(x)=2 x$

| $x$ | $f(x)=2 x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=2(-2)=-4$ | $(-2,-4)$ |
| -1 | $f(-1)=2(-1)=-2$ | $(-1,-2)$ |
| 0 | $f(0)=2(0)=0$ | $(0,0)$ |
| 1 | $f(1)=2(1)=2$ | $(1,2)$ |
| 2 | $f(2)=2(2)=4$ | $(2,4)$ |


| $g(x)$ | $=2 x-3(x)=2 x-3$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=2(-2)-3=-7$ | $(-2,-7)$ |
| -1 | $g(-1)=2(-1)-3=-5$ | $(-1,-5)$ |
| 0 | $g(0)=2(0)-3=-3$ | $(0,-3)$ |
| 1 | $g(1)=2(1)-3=-1$ | $(1,-1)$ |
| 2 | $g(2)=2(2)-3=1$ | $(2,1)$ |



The graph of $g$ is the graph of $f$ shifted down by 3 units.
2. a. The graph represents a function. It passes the vertical line test.
b. The graph represents a function. It passes the vertical line test.
c. The graph does not represent a function. It fails the vertical line test.
3. a. $f(5)=400$
b. When $x$ is 9 , the function's value is 100 . i.e. $f(9)=100$
c. The minimum $T$ cell count during the asymptomatic stage is approximately 425.
4. a. The domain is $[-2,1]$.

The range is $[0,3]$.
b. The domain is $(-2,1]$.

The range is $[-1,2)$.
c. The domain is $[-3,0)$.

The range is $\{-3,-2,-1\}$.

### 2.2 Concept and Vocabulary Check

1. ordered pairs
2. more than once; function
3. $[1,3)$; domain
4. $[1, \infty)$; range

### 2.2 Exercise Set

1. 

| $x$ | $f(x)=x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=-2$ | $(-2,-2)$ |
| -1 | $f(-1)=-1$ | $(-1,-1)$ |
| 0 | $f(0)=0$ | $(0,0)$ |
| 1 | $f(1)=1$ | $(1,1)$ |
| 2 | $f(2)=2$ | $(2,2)$ |


| $x$ | $g(x)=x+3$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=-2+3=1$ | $(-2,1)$ |
| -1 | $g(-1)=-1+3=2$ | $(-1,2)$ |
| 0 | $g(0)=0+3=3$ | $(0,3)$ |
| 1 | $g(1)=1+3=4$ | $(1,4)$ |
| 2 | $g(2)=2+3=5$ | $(2,5)$ |



The graph of $g$ is the graph of $f$ shifted up 3 units.
2.

| $x$ | $f(x)=x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=-2$ | $(-2,-2)$ |
| -1 | $f(-1)=-1$ | $(-1,-1)$ |
| 0 | $f(0)=0$ | $(0,0)$ |
| 1 | $f(1)=1$ | $(1,1)$ |
| 2 | $f(2)=2$ | $(2,2)$ |


| $x$ | $g(x)=x-4$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=-2-4=-6$ | $(-2,-6)$ |
| -1 | $g(-1)=-1-4=-5$ | $(-1,-5)$ |
| 0 | $g(0)=0-4=-4$ | $(0,-4)$ |
| 1 | $g(1)=1-4=-3$ | $(1,-3)$ |
| 2 | $g(2)=2-4=-2$ | $(2,-2)$ |

The graph of $g$ is the graph of $f$ shifted down 4 units.
3.

| $x$ | $f(x)=-2 x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=-2(-2)=4$ | $(-2,4)$ |
| -1 | $f(-1)=-2(-1)=2$ | $(-1,2)$ |
| 0 | $f(0)=-2(0)=0$ | $(0,0)$ |
| 1 | $f(1)=-2(1)=-2$ | $(1,-2)$ |
| 2 | $f(2)=-2(2)=-4$ | $(2,-4)$ |


| $x$ | $g(x)=-2 x-1$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=-2(-2)-1=3$ | $(-2,3)$ |
| -1 | $g(-1)=-2(-1)-1=1$ | $(-1,1)$ |
| 0 | $g(0)=-2(0)-1=-1$ | $(0,-1)$ |
| 1 | $g(1)=-2(1)-1=-3$ | $(1,-3)$ |
| 2 | $g(2)=-2(2)-1=-5$ | $(2,-5)$ |



The graph of $g$ is the graph of $f$ shifted down 1 unit.
4.

| $x$ | $f(x)=-2 x$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=-2(-2)=4$ | $(-2,4)$ |
| -1 | $f(-1)=-2(-1)=2$ | $(-1,2)$ |
| 0 | $f(0)=-2(0)=0$ | $(0,0)$ |
| 1 | $f(1)=-2(1)=-2$ | $(1,-2)$ |
| 2 | $f(2)=-2(2)=-4$ | $(2,-4)$ |
| $x$ | $g(x)=-2 x+3$ | $(x, y)$ |
| -2 | $g(-2)=-2(-2)+3=7$ | $(-2,7)$ |
| -1 | $g(-1)=-2(-1)+3=5$ | $(-1,5)$ |
| 0 | $g(0)=-2(0)+3=3$ | $(0,3)$ |
| 1 | $g(1)=-2(1)+3=1$ | $(1,1)$ |
| 2 | $g(2)=-2(2)+3=-1$ | $(2,-1)$ |



The graph of $g$ is the graph of $f$ shifted up 3 units.
5.

| $x$ | $f(x)=x^{2}$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=(-2)^{2}=4$ | $(-2,4)$ |
| -1 | $f(-1)=(-1)^{2}=1$ | $(-1,1)$ |
| 0 | $f(0)=(0)^{2}=0$ | $(0,0)$ |
| 1 | $f(1)=(1)^{2}=1$ | $(1,1)$ |
| 2 | $f(2)=(2)^{2}=4$ | $(2,4)$ |


| $x$ | $g(x)=x^{2}+1$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=(-2)^{2}+1=5$ | $(-2,5)$ |
| -1 | $g(-1)=(-1)^{2}+1=2$ | $(-1,2)$ |
| 0 | $g(0)=(0)^{2}+1=1$ | $(0,1)$ |
| 1 | $g(1)=(1)^{2}+1=2$ | $(1,2)$ |
| 2 | $g(2)=(2)^{2}+1=5$ | $(2,5)$ |$\quad$|  |
| :--- |



The graph of $g$ is the graph of $f$ shifted up 1 unit.
6.

| $x$ | $f(x)=x^{2}$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=(-2)^{2}=4$ | $(-2,4)$ |
| -1 | $f(-1)=(-1)^{2}=1$ | $(-1,1)$ |
| 0 | $f(0)=(0)^{2}=0$ | $(0,0)$ |
| 1 | $f(1)=(1)^{2}=1$ | $(1,1)$ |
| 2 | $f(2)=(2)^{2}=4$ | $(2,4)$ |


| $x$ | $g(x)=x^{2}-2$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=(-2)^{2}-2=2$ | $(-2,2)$ |
| -1 | $g(-1)=(-1)^{2}-2=-1$ | $(-1,-1)$ |
| 0 | $g(0)=(0)^{2}-2=-2$ | $(0,-2)$ |
| 1 | $g(1)=(1)^{2}-2=-1$ | $(1,-1)$ |
| 2 | $g(2)=(2)^{2}-2=2$ | $(2,2)$ |



The graph of $g$ is the graph of $f$ shifted down 2 units.
7.

| $x$ | $f(x)=\|x\|$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=\|-2\|=2$ | $(-2,2)$ |
| -1 | $f(-1)=-1=1$ | $(-1,1)$ |
| 0 | $f(0)=\mid 0=0$ | $(0,0)$ |
| 1 | $f(1)=\|1\|=1$ | $(1,1)$ |
| 1 | $f(2)=\|2\|=2$ | $(2,2)$ |


| $x$ | $g(x)=\|x\|-2$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=-2 \mid-2=0$ | $(-2,0)$ |
| -1 | $g(-1)=\|-1\|-2=-1$ | $(-1,-1)$ |
| 0 | $g(0)=\|0\|-2=-2$ | $(0,-2)$ |
| 1 | $g(1)=\|1\|-2=-1$ | $(1,-1)$ |
| 2 | $g(2)=\|2\|-2=0$ | $(2,0)$ |



The graph of $g$ is the graph of $f$ shifted down 2 units.
8.

| $x$ | $f(x)=x$ |  |
| :---: | :---: | :---: |
| $(x, y)$ |  |  |
| -2 | $f(-2)=\|-2\|=2$ | $(-2,2)$ |
| -1 | $f(-1)=-1 \mid=1$ | $(-1,1)$ |
| 0 | $f(0)=\|0\|=0$ | $(0,0)$ |
| 1 | $f(1)=\mid 1=1$ | $(1,1)$ |
| 2 | $f(2)=2 \mid=2$ | $(2,2)$ |
| $x$ | $g(x)=\|x\|+1$ | $(x, y)$ |
| -2 | $g(-2)=-2 \mid+1=3$ | $(-2,3)$ |
| -1 | $g(-1)=-1+1=2$ | $(-1,2)$ |
| 0 | $g(0)=\|0\|+1=1$ | $(0,1)$ |
| 1 | $g(1)=\|1\|+1=2$ | $(1,2)$ |
| 2 | $g(2)=\|2\|+1=3$ | $(2,3)$ |



The graph of $g$ is the graph of $f$ shifted up 1 unit.
9.

| $x$ | $f(x)=x^{3}$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=(-2)^{3}=-8$ | $(-2,-8)$ |
| -1 | $f(-1)=(-1)^{3}=-1$ | $(-1,-1)$ |
| 0 | $f(0)=(0)^{3}=0$ | $(0,0)$ |
| 1 | $f(1)=(1)^{3}=1$ | $(1,1)$ |
| 2 | $f(2)=(2)^{3}=8$ | $(2,8)$ |


| $x$ | $g(x)=x^{3}+2$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=(-2)^{3}+2=-6$ | $(-2,-6)$ |
| -1 | $g(-1)=(-1)^{3}+2=1$ | $(-1,1)$ |
| 0 | $g(0)=(0)^{3}+2=2$ | $(0,2)$ |
| 1 | $g(1)=(1)^{3}+2=3$ | $(1,3)$ |
| 2 | $g(2)=(2)^{3}+2=10$ | $(2,10)$ |



The graph of $g$ is the graph of $f$ shifted up 2 units.
10.

| $x$ | $f(x)=x^{3}$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $f(-2)=(-2)^{3}=-8$ | $(-2,-8)$ |
| -1 | $f(-1)=(-1)^{3}=-1$ | $(-1,-1)$ |
| 0 | $f(0)=(0)^{3}=0$ | $(0,0)$ |
| 1 | $f(1)=(1)^{3}=1$ | $(1,1)$ |
| 2 | $f(2)=(2)^{3}=8$ | $(2,8)$ |


| $x$ | $g(x)=x^{3}-1$ | $(x, y)$ |
| :---: | :---: | :---: |
| -2 | $g(-2)=(-2)^{3}-1=-9$ | $(-2,-9)$ |
| -1 | $g(-1)=(-1)^{3}-1=-2$ | $(-1,-2)$ |
| 0 | $g(0)=(0)^{3}-1=-1$ | $(0,-1)$ |
| 1 | $g(1)=(1)^{3}-1=0$ | $(1,0)$ |
| 2 | $g(2)=(2)^{3}-1=7$ | $(2,7)$ |



The graph of $g$ is the graph of $f$ shifted down 1 unit.
14. The graph does not represent a function. It fails the vertical line test.
15. The graph represents a function. It passes the vertical line test.
16. The graph does not represent a function. It fails the vertical line test.
17. The graph does not represent a function. It fails the vertical line test.
18. The graph represents a function. It passes the vertical line test.
19. $f(-2)=-4$
20. $f(2)=-4$
21. $f(4)=4$
22. $f(-4)=4$
23. $f(-3)=0$
24. $f(-1)=0$
25. $g(-4)=2$
26. $g(2)=-2$
27. $g(-10)=2$
28. $g(10)=-2$
29. When $x=-2, g(x)=1$.
30. When $x=1, g(x)=-1$.
31. The domain is $[0,5)$.

The range is $[-1,5)$.
11. The graph represents a function. It passes the vertical line test.
12. The graph represents a function. It passes the vertical line test.
13. The graph does not represent a function. It fails the vertical line test.
32. The domain is $(-5,0]$. The range is $[-3,3)$.
33. The domain is $[0, \infty)$.

The range is $[1, \infty)$.
34. The domain is $[0, \infty)$.

The range is $[0, \infty)$.
35. The domain is $[-2,6]$.

The range is $[-2,6]$.
36. The domain is $[-3,2]$.

The range is $[-5,5]$.
37. The domain is $(-\infty, \infty)$

The range is $(-\infty,-2]$
38. The domain is $(-\infty, \infty)$.

The range is $[0, \infty)$.
39. The domain is $\{-5,-2,0,1,3\}$.

The range is $\{2\}$.
40. The domain is $\{-5,-2,0,1,4\}$.

The range is $\{-2\}$.
41. a. The domain is $(-\infty, \infty)$.
b. The range is $[-4, \infty)$
c. $f(-3)=4$
d. 2 and 6 ; i.e. $f(2)=f(6)=-2$
e. $f$ crosses the $x$-axis at $(1,0)$ and $(7,0)$.
f. $f$ crosses the $y$-axis at $(0,4)$.
g. $f(x)<0$ on the interval $(1,7)$.
h. $f(-8)$ is positive.
42. a. The domain is $(-\infty, 6]$.
b. The range is $(-\infty, 1]$.
c. $f(-4)=-1$
d. -6 and 6 ; i.e. $f(-6)=f(6)=-3$
e. $f$ crosses the $x$-axis at $(-3,0)$ and $(3,0)$.
f. $f$ crosses the $y$-axis at $(0,1)$.
43. a. $G(30)=-0.01(30)^{2}+(30)+60=81$ In 2010, the wage gap was $81 \%$. This is represented as $(30,81)$ on the graph.
b. $\quad G(30)$ underestimates the actual data shown by the bar graph by $2 \%$.
44. a. $\quad G(10)=-0.01(10)^{2}+(10)+60=69$

In 1990, the wage gap was $69 \%$. This is represented as $(10,69)$ on the graph.
b. $\quad G(10)$ underestimates the actual data shown by the bar graph by $2 \%$.

$$
2
$$

45. $f(20)=0.4(20)-36(20)+1000$

$$
\begin{aligned}
& =0.4(400)-720+1000 \\
& =160-720+1000 \\
& =-560+1000=440
\end{aligned}
$$

Twenty-year-old drivers have 440 accidents per 50 million miles driven.
This is represented on the graph by point $(20,440)$.
46. $f(50)=0.4(50)^{2}-36(50)+1000$

$$
\begin{aligned}
& =0.4(2500)-1800+1000 \\
& =1000-1800+1000=200
\end{aligned}
$$

Fifty-year-old drivers have 200 accidents per 50 million miles driven.
This is represented on the graph by point $(50,200)$.
47. The graph reaches its lowest point at $x=45$.

$$
\begin{aligned}
f(45) & =0.4(45)^{2}-36(45)+1000 \\
& =0.4(2025)-1620+1000 \\
& =810-1620+1000 \\
& =-810+1000 \\
& =190
\end{aligned}
$$

Drivers at age 45 have 190 accidents per 50 million miles driven. This is the least number of accidents for any driver between ages 16 and 74 .
48. Answers will vary.

One possible answer is age 16 and age 74 .

$$
\begin{aligned}
f(16) & =0.4(16)^{2}-36(16)+1000 \\
& =0.4(256)-576+1000 \\
& =102.4-576+1000=526.4
\end{aligned}
$$

g. $f(x)>0$ on the interval $(-3,3)$.
h. $f(-2)$ is positive.

$$
\begin{aligned}
f(74) & =0.4(74)-36(74)+1000 \\
& =0.4(5476)-2664+1000 \\
& =2190.4-2664+1000=526.4
\end{aligned}
$$

Both 16 -year-olds and 74 -year-olds have approximately
526.4 accidents per 50 million miles driven.
49. $f(3)=0.91$

The cost of mailing a first-class letter weighing 3 ounces is $\$ 0.91$.
50. $f(3.5)=1.12$

The cost of mailing a first-class letter weighing 3.5 ounces is $\$ 1.12$.
51. The cost to mail a letter weighing 1.5 ounces is $\$ 0.70$.
52. The cost to mail a letter weighing 1.8 ounces is $\$ 0.70$.
53. - 56. Answers will vary.
57. The number of physician's visits per year based on age first decreases and then increases over a person's lifetime.


These are the approximate coordinates of the point (20.3, 4.0). The means that the minimum number of physician's visits per year is approximately 4 . This occurs around age 20.
58. makes sense
59. makes sense
60. does not make sense; Explanations will vary. Sample explanation: The domain is the set of number of years that people work for a company.
61. does not make sense; Explanations will vary. Sample explanation: The domain is the set of the various ages of the people.
62. false; Changes to make the statement true will vary. A sample change is: The graph of a vertical line is not a function.
63. true
64. true
65. false; Changes to make the statement true will vary. A sample change is: The range of $f$ is $[-2,2)$.
66. true
67. false; Changes to make the statement true will vary. A sample change is: $f(0)=0.6$
68. $\sqrt{f(-1.5)+f(-0.9)}-[f(\pi)]^{2}+f(-3) \div f(1) \cdot f(-\pi)$
$=\sqrt{1+0}-[-4]^{2}+2 \div(-2)(3)$
$=\sqrt{1}-16+(-1)(3)$
$=1-16-3$
$=-15-3$
$=-18$
69. $\sqrt{f(-2.5)-f(1.9)}-[f(-\pi)]^{2}+f(-3) \div f(1) \cdot f(\pi)$
$=\sqrt{2-(-2)}-[3]^{2}+2 \div(-2)(-4)$
$=\sqrt{4}-9+(-1)(-4)$
$=2-9+4$
$=-3$
70. The relation is a function. Every element in the domain corresponds to exactly one element in the range.
71. $12-2(3 x+1)=4 x-5$

$$
\begin{aligned}
12-6 x-2 & =4 x-5 \\
10-6 x & =4 x-5 \\
-6 x-4 x & =-5-10 \\
-10 x & =-15 \\
\frac{-10 x}{-10} & =\frac{-15}{-10}
\end{aligned}
$$

$$
x=\frac{3}{2}
$$

The solution set is $\left\{\frac{3}{2}\right\}$.
72. Let $x=$ the width of the rectangle.

Let $3 x+8=$ length of the rectangle.
$P=2 l+2 w$
$624=2(3 x+8)+2 x$

$$
624=6 x+16+2 x
$$

$$
624=8 x+16
$$

$$
-8 x=-608
$$

$$
x=76
$$

$3 x+8=236$
The dimensions of the rectangle are 76 yards by 236 yards.
73. 3 must be excluded from the domain of $f$ because it would cause the denominator, $x-3$, to be equal to zero. Division by 0 is undefined.
74. $f(4)+g(4)=\left(4^{2}+4\right)+(4-5)$

$$
\begin{aligned}
& =20+(-1) \\
& =19
\end{aligned}
$$

75. $-2.6 x^{2}+49 x+3994-\left(-0.6 x^{2}+7 x+2412\right)$
$=-2.6 x^{2}+49 x+3994+0.6 x^{2}-7 x-2412$
$=-2 x^{2}+42 x+1582$

### 2.3 Check Points

1. a. The function contains neither division nor a square root. For every real number, $x$, the algebraic expression $\frac{1}{2} x+3$ is a real number. Thus, the domain of $f$ is the set of all real numbers. Domain of $f$ is $(-\infty, \infty)$.
b. The function $g(x)=\frac{7 x+4}{x+5}$ contains division. Because division by 0 is undefined, we must exclude from the domain the value of $x$ that causes $x+5$ to be 0 . Thus, $x$ cannot equal -5 .
Domain of $g$ is $(-\infty,-5)$ or $(-5, \infty)$.
2. a. $(f+g)(x)=f(x)+g(x)$

$$
\begin{aligned}
& =\left(3 x^{2}+4 x-1\right)+(2 x+7) \\
& =3 x^{2}+4 x-1+2 x+7 \\
& =3 x^{2}+6 x+6
\end{aligned}
$$

b. $(f+g)(x)=3 x^{2}+6 x+6$

$$
\begin{aligned}
(f+g)(4) & =3(4)^{2}+6(4)+6 \\
& =78
\end{aligned}
$$

3. a. $(f-g)(x)=\frac{5}{x}-\frac{7}{x-8}$
b. The domain of $f-g$ is the set of all real numbers that are common to the domain of $f$ and the domain of $g$. Thus, we must find the domains of $f$ and $g$.
Note that $f(x)=\frac{5}{x}$ is a function involving division. Because division by 0 is undefined, $x$ cannot equal 0 .
The function $g(x)=\frac{7}{x-8}$ is also a function involving division. Because division by 0 is undefined, $x$ cannot equal

## 8.

To be in the domain of $f-g, x$ must be in both the domain of $f$ and the domain of $g$.
This means that $x \neq 0$ and $x \neq 8$.

Domain of $f-g=(-\infty, 0)$ or $(0,8)$ or $(8, \infty)$.
4. a. $(f+g)(5)=f(5)+g(5)=\left[5^{2}-2 \cdot 5\right]+[5+3]=23$
b. $(f-g)(x)=f(x)-g(x)=\left[x^{2}-2 x\right]-[x+3]=x^{2}-3 x-3$
$(f-g)(-1)=(-1)^{2}-3(-1)-3=1$
c. $\binom{f}{g}(x)=\frac{f(\underline{x})}{g(x)}=\frac{x^{2}-2 x}{x+3}$
$(f) \quad(7)^{2}-2(7) \quad 35 \quad 7$


$$
\begin{array}{llll}
(g) & (7)+3 & 10 & 2
\end{array}
$$

d. $(f g)(-4)=f(-4) \cdot g(-4)$

$$
\begin{aligned}
& =\left((-4)^{2}-2(-4)\right)((-4)+3) \\
& =(24)(-1) \\
& =-24
\end{aligned}
$$

5. a. $(B+D)(x)=B(x)+D(x)$

$$
\begin{aligned}
& =\left(-2.6 x^{2}+49 x+3994\right)+\left(-0.6 x^{2}+7 x+2412\right) \\
& =-2.6 x^{2}+49 x+3994-0.6 x^{2}+7 x+2412 \\
& =-3.2 x^{2}+56 x+6406
\end{aligned}
$$

b. $(B+D)(x)=-3.2 x^{2}+56 x+6406$

$$
\begin{aligned}
(B+D)(5) & =-3.2(3)^{2}+56(3)+6406 \\
& =6545.2
\end{aligned}
$$

The number of births and deaths in the U.S. in 2003 was 6545.2 thousand.
c. $(B+D)(x)$ overestimates the actual number of births and deaths in 2003 by 7.2 thousand.

### 2.3 Concept and Vocabulary Check

1. zero
2. negative
3. $f(x)+g(x)$
4. $f(x)-g(x)$
5. $f(x) \cdot g(x)$
6. $\frac{f(x)}{g(x)} ; g(x)$
7. $(-\infty, \infty)$
8. $(2, \infty)$
9. $(0,3) ;(3, \infty)$

### 2.3 Exercise Set

1. Domain of $f$ is $(-\infty, \infty)$.
2. Domain of $f$ is $(-\infty, \infty)$.
3. Domain of $g$ is $(-\infty,-4)$ or $(-4, \infty)$.
4. Domain of $g$ is $(-\infty,-5)$ or $(-5, \infty)$.
5. Domain of $f$ is $(-\infty, 3)$ or $(3, \infty)$.
6. Domain of $f$ is $(-\infty, 2)$ or $(2, \infty)$.
7. Domain of $g$ is $(-\infty, 5)$ or $(5, \infty)$.
8. Domain of $g$ is $(-\infty, 6)$ or $(6, \infty)$.
9. Domain of $f$ is $(-\infty,-7)$ or $(-7,9)$ or $(9, \infty)$.
10. Domain of $f$ is $(-\infty,-8)$ or $(-8,10)$ or $(10, \infty)$.
11. $(f+g)(x)=(3 x+1)+(2 x-6)$

$$
\begin{aligned}
& =3 x+1+2 x-6 \\
& =5 x-5
\end{aligned}
$$

$$
\begin{aligned}
(f+g)(5) & =5(5)-5 \\
& =25-5=20
\end{aligned}
$$

12. $(f+g)(x)=(4 x+2)+(2 x-9)$

$$
\begin{aligned}
& =4 x+2+2 x-9 \\
& =6 x-7
\end{aligned}
$$

$$
(f+g)(5)=6(5)-7=30-7=23
$$

13. $(f+g)(x)=(x-5)+\left(3 x^{2}\right)$

$$
\begin{aligned}
& =x-5+3 x^{2} \\
& =3 x^{2}+x-5
\end{aligned}
$$

$$
\begin{aligned}
(f+g)(5) & =3(5)^{2}+5-5 \\
& =3(25)=75
\end{aligned}
$$

14. $(f+g)(x)=(x-6)+\left(2 x^{2}\right)$

$$
\begin{aligned}
& =x-6+2 x^{2} \\
& =2 x^{2}+x-6
\end{aligned}
$$

$$
\begin{aligned}
(f+g)(5) & =2(5)^{2}+5-6 \\
& =2(25)+5-6 \\
& =50+5-6=49
\end{aligned}
$$

15. $(f+g)(x)$

$$
\begin{aligned}
& =\left(2 x^{2}-x-3\right)+(x+1) \\
& =2 x^{2}-x-3+x+1
\end{aligned}
$$

$$
=2 x^{2}-2
$$

$$
\begin{aligned}
(f+g)(5) & =2(5)^{2}-2 \\
& =2(25)-2 \\
& =50-2=48
\end{aligned}
$$

16. $(f+g)(x)=\left(4 x^{2}-x-3\right)+(x+1)$

$$
\begin{aligned}
& =4 x^{2}-x-3+x+1 \\
& =4 x^{2}-2
\end{aligned}
$$

$$
\begin{aligned}
(f+g)(5) & =4(5)^{2}-2=4(25)-2 \\
& =100-2=98
\end{aligned}
$$

17. $(f+g)(x)=(5 x)+(-2 x-3)$

$$
\begin{aligned}
& =5 x-2 x-3 \\
& =3 x-3
\end{aligned}
$$

$$
\begin{aligned}
(f-g)(x) & =(5 x)-(-2 x-3) \\
& =5 x+2 x+3 \\
& =7 x+3
\end{aligned}
$$

$(f g)(x)=(5 x)(-2 x-3)$

$$
=-10 x^{2}-15 x
$$

$(f)(x)=\frac{5 x}{-2 x-3}$
18. $(f+g)(x)=(-4 x)+(-3 x+5)$

$$
\begin{aligned}
& =-4 x-3 x+5 \\
& =-7 x+5
\end{aligned}
$$

$$
(f-g)(x)=(-4 x)-(-3 x+5)
$$

$$
=-4 x+3 x-5
$$

$$
=-x-5
$$

$(f g)(x)=(-4 x)(-3 x+5)$ $=12 x^{2}-20 x$
$\left(\frac{f}{g}\right)(x)=\frac{-4 x}{-3 x+5}$
19. Domain of $f+g=(-\infty, \infty)$.
20. Domain of $f+g=(-\infty, \infty)$.
21. Domain of $f+g=(-\infty, 5)$ or $(5, \infty)$.
22. Domain of $f+g=(-\infty, 6)$ or $(6, \infty)$.
23. Domain of $f+g=(-\infty, 0)$ or $(0,5)$ or $(5, \infty)$.
24. Domain of $f+g=(-\infty, 0)$ or $(0,6)$ or $(6, \infty)$.
25. Domain of $f+g=f+g=(-\infty,-3)$ or $(-3,2)$ or $(2, \infty)$.
26. Domain of $f+g=f+g=(-\infty,-8)$ or $(-8,4)$ or $(4, \infty)$.
27. Domain of $f+g=(-\infty, 2)$ or $(2, \infty)$.
28. Domain of $f+g=(-\infty, 4)$ or $(4, \infty)$.
29. Domain of $f+g=(-\infty, \infty)$.
30. Domain of $f+g=(-\infty, \infty)$.
31. $(f+g)(x)=f(x)+g(x)$

$$
=x^{2}+4 x+2-x
$$

$$
=x^{2}+3 x+2
$$

$$
(f+g)(3)=(3)^{2}+3(3)+2=20
$$

32. $(f+g)(x)=f(x)+g(x)$

$$
=x^{2}+4 x+2-x
$$

$$
=x^{2}+3 x+2
$$

$$
(f+g)(4)=(4)^{2}+3(4)+2=30
$$

33. $f(-2)+g(-2)=\left((-2)^{2}+4(-2)\right)+(2-(-2))=-4+4=0$
34. $f(-3)+g(-3)=\left((-3)^{2}+4(-3)\right)+(2-(-3))=-3+5=2$
35. $(f-g)(x)=f(x)-g(x)$

$$
\begin{aligned}
& =\left(x^{2}+4 x\right)-(2-x) \\
& =x^{2}+4 x-2+x \\
& =x^{2}+5 x-2 \\
(f-g)(5) & =(5)^{2}+5(5)-2 \\
& =25+25-2=48
\end{aligned}
$$

36. $(f-g)(x)=f(x)-g(x)$
```
    = +30-2=64
    (
    x
    2
    +
    4
    x
    )
    (
    2
    x
    )
    =
    x
2
+
4
x
2
+
x
=
x
2
+
5
x
-
(f -
g)(6
)=
(6)
+
5(6)
-2
=
3
6
```

37. $f(-2)-g(-2)=\left((-2)^{2}+4(-2)\right)-(2-(-2))=-4-4=-8$
38. $f(-3)-g(-3)=\left((-3)^{2}+4(-3)\right)-(2-(-3))=-3-5=-8$
39. $(f g)(-2)=f(-2) \cdot g(-2)=\left((-2)^{2}+4(-2)\right) \cdot(2-(-2))=-4(4)=-16$
40. $(f g)(-3)=f(-3) \cdot g(-3)=\left((-3)^{2}+4(-3)\right) \cdot(2-(-3))=-3(5)=-15$
41. $(f g)(5)=f(5) \cdot g(5)=\left((5)^{2}+4(5)\right) \cdot(2-(5))=45(-3)=-135$
42. $(f g)(6)=f(6) \cdot g(6)=\left((6)^{2}+4(6)\right) \cdot(2-(6))=60(-4)=-240$
43. 

$(f)()^{f(\underline{x})} \underline{x}^{2}+4 x$
$(g)^{x}=g(x)=2-x$
$\binom{f}{g}(1)=\frac{(1)^{2}+4(1)}{2-(1)}=\frac{1+4}{1}=\frac{5}{1}=5$
44. $\binom{f}{g}(x)=\begin{aligned} & f(\underline{x}) \\ & g(x)\end{aligned}=\frac{x^{2}}{2} \frac{+4 x}{x}$

1
$\binom{f}{g}(3)=\frac{(3)^{2}+4(3)}{2-3}=\frac{9+12}{-1}=\frac{21}{-1}=-21$
45. $(f)() \quad \underline{f}(\underline{x}) \quad \underline{x}^{2}+4 x$

$$
(g)^{x}=g_{g}(x)=2-x
$$

$$
(f)(-1)=\frac{(-1)^{2}+4(-1)}{2-(-1)}
$$

$$
=\frac{1-4}{3}=\frac{-3}{3}=-1
$$

46. 

$(f)_{()} \quad \underline{(x)} \quad \underline{x}^{2}+4 x$
$(g) x=g(x)=2-x$
$\left(\frac{f}{g}\right)(0)=\frac{(0)^{2}+4(0)}{2-0}=\frac{0+0}{2}=\frac{0}{2}=0$
47. Domain of $f+g=(-\infty, \infty)$.
48. Domain of $f+g=(-\infty, \infty)$.
49.

$$
\begin{aligned}
& (f)()^{f(x)} \underline{x}^{2}+4 x \\
& (g)^{x}=\begin{array}{l}
g(x)
\end{array}=2-x
\end{aligned}
$$

Domain of $\frac{f}{g}=(-\infty, 2)$ or $(2, \infty)$.
50. $(f g)(x)=f(x) \cdot g(x)=\left(x^{2}+4 x\right)(2-x)$

Domain of $f g=(-\infty, \infty)$.
51. $(f+g)(-3)=f(-3)+g(-3)=4+1=5$
52. $(g-f)(-2)=g(-2)-f(-2)=2-3=-1$
53. $(f g)(2)=f(2) g(2)=(-1)(1)=-1$
54. $(g)(3)=\xrightarrow{g(3)}=\frac{0}{}=0$

$$
(f) \quad f(3) \quad-3
$$

55. The domain of $f+g$ is $[-4,3]$.
56. The domain of $\frac{f}{g}$ is $(4,3)$.
57. The graph of $f+g$

58. The graph of $f-g$

59. $(f+g)(1)-(g-f)(-1)$
$=f(1)+g(1)-[g(-1)-f(-1)]$
$=f(1)+g(1)-g(-1)+f(-1)$
$=-6+-3-(-2)+3$
$=-6+-3+2+3=-4$
60. $(f+g)(-1)-(g-f)(0)$
$=f(-1)+g(-1)-[g(0)-f(0)]$
$=3+(-2)-[4-(-2)]$

$$
=3+-2-(4+2)=3+-2-6=-5
$$

61. $(f g)(-2)-\left[\left(\frac{f}{g}\right)(1)\right]^{2}$
$=f(-2) g(-2)-\left[\frac{f(1)}{g(1)}\right]^{2}$
$=5 \cdot 0-\left[\frac{-6}{-3}\right]^{2}=0-2^{2}=0-4=-4$
62. $(f g)(2)-\left[\begin{array}{c}(g) \\ f\end{array}(0)\right]^{2}$
$=f(2) g(2)-\left[\begin{array}{l}g(\underline{0}) \\ f(0)\end{array}\right]^{2}$
$=0(1)-(\underline{4})^{2}=0-(-2)^{2}$

$$
-2
$$

$$
=0-4=-4
$$

63. a. $(M+F)(x)=M(x)+F(x)=(1.5 x+115)+(1.4 x+121)=2.9 x+236$
b. $\quad(M+F)(x)=2.9 x+236$
$(M+F)(20)=2.9(25)+236=308.5$
The total U.S. population in 2010 was 308.5 million.
c. The result in part (b) underestimates the actual total by 0.5 million.
64. a. $(F-M)(x)=F(x)-M(x)=(1.4 x+121)-(1.5 x+115)=-0.1 x+6$
b. $\quad(F-M)(x)=-0.1 x+6$
$(F-M)(20)=-0.1(20)+6=4$
In 2005 there were 4 million more women than men.
c. The result in part (b) is the same as the actual difference.
65. a.
$(\underline{M})_{(x)}=\underline{(\underline{M(x)})}=\underline{1.5 x+115}$

$$
F \quad(F(x)) \quad 1.4 x+121
$$

b. $\quad\left(\frac{M}{F}\right)(x)=\frac{1.5 x+115}{1.4 x+121}$
$\left(\frac{M}{F}\right)_{(15)}=\frac{1.5(15)+115}{1.4(15)+121} \approx 0.968$
In 2000 the ratio of men to women was 0.968 .
c. The result in part (b) underestimates the actual ratio of $\frac{138}{143} \approx 0.965$ by about 0.003 .
66. First, find $(R-C)(x)$.

$$
\begin{gathered}
(R-C)(x)=65 x-(600,000+45 x) \\
=65 x-600,000-45 x \\
=20 x-600,000 \\
(R-C)(20,000) \\
=20(20,000)-600,000 \\
=400,000-600,000=-200,000
\end{gathered}
$$

This means that if the company produces and sells 20,000 radios, it will lose $\$ 200,000$.

$$
(R-C)(30,000)
$$

$$
=20(30,000)-600,000
$$

$$
=600,000-600,000=0
$$

If the company produces and sells 30,000 radios, it will break even with its costs equal to its revenue.

$$
\begin{aligned}
& (R-C)(40,000) \\
= & 20(40,000)-600,000 \\
= & 800,000-600,000=200,000
\end{aligned}
$$

This means that if the company produces and sells 40,000 radios, it will make a profit of $\$ 200,000$.
67. - 70. Answers will vary.
71. $y_{1}=2 x+3 \quad y_{2}=2-2 x \quad y_{3}=y_{1}+y_{2}$

72.

73. $y_{1}=x \quad y_{2}=x-4 \quad y_{3}=y_{1} \cdot y_{2}$

74. $y_{1}=x^{2}-2 x \quad y_{2}=x$
$y_{3}=\frac{y_{1}}{y_{2}}$
75.


No $y$-value is displayed because undefined at $x=0$.
76. makes sense
77. makes sense
78. makes sense
79. makes sense
80. true
81. true
82. true
83. false; Changes to make the statement true will vary. A sample change is: $f(a)$ or $f(b)$ is 0 .
84. $R=3(a+b)$

$$
\begin{aligned}
R & =3 a+3 b \\
R-3 a & =3 b \\
b & =\frac{R-3 a}{} \text { or } b=\underline{R}-a
\end{aligned}
$$

85. $3(6-x)=3-2(x-4)$

$$
\begin{aligned}
18-3 x & =3-2 x+8 \\
18-3 x & =11-2 x \\
18 & =11+x \\
7 & =x
\end{aligned}
$$

The solution set is $\{7\}$.
86. $f(b+2)=6(b+2)-4$

$$
=6 b+12-4=6 b+8
$$

87. a. $4 x-3 y=6$

$$
4 x-3(0)=6
$$

$$
4 x=6
$$

$$
x=\frac{3}{2}
$$

b. $\quad 4 x-3 y=6$

$$
4(0)-3 y=6
$$

$$
-3 y=6
$$

$$
y=-2
$$

88. a.

| $x$ | $y=2 x+4$ | $(x, y)$ |
| :---: | :---: | :---: |
| -3 | $2(-3)+4=-2$ | $(-3,-2)$ |
| -2 | $2(-2)+4=0$ | $(-2,0)$ |
| -1 | $2(-1)+4=2$ | $(-1,2)$ |
| 0 | $2(0)+4=4$ | $(0,4)$ |
| 1 | $2(1)+4=6$ | $(1,6)$ |


b. The graph crosses the $x$-axis at the point $(-2,0)$.
c. The graph crosses the $y$-axis at the point $(0,4)$.
89. $5 x+3 y=-12$

$$
\begin{aligned}
3 y & =-5 x-12 \\
\frac{3 y}{3} & =\frac{-5 x}{3}-\frac{12}{3}
\end{aligned}
$$

## Mid-Chapter Check Point - Chapter 2

1. The relation is not a function.

The domain is $\{1,2\}$.
The range is $\{-6,4,6\}$.
2. The relation is a function.

The domain is $\{0,2,3\}$.
The range is $\{1,4\}$.
3. The relation is a function.

The domain is $[-2,2)$.
The range is $[0,3]$.
4. The relation is not a function.

The domain is $(-3,4]$.
The range is $[-1,2]$.
5. The relation is not a function.

The domain is $\{-2,-1,0,1,2\}$.
The range is $\{-2,-1,1,3\}$.
6. The relation is a function.

The domain is $(-\infty, 1]$.
The range is $[-1, \infty)$.
7. The graph of $f$ represents the graph of a function because every element in the domain corresponds to exactly one element in the range. It passes the vertical line test.
8. $f(-4)=3$
9. The function $f(x)=4$ when $x=-2$.
10. The function $f(x)=0$ when $x=2$ and $x=-6$.
11. The domain of $f$ is $(-\infty, \infty)$.
12. The range of $f$ is $(-\infty, 4]$.
13. The domain is $(-\infty, \infty)$.
14. The domain of $g$ is $(-\infty,-2)$ or $(-2,2)$ or $(2, \infty)$.
15. $f(0)=0^{2}-3(0)+8=8$
$g(-10)=-2(-10)-5=20-5=15$
$f(0)+g(-10)=8+15=23$

$$
y=-\frac{5}{3} x-4
$$

16. $f(-1)=(-1)^{2}-3(-1)+8=1+3+8=12$
$g(3)=-2(3)-5=-6-5=-11$
$f(-1)-g(3)=12-(-11)=12+11=23$
17. $f(a)=a^{2}-3 a+8$

$$
\begin{aligned}
g(a+3) & =-2(a+3)-5 \\
& =-2 a-6-5=-2 a-11
\end{aligned}
$$

$$
\begin{aligned}
f(a)+g(a+3) & =a^{2}-3 a+8+-2 a-11 \\
& =a^{2}-5 a-3
\end{aligned}
$$

18. $(f+g)(x)=x^{2}-3 x+8+-2 x-5$

$$
\begin{gathered}
=x^{2}-5 x+3 \\
(f+g)(-2)=(-2)^{2}-5(-2)+3 \\
=4+10+3=17
\end{gathered}
$$

19. $(f-g)(x)=x^{2}-3 x+8-(-2 x-5)$

$$
=x^{2}-3 x+8+2 x+5
$$

$$
=x^{2}-x+13
$$

$$
(f-g)(5)=(5)^{2}-5+13
$$

$$
=25-5+13=33
$$

20. $f(-1)=(-1)^{2}-3(-1)+8$

$$
=1+3+8=12
$$

$$
\begin{aligned}
& g(-1)=-2(-1)-5=2-5=-3 \\
& (f g)(-1)=12(-3)=-36
\end{aligned}
$$

2
21. $(f)(x)=\underline{x-3 x+8}$

$$
g \quad-2 x-5
$$

2

$$
\begin{aligned}
(f)(-4) & =\frac{(-4)-3(-4)+8}{(g)} \\
& =\frac{16+12+8}{8-5}=\frac{36}{3}=12
\end{aligned}
$$

22. The domain of $f$ is $(-\infty,-\underline{5})$ or $\left(-\frac{5}{, \infty}\right)$.

$$
\begin{array}{lll}
g & 2 & 2
\end{array}
$$

5. Begin by plotting the $y$-intercept of 0 . Then use the
slope of $\frac{-2}{3}$ to plot more points.
$f(x)=-\frac{2}{3} x^{\prime} y_{\text {f }}^{\prime 2}$
6. $y=3$ is a horizontal line.

7. $x=-3$ is a vertical line.

8. $m=\underline{\underline{y}}-\underline{y}_{1}=\frac{4.4-4.65}{}=\frac{-0.25}{}=-0.05$

$$
x_{2}-x_{1} \quad 2010-2005 \quad 5
$$

From 2005 through 2010, the average waste produced per person in the U.S. decreased by 0.05 pound per day each year.
9. $m=\underline{y_{2}}-\underline{y}_{1}=\frac{0.05-0.03}{}=\frac{0.02}{} \approx 0.01$

$$
\begin{array}{ccc}
x_{2}-x_{1} & 3-1 & 2
\end{array}
$$

The average rate of change between 1 hour and 3 hours is 0.01 . This means that the drug's concentration is increasing at an average rate of 0.01 milligram per 100 milliliters per hour.
10. a. We will use the line segment passing through
$(60,390)$ and $(0,310)$ to obtain a model. We need values for $m$, the slope, and $b$, the $y$-intercept.
$m=\frac{y_{2}}{x_{2}-x_{1}} \frac{-x_{1}}{60-0}=\frac{390-310}{60} \approx 1.33$
The point $(0,310)$ gives us the $y$-intercept of 310 .
Thus, $C(x)=m x+b$

$$
C(x)=1.33 x+310
$$

b. $\quad C(x)=1.33 x+310$

$$
\begin{aligned}
C(100) & =1.33(100)+310 \\
& =443
\end{aligned}
$$

The model predicts the average atmospheric concentration of carbon dioxide will be 443 parts per million in 2050.

### 2.4 Concept and Vocabulary Check

1. scatterplot; regression
2. standard
3. $x$-intercept; zero
4. $y$-intercept; zero
5. $\frac{y_{2}-y_{1}}{x-x}$

21
6. positive
7. negative
8. zero
9. undefined
10. $y=m x+b$
11. $(0,3) ; 2 ; 5$
12. horizontal
13. vertical
14. $y ; x$

### 2.4 Exercise Set

1. $x+y=4$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
x+y & =4 \\
x+0 & =4 \\
x & =4
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.
$x+y=4$
$0+y=4$
$y=4$

| $x+y=4 \quad y_{\mathcal{A}}$ |
| :--- |
|  |

2. $x+y=2$

Find the $x$-intercept by setting $y=0$.
$x+0=2$
$x=2$
Find the $y$-intercept by setting $x=0$.
$0+y=2$
$y=2$
$x+y=2 \quad y$

$(3,-1)$
3. $x+3 y=6$

Find the $x$-intercept by setting $y=0$.
$x+3(0)=6$

$$
x=6
$$

Find the $y$-intercept by setting $x=0$.
$(0)+3 y=6$

$$
y=2
$$

4. $2 x+y=4$

Find the $x$-intercept by setting $y=0$.
$2 x+0=4$
$2 x=4$
$x=2$
Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
2(0)+y & =4 \\
y & =4
\end{aligned}
$$


5. $6 x-2 y=12$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
6 x-2(0) & =12 \\
6 x & =12 \\
x & =2
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
6(0)-2 y & =12 \\
-2 y & =12 \\
y & =-6
\end{aligned}
$$



6. $6 x-9 y=18$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
6 x-9(0) & =18 \\
6 x & =18 \\
x & =3
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{array}{r}
6(0)-9 y=18 \\
0-9 y=18 \\
-9 y=18 \\
y=-2
\end{array}
$$


7. $3 x-y=6$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
3 x-0 & =6 \\
3 x & =6 \\
x & =2
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
3(0)-y & =6 \\
-y & =6 \\
y & =-6
\end{aligned}
$$


8. $x-4 y=8$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
x+4(0) & =8 \\
x+0 & =8 \\
x & =8
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
0-4 y & =8 \\
-4 y & =8 \\
y & =-2
\end{aligned}
$$


9. $x-3 y=9$

Find the $x$-intercept by setting $y=0$.
$x-3(0)=9$

$$
x=9
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
(0)-3 y & =9 \\
-3 y & =9 \\
y & =-3
\end{aligned}
$$


10. $2 x-y=5$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
2 x-0 & =5 \\
2 x & =5 \\
x & =\frac{5}{2}
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
2(0)-y & =5 \\
-y & =5 \\
y & =-5
\end{aligned}
$$


11. $2 x=3 y+6$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
2 x & =3(0)+6 \\
2 x & =6 \\
x & =3
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
2(0) & =3 y+6 \\
0 & =3 y+6 \\
-6 & =3 y \\
-2 & =y
\end{aligned}
$$


12. $3 x=5 y-15$

Find the $x$-intercept by setting $y=0$.
$3 x=5(0)-15$
$3 x=0-15$
$3 x=-15$
$x=-5$
Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
3(0) & =5 y-15 \\
0 & =5 y-15 \\
15 & =5 y \\
3 & =y
\end{aligned}
$$


13. $6 x-3 y=15$

Find the $x$-intercept by setting $y=0$.
$6 x-3(0)=15$
$6 x=15$
$x=\frac{15}{6}=\frac{5}{2}$
Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
& 6(0)-3 y=15 \\
& -3 y=15 \\
& y=-5
\end{aligned}
$$

14. $8 x-2 y=12$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
8 x-2(0) & =12 \\
8 x & =12 \\
x & =\frac{12}{8} \\
x & =\underline{3}
\end{aligned}
$$

$$
2
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{array}{r}
8(0)-2 y=12 \\
-2 y=12 \\
y=-6
\end{array}
$$


15. $m=\frac{8-4}{=}=4$

$$
3-2 \quad 1
$$

The line rises.
16. $m=\frac{4-1}{5-3}=\frac{3}{2}$

The line rises.
17. $m=\frac{5-4}{}=\frac{1}{}=\frac{1}{}$

$$
2-(-1) \quad 2+1 \quad 3
$$

The line rises.

$$
\underline{5-(-2)} \quad \underline{5+2} \quad \underline{7}
$$

18. $m=\underset{2-(-3)}{ }=$

The line rises.
19. $m=\frac{5-5}{}=\frac{0}{}=0$

$$
-1-2 \quad-3
$$

The line is horizontal.
$\underline{3-(-1)} \quad \underline{3+1} \quad \underline{4} \quad \underline{1}$
22. $m=-6-2=-8=-8=-2$

The line falls.
23. $m=\frac{6-(-4)}{-3-(-7)}=\frac{10}{4}=\frac{5}{2}$

The line rises.
24. $m=\begin{gathered}-(-4) \\ -1-(-3)\end{gathered}=\begin{gathered}10 \\ 2\end{gathered}=5$

The line rises.
25. $m=\frac{4^{-(-2)}}{\frac{1}{2}-\frac{7}{2}}=\frac{4^{\frac{1}{4}}}{0}=$ undefined
undefined slope; The line is vertical.

$$
\underline{1}_{-(-6)} \quad \underline{1}_{+6}
$$

26. $m=\frac{6}{\frac{3}{2}-\frac{3}{2}}=\frac{6}{0}=$ undefined
undefined sl $m=\begin{aligned} & \underline{5-(-2)} \quad \underline{5+2} \quad \underline{7} \\ & 2-(-3)\end{aligned}=\begin{aligned} & 2+3\end{aligned}$ ope; The line is vertical.
27. Line 1 goes through $(-3,0)$ and $(0,2)$.
$m=\frac{2-0}{}=\underline{2}$
$0-(-3) \quad 3$
Line 2 goes through $(2,0)$ and $(0,4)$.
$m=\underline{4-0}=\underline{4}=-2$
$0-2 \quad-2$
Line 3 goes through $(0,-3)$ and $(2,-4)$.
$m=\frac{-4-(-3)}{2-0}=\frac{-4+3}{2}=\frac{-1}{1}$
28. $L_{1}$ passes through $(1,0)$ and $(0,-1)$.

$=$
29. $m=\xrightarrow{\underline{-3-(-3)}}=\underline{-3+3}=\underline{0}=0$

$$
4-(-6) \quad 4+6 \quad 10
$$

The line is horizontal.
21. $m=\frac{-3-1}{-4-(-7)}=\frac{-4}{-4+7}=\frac{-4}{3}=-\frac{4}{3}$

The line falls.

```
\overline{1}
    L2 passes through (4,-2) and (1,-4).
```

$$
\begin{gathered}
m=\frac{-4-(-2)}{}=\frac{-4+2}{}=\frac{-2}{2}=\frac{2}{-4}-3=3
\end{gathered}
$$

$L_{3}$ passes through $(-4,2)$ and $(-3,0)$.
$m=\frac{0-2}{-2}=\frac{-2}{-2}=\frac{-2}{-3+4}=-$
29. $y=2 x+1$
$m=2 \quad y$-intercept $=1$
$y=2 x+1 \quad y$

30. $y=3 x+2$
$m=3 \quad y$-intercept $=2$

31. $y=-2 x+1$
$m=-2 \quad y$-intercept $=1$

32. $f(x)=-3 x+2$
$m=-3 \quad y-$ intercept $=2$

33. $f(x)=\frac{3}{4} x-2$
$m=\frac{3}{4} \quad y$-intercept $=-2$
$f(x)=\frac{3}{4} x+2$
34. $f(x)=\frac{3}{4} x-3$
$m=\frac{3}{4} \quad y-$ intercept $=-3$

35. $f(x)=-\frac{3}{5} x+7$
$m=-\frac{3}{5} \quad y-$ intercept $=7$
$f(x)=-\frac{3}{5} x+7 \quad y_{1}$
36. $f(x)=-\frac{2}{5} x+6$
$m=-\frac{2}{5} \quad y-$ intercept $=6$

$$
f(x)=-\frac{2}{5} x+6
$$

37. $y=-\frac{1}{2} x$
$m=-\frac{1}{2} \quad y-$ intercept $=0$

38. $y=-{ }^{1} x$
$m=-\frac{3}{3} \quad y-$ intercept $=0$
$y=-\frac{1}{3} x$

39. $y=-\frac{1}{2}$
$m=0 \quad y-$ intercept $=-\frac{1}{2}$
40. $y=-\frac{1}{3}$

$$
m=0 \quad y-\text { intercept }=-\frac{1}{3}
$$


41. a. $2 x+y=0$
$y=-2 x$
b. $m=-2 \quad y$-intercept $=0$
c. $y=-2 x y_{4}$

42. a. $3 x+y=0$

$$
y=-3 x
$$

b. $\quad m=-3 \quad y$-intercept $=0$
c. $y=-3 x \quad y_{\text {A }}$

43. a. $5 y=4 x$

$$
y=\frac{4}{5} x
$$

$\underline{4}$
b. $\quad m={ }_{5} \quad y$-intercept $=0$
c. $y=\frac{4}{5} x$

44. a. $4 y=3 x$

$$
y=\frac{3}{4} x
$$

b. $\quad m=\frac{3}{4} \quad y$-intercept $=0$
c.

45. a. $3 x+y=2$

$$
y=-3 x+2
$$

b. $\quad m=-3 \quad y$-intercept $=2$
c. $y=-3 x+2 y$

46. a. $2 x+y=4$
$y=-2 x+4$
b. $m=-2 \quad y$-intercept $=4$

c. $y=-\mathbf{2 x + 4}$| $\boldsymbol{y}$ A |
| :---: |

47. a. $5 x+3 y=15$

$$
\begin{aligned}
3 y & =-5 x+15 \\
y & =-\frac{5}{3} x+5
\end{aligned}
$$

b. $\quad m=-\frac{5}{3} \quad y$-intercept $=5$
c.

48. a. $7 x+2 y=14$

$$
\begin{aligned}
2 y & =-7 x+14 \\
y & =-\frac{7}{2} x+7
\end{aligned}
$$

b. $m=-\frac{7}{2} \quad y-$ intercept $=7$
c.

49. $y=3$

50. $y=5$

51. $f(x)=-2$
$y=-2$

52. $f(x)=-4$ which is the same as $y=-4$

53. $3 y=18$
$y=6$

54. $5 y=-30$

$$
y=-6
$$


55. $f(x)=2$

$$
y=2
$$


56. $f(x)=1$ or $y=1$

57. $x=5$

58. $x=4$

59. $3 x=-12$
$x=-4$

60. $4 x=-12$

$$
x=-3
$$


61. $x=0$

This is the equation of the $y$-axis.

62. $y=0$

This is the equation of the $x$-axis.

63. $m=\frac{0-a}{=}=-\underline{a}$

$$
b-0 \quad b \quad b
$$

Since $a$ and $b$ are both positive, $-\frac{a}{b}$ is negative.
Therefore, the line falls.
64. $m=\frac{-b-0}{}=\frac{-b}{}=-\underline{b}$

$$
0-(-a) \quad a \quad a
$$

The line falls.
65. $m=\frac{(b+c)-b}{a-a} \stackrel{c}{=}$

The slope is undefined.
The line is vertical.
66. $m=\underline{(a+c)-c}=\underline{a}$

$$
a-(a-b) \quad b
$$

The line rises.
67. $A x+B y=C$

$$
\begin{aligned}
B y & =-A x+C \\
y & =-\frac{A}{B} x+\frac{C}{B}
\end{aligned}
$$

The slope is $-\frac{A}{B}$ and the $y$-intercept is $\frac{C}{B}$.
68. $A x=B y-C$

$$
A x+C=B y
$$

$\frac{A}{B} x+\frac{C}{B}=y$
The slope is $\frac{A}{B}$ and the $y$-intercept is $\frac{C}{B}$.
69. $-3=\frac{4-y}{1-3}$
70. $\frac{1}{3}=\frac{-4-y}{4-(-2)}$
$\frac{1}{3}=\frac{-4-y}{4+2}$
$\frac{1}{3}=\frac{-4-y}{6}$
$6=3(-4-y)$
$6=-12-3 y$
$18=-3 y$
$-{ }^{6}={ }^{y}$
71. $3 x-4 f(x)=6$
$-4 f(x)=-3 x+6$
$f(x)=\frac{3}{4} x-\frac{3}{2}$
$3 x-4 f(x)=6$
72. $6 x-5 f(x)=20$
$-5 f(x)=-6 x+20$
$f(x)=\frac{6}{5} x-4$
$6 x-5 f(x)=20 y_{\uparrow}$

73. Using the slope-intercept form for the equation of a line:
$-1=-2(3)+b$
$-1=-6+b$
$5=b$
$-3=4$
$-y \quad 74$.

$$
\begin{aligned}
& -6=\begin{array}{l}
3 \\
- \\
2
\end{array} \\
& \\
& \begin{array}{l}
-2)+b \\
6=4-y \\
2=-y \\
-2=y
\end{array}
\end{aligned}
$$

$$
-6=-3+b
$$

$$
-3=b
$$

75. The line with slope $m_{1}$ is the steepest rising line so its slope is the biggest positive number. Then the line with slope $m_{3}$ is next because it is the only other
line whose slope is positive. Since the line with slope $m_{2}$ is less steep but decreasing, it is next. The slope $m_{4}$ is the smallest because it is negative and the line with slope $m_{4}$ is steeper than the line with slope $m_{3}$, so its slope is more negative.
Decreasing order: $m_{1}, m_{3}, m_{2}, m_{4}$
76. Decreasing order: $b_{2}, b_{1}, b_{4}, b_{3}$
77. The slope is 55.7. This means Smartphone sales are increasing by 55.7 million each year.
78. The slope is 2 . This means the amount spent by the drug industry to market drugs to doctors is
increasing by $\$ 2$ billion each year.
79. The slope is -0.52 . This means the percentage of U.S. adults who smoke cigarettes is decreasing by $0.52 \%$ each year.
80. The slope is -0.28 . This means the percentage of U.S. taxpayers audited by the IRS is decreasing by $0.28 \%$ each year.
81. a. $30 \%$ of marriages in which the wife is under 18 when she marries end in divorce within the first five years.
b. $50 \%$ of marriages in which the wife is under 18 when she marries end in divorce within the first ten years.
c. $m=\underline{y}_{\underline{2}}-\underline{y} \underline{1}=\frac{50-30}{}=\underline{20}=4$

$$
\begin{array}{lll}
x_{2}-x_{1} & 10-5 & 5
\end{array}
$$

There is an average increase of $4 \%$ of marriages ending in divorce per year.
82. a. $15 \%$ of marriages in which the wife is over age 25 when she marries end in divorce within the first five years.
b. $25 \%$ of marriages in which the wife is over age 25 when she marries end in divorce within the first ten years.
83. a. The $y$-intercept is 254 . This represents if no women in a country are literate, the mortality rate of children under five is 254 per thousand.
b. $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{110-254}{60-0}=\frac{-144}{60}=-2.4$

For each $1 \%$ of adult females who are literate, the mortality rate of children under five decreases by 2.4 per thousand.
c. $f(x)=-2.4 x+254$
d. $f(50)=-2 \cdot 4(50)+254=134$

A country where $50 \%$ of adult females are literate is predicted to have a mortality rate of children under five of 134 per thousand.
$m=\frac{\underline{y_{2}}-y_{1}}{x_{2}-x_{1}}=\frac{\underline{6.7-3.1}}{20-0}=\frac{\underline{3.6}}{20}=$

The percentage of America's black population that is foreign-born is increasing by 0.18 each year. The rate of change is $0.18 \%$ per year..
b. $C(x)=0.18 x+3.1$
c. $\quad C(x)=0.18 x+3.1$
$C(80)=0.18(80)+3.1$
$=17.5$
The percentage of America's black population that will be foreign-born in 2060 is $17.5 \%$..
85. $P(x)=0.24 x+29$
86. $P(x)=0.24 x+30$
87. - 104. Answers will vary.
105. $y=2 x+4$


Two points found using [TRACE] are $(0,4)$ and
$(2,8)$
c. $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{25-15}{10-5}=\frac{10}{5}=2$

There is an average increase of $2 \%$ of marriages ending in divorce per year.
$m=\frac{8-4}{=}=2$

$$
2-0 \quad 2
$$

This is the same as the coefficient of $x$ in the line's equation.
106. $y=-3 x+6$


Two points found using [TRACE] are $(0,6)$ and $(2,0)$. Based on these points, the slope is:

$$
\begin{aligned}
m= & \frac{6-0}{}=\frac{6}{}=-3 . \\
& 0-2
\end{aligned}
$$

This is the same as the coefficient of $x$ in the line's equation.
107. $y=-\frac{1}{2} x-5$


Two points found using [TRACE] are $(0,-5)$ and $(1,-5.5)$. Based on these points, the slope is:
$m=\begin{aligned} & \underline{-5.5-(-5)} \underline{-5.5+5}=\underline{-0.5} \\ & 1-0=1=1=-0.5 .\end{aligned}$
This is the same as the coefficient of $x$ in the line's equation.
108. $y=\frac{3}{4} x-2$


Two points found using [TRACE] are $(0,-2)$ and
109. does not make sense; Explanations will vary. Sample explanation: Linear functions never change from rising to falling.
110. does not make sense; Explanations will vary. Sample explanation: Since this value is increasing, it will have a positive slope.
111. does not make sense; Explanations will vary. Sample explanation: This function suggests that the average salary in 2000 was $\$ 1700$, and that there is an annual raise of $\$ 49,100$. The function would make sense if the $x$ was with the 1700 . i.e. $S(x)=1700 x+49,100$
112. makes sense
113. false; Changes to make the statement true will vary. A sample change is: One nonnegative slope is 0 . A line with slope equal to zero does not rise from left to right.
114. false; Changes to make the statement true will vary. A sample change is: Slope-intercept form is $y=m x+b$. Vertical lines have equations of the form $x=a$. Equations of this form have undefined slope and cannot be written in slope-intercept form.
115. true
116. false; Changes to make the statement true will vary. A sample change is: The graph of $x=7$ is a
vertical line that passes through the point $(7,0)$.
117. We are given that the $x$-intercept is -2 and the $y$-intercept is 4 . We can use the points $(-2,0)$ and $(0,4)$ to find the slope.
$m=\frac{4-0}{0-(-2)}=\frac{4}{0+2}=\frac{4}{2}=2$
$(1,-1.25)$. Based on these points, the slope is:

$$
m=\frac{-2-(-1.25)}{}=\frac{-0.75}{}=0.75 .
$$

Using the slope and one of the intercepts, we can write the line in point-slope form.

$$
\begin{aligned}
& y-y_{1}=m\left(x-x_{1}\right) \\
& y-0=2(x-(-2))
\end{aligned}
$$

$$
0-1 \quad-1
$$

This is equivalent to the coefficient of $x$ in the line's equation.

Find the $x$ - and $y$-coefficients for the equation of the line with right-hand-side equal to 12 . Multiply
both sides of $-2 x+y=4$ by 3 to obtain 12 on the
right-hand-side.
$-2 x+y=4$
$3(-2 x+y)=3(4)$
$-6 x+3 y=12$
The coefficients are -6 and 3 .
118. We are given that the $y$-intercept is -6 and the slope is $\frac{1}{2}$.
So the equation of the line is $y=\frac{1}{2} x-6$.
We can put this equation in the form $a x+b y=c$ to find the missing coefficients.
$y=\frac{1}{2} x-6$
$y-\frac{1}{2} x=-6$
$2\left(y-\frac{1}{x}\right)=2(-6)$

## 2

$2 y-x=-12$
$x-2 y=12$
Therefore, the coefficient of $x$ is 1 and the coefficient of $y$ is -2 .
119. a. $f\left(x_{1}+x_{2}\right)=m\left(x_{1}+x_{2}\right)+b$

$$
=m x_{1}+m x_{2}+b
$$

b. $f\left(x_{1}\right)+f\left(x_{2}\right)$

$$
\begin{aligned}
& =m x_{1}+b+m x_{2}+b \\
& =m x_{1}+m x_{2}+2 b
\end{aligned}
$$

c. no
120. $\left(\frac{4 x^{2}}{y^{-3}}\right)^{2}=\left(4 x^{2} y^{3}\right)^{2}=4^{2}\left(x^{2}\right)^{2}\left(y^{3}\right)^{2}$

$$
=16 x^{4} y^{6}
$$

121. $\left(8 \times 10^{-7}\right)\left(4 \times 10^{3}\right)=32 \times 10^{-4}$

$$
\begin{aligned}
& =\left(3.2 \times 10^{1}\right) \times 10^{-4} \\
& =3.2 \times 10^{-3}
\end{aligned}
$$

122. $5-[3(x-4)-6 x=5-[3 x-12-6 x]$

$$
\begin{aligned}
& =5-3 x+12+6 x \\
& =3 x+17
\end{aligned}
$$

123. $y-5=7(x+4)$
$y-5=7 x+28$
$y=7 x+33$
124. $y+3=-\frac{7}{3}(x-1)$
$y+3=-\frac{7}{3} x+\frac{7}{3}$
$y+3-3=-\frac{7}{3} x+\frac{7}{3}-3$

$$
y=-\frac{7}{-} x-\frac{2}{-}
$$

$$
3 \quad 3
$$

125. a. $x+4 y-8=0$

$$
\begin{aligned}
4 y & =-x+8 \\
\frac{4 y}{4} & =\frac{-x+8}{4} \\
y & \underline{1}_{x+2}
\end{aligned}
$$

$$
=-4
$$

The slope is $-\frac{1}{4}$.
b. $-\frac{1}{4} \cdot m_{2}=-1$
$\underline{1} \cdot m_{2}=1$
$4 m_{2}=4$
The slope of the second line is 4 .

### 2.5 Check Points

1. Slope $=-2$, passing through $(4,-3)$

Point-Slope Form

$$
\begin{array}{r}
y-y_{1}=m\left(x-x_{1}\right) \\
y-(-3)=-2(x-4) \\
y+3=-2(x-4)
\end{array}
$$

Slope-Intercept Form

$$
\begin{aligned}
y+3 & =-2(x-4) \\
y+3 & =-2 x+8 \\
y & =-2 x+5 \\
f(x) & =-2 x+5
\end{aligned}
$$

2. a. Passing through $(6,-3)$ and $(2,5)$

First, find the slope.
$m=\underline{5-(-3)}=\underline{8}=-2$

$$
2-6 \quad-4
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-5 & =-2(x-2)
\end{aligned}
$$

or

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-3) & =-2(x-6) \\
y+3 & =-2(x-6)
\end{aligned}
$$

Answers vary due to rounding and choice of point.
If point $(40,79.7)$ is chosen, $f(x)=0.17 x+72.9$
and the life expectancy of American women in 2020 is predicted to be 83.1 years.
4. Since the line is parallel to $y=3 x+1$, we know it will have slope $m=3$. We are given that it passes through $(-2,5)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-5 & =3(x-(-2)) \\
y-5 & =3(x+2)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-5 & =3(x+2) \\
y-5 & =3 x+6 \\
y & =3 x+11 \\
f(x) & =3 x+11
\end{aligned}
$$

5. a. Solve the given equation for $y$ to obtain slopeintercept form.
$x+3 y=12$

$$
3 y=-x+12
$$

$$
y=-\frac{1}{3} x+4
$$

$$
y=0.17 x+73
$$

$$
f(x)=0.17 x+73
$$

b. Slope-Intercept Form

$$
\begin{aligned}
y-5 & =-2(x-2) \\
y-5 & =-2 x+4 \\
y & =-2 x+9 \\
f(x) & =-2 x+9
\end{aligned}
$$

3. First, find the slope.
$m=\frac{79.7-74.7}{40-10}=\frac{5}{30} \approx 0.17$
Then use the slope and one of the points to write the equation in point-slope form.
Using the point (10, 74.7):

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

$y-74.7=0.17(x-10)$

Since the slope of the given line is $-\frac{1}{3}$, the slope of any line perpendicular to the given line is 3 .
b. We use the slope of 3 and the point $(-2,-6)$ to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-6) & =3(x-(-2)) \\
y+6 & =3(x+2)
\end{aligned}
$$

Next, since 2020 is 60 years after 1960, substitute
60 into the function: $f(60)=0.17(60)+73=83.2$.
This means that the life expectancy of American women in 2020 is predicted to be 83.2 years.

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+6 & =3(x+2) \\
y+6 & =3 x+6 \\
y & =3 x \\
f(x) & =3 x
\end{aligned}
$$

### 2.5 Concept and Vocabulary Check

1. $y-y_{1}=m\left(x-x_{1}\right)$
2. equal/the same
3. -1
4. $-\frac{1}{}$

5
5. $\frac{5}{3}$
6. $-4 ;-4$
7. $\frac{1}{2} ;-2$

### 2.5 Exercise Set

1. Slope $=3$, passing through $(2,5)$

Point-Slope Form

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-5 & =3(x-2)
\end{aligned}
$$

Slope-Intercept Form
$y-5=3(x-2)$
$y-5=3 x-6$

$$
y=3 x-1
$$

$f(x)=3 x-1$
2. Slope $=4$, passing through $(3,1)$

Point-Slope Form
$y-1=4(x-3)$
Slope-Intercept Form
$y-1=4(x-3)$
$y-1=4 x-12$

$$
y=4 x-11
$$

$f(x)=4 x-11$
3. Slope $=5$, passing through $(-2,6)$

Point-Slope Form

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-6 & =5(x-(-2))
\end{aligned}
$$

4. Slope $=8$, passing through $(-4,1)$

Point-Slope Form
$y-1=8(x-(-4))$
$y-1=8(x+4)$
Slope-Intercept Form
$y-1=8 x+32$

$$
y=8 x+33
$$

$f(x)=8 x+33$
5. Slope $=-4$, passing through $(-3,-2)$

Point-Slope Form

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-2) & =-4(x-(-3))
\end{aligned}
$$

$$
y+2=-4(x+3)
$$

Slope-Intercept Form
$y+2=-4(x+3)$
$y+2=-4 x-12$
$y=-4 x-14$
$f(x)=-4 x-14$
6. Slope $=-6$, passing through $(-2,-4)$

Point-Slope Form

$$
\begin{gathered}
y-(-4)=-6(x-(-2)) \\
y+4=-6(x+2) \\
\text { Slope-Intercept Form } \\
y+4=-6 x-12 \\
y=-6 x-16 \\
f(x)=-6 x-16
\end{gathered}
$$

7. Slope $=-5$, passing through $(-2,0)$

Point-Slope Form

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

$$
\begin{aligned}
& \quad y-6=5(x+2) \text { Slope-Intercept } \\
& \text { Form } y-6=5(x+2) \\
& y-6=5 x+10 \\
& \quad y=5 x+16 \\
& f(x)=5 x+16
\end{aligned}
$$

$\quad y-0=-5(x-(-2))$
$y-$
$0=$
$-5(x$
$+2)$
Slope
-
Interc
ept
Form
$y-0$
$=$
$-5(x$
$+2)$
$\quad y$
$\quad=$
$\quad-$
$\quad 5$
$\quad($
$x$
$\quad+$
2
8. Slope $=-4$, passing through $(0,-3)$

Point-Slope Form

$$
\begin{array}{r}
y-(-3)=-4(x-0) \\
y+3=-4(x-0)
\end{array}
$$

Slope-Intercept Form $y+3=-4 x$

$$
y=-4 x-3
$$

$$
f(x)=-4 x-3
$$

9. Slope $=-1$, passing through $\left(-2,-\frac{1}{2}\right)$

Point-Slope Form

$$
\begin{gathered}
y-y_{1}=m\left(x-x_{1}\right) \\
y-\left(-\frac{1}{2}\right)=-1(x-(-2)) \\
y+\frac{1}{2}=-1(x+2)
\end{gathered}
$$

Slope-Intercept Form

$$
y+^{\frac{1}{2}}=-1(x+2)
$$

2
$y+\frac{1}{2}=-x-2$
$y=-x-\frac{5}{2}$
$f(x)=-x-\frac{5}{2}$
10. Slope $=-1$, passing through $\left(-\frac{1}{4},-4\right)$

Point-Slope Form

$$
\begin{aligned}
y-(-4) & =-1\left(x-\left(-\frac{1}{4}\right)\right) \\
y+4 & =-1\left(x+\frac{1}{4}\right)
\end{aligned}
$$

Slope-Intercept Form

$$
\begin{aligned}
y+4 & =-x-\frac{1}{4} \\
y & =-x-\frac{1}{4}-4 \\
y & =-x-\frac{17}{4}
\end{aligned}
$$

$f(x)=-x-\frac{4}{4}$
11. Slope $={ }_{4}$, passing through $(0,0)$

Point-Slope Form

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-0 & =\frac{1}{4}(x-0)
\end{aligned}
$$

Slope-Intercept Form
$y-0=\frac{1}{4}(x-0)$

$$
y=\frac{1}{4} x
$$

$f(x)=\frac{1}{4} x$
12. Slope $=\frac{1}{5}$, passing through $(0,0)$

## Point-Slope Form

$y-0={ }_{5}^{\frac{1}{( }} x-0$
Slope-Intercept Form

$$
y=\frac{1}{5} x
$$

$$
f(x)=\frac{1}{5} x
$$

13. Slope $=-^{\overline{3}}$, passing through $(6,-4)$

Point-Slope Form

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-4) & =-\frac{2}{3}(x-6) \\
y+4 & =-\frac{2}{3}(x-6)
\end{aligned}
$$

Slope-Intercept Form

$$
\begin{aligned}
& y+4=-\frac{2}{3}(x-6) \\
& y+4=-\frac{2}{-} x+4
\end{aligned}
$$

$$
\begin{aligned}
y & =-\frac{2}{3} x \\
f(x) & =-\frac{2}{3} x
\end{aligned}
$$

14. Slope $=-\frac{2}{5}$, passing through $(15,-4)$

Point-Slope Form

$$
\begin{aligned}
& y-(-4)=-\frac{2}{5}(x-15) \\
& \underline{2} \\
& y+4=-{ }_{5}(x-15)
\end{aligned}
$$

Slope-Intercept Form

$$
\begin{aligned}
y+4 & =-\frac{2}{5} x+6 \\
y & =-\frac{2}{5} x+2
\end{aligned}
$$

$$
f(x)=-{ }^{2} x+2
$$

15. Passing through $(6,3)$ and $(5,2)$

First, find the slope.

$$
\begin{aligned}
m= & \frac{2-3}{}=\frac{-1}{5-6}=1 \\
& =1
\end{aligned}
$$

Then use the slope and one of the points to write the equation in point-slope form.
$y-y_{1}=m\left(x-x_{1}\right)$

$$
y-3=1(x-6)
$$

or
$y-2=1(x-5)$
Slope-Intercept Form
$y-2=1(x-5)$
$y-2=x-5$
$y=x-3$
$f(x)=x-3$
16. Passing through $(1,3)$ and $(2,4)$

First, find the slope.
$m=\frac{4-3}{2-1}=\frac{1}{1}=1$
Then use the slope and one of the points to write the equation in point-slope form.
$y-4=1(x-2) \quad$ or $\quad y-3=1(x-1)$

Slope-Intercept Form

$$
\begin{aligned}
y-4 & =1 x-2 \\
y & =x+2 \\
f(x) & =x+2
\end{aligned}
$$

17. Passing through $(-2,0)$ and $(0,4)$

First, find the slope.

$$
\begin{gathered}
m=\frac{4-0}{0-(-2)}=\frac{4}{2}=2 \\
\end{gathered}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-4 & =2(x-0)
\end{aligned}
$$

or
18. Passing through $(2,0)$ and $(0,-1)$

First, find the slope.

$$
\begin{array}{r}
m=\frac{-1-0}{}=\frac{-1}{}=\frac{1}{0-2}-2 \quad 2
\end{array}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
y-0=\frac{1}{-}(x-2) \text { or } y-(-1)=\frac{1}{1}(x-0)
$$

$$
y+1=\frac{2}{2}(x-0)
$$

Slope-Intercept Form

$$
\begin{aligned}
y & =\frac{1}{2} x-1 \\
f(x) & =\frac{1}{2} x-1
\end{aligned}
$$

19. Passing through $(-6,13)$ and $(-2,5)$

First, find the slope.

$$
\begin{aligned}
m= & \frac{5-13}{}=\frac{-8}{-2-(-6) \quad-2+6}=-2
\end{aligned}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

$$
y-5=-2(x-(-2))
$$

$$
y-5=-2(x+2)
$$

or
$y-13=-2(x-(-6))$
$y-13=-2(x+6)$
Slope-Intercept Form
$y-13=-2(x+6)$
$y-13=-2 x-12$

$$
y=-2 x+1
$$

$f(x)=-2 x+1$
20. Passing through $(-3,2)$ and $(2,-8)$

First, find the slope.

$$
m=\frac{-8-2}{}=\frac{-10}{}=\frac{-10}{}=-2
$$

$$
\begin{aligned}
& y-0=2(x-(-2)) \\
& \begin{array}{c}
y-0=2(x+2) \\
\text { Slope-Intercept Form } \\
y-0=2(x+2) \\
y=2 x+4 \\
f(x)=2 x+4
\end{array}
\end{aligned}
$$

$$
2-(-3) \quad 2+3 \quad 5
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{gathered}
y-(-8)=-2(x-2) \\
y+8=-2(x-2) \\
\text { or } \\
y-2=-2(x-(-3)) \\
y-2=-2(x+3)
\end{gathered}
$$

Slope-Intercept Form

$$
\begin{aligned}
y-(-8) & =-2(x-2) \\
y+8 & =-2 x+4 \\
y & =-2 x-4 \\
f(x) & =-2 x-4
\end{aligned}
$$

21. Passing through $(1,9)$ and $(4,-2)$

First, find the slope.

$$
m=\frac{-2-9}{4-1}=\frac{-11}{3}=-\frac{11}{3}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-2) & =-\frac{11}{3}(x-4) \\
y+2 & =-\frac{11}{3}(x-4)
\end{aligned}
$$

or

$$
y-9=-\frac{11}{3}(x-1)
$$

Slope-Intercept Form
$y-9=-\frac{11}{3}(x-1)$
$y-9=-\frac{11}{3} x+\frac{11}{3}$

$$
y=-\frac{11}{x+} \underline{38}
$$

$f(x)=-\frac{11}{3} x+\frac{3}{3} \begin{gathered}3 \\ 3\end{gathered}$
22. Passing through $(4,-8)$ and $(8,-3)$

First, find the slope.

$$
m=\frac{\underline{-3-(-8)}}{8-4}=\underline{-3+8}=\frac{5}{4}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
& y-(-3)=\frac{5}{4}(x-8) \\
& y+3=\frac{5}{4}(x-8) \\
& \text { or } \\
& y-(-8)=\frac{5}{4}(x-4) \\
& y+8=\frac{5}{}(x-4)
\end{aligned}
$$

Slope-Intercept Form
$y+3=\frac{5}{4} x-10$
$y=\frac{5}{4} x-13$
$f(x)=\frac{5}{4} x-13$
23. Passing through $(-2,-5)$ and $(3,-5)$

First, find the slope.

$$
\begin{gathered}
m=\frac{-5-(-5)}{}=\frac{0}{}=0 \\
3-(-2) \quad 5
\end{gathered}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-5) & =0(x-3) \\
y+5 & =0(x-3)
\end{aligned}
$$

or
$y-(-5)=0(x-(-2))$

$$
y+5=0(x+2)
$$

Slope-Intercept Form
$y+5=0(x+2)$
$y+5=0$
$y=-5$
$f(x)=-5$
24. Passing through $(-1,-4)$ and $(3,-4)$

First, find the slope.
$m=\frac{-4-(-4)}{3-(-1)}=\frac{0}{4}=0$
Then use the slope and one of the points to write the equation in point-slope form.

## 4

$$
\begin{gathered}
y-(-4)=0(x-(-1)) \\
y+4=0(x+1) \\
\text { or } \\
y-(-4)=0(x-3) \\
y+4=0(x-3) \\
\text { Slope-Intercept Form } \\
y+4=0 \\
y=-4 \\
f(x)=-4
\end{gathered}
$$

25. Passing through $(7,8)$ with $x$-intercept $=3$

If the line has an $x$-intercept $=3$, it passes through the point $(3,0)$.
First, find the slope.

$$
m=\frac{8-0}{7-3}=\frac{8}{4}=2
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

$$
y-0=2(x-3)
$$

$$
y-0=2(x-3)
$$

or
$y-8=2(x-7)$
Slope-Intercept Form
$y-8=2(x-7)$
$y-8=2 x-14$

$$
y=2 x-6
$$

$f(x)=2 x-6$
26. Passing through $(-4,5)$ and with $y$-intercept $=-3$

If the line has a $y$-intercept $=-3$, it passes through
$(0,-3)$.
First, find the slope.

$$
\begin{aligned}
& m=\frac{-3-5}{-2}=\frac{-8}{}=\frac{-8}{}= \\
& \quad 0-(-4) \quad 0+44
\end{aligned}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-(-3) & =-2(x-0) \\
y+3 & =-2(x-0)
\end{aligned}
$$

or
$y-5=-2(x-(-4))$
$y-5=-2(x+4)$
Slope-Intercept Form
$y+3=-2 x$
$y=-2 x-3$
$f(x)=-2 x-3$

Then use the slope and one of the points to write the
equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-0 & =\frac{1}{2}(x-2)
\end{aligned}
$$

or

$$
\begin{aligned}
y-(-1) & =\frac{1}{2}(x-0) \\
y+1 & =\frac{1}{2}(x-0)
\end{aligned}
$$

Slope-Intercept Form

$$
\begin{aligned}
y-(-1) & =\frac{1}{2}(x-0) \\
y+1 & =\frac{1}{2} x \\
y & =\frac{1}{2} x-1 \\
f(x)= & \frac{1}{2} x-1
\end{aligned}
$$

28. $x$-intercept $=-2$ and $y$-intercept $=4$

If the line has an $x$-intercept $=-2$, it passes through the point $(-2,0)$. If the line has a $y$-intercept $=4$, it passes through $(0,4)$.
First, find the slope.

$$
\begin{gathered}
m=\frac{4-0}{}=\frac{4}{=}=2 \\
\\
0-(-2) \quad 2
\end{gathered}
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{gathered}
y-4=2(x-0) \\
\text { or } \\
y-0=2(x-(-2)) \\
y-0=2(x+2) \\
\text { Slope-Intercept Form } \\
y-4=2 x \\
y=2 x+4 \\
f(x)=2 x+4
\end{gathered}
$$

29. For $y=5 x, m=5$.
30. $x$-intercept $=2$ and $y$-intercept $=-1$

If the line has an $x$-intercept $=2$, it passes through the point $(2,0)$. If the line has a $y$-intercept $=-1$, it passes through $(0,-1)$.

First, find the slope.
$m=\frac{-1-0}{0-2}=\frac{-1}{}=\frac{1}{}$
a. A line parallel to this line would have the same slope, $m=5$.
b. A line perpendicular to it would have slope $m=-\frac{1}{5}$.
30. a. Parallel: $m=3$
b. Perpendicular: $m=-\frac{1}{3}$
31. For $y=-7 x, m=-7$.
a. A line parallel to this line would have the same slope, $m=-7$.
b. A line perpendicular to it would have slope $m=\frac{1}{7}$.
32. a. Parallel: $m=-9$
b. Perpendicular: $m=\frac{1}{9}$
33. For $y=\frac{1}{2} x+3, m=\frac{1}{2}$.
a. A line parallel to this line would have the same slope, $m=\frac{1}{2}$.
b. A line perpendicular to it would have slope $m=-2$.
34. a. Parallel: $m=\frac{1}{4}$
b. Perpendicular: $m=-4$
35. For $y=-\frac{2}{5} x-1, m=-\frac{2}{5}$.
a. A line parallel to this line would have the same slope, $m=-\frac{2}{5}$.
b. A line perpendicular to it would have slope $m=\frac{5}{2}$.
36. a. Parallel: $m=-\frac{3}{7}$
b
37. To find the slope, we rewrite the equation in slopeintercept form.
$4 x+y=7$

$$
y=-4 x+7
$$

So, $m=-4$.
a. A line parallel to this line would have the same slope, $m=-4$.
b. A line perpendicular to it would have slope $m=\frac{1}{4}$.
38. $8 x+y=11$

$$
y=-8 x+11
$$

a. Parallel: $m=-8$
b. Perpendicular: $m=\frac{1}{8}$
39. To find the slope, we rewrite the equation in slopeintercept form. $2 x+4 y=8$

$$
4 y=-2 x+8
$$

$$
y=-\frac{1}{2} x+2
$$

So, $m \quad \underline{1}$.

$$
=-{ }_{2}
$$

a. A line parallel to this line would have the same slope, $m=-\frac{1}{2}$.
b. A line perpendicular to it would have slope $m=2$.
40. $3 x+2 y=6$
$2 y=-3 x+6$
$y=-\frac{3}{2} x+3$
a. Parallel: $m=-\frac{3}{2}$

2
Perpendicular:

$$
m=\frac{7}{3} \begin{array}{ll}
\text { b. } \\
3 & \text { Perpe } \\
\text { ndicu } \\
& \text { lar: } \\
& m=
\end{array}
$$

41. To find the slope, we rewrite the equation in slopeintercept form.
$2 x-3 y=5$
$-3 y=-2 x+5$

$$
y=\frac{2}{3} x-\frac{5}{3}
$$

So, $m=\frac{2}{3}$.
a. A line parallel to this line would have the same slope, $m=\frac{2}{3}$.
b. A line perpendicular to it would have slope

$$
m=-\underline{3} .
$$

2
42. $3 x-4 y=-7$

$$
\begin{aligned}
-4 y & =-3 x-7 \\
y & =\frac{3}{4} x+\frac{7}{4}
\end{aligned}
$$

a. Parallel: $m=\underline{3}$

$$
4
$$

b. Perpendicular: $m=-\underline{4}$

3
43. We know that $x=6$ is a vertical line with undefined slope.
a. A line parallel to it would also be vertical with undefined slope.
b. A line perpendicular to it would be horizontal with slope $m=0$.
44. $y=9$ is a horizontal line with slope $m=0$.
a. Parallel: $m=0$
b. Perpendicular: $m$ is undefined
45. Since $L$ is parallel to $y=2 x$, we know it will have slope $m=2$. We are given that it passes through
$(4,2)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-2 & =2(x-4)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-2 & =2(x-4) \\
y-2 & =2 x-8 \\
y & =2 x-6
\end{aligned}
$$

In function notation, the equation of the line is $f(x)=2 x-6$.
46. $L$ will have slope $m=-2$. Using the point and the slope, we have $y-4=-2(x-3)$. Solve for $y$ to
obtain slope-intercept form.
$y-4=-2 x+6$
$y=-2 x+10$
$f(x)=-2 x+10$
47. Since $L$ is perpendicular to $y=2 x$, we know it will have slope $m=-\frac{1}{2}$. We are given that it passes through
$(2,4)$. We use the slope and point to write the equation in point-slope form.

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

$$
y-4=-\frac{1}{2}(x-2)
$$

Solve for $y$ to obtain slope-intercept form.
$y-4=-\frac{1}{2}(x-2)$
$y-4=-{ }_{2} x+1$
$y=-\frac{1}{2} x+5$

In function notation, the equation of the line is

$$
f(x)=-\frac{2}{2} x+5
$$

48. $L$ will have slope $m=\frac{1}{2}$. The line passes through
$(-1,2)$. Use the slope and point to write the equation in point-slope form.
$y-2=\frac{1}{2}(x-(-1))$
$y-2=\frac{1}{2}(x+1)$
Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-2 & =\frac{1}{2} x+\frac{1}{2} \\
y & =\frac{1}{2} x+\frac{1}{2}+2 \\
y & =\frac{1}{2} x+\frac{5}{2} \\
f(x) & =\frac{1}{2} x+\frac{5}{2}
\end{aligned}
$$

49. Since the line is parallel to $y=-4 x+3$, we know it
will have slope $m=-4$. We are given that it passes
through $(-8,-10)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-10) & =-4(x-(-8)) \\
y+10 & =-4(x+8)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+10 & =-4(x+8) \\
y+10 & =-4 x-32 \\
y & =-4 x-42
\end{aligned}
$$

In function notation, the equation of the line is
$f(x)=-4 x-42$.
50. $L$ will have slope $m=-5$. The line passes through
$(-2,-7)$. Use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-(-7) & =-5(x-(-2)) \\
y+7 & =-5(x+2)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+7 & =-5 x-10 \\
y & =-5 x-17 \\
f(x) & =-5 x-17
\end{aligned}
$$

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-3) & =-5(x-2) \\
y+3 & =-5(x-2)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+3 & =-5(x-2) \\
y+3 & =-5 x+10 \\
y & =-5 x+7
\end{aligned}
$$

In function notation, the equation of the line is $f(x)=-5 x+7$.
52. $L$ will have slope $m=-3$. The line passes through $(-4,2)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
& y-2=-3(x-(-4)) \\
& y-2=-3(x+4)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.
$y-2=-3 x-12$

$$
y=-3 x-10
$$

$f(x)=-3 x-10$
53. To find the slope, we rewrite the equation in slopeintercept form.
$2 x-3 y=7$

$$
-3 y=-2 x+7
$$

$$
y=\frac{2}{3} x-\frac{7}{3}
$$

$2 \quad 7$
Since the line is parallel to $y=3{ }_{3} x-3$, we know it will have slope $m=\frac{2}{3}$. We are given that it passes
through ( $-2,2$ ). We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-2 & =\frac{2}{3}(x-(-2)) \\
y-2 & =\frac{2}{3}(x+2)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
& y-2=\frac{2}{3}(x+2) \\
& y-2=\frac{2}{3} x+\frac{4}{3}
\end{aligned}
$$

51. Since the line is perpendicular to $y=\frac{1}{5} x+6$, we know it will have slope $m=-5$. We are given that it passes through $(2,-3)$. We use the slope and point to write the equation in point-slope form.
$\underline{2} \quad 10$

$$
y=3^{x+} 3
$$

In function notation, the equation of the line is

$$
f(x)=\frac{2}{3} x+\frac{10}{3}
$$

54. Find the slope.
$3 x-2 y=5$

$$
\begin{aligned}
-2 y & =-3 x+5 \\
y & =\frac{3}{2} x-\frac{5}{2}
\end{aligned}
$$

Since the lines are parallel, it will have slope
$m=\frac{3}{2}$. The line passes through $(-1,3)$. Use the
slope and point to write the equation in point-slope form.
$y-3=\frac{3}{2}(x-(-1))$
$y-3=\frac{3}{2}(x+1)$
Solve for $y$ to obtain slope-intercept form.
$y-3=\frac{3}{2} x+\frac{3}{2}$
$y=\frac{3}{2} x+\frac{3}{2}+3$
$y=\frac{3}{x} x+\underline{9}$
22
$f(x)=\underline{3} x+\underline{9}$

## 22

55. To find the slope, we rewrite the equation in slopeintercept form.

$$
\begin{aligned}
x-2 y & =3 \\
-2 y & =-x+3 \\
y & =1_{x-}-\underline{3}
\end{aligned}
$$

$2 \quad 2$
Since the line is perpendicular to $y=\frac{1}{2} x-\frac{3}{2}$, we know it will have slope $m=-2$. We are given that
it passes through $(4,-7)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-7) & =-2(x-4) \\
y+7 & =-2(x-4)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+7 & =-2(x-4) \\
y+7 & =-2 x+8 \\
y & =-2 x+1
\end{aligned}
$$

56. Find the slope.

$$
\begin{aligned}
x+7 y & =12 \\
7 y & =-x+12 \\
y & =-\frac{1}{7} x+\frac{12}{7}
\end{aligned}
$$

Since the lines are perpendicular, the slope is $m=7$.
The line passes through $(5,-9)$. Use the slope and point to write the equation in point-slope form.

$$
\begin{array}{r}
y-(-9)=7(x-5) \\
y+9=7(x-5)
\end{array}
$$

Solve for $y$ to obtain slope-intercept form.
$y+9=7(x-5)$
$y+9=7 x-35$
$y=7 x-44$
$f(x)=7 x-44$
57. Since the line is perpendicular to $x=6$ which is a vertical line, we know the graph of $f$ is a horizontal line with 0 slope. The graph of $f$ passes through
$(-1,5)$, so the equation of $f$ is $f(x)=5$.
58. Since the line is perpendicular to $x=-4$ which is a vertical line, we know the graph of $f$ is a horizontal line with 0 slope. The graph of $f$ passes through
$(-2,6)$, so the equation of $f$ is $f(x)=6$.
59. First we need to find the slope of the line with $x$ - intercept of 2 and $y$-intercept of -4 . This
line will pass through $(2,0)$ and $(0,-4)$. We use these points to find the slope.
$m=\frac{-4-0}{}=\frac{-4}{=2}$
0-2 -2
Since the graph of $f$ is perpendicular to this line, it
will have slope $m=-\frac{1}{2}$.

In function notation, the equation of the line is
$f(x)=-2 x+1$.

Use the point
$(-6,4)$ and the slope $-\frac{1}{2}$
to find the

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-4 & =-\frac{1}{2}(x-(-6)) \\
y-4 & =-\frac{1}{2}(x+6) \\
y-4 & =-\frac{1}{2} x-3 \\
y & =-\frac{1}{2} x+1 \\
f(x) & \frac{1}{x} x+1 \\
& =-2
\end{aligned}
$$

60. First we need to find the slope of the line with
$x$ - intercept of 3 and $y$-intercept of -9 . This line will pass through $(3,0)$ and $(0,-9)$. We use these points to find the slope.

$$
\begin{gathered}
m=\frac{-9-0}{}=\frac{-9}{}=3 \\
0-3-3
\end{gathered}
$$

Since the graph of $f$ is perpendicular to this line, it will have slope $m=-\frac{1}{3}$.

Use the point $(-5,6)$ and the slope $-\frac{1}{3}$ to find the equation of the line.
$y-y_{1}=m\left(x-x_{1}\right)$
$y-6=-\frac{1}{3}(x-(-5))$
$y-6=-\frac{1}{}(x+5)$
$y-6=-\frac{1}{3} x-\frac{5}{3}$
$y=-\frac{1}{3} x+\frac{13}{3}$
$f(x)=-\frac{1}{3} x+\frac{13}{3}$
61. First put the equation $3 x-2 y=4$ in slope-intercept form.
$3 x-2 y=4$
62. First put the equation $4 x-y=6$ in slope-intercept form.

$$
\begin{aligned}
4 x-y & =6 \\
-y & =-4 x+6 \\
y & =4 x-6
\end{aligned}
$$

The equation of $f$ will have slope $-\frac{1}{4}$ since it is perpendicular to the line above and the same $y$ - intercept -6 .
( ) $\underline{1}$
So the equation of $f$ is $f x=-{ }_{4} x-6$.
63. The graph of $f$ is just the graph of $g$ shifted down 2 units. So subtract 2 from the equation of $g(x)$ to obtain the equation of $f(x)$.
$f(x)=g(x)-2=4 x-3-2=4 x-5$
64. The graph of $f$ is just the graph of $g$ shifted up 3 units. So add 3 to the equation of $g(x)$ to obtain the equation of $f(x)$.
$f(x)=g(x)+3=2 x-5+3=2 x-2$
65. To find the slope of the line whose equation is $A x+B y=C$, put this equation in slope-intercept form by solving for $y$.

$$
\begin{aligned}
A x+B y & =C \\
B y & =-A x+C \\
y & =-\frac{A}{B} x+\frac{C}{B}
\end{aligned}
$$

The slope of this line is $m=-\frac{A}{B}$ so the slope of the line that is parallel to it is the same, $-\frac{A}{B}$.
66. From exercise 65, we know the slope of the line is $-\frac{A}{B}$. So the slope of the line that is perpendicular

$$
\begin{aligned}
-2 y & =-3 x+4 \\
y & =\frac{3}{2} x-2
\end{aligned}
$$

The equation of $f$ will have slope $-\frac{2}{3}$ since it is
perpendicular to the line above and the same $y$-intercept -2 .
So the equation of $f$ is $f(x)=-\frac{2}{3} x-2$.
would be $\frac{B}{A}$.
67. a. First, find the slope using $(20,38.9)$ and
$(30,47.8)$.
$m=\frac{47.8-38.9}{30-20}=\frac{8.9}{10}=0.89$
Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-47.8 & =0.89(x-30)
\end{aligned}
$$

or
$y-38.9=0.89(x-20)$
b. $y-47.8=0.89(x-30)$
$y-47.8=0.89 x-26.7$
$y=0.89 x+21.1$
$f(x)=0.89 x+21.1$
c. $f(40)=0.89(40)+21.1=56.7$

The linear function predicts the percentage of never- married American females, ages 25-29, to be $56.7 \%$ in 2020.
68. a. First, find the slope using $(20,51.7)$ and
$(30,62.6)$.
$m=\frac{62.6-51.7}{30-20}=10.9=1.09$
Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-62.6 & =1.09(x-30)
\end{aligned}
$$

or
$y-51.7=1.09(x-20)$
b. $y-62.6=1.09(x-30)$

$$
\begin{aligned}
y-62.6 & =1.09 x-32.7 \\
y & =1.09 x+29.9 \\
f(x) & =1.09 x+29.9
\end{aligned}
$$

c. $f(35)=1.09(35)+29.9=68.05$

The linear function predicts the percentage of never-married American males, ages $25-29$, to be $68.05 \%$ in 2015.
69. $\mathbf{a} / \mathrm{b}$.


Use the two points $(1,40.8)$ and
$(6,296.6)$ to find the slope.
$m=\frac{296.6-40.8}{6-1}=\frac{255.8}{5}=51.16$
Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-40.8 & =51.16(x-1)
\end{aligned}
$$

or
$y-296.6=51.16(x-6)$
Solve for $y$ to obtain slope-intercept form.
$y-40.8=51.16(x-1)$
$y-40.8=51.16 x-51.16$
$y=51.16 x-10.36$

$$
f(x)=51.16 x-10.36
$$

c. $\quad f(x)=51.16 x-10.36$
$f(11)=51.16(11)-10.36$ $=552.4$
The function predicts that 552.4 million smartphones will be sold in 2015.
70. $\mathbf{a} / \mathrm{b}$.

Number of U.S. Lawsuits by Smartphone Companies for Competitors Stealing Patents


Use the two points $(3,49)$ and $(6,97)$ to find the slope.

$$
m=\frac{97-49}{6-3}=\frac{48}{3}=16
$$

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
& y-y_{1}=m\left(x-x_{1}\right) \\
& y-49=16(x-3)
\end{aligned}
$$

or

$$
y-97=16(x-6)
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-49 & =16(x-3) \\
y-49 & =16 x-48 \\
y & =16 x+1 \\
f(x) & =16 x+1
\end{aligned}
$$

c. $\quad f(x)=16 x+1$

$$
\begin{aligned}
f(12) & =16(12)+1 \\
& =193
\end{aligned}
$$

The function predicts that there will be 193 lawsuits by Smartphone companies for patent infringement in 2016.
71. a. $m=\frac{970-582}{2016-2007}=\frac{388}{9} \approx 43.1$

The cost of Social Security is projected to increase at a rate of approximately $\$ 43.1$ billion per year.
b. $\quad m=\frac{909-446}{2016-2007}=\frac{463}{9} \approx 51.4$

The cost of Medicare is projected to increase at a rate of approximately $\$ 51.4$ billion per year.
c. No, the slopes are not the same. This means that the cost of Medicare is projected to increase at a faster rate than the cost of Social Security.
72. a. $m=\frac{970-582}{2016-2007}=\frac{388}{9} \approx 43.1$

The cost of Social Security is projected to increase at a rate of approximately $\$ 43.1$ billion per year.
b. $\quad m=\frac{392-195}{2016-2007}=\frac{197}{9} \approx 21.9$

The cost of Medicaid is projected to increase at a rate of approximately $\$ 21.9$ billion per year.
c. No, the slopes are not the same. This means that the cost of Social Security is projected to increase at a faster rate than the cost of Medicaid.
73. - 79. Answers will vary.
80. a. Answers will vary.

b. Answers will vary.

81. a. Answers will vary.

| Normal | FLOAT A | Jto Refl | Radian | MP | $\square$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| L1 | L2 | L3 | L4 | Ls | 1 |
| 0 | 15.8 | --- | -- | ------ |  |
| 1 | 40.8 |  |  | -- |  |
| 2 | 60.1 |  |  |  |  |
| 3 | 88.6 |  |  |  |  |
| 4 5 | 139.3 |  |  |  |  |
| 5 | 296.6 |  |  |  |  |
| ------ | ------ |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| $L 1(1)=0$ |  |  |  |  |  |

b. Answers will vary.

c. Answers will vary.

d. Answers will vary.

82. a. Answers will vary.

b. Answers will vary.

c. Answers will vary.

d. Answers will vary.

83. makes sense
84. makes sense
85. makes sense
86. does not make sense; Explanations will vary.

Sample explanation: If we know the slope and the $y$ intercept, it may be easier to write the slopeintercept form of the equation.
87. true
88. true
89. true
90. true
91. $B y=8 x-1$

$$
y=\frac{8}{B} x-1
$$

Since $\frac{8}{B}$ is the slope, $\frac{8}{B}$ must equal -2 .

$$
\begin{aligned}
\underline{8} & =-2 \\
8 & =-2 B
\end{aligned}
$$

$$
-4=B
$$

92. The slope of the line containing $(1,-3)$ and $(-2,4)$
has slope

$$
m=\begin{aligned}
& \underline{4-(-3)} \\
& -2-1
\end{aligned}=\begin{aligned}
& \underline{4+3} \\
& -3
\end{aligned}=\underline{7} \quad \underline{7} .
$$

Solve $A x+y=2$ for $y$ to obtain slope-intercept form.
$A x+y=2$
$y=-A x+2$
So the slope of this line is $-A$.
This line is perpendicular to the line above so its slope is $\underline{3}$.

Therefore, $-A=\underline{3}$
93. Find the slope of the line by using the two points,
$(-3,0)$, the $x$-intercept and $(0,-6)$, the
$y$-intercept.
$m=\frac{-6-0}{0-(-3)}=\frac{-6}{3}=-2$
So the equation of the line is $y=-2 x-6$.
Substitute -40 for $x$ :

$$
y=-2(-40)-6=80-6=74
$$

This is the $y$-coordinate of the first ordered pair.
Substitute -200 for $y$ :

$$
\begin{aligned}
-200 & =-2 x-6 \\
-194 & =-2 x \\
97 & =x
\end{aligned}
$$

This is the $x$-coordinate of the second ordered pair.
Therefore, the two ordered pairs are $(-40,74)$ and $(97,-200)$.
94. First find the slope.

$$
\begin{aligned}
m= & \frac{b-0}{=}= \\
& \frac{b}{b}=-a \quad-a \quad a
\end{aligned}
$$

Use the slope and point to write the equation in point-slope form.
$y-b=-\frac{b}{a}(x-0)$
Solve this equation for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-b & =-\frac{\underline{b}^{a}}{a} x \\
y & =-\frac{b^{a}}{a} x+b
\end{aligned}
$$

Divide both sides by $b$.

$$
\begin{aligned}
\frac{y}{b} & =-\frac{x}{a}+1 \\
\frac{x}{a}+\frac{y}{b} & =1
\end{aligned}
$$

This is called intercept form because the variable $x$ is being divided by the $x$-intercept, $a$, and the variable $y$ is being divided by the $y$-intercept, $b$.
95. $f(-2)=3(-2)^{2}-8(-2)+5$

$$
\begin{aligned}
& =3(4)+16+5 \\
& =12+16+5=33
\end{aligned}
$$

96. $f(-1)=(-1)^{2}-3(-1)+4=1+3+4=8$
$g(-1)=2(-1)-5=-2-5=-7$
$(f g)(-1)=(f)(-1) \cdot(g)(-1)=8(-7)=-56$
97. Let $x=$ the measure of the smallest angle.
$x+20=$ the measure of the second angle.
$2 x=$ the measure of the third angle.

$$
\begin{aligned}
x+(x+20)+2 x & =180 \\
x+x+20+2 x & =180 \\
4 x+20 & =180 \\
4 x & =160 \\
x & =40
\end{aligned}
$$

Find the other angles.
$x+20=40+20=60$
$2 x=2(40)=80$
The angles are $40^{\circ}, 60^{\circ}$, and $80^{\circ}$.
98. a.

$$
\begin{aligned}
2 x-y & =-4 \\
2(-5)-(-6) & =-4 \\
-10+6 & =-4 \\
-4 & =-4, \text { true }
\end{aligned}
$$

The point satisfies the equation.
b. $\quad 3 x-5 y=15$
$3(-5)-5(-6)=15$
$-15+30=15$
$15=15$, true
The point satisfies the equation.
99. The graphs intersect at $(3,-4)$.

100. $7 x-2(-2 x+4)=3$

$$
7 x+4 x-8=3
$$

$$
11 x-8=3
$$

$$
11 x=11
$$

$$
x=1
$$

The solution set is $\{1\}$.

## Chapter 2 Review

1. The relation is a function.

Domain $\{3,4,5\}$
Range \{10\}
2. The relation is a function.

Domain $\{1,2,3,4\}$
Range $\{-6, \pi, 12,100\}$
3. The relation is not a function.

Domain $\{13,15\}$
Range $\{14,16,17\}$
4. a. $f(0)=7(0)-5=0-5=-5$
b. $f(3)=7(3)-5=21-5=16$
c. $f(-10)=7(-10)-5=-75$
d. $f(2 a)=7(2 a)-5=14 a-5$
e. $f(a+2)=7(a+2)-5$

$$
=7 a+14-5=7 a+9
$$

5. a. $g(0)=3(0)^{2}-5(0)+2=2$

$$
\text { b. } \quad \begin{aligned}
g(5) & =3(5)^{2}-5(5)+2 \\
& =3(25)-25+2 \\
& =75-25+2=52
\end{aligned}
$$

c. $g(-4)=3(-4)^{2}-5(-4)+2=70$
d. $g(b)=3(b)^{2}-5(b)+2$

$$
=3 b^{2}-5 b+2
$$

e. $g(4 a)=3(4 a)^{2}-5(4 a)+2$
$=3\left(16 a^{2}\right)-20 a+2$
$=48 a^{2}-20 a+2$
6. $g$ shifts the graph of $f$ down one unit.

7. $g$ shifts the graph of $f$ up two units.

8. The vertical line test shows that this is not the graph of a function.
9. The vertical line test shows that this is the graph of a function.
10. The vertical line test shows that this is the graph of a function.
11. The vertical line test shows that this is not the graph of a function.
12. The vertical line test shows that this is not the graph of a function.
13. The vertical line test shows that this is the graph of a function.
14. $f(-2)=-3$
15. $f(0)=-2$
16. When $x=3, f(x)=-5$.
17. The domain of $f$ is $[-3,5)$.
18. The range of $f$ is $[-5,0]$.
19. a. The eagle's height is a function of its time in flight because every time, $t$, is associated with at most one height.
b. $f(15)=0$

At time $t=15$ seconds, the eagle is at height zero. This means that after 15 seconds, the eagle is on the ground.
c. The eagle's maximum height is 45 meters.
d. For $x=7$ and 22, $f(x)=20$. This means that
at times 7 seconds and 22 seconds, the eagle is at a height of 20 meters.
e. The eagle began the flight at 45 meters and remained there for approximately 3 seconds. At
that time, the eagle descended for 9 seconds. It landed on the ground and stayed there for 5 seconds. The eagle then began to climb back up to a height of 44 meters.
20. The domain of $f$ is $(-\infty, \infty)$.
21. The domain of $f$ is $(-\infty,-8)$ or $(-8, \infty)$.
22. The domain of $f$ is $(-\infty, 5)$ or $(5, \infty)$.
23. a. $(f+g)(x)=(4 x-5)+(2 x+1)$

$$
\begin{aligned}
& =4 x-5+2 x+1 \\
& =6 x-4
\end{aligned}
$$

b. $\quad(f+g)(3)=6(3)-4$

$$
=18-4=14
$$

24. a. $(f+g)(x)$

$$
\begin{aligned}
& =\left(5 x^{2}-x+4\right)+(x-3) \\
& =5 x^{2}-x+4+x-3=5 x^{2}+1
\end{aligned}
$$

b. $(f+g)(3)=5(3)^{2}+1=5(9)+1$

$$
=45+1=46
$$

25. The domain of $f+g$ is $(-\infty, 4)$ or $(4, \infty)$.
26. The domain of $f+g$ is $(-\infty,-6)$ or $(-6,-1)$ or $(-1, \infty)$.
27. $f(x)=x^{2}-2 x, \quad g(x)=x-5$

$$
\begin{aligned}
(f+g)(x) & =\left(x^{2}-2 x\right)+(x-5) \\
& =x^{2}-2 x+x-5 \\
& =x^{2}-x-5 \\
(f+g)(-2) & =(-2)^{2}-(-2)-5 \\
& =4+2-5=1
\end{aligned}
$$

29. $f(x)=x^{2}-2 x, \quad g(x)=x-5$

$$
\begin{aligned}
(f-g)(x) & =\left(x^{2}-2 x\right)-(x-5) \\
& =x^{2}-2 x-x+5 \\
& =x^{2}-3 x+5 \\
& { }^{2} \\
(f-g)(x) & =x-3 x+5
\end{aligned}
$$

$$
\begin{aligned}
(f-g)(1) & =(1)^{2}-3(1)+5 \\
& =1-3+5=3
\end{aligned}
$$

30. From Exercise 29 we know
$(f-g)(x)=x^{2}-3 x+5$. We can use this to find
$f(4)-g(4)$.
$f(4)-g(4)=(f-g)(4)$

$$
\begin{aligned}
& =(4)^{2}-3(4)+5 \\
& =16-12+5=9
\end{aligned}
$$

31. Since $(f g)(-3)=f(-3) \cdot g(-3)$, find $f(-3)$ and $g(-3)$ first.
$f(-3)=(-3)^{2}-2(-3)$

$$
=9+6=15
$$

$g(-3)=-3-5=-8$
$(f g)(-3)=f(-3) \cdot g(-3)$

$$
=15(-8)=-120
$$

32. $f(x)=x^{2}-2 x, \quad g(x)=x-5$
$\left(\frac{f}{g}\right)(x)=\frac{x^{2}-2 x}{x-5}$
$(f)_{(4)}=\frac{(4)^{2}-2(4)}{}=\underline{16-8}$
$\begin{array}{rlr}(g) & 4-5 & -1 \\ = & -8 \\ -1 & =-8\end{array}$
33. $(f-g)(x)=x-3 x+5$

The domain of $f-g$ is $(-\infty, \infty)$.
28. From Exercise 27 we know
$(f+g)(x)=x^{2}-x-5$. We can use this to find

$$
\begin{aligned}
& f(3)+g(3) \\
& \begin{aligned}
f(3)+g(3) & =(f+g)(3) \\
& =(3)^{2}-(3)-5 \\
& =9-3-5=1
\end{aligned}
\end{aligned}
$$

34. $(\underline{f})(x)=\frac{x^{2}-2 x}{}$
( $g$ ) $\quad x-5$

The domain of $\frac{f}{g}$ is $(-\infty, 5)$ or $(5, \infty)$.
35. $x+2 y=4$

Find the $x$-intercept by setting $y=0$ and the $y-$ intercept by setting $x=0$.

$$
\begin{array}{rlrl}
x+2(0) & =4 & 0+2 y & =4 \\
x+0 & =4 & 2 y & =4 \\
x & =4 & y & =2
\end{array}
$$

Choose another point to use as a check.
Let $x=1$.
$1+2 y=4$
$2 y=3$
$y=\frac{3}{2}$
$x+2 y=4 y_{A}$
36. $2 x-3 y=12$

Find the $x$-intercept by setting $y=0$ and the $y-$
intercept by setting $x=0$.

$$
\begin{array}{rlrl}
2 x-3(0) & =12 & 2(0)-3 y & =12 \\
2 x+0 & =12 & 0-3 y & =12 \\
2 x & =12 & -3 y & =12 \\
x & =6 & y & =-4
\end{array}
$$

Choose another point to use as a check.
Let $x=1$.

$$
\begin{aligned}
2(1)-3 y & =12 \\
2-3 y & =12 \\
-3 y & =10 \\
y & =-\underline{10}
\end{aligned}
$$

3

37. $4 x=8-2 y$

Find the $x$-intercept by setting $y=0$ and the $y$ intercept by setting $x=0$.

$$
\begin{array}{rlrl}
4 x & =8-2(0) & 4(0) & =8-2 y \\
4 x & =8-0 & 0 & =8-2 y \\
4 x & =8 & 2 y & =8
\end{array}
$$

$x=2$

$$
y=4
$$

Choose another point to use as a check. Let $x=1$.

$$
\begin{aligned}
4(1) & =8-2 y \\
4 & =8-2 y \\
-4 & =-2 y \\
2 & =y
\end{aligned}
$$


38. $m=\frac{2-\left(\frac{-4}{}\right)}{5-2}=\frac{6}{3}=2$

The line through the points rises.
39. $m=\frac{3-(-3)}{}=\frac{6}{2}=-\underline{2}$

$$
\begin{array}{lll}
-2-7 & -9 & 3
\end{array}
$$

The line through the points falls.
40. $m=\frac{2-(-1)}{-3}$

$$
3-3 \quad 0
$$

$m$ is undefined. The line through the points is vertical.
41. $m=\frac{4-4}{-3-(-1)}=\frac{0}{-2}=0$

The line through the points is horizontal.
42. $y=2 x-1$
$m=2 \quad y-$ intercept $=-1$

43. $f(x)=-\frac{1}{2} x+4$
$m=-\frac{1}{2} \quad y-$ intercept $=4$
$f(x)=-\frac{1}{2} x+4 y_{4}$
44. $y=\frac{2}{3} x$
$m=\frac{2}{3}$

$$
y-\text { intercept }=0
$$

$y=\frac{2}{3} x$

45. To rewrite the equation in slope-intercept form, solve for $y$.

$$
\begin{aligned}
2 x+y & =4 \\
y & =-2 x+4
\end{aligned}
$$

$m=-2 \quad y-$ intercept $=4$
46. $-3 y=5 x$

$$
y=-\frac{5}{3} x
$$

$m=-\underline{5} \quad y-$ intercept $=0$
47. $5 x+3 y=6$

$$
\begin{gathered}
3 y=-5 x+6 \\
y=-\frac{5}{3} x+2 \\
m=-\frac{5}{3} \quad y-\text { intercept }=2
\end{gathered}
$$

48. $y=2$

49. $7 y=-21$

$$
y=-3
$$


50. $f(x)=-4$
$y=-4$

51. $x=3$

52. $2 x=-10$

$$
x=-5
$$



$$
f(t)=-0.27 t+70.45, \text { the slope is }-0.27 . \mathrm{A}
$$

slope of -0.27 indicates that the record time for the women's 400-meter has been decreasing by 0.27 seconds per year since 1900 .
54. a. $m=\frac{1163-617}{1998-1994}=\frac{546}{4} \approx 137$

There was an average increase of approximately 137 discharges per year.
b. $\quad m=\frac{623-1273}{}=\frac{-650}{}=-130$

$$
2006-20015
$$

There was an average decrease of approximately 130 discharges per year.
55. a. Find the slope of the line by using the two points $(0,32)$ and $(100,212)$.
$m=\frac{212-32}{100-0}=\frac{180}{100}=\frac{9}{5}$
We use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-32 & =\frac{9}{5}(x-0) \\
y-32 & =\frac{9}{x} x \\
y & =\frac{9}{5} x+32 \\
F & =\frac{9}{5} C+32
\end{aligned}
$$

b. Let $C=30$.
$F=\frac{9}{5}(30)+32=54+32=86$
The Fahrenheit temperature is $86^{\circ}$ when the Celsius temperature is $30^{\circ}$.
56. Slope $=-6$, passing through $(-3,2)$

## Point-Slope Form

$y-y_{1}=m\left(x-x_{1}\right)$
$y-2=-6(x-(-3))$
$y-2=-6(x+3)$
Slope-Intercept Form
$y-2=-6(x+3)$
$y-2=-6 x-18$
$y=-6 x-16$
$f(x)=-6 x-16$
57. Passing through $(1,6)$ and $(-1,2)$

First, find the slope.

Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{array}{rl}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-6 & =2(x-1) \\
\text { or } \\
y-y & =m(x-x) \\
1 & 1 \\
y-2 & =2(x-(-1)) \\
y-2 & =2(x+1)
\end{array}
$$

Slope-Intercept Form
$y-6=2(x-1)$
$y-6=2 x-2$
$y=2 x+4$
$f(x)=2 x+4$
58. Rewrite $3 x+y=9$ in slope-intercept form.
$3 x+y=9$

$$
y=-3 x+9
$$

Since the line we are concerned with is parallel to
this line, we know it will have slope $m=-3$. We are given that it passes through $(4,-7)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{array}{r}
y-y_{1}=m\left(x-x_{1}\right) \\
y-(-7)=-3(x-4) \\
y+7=-3(x-4)
\end{array}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+7 & =-3(x-4) \\
y+7 & =-3 x+12 \\
y & =-3 x+5
\end{aligned}
$$

In function notation, the equation of the line is
$f(x)=-3 x+5$.
59. The line is perpendicular to $y=\frac{1}{3} x+4$, so the
slope is -3 . We are given that it passes through $(-2,6)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y= & m(x-x) \\
& m=\stackrel{6-2}{ }=\frac{4}{}=2
\end{aligned}
$$

$$
\begin{gathered}
1 \\
1 \\
y-6=-3(x-(-2)) \\
y-6=-3(x+2)
\end{gathered}
$$

Solve for $y$ to obtain slope-intercept form.

$$
1-(-1) \quad 2
$$

$$
\begin{aligned}
y-6 & =-3(x+2) \\
y-6 & =-3 x-6 \\
y & =-3 x
\end{aligned}
$$

In function notation, the equation of the line is

$$
f(x)=-3 x
$$

60. a. First, find the slope using the points $(2,28.2)$ and $(4,28.6)$.
$m=\frac{28.6-28.2}{4-2}=\frac{0.4}{2}=0.2$
Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{gathered}
y-y_{1}=m\left(x-x_{1}\right) \\
y-28.2=0.2(x-2)
\end{gathered}
$$

or

$$
y-28.6=0.2(x-4)
$$

b. Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-28.2 & =0.2(x-2) \\
y-28.2 & =0.2 x-0.4 \\
y & =0.2 x+27.8 \\
f(x) & =0.2 x+27.8
\end{aligned}
$$

c. $f(x)=0.2 x+27.8$
$f(7)=0.2(12)+27.8$

$$
=30.2
$$

The linear function predicts men's average age of first marriage will be 30.2 years in 2020 .
7. The vertical line test shows that this is not the graph of a function.
8. $f(6)=-3$
9. $f(x)=0$ when $x=-2$ and $x=3$.
10. The domain of $f$ is $(-\infty, \infty)$.
11. The range of $f$ is $(-\infty, 3]$.
12. The domain of $f$ is $(-\infty, 10)$ or $(10, \infty)$.
13. $f(x)=x^{2}+4 x$ and $g(x)=x+2$

$$
\begin{aligned}
(f+g)(x) & =f(x)+g(x) \\
& =\left(x^{2}+4 x\right)+(x+2) \\
& =x^{2}+4 x+x+2 \\
& =x^{2}+5 x+2
\end{aligned}
$$

$$
\begin{aligned}
(f+g)(3) & =(3)^{2}+5(3)+2 \\
& =9+15+2=26
\end{aligned}
$$

14. $f(x)=x^{2}+4 x$ and $g(x)=x+2$

$$
\begin{aligned}
(f-g)(x) & =f(x)-g(x) \\
& =\left(x^{2}+4 x\right)-(x+2) \\
& =x^{2}+4 x-x-2 \\
& =x^{2}+3 x-2 \\
(f-g)(-1) & =(-1)^{2}+3(-1)-2 \\
& =1-3-2=-4
\end{aligned}
$$

15. We know that $(f g)(x)=f(x) \cdot g(x)$. So, to find $(f g)(-5)$, we use $f(-5)$ and $g(-5)$.

$$
\begin{aligned}
& f(-5)=(-5)^{2}+4(-5)=25-20=5 \\
& g(-5)=-5+2=-3 \\
& \begin{aligned}
(f g)(-5) & =f(-5) \cdot g(-5) \\
& =5(-3)=-15
\end{aligned}
\end{aligned}
$$

16. $f(x)=x^{2}+4 x$ and $g(x)=x+2$
17. $g$ shifts the graph of $f$ up 2 units.


$$
\begin{aligned}
& \left(\frac{f}{g}\right)(x)=\frac{x^{2}+4 x}{x+2} \\
& (f) \quad(\underline{2})^{2}+4(\underline{2}) \quad \underline{4+8} \underline{12} \\
& (g)^{(2)}=2+2={ }_{4}=3
\end{aligned}
$$

6. The vertical line test shows that this is the graph of a function.
7. Domain of $\frac{f}{g}$ is $(-\infty,-2)$ or $(-2, \infty)$.
8. $4 x-3 y=12$

Find the $x$-intercept by setting $y=0$.

$$
\begin{aligned}
4 x-3(0) & =12 \\
4 x & =12 \\
x & =3
\end{aligned}
$$

Find the $y$-intercept by setting $x=0$.

$$
\begin{aligned}
& 4(0)-3 y=12 \\
& -3 y=12 \\
& y=-4
\end{aligned}
$$

19. $f(x)=-\frac{1}{3} x+2$
$m=-\frac{1}{3} \quad y$-intercept $=2$

20. $f(x)=4$

$$
y=4
$$

An equation of the form $y=b$ is a horizontal line.

21. $m=\underline{4-2}=\frac{2}{=}=-\frac{1}{}$

$$
\begin{array}{ccc}
1-5 & -4 & 2
\end{array}
$$

22. $m=\frac{5-(-5)}{4-4}=\frac{10}{0}$
$m$ is undefined
The line through the points is vertical.
23. $V(10)=3.6(10)+140$

$$
=36+140=176
$$

In the year 2005, there were 176 million Super Bowl viewers.
24. The slope is 3.6. This means the number of Super Bowl viewers is increasing at a rate of 3.6 million per year.
25. Passing through $(-1,-3)$ and $(4,2)$

First, find the slope.
$m=\frac{2-(-3)}{4-(-1)}=\frac{5}{5}=1$
Then use the slope and one of the points to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-3) & =1(x-(-1)) \\
y+3 & =1(x+1)
\end{aligned}
$$

or
$y-2=1(x-4)$
$y-2=x-4$
Slope-Intercept Form

$$
\begin{aligned}
y-2 & =x-4 \\
y & =x-2
\end{aligned}
$$

In function notation, the equation of the line is
$f(x)=x-2$.
26. The line is perpendicular to $y=-\frac{1}{2} x-4$, so the
slope is 2 . We are given that it passes through $(-2,3)$. We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-3 & =2(x-(-2)) \\
y-3 & =2(x+2)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y-3 & =2(x+2) \\
y-3 & =2 x+4 \\
y & =2 x+7
\end{aligned}
$$

The line through the points falls.

In function notation, the equation of the line is $f(x)=2 x+7$.
27. The line is parallel to $x+2 y=5$.

Put this equation in slope-intercept form by solving for $y$.

$$
\begin{aligned}
& x+2 y=5 \\
& 2 y=-x+5 \\
& y=-\frac{1}{2} x+\frac{5}{2}
\end{aligned}
$$

Therefore the slopes are the same; $m=-\frac{1}{2}$.
We are given that it passes through $(6,-4)$.
We use the slope and point to write the equation in point-slope form.

$$
\begin{aligned}
& y-y_{1}=m\left(x-x_{1}\right) \\
& y-(-4)=-\frac{1}{-}(x-6) \\
& 2 \\
& y+4=-\frac{1}{-}(x-6)
\end{aligned}
$$

## 2

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
& y+4=-\frac{1}{2}(x-6) \\
& y+4=-\frac{1}{2} x+3
\end{aligned}
$$

$$
y=-{ }^{\frac{1}{x}} x-1
$$

2
In function notation, the equation of the line is $f(x)=-\frac{1}{x-1}$.

2
28. a. First, find the slope using the points $(3,0.053)$ and $(7,0.121)$.
$m=\frac{0.121-0.053}{7-3}=\frac{0.068}{4}=0.017$
Then use the slope and a point to write the equation in point-slope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-0.053 & =0.017(x-3)
\end{aligned}
$$

or

$$
y-0.121=0.017(x-7)
$$

b. $y-0.053=0.017(x-3)$
c. $f(x)=0.017 x+0.002$
$f(8)=0.017(8)+0.002$

$$
=0.138
$$

The function predicts that the blood alcohol concentration of a 200 -pound person who consumes 8 one-ounce beers in an hour will be 0.138 .

## Cumulative Review Exercises

1. $\{0,1,2,3\}$
2. False. $\pi$ is an irrational number.

$$
8-3^{2} \div 9
$$

3. 

$|-5|-\left[5-(18 \div 6)^{2}\right.$
$=\frac{8-9 \div 9}{5-[5-(3)]} 2=\frac{8-1}{5-[2]^{2}}$
$=\frac{7}{5-4}=\frac{7}{1}=7$
$0 \quad 2$
4. $4-(2-9)+3 \div 1+3$
$=4-(-7)^{0}+9 \div 1+3=4-1+9 \div 1+3$
$=4-1+9+3=3+9+3=15$
5. $3-[2(x-2)-5 x$

$$
\begin{aligned}
& =3-[2 x-4-5 x]=3-[-3 x-4] \\
& =3+3 x+4=3 x+7
\end{aligned}
$$

6. $2+3 x-4=2(x-3)$

$$
\begin{aligned}
3 x-2 & =2 x-6 \\
x-2 & =-6 \\
x & =-4
\end{aligned}
$$

The solution set is $\{-4\}$.
7. $4 x+12-8 x=-6(x-2)+2 x$

$$
12-4 x=-6 x+12+2 x
$$

$$
\begin{aligned}
y-0.053 & =0.017 x-0.051 \\
y & =0.017 x+0.002
\end{aligned}
$$

$$
f(x)=0.017 x+0.002
$$

$$
\begin{aligned}
12-4 x & =-4 x+12 \\
12 & =12 \\
0 & =0
\end{aligned}
$$

The solution set is $\{x \mid x$ is a real number $\}$ or $(-\infty, \infty)$ or The equation is an identity.
8. $\frac{x-2}{4}=\frac{2 x+6}{3}$
$4(2 x+6)=3(x-2)$

$$
8 x+24=3 x-6
$$

$$
5 x+24=-6
$$

$$
5 x=-30
$$

$$
x=-6
$$

The solution set is $\{-6\}$.
9. Let $x=$ the price before reduction

$$
\begin{aligned}
x-0.20 x & =1800 \\
0.80 x & =1800 \\
x & =2250
\end{aligned}
$$

The price of the computer before the reduction was $\$ 2250$.
10. $A=p+p r t$
$A-p=p r t$
$\frac{A-p}{p r}=t$
11. $\left(3 x^{4} y^{-5}\right)^{-2}=\left(\frac{\left(3 x^{4}\right)^{-2}}{\left(y^{5}\right)}=\left\lvert\,=\left(\left.\frac{\left.y^{5}\right)^{2}}{\left(3 x^{4}\right)}\right|^{2}=\frac{y^{10}}{9 x^{8}}\right.\right.\right.$
12. $\left(\frac{3 x^{2} y^{-4}}{)^{2}}=\left(\frac{3 x^{2} x^{3}}{x^{3}}\right)^{2}\right.$
$\left(x^{-3} y^{2}\right) \quad\left(y^{2} y^{4}\right)$

$$
=\left(\overline{y^{6}}\right)=\frac{\left(3 x^{5}\right)^{2}}{y^{12}}
$$

13. $\left(7 \times 10^{-8}\right)\left(3 \times 10^{2}\right)$
$=(7 \times 3)\left(10^{-8} \times 10^{2}\right)=21 \times 10^{-6}$
$=(2.1 \times 10) \times 10^{-6}=2.1\left(10 \times 10^{-6}\right)$
$=2.1 \times 10^{-5}$
14. The relation is a function.

Domain $\{1,2,3,4,6\}$
Range $\{5\}$
15. $g$ shifts the graph of $f$ up three units.

16. The domain of $f$ is $(-\infty, 15)$ or $(15, \infty)$.
17. $(f-g)(x)$
$=\left(3 x^{2}-4 x+2\right)-\left(x^{2}-5 x-3\right)$
$=3 x^{2}-4 x+2-x^{2}+5 x+3$
$=2 x^{2}+x+5$

$$
\begin{aligned}
(f-g)(-1) & =2(-1)^{2}+(-1)+5 \\
& =2(1)-1+5=2-1+5=6
\end{aligned}
$$

18. $f(x)=-2 x+4$

$$
y=-2 x+4
$$

$m=-2 \quad y$-intercept $=4$
$f(x)=-2 x+4 \quad y_{\text {f }}$
19. $x-2 y=6$

Rewrite the equation of the line in slope-intercept form.

$$
\begin{aligned}
& x-2 y=6 \\
& -2 y=-x+6 \\
& \quad \frac{1}{2} \\
& y=\frac{x-3}{2} \\
& m=\frac{1}{2} \quad y \text {-intercept }=-3
\end{aligned}
$$


20. The line is parallel to $y=4 x+7$, so the slope is 4 .

We are given that it passes through $(3,-5)$. We use the slope and point to write the equation in pointslope form.

$$
\begin{aligned}
y-y_{1} & =m\left(x-x_{1}\right) \\
y-(-5) & =4(x-3) \\
y+5 & =4(x-3)
\end{aligned}
$$

Solve for $y$ to obtain slope-intercept form.

$$
\begin{aligned}
y+5 & =4(x-3) \\
y+5 & =4 x-12 \\
y & =4 x-17
\end{aligned}
$$

In function notation, the equation of the line is $f(x)=4 x-17$.

