

**Solution Manual for Mathematics A Practical Odyssey 8th Edition
Johnson Mowry 130510417X 9781305104174**

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SECTION 2.1

1. a. “The set of all black automobiles” is well-defined because an automobile is either black or not black.
b. “The set of all inexpensive automobiles” is not well-defined because we need a level of cost (e.g., under \$8,000) specified to determine whether an automobile is expensive or inexpensive.
c. “The set of all prime numbers” is well-defined as it can be determined whether or not a number is prime or not prime.
d. “The set of all large numbers” is not well-defined because different people will have different definitions for large.
2. a. $n(A) = 7$
b. True
c. False
d. True
3. Proper: { }, {Lennon}, {McCartney};
Improper: {Lennon, McCartney}
4. Proper: { }; Improper: {0}
5. Proper: { }, {yes}, {no}, {undecided}, {yes, no}, {yes, undecided}, {no, undecided}
Improper: {yes, no, undecided}
6. Proper: { }, {classical}, {country}, {jazz}, {rock}, {classical, country}, {classical, jazz}, {classical, rock}, {country, jazz}, {country, rock}, {jazz, rock}, {classical, country, jazz}, {classical, country, rock}, {classical, jazz, rock},
8. a. {2, 7}
b. {2, 3, 4, 5, 6, 7}
c. {0, 1, 4, 6, 8, 9}
d. {0, 1, 3, 5, 8, 9}
9. a. { }
b. {0, 1, 2, 3, 4, 5, 6, 7, 8, 9}
c. {0, 2, 4, 6, 8}
d. {1, 3, 5, 7, 9}
10. a. { }
b. {3, 4, 6, 8, 9}
c. {0, 1, 2, 4, 5, 7, 8}
d. {0, 1, 2, 3, 5, 6, 7, 9}
11. {Friday}
12. {Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday}

{country, jazz, rock}

Improper: {classical, country, jazz, rock}

7. a. {4, 5}
b. {1, 2, 3, 4, 5, 6, 7, 8}
c. {0, 6, 7, 8, 9}
d. {0, 1, 2, 3, 9}

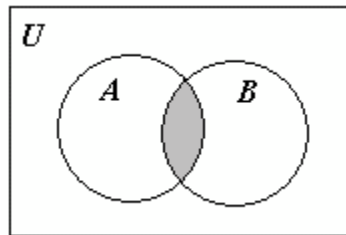
13. {Monday, Tuesday, Wednesday, Thursday}

14. {Saturday, Sunday}

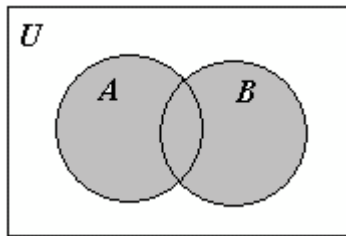
15. {Friday, Saturday, Sunday}

16. {Monday, Tuesday, Wednesday, Thursday}

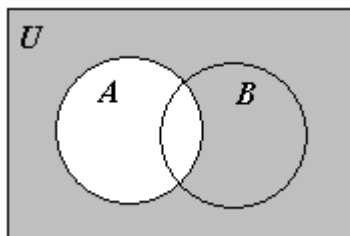
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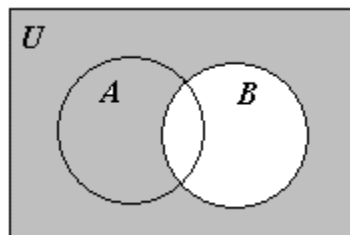
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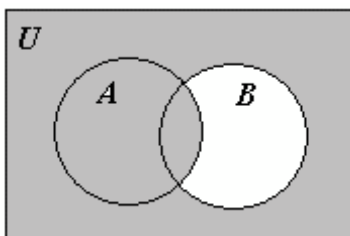
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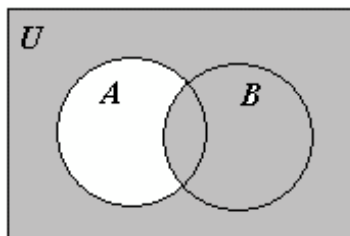
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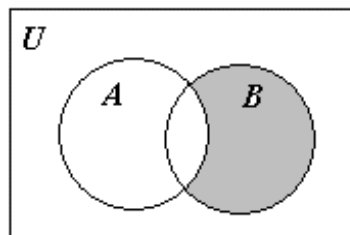
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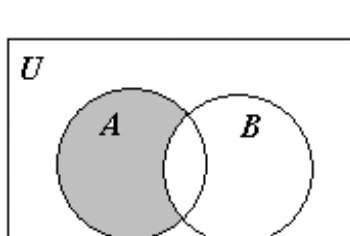
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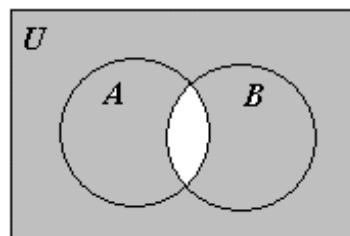
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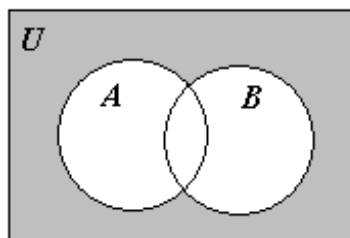
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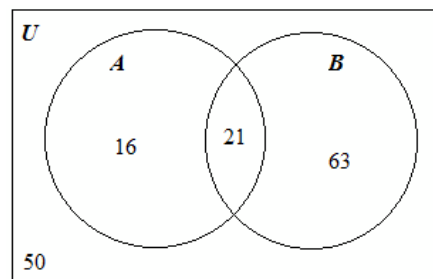
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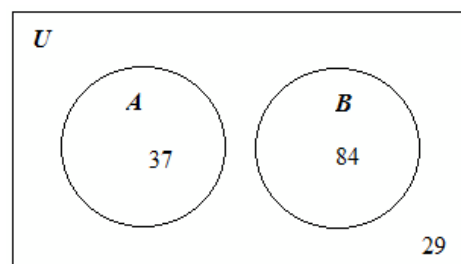
26.



- 27.a. Rearranging the Cardinal Number Formula for the Union of Sets:
 $n(A \cap B) = n(A) + n(B) - n(A \cup B)$
 $n(A \cap B) = 37 + 84 - 100$
 $n(A \cap B) = 21$



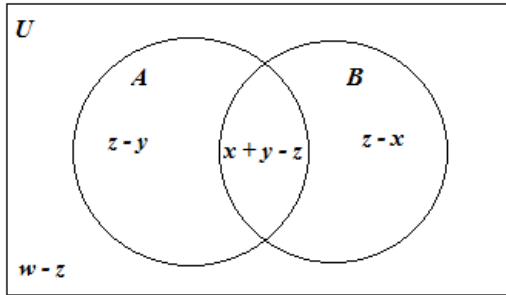
- b. Using the formula from part a:
 $n(A \cap B) = n(A) + n(B) - n(A \cup B)$
 $n(A \cap B) = 37 + 84 - 121$
 $n(A \cap B) = 0$



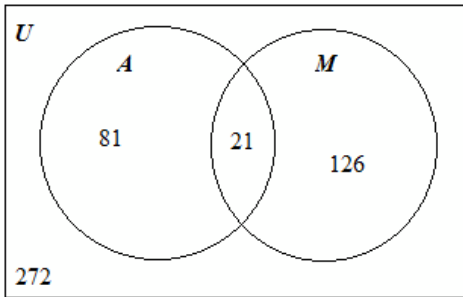
28. a. $A \subseteq (A \cup B)$. Thus,
 $n(A) \leq n(A \cup B)$. Hence, $x \leq z$.

b. $w \geq z, w > y, y \leq z, x < w$

c. Rearranging the Cardinal Number
 Formula for the Union of Sets:
 $n(A \cap B) = n(A) + n(B) - n(A \cup B)$
 $n(A \cap B) = x + y - z$

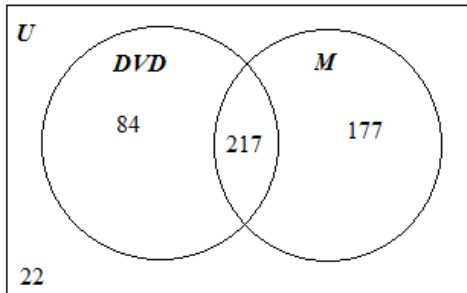


29. a.



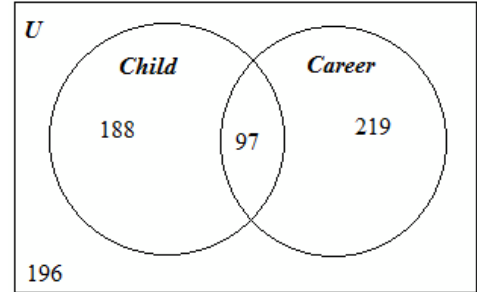
b. $\frac{81+21+126}{500} = \frac{228}{500} = 0.456 = 45.6\%$

30. a.



b. $\frac{84+217+177}{500} = \frac{478}{500} = 0.956 = 95.6\%$

31. a. Rearranging the Cardinal Number
 Formula for the Union of Sets:



$$n(\text{child} \cap \text{career}) = n(\text{child}) + n(\text{career}) - n(\text{child} \cup \text{career})$$

$$n(\text{child} \cap \text{career}) = 285 + 316 - (700 - 196)$$

$$n(\text{child} \cap \text{career}) = 97$$

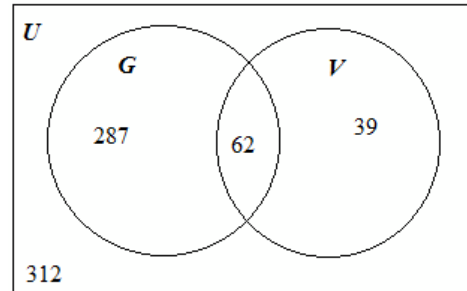
b. $\frac{97}{700} \approx 0.13857 = 13.857\%$

32. a. Rearranging the Cardinal Number
 Formula for the Union of Sets:

$$n(G \cap V) = n(G) + n(V) - n(G \cup V)$$

$$n(G \cap V) = 349 + 101 - (700 - 312)$$

$$n(G \cap V) = 62$$



b. $\frac{62}{700} \approx 0.08857 = 8.857\%$

For questions 33 – 36, the following facts are useful:

$$n(U) = 50$$

$$n(A) = 4, \text{ since } A = \{\text{Alabama, Alaska, Arizona, Arkansas}\}$$

$$n(I) = 4, \text{ since } I = \{\text{Idaho, Illinois, Indiana, Iowa}\}$$

$$n(M) = 8, \text{ since } M = \{\text{Maine, Maryland, Massachusetts, Michigan, Minnesota, Mississippi, Missouri, Montana}\}$$

$$n(N) = 8, \text{ since } N = \{\text{Nebraska, Nevada, New Hampshire, New Jersey, New Mexico, New York, North Carolina, North Dakota}\}$$

$$n(O) = 3, \text{ since } O = \{\text{Ohio, Oklahoma, Oregon}\}$$

$$33. n(M^c) = n(U) - n(M) = 50 - 8 = 42$$

$$34. n(A \cup N) = n(A) + n(N) - n(A \cap N) = 4 + 8 - 0 = 12$$

35. Rearranging the Cardinal Number

Formula for the Union of Sets:

$$n(I' \cap O') = n(I') + n(O') - n(I' \cup O')$$

$$\text{But, } n(I') = n(U) - n(I) = 50 - 4 = 46$$

$$\text{and } n(O') = n(U) - n(O) = 50 - 3 = 47$$

$$\text{. Thus, } n(I' \cap O') = 46 + 47 - 50 = 43$$

$$36. n(M \cap I) = 0, \text{ since no state can start with both M and I.}$$

For questions 37 – 40, the following facts are useful:

$$n(U) = 12$$

$$n(J) = 3, \text{ since } J = \{\text{January, June, July}\}$$

$$n(Y) = 4, \text{ since } Y = \{\text{January, February, May, July}\}$$

$$n(V) = 3, \text{ since } V = \{\text{April, August, October}\}$$

$$n(R) = 4, \text{ since } R = \{\text{September, October, November, December}\}$$

$$37. n(R^c) = n(U) - n(R) = 12 - 4 = 8$$

$$38. n(J \cap V) = 0, \text{ since no month starts with J and begins with a vowel.}$$

$$39. n(J \cup Y) = n(J) + n(Y) - n(J \cap Y) = 3 + 4 - 2 = 5$$

$$40. n(V \cap R) = 1, \text{ since October is the only month that starts with a vowel and ends with the letter R.}$$

$$41. n(S \cup A) = n(S) + n(A) - n(S \cap A) = 13 + 4 - 1 = 16$$

Note: $n(S \cap A) = 1$, since there is only one ace which is also a spade.

$$42. n(C \cup T) = n(C) + n(T) - n(C \cap T) = 13 + 4 - 1 = 16$$

Note: $n(C \cap T) = 1$, since there is only one two which is also a club.

$$43. n(F \cup B) = n(F) + n(B) - n(F \cap B) = 12 + 26 - 6 = 32$$

Note: $n(F \cap B) = 6$, since there are six face cards that are also black.

$$44. n(F \cup D) = n(F) + n(D) - n(F \cap D) = 12 + 13 - 3 = 22$$

$$45. n(F \cap B) = 6, \text{ since there are 6 black face cards.}$$

$$46. n(F \cap D) = 3, \text{ since there are 3 face cards which are diamonds.}$$

$$47. n(A \cup E) = n(A) + n(E) - n(A \cap E) = 4 + 4 - 0 = 8$$

Note: $n(A \cap E) = 0$, since there are no aces which are also eights.

$$48. n(T \cup S) = n(T) + n(S) - n(T \cap S) = 4 + 4 - 0 = 8$$

Note: $n(T \cap S) = 0$, since there are no threes which are also sixes.

$$49. n(A \cap E) = 0, \text{ since there are no aces which are also eights.}$$

50. $n(T \cap S) = 0$, since there are no threes which are also sixes.

51. a. $\{1, 2, 3\}$
b. $\{1, 2, 3, 4, 5, 6\}$
c. $E \subseteq F$
d. $E \subseteq F$

52. a. A , Example: $A = \{1, 2\}, B = \{1, 2, 3\}$
b. B , Example: $A = \{1, 2\}, B = \{1, 2, 3\}$

53. a. $\{\}, \{a\}$ 2 subsets
b. $\{\}, \{a\}, \{b\}, \{a, b\}$ 4 subsets
c. $\{\}, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{a, b, c\}$ 8 subsets
d. $\{\}, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}, \{a, b, c, d\}$ 16 subsets
e. Yes! The number of subsets of $A = 2^{n(A)}$
f. Since $n(A) = 6$, the number of subsets is $2^6 = 64$.

54. Prove: $n(U) = n(A) + n(A')$

Proof: Note that $A \cup A' = U$
 $n(U) = n(A \cup A')$

$$= n(A) + n(A') - n(A \cap A')$$

Thus, $n(U) = n(A) + n(A')$ since

$$A \cap A' = \{\}$$

55. The two sets are disjoint.

56. $A = B = \{\}$

57. The set $\{0\}$ contains one member, namely 0. The other set, \emptyset , contains no elements.

58. 0 is a number, not a set. $\{0\}$ is a set containing one element, namely 0.

59. Only if $A = \{\}$

61. The roster method is advantageous if the number of elements is small. Set-builder notation is advantageous when the number of elements is large.

62. a. x is an element in the intersection of A and B if and only if x is an element in A and x is an element in B .
b. x is an element in the complement of A if and only if x is not an element in A .
c. A is a subset of B if and only if the following is true: If x is an element of A , then x is an element of B .

63. Venn was a professor of moral sciences at Cambridge.

64. Venn utilized diagrams to analyze logical arguments. Venn's contribution was to make these diagrams uniform.

65. a. doesn't conform because M & O are in the same group
b. doesn't conform because J & P are in the same group
c. doesn't conform because N is in

John's group, but P is not in Juneko's group.

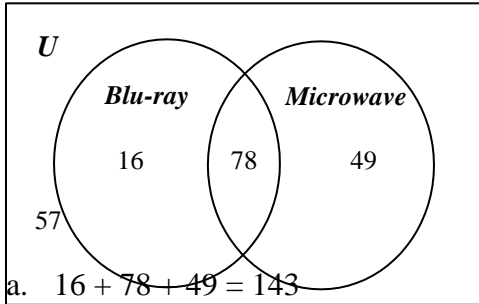
60. If A is a proper subset of B , there must be at least one element in B that is not in A .

- d. conforms
 - e. doesn't conform because M & O are in the same group
66. (a) J; If N is in John's group, then P must be in Juneko's group. But, if P is in Juneko's group, then J must be in John's group.
67. (c) L, M, P; Juneko's group must contain both M & P and Juneko's group can't contain O or J.
68. (b) If J is in Juneko's group, P can't be in it. But, if N was in John's group, then P would have to be in Juneko's group.

69. e. If K is in John's group, then M must be in Juneko's group. But, M & O cannot be in the same group, so O cannot be in Juneko's group. O could be in John's group, but it could also be the poster that is not used. Nothing is known about J, L, or N which means answer (e) is the only one that can be true.

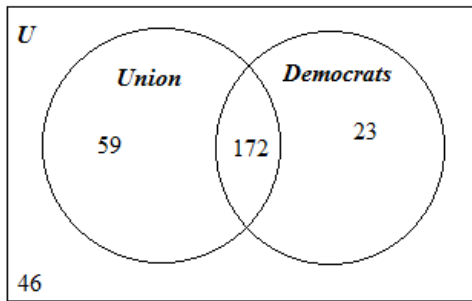
SECTION 2.2

1.



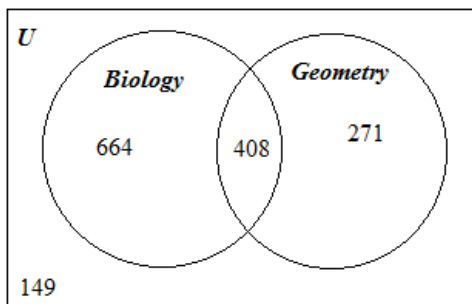
- a. $16 + 78 + 49 = 143$
- b. 16
- c. 49
- d. 57

2.



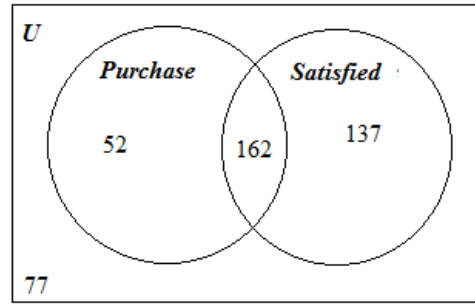
- a. $59 + 172 + 23 = 254$
- b. 59
- c. 23
- d. 46

3.



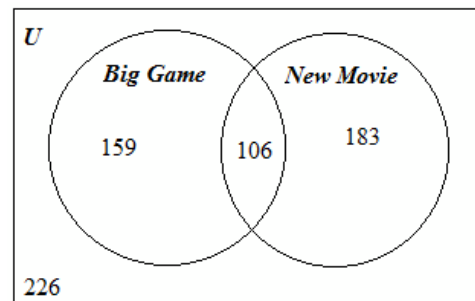
- a. 408
- b. $664 + 408 + 217 = 1,343$
- c. 664
- d. 149

4.



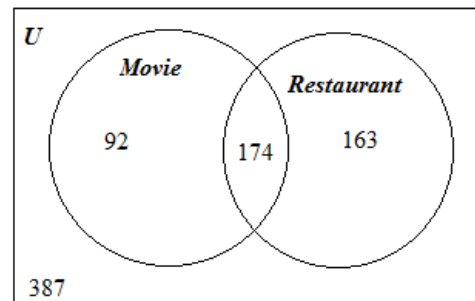
- a. 162
- b. 351
- c. 137
- d. 77

5.

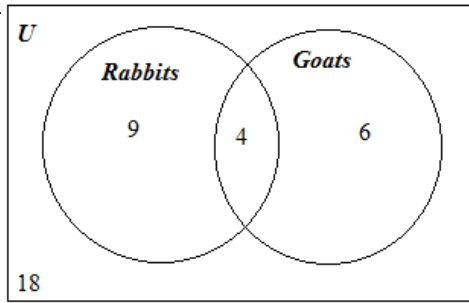


- a. 106
- b. 448
- c. 256
- d. 159

6.

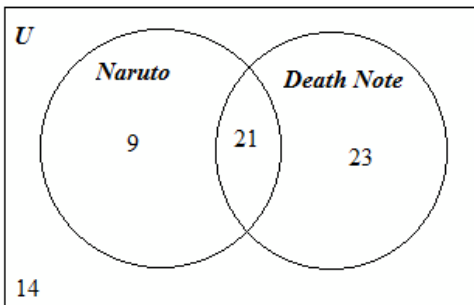


- a. 174
- b. 429
- c. 337
- d. 163



- a. $\frac{19}{37} \approx 0.51351 = 51.351\%$
- b. $\frac{9}{37} \approx 0.24324 = 24.324\%$
- c. $\frac{6}{37} \approx 0.162162 = 16.216\%$

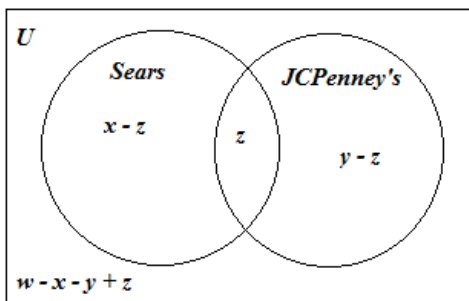
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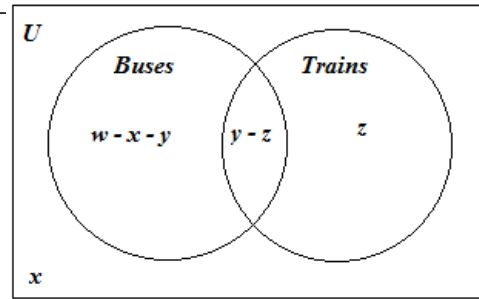
- a. $\frac{53}{67} \approx 0.79104 = 79.104\%$
- b. $\frac{9}{67} \approx 0.13433 = 13.433\%$
- c. $\frac{23}{67} \approx 0.34328 = 34.328\%$

67

9.



$$w - (x - z) - z - (y - z) = w - x - y + z$$



$$w - (y - z) - z - x = w - x - y$$

- a. $y - z$
- b. $w - x - y$
- c. $(w - x - y) + (y - z) = w - x - z$
- d. $(w - x - y) + (y - z) + z = w - x$

11. Find the total number of people surveyed:

$$63 + 77 + 69 + 104 + 57 + 29 + 67 + 64 = 530$$

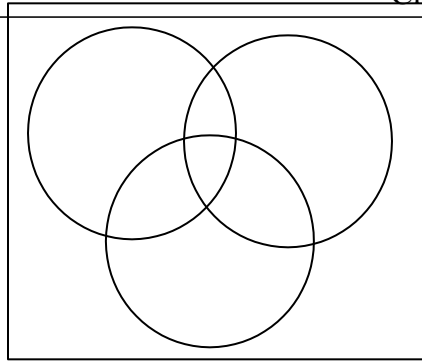
a. $\frac{n(\text{cell phones})}{n(\text{surveyed})} = \frac{57 + 77 + 69 + 29}{530} \approx 0.438 = 43.8\%$

b. $\frac{n(\text{only a cell phone})}{n(\text{surveyed})} = \frac{57}{530} \approx 0.108 = 10.8\%$

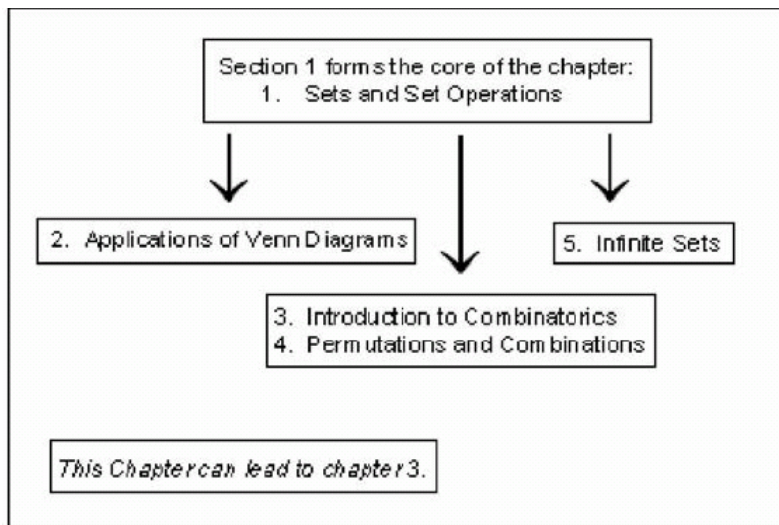
U

- a. $(x - z) + z + (y - z) = x + y - z$
- b. $x - z$
- c. $y - z$
- d. $w - x - y + z$

	<i>Tablets</i>	<i>Cell phones</i>	
	63	77	57
		69	
	104	29	
	67		
64	<i>Blu-ray</i>		



Chapter 2 Sets and Counting



This chapter focuses on using sets and counting techniques to sort information regarding surveys and sample spaces. Several sections contain exercises pertaining to questions similar to those typically encountered on the Graduate Record Examination (GRE) or the Law School Admission Test (LSAT); this feature is called “The Next Level.”

Section 2.1 forms the core of the chapter. Sections 2.2 through 2.5 are optional. Section 2.2 utilizes

Venn diagrams in the analysis of surveys. Section 2.3 and 2.4 provide an investigation of combinatorics: tree diagrams and the multiplying principle, permutations, and combinations.

Section 2.5 provides a brief study of countable versus uncountable infinite sets. Most of the chapter is used to service Chapter 3, Probability. Specifically, section 2.1 is prerequisite for section 3.2, and sections 2.3 and 2.4 are prerequisites for sections 3.4 and 3.5.

2.1 Sets and Set Operations

Topics

set notation

Venn diagrams

Cardinal number of a set

Subset (the distinction of proper versus improper is required for section 2.5.)

Set operations:

intersection (page 77)

union (page 78)

complementation (page 80)

cardinal number rules:

for the union/intersection of sets (page 79)

for the complement of a set (page 82)

comparison of the set operations and the logical connectives from Chapter 1. (charts on page 83)

Historical Note on John Venn, page 81

Exercises

- 1: determining whether or not sets are well-defined
- 2: true/false questions regarding set notation
- 3–6: listing all possible subsets
- 7–16: listing the elements of specified sets
- 17–26: shading the appropriate regions of Venn diagrams
- 27–28: use of the Cardinal Number Rule for the Union/Intersection of Sets
- 29–32: applications of the Cardinal Number Rule for the Union/Intersection of Sets
- 33–40: interpreting set-builder notation, set operations, and cardinal numbers
- 41–50: the Cardinal Number is applied to a standard deck of playing cards
- 51–52: interpretation of set operations
- 53: development of the relationship between $n(A)$ and the number of subsets of A
- 54: proof of Cardinal Number Formula
- 55–62: Concept Questions
- 63–64: History Questions
- 65–69: The Next Level

2.2

Applications of Venn Diagrams

Topics

using Venn diagrams to sort the information obtained from a survey

De Morgan's Laws

Historical Note on Augustus D Morgan, page 81

Topic X: Blood Types/Set Theory in the Real World, page 82

Exercises

- 1–10: analyzing surveys that consist of two categories
- 11–20: analyzing surveys that consist of three categories
- 21–22: analyzing surveys that consist of four categories
- 23–26: using De Morgan's Laws to simplify set operations
- 27–32: shading the appropriate regions of Venn diagrams
- 33–34: using Venn diagrams to prove set operation identities
- 35–43: exercises regarding Set Theory in the Real World: Blood Types
- 44–45: History Questions
- 46–52: 82
- 53: Project

2.3 Introduction to Combinatorics

Topics

tree diagrams

The Fundamental Principle of counting
factorials

Exercises

- 1–4: constructing tree diagrams to list all possible outcomes
- 5–22: applications of the Fundamental Principle of Counting
- 23–46: factorial arithmetic
- 47–48: Concept Question
- 49: History Questions
- 50–54: The Next Level

2.4 Permutations and Combinations

Topics

with versus without replacement
permutations (formula on page 108)
combinations (formula on page 111)
Pascal's triangle
Historical Note on Chu Shih-chich, page 116
combinatoric flowchart, page 115
permutations of identical items (formula on page 118)

Exercises

- 1–12: evaluating expressions of the form ${}_nP_r$ and ${}_nC_r$
- 13–16: listing all possible permutations and combinations of given elements
- 17–26: applications of combinatorics
- 27–32: using combinations to determine the number of possible poker hands
- 33–44: various types of lotteries are examined
- 45–48: analyzing patterns in Pascal's Triangle
- 49–60: permutations of identical items
- 61–62: Concept Questions
- 63–67: The Next Level
- 68: Project

2.5 Infinite Sets

Topics

Historical Note on Georg Cantor, page 124

one-to-one correspondence and equivalent sets

countable sets and \aleph_0 uncountable sets and points on a line exercises

Exercises

1–10: one-to-one correspondences between finite sets

11–16: investigating countable infinite sets and their correspondences

17–23: draw geometric figures to obtain one-to-one correspondence between uncountable infinite sets

24: Concept Question

25–27: History Questions

28: Project