

Solution Manual for Mechanics of Materials 10th Edition Hibbeler

0134319656 9780134319650

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2-1.

An air-filled rubber ball has a diameter of 6 in. If the air pressure within the ball is increased until the diameter becomes 7 in., determine the average normal strain in the rubber.

Solution

$$d_0 = 6 \text{ in.}$$

$$d = 7 \text{ in.}$$

$$P = \frac{pd - pd_0}{pd_0} = \frac{7 - 6}{6} = 0.167 \text{ in./in.}$$

Ans.

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Ans:

$$P = 0.167 \text{ in.} > \text{in.}$$

2-2.

A thin strip of rubber has an unstretched length of 15 in. If it is stretched around a pipe having an outer diameter of 5 in., determine the average normal strain in the strip.

Solution

$$L_0 = 15 \text{ in.}$$

$$L = p(5 \text{ in.})$$

$$P = \frac{L - L_0}{L_0} = \frac{5p - 15}{15} = 0.0472 \text{ in./in.}$$

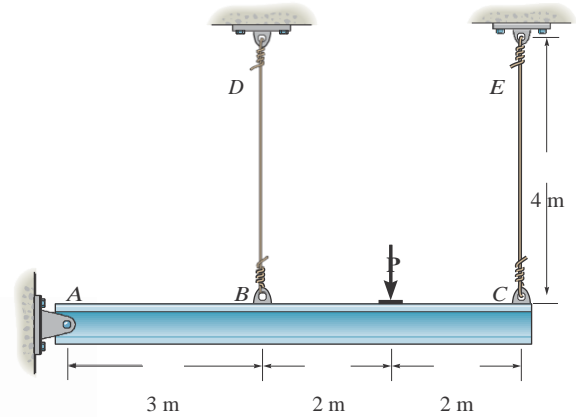
Ans.

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Ans:
P = 0.0472 in. > in.

2-3.

If the load P on the beam causes the end C to be displaced 10 mm downward, determine the normal strain in wires CE and BD .



Solution

$$\frac{L_{BD}}{3} = \frac{L_{CE}}{7}$$

$$L_{BD} = \frac{3(10)}{7} = 4.286 \text{ mm}$$

$$P_{CE} = \frac{L_{CE}}{L} = \frac{10}{4000} = 0.00250 \text{ mm/mm}$$

Ans.

$$P_{BD} = \frac{L_{BD}}{L} = \frac{4.286}{4000} = 0.00107 \text{ mm/mm}$$

Ans.



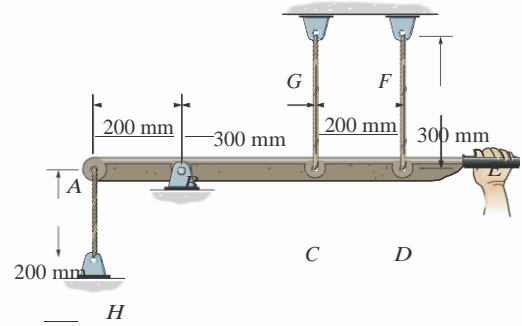
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Ans:

$$P_{CE} = 0.00250 \text{ mm} > \text{mm}, P_{BD} = 0.00107 \text{ mm} > \text{mm}$$

*2-4.

The force applied at the handle of the rigid lever causes the lever to rotate clockwise about the pin B through an angle u . The wires are unstretched when the lever is in the horizontal position.



Solution

Geometry: The lever arm rotates through an angle of $u = \frac{2}{180} \pi \text{ rad} = 0.03491 \text{ rad}$.

Since u is small, the displacements of points A , C , and D can be approximated by

$$d_A = 200(0.03491) = 6.9813 \text{ mm}$$

$$d_C = 300(0.03491) = 10.4720 \text{ mm}$$

$$d_D = 500(0.03491) = 17.4533 \text{ mm}$$

Average Normal Strain: The unstretched length of wires AH , CG , and DF are

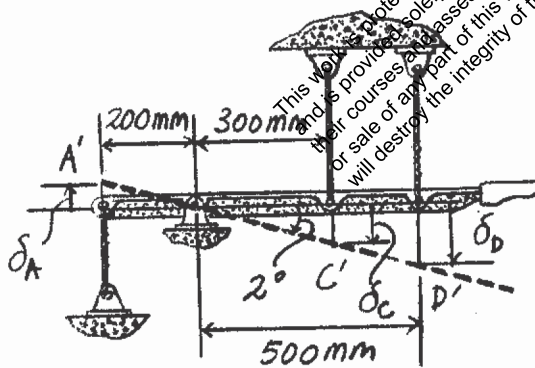
$L_{AH} = 200 \text{ mm}$, $L_{CG} = 300 \text{ mm}$, and $L_{DF} = 300 \text{ mm}$. We obtain

$$(P_{\text{avg}})_{AH} = \frac{d_A}{L_{AH}} = \frac{6.9813}{200} = 0.0349 \text{ mm/mm}$$

$$(P_{\text{avg}})_{CG} = \frac{d_C}{L_{CG}} = \frac{10.4720}{300} = 0.0349 \text{ mm/mm}$$

$$(P_{\text{avg}})_{DF} = \frac{d_D}{L_{DF}} = \frac{17.4533}{300} = 0.0582 \text{ mm/mm}$$

Ans.



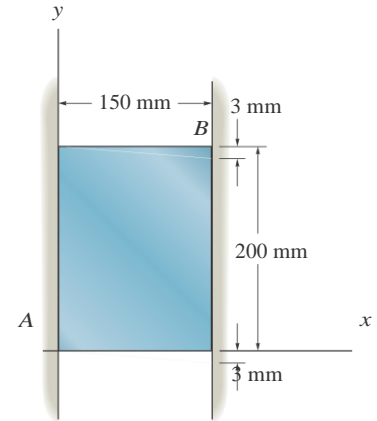
(a)

Ans:

$$\begin{aligned}(P_{\text{avg}})_{AH} &= 0.0349 \text{ mm}^2/\text{mm} \\(P_{\text{avg}})_{CG} &= 0.0349 \text{ mm}^2/\text{mm} \\(P_{\text{avg}})_{DF} &= 0.0582 \text{ mm}^2/\text{mm}\end{aligned}$$

2-5.

The rectangular plate is subjected to the deformation shown by the dashed line. Determine the average shear strain γ_{xy} in the plate.



Solution

Geometry:

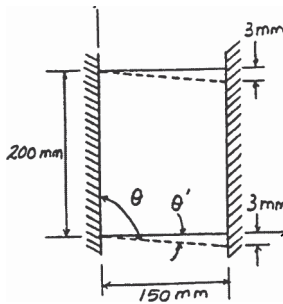
$$u = \tan^{-1} \frac{3}{150} = 0.0200 \text{ rad}$$

$$u = a \frac{P}{2} + 0.0200b \text{ rad}$$

Shear Strain:

$$\gamma_{xy} = \frac{P}{2} - u = \frac{P}{2} - a \frac{P}{2} + 0.0200b$$

$$= -0.0200 \text{ rad}$$



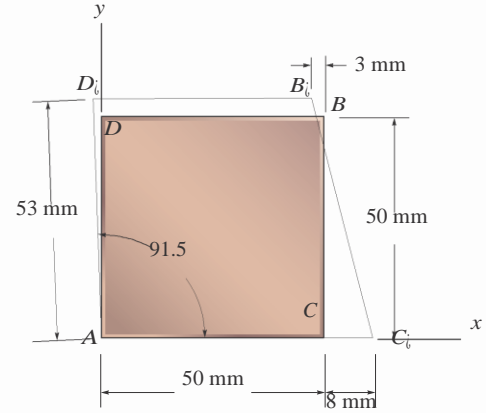
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Ans:

$$g_{xy} = -0.0200 \text{ rad}$$

2-6.

The square deforms into the position shown by the dashed lines. Determine the shear strain at each of its corners, $A, B, C,$ and $D,$ relative to the x, y axes. Side DB remains horizontal.



Solution

Geometry:

$$BC = \sqrt{(8+3)^2 + (53 \sin 88.5)^2} = 54.1117 \text{ mm}$$

$$CD = \sqrt{53^2 + 58^2 - 2(53)(58) \cos 91.5} = 79.5860 \text{ mm}$$

$$BD = 50 + 53 \sin 1.5 - 3 = 48.3874 \text{ mm}$$

$$(BD)^2 + (BC)^2 - (CD)^2$$

$$\cos u = \frac{2(BD)(BC)}{2(48.3874)(54.1117)} = \frac{48.3874^2 + 54.1117^2 - 79.5860^2}{2(48.3874)(54.1117)} = -0.20328$$

$$u = 101.73$$

$$b = 180 - u = 78.27$$

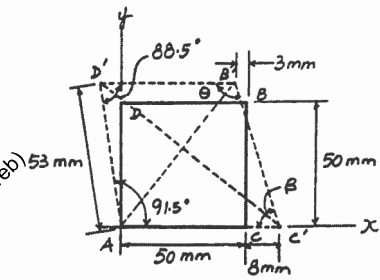
Shear Strain:

$$(g_A)_{xy} = \frac{p}{2} - \frac{p a}{180} b = -0.0262 \text{ rad} \quad \text{Ans.}$$

$$(g_B)_{xy} = \frac{p}{2} - u = \frac{p}{2} - \frac{p a}{180} 101.73 = -0.205 \text{ rad} \quad \text{Ans.}$$

$$(g_C)_{xy} = b - \frac{p}{2} = \frac{p a}{180} 78.27 - \frac{p}{2} = 0.205 \text{ rad} \quad \text{Ans.}$$

$$(g_D)_{xy} = \frac{p a}{180} 88.5 - \frac{p}{2} = -0.0262 \text{ rad} \quad \text{Ans.}$$



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Ans:

$$(g_A)_{xy} = -0.0262 \text{ rad}$$

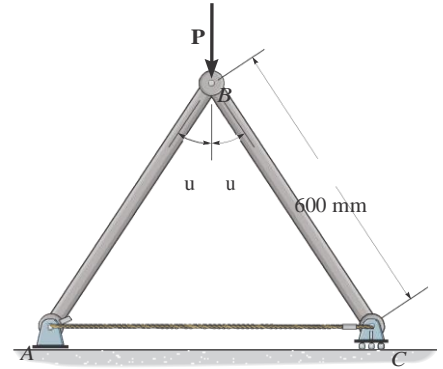
$$(g_B)_{xy} = -0.205 \text{ rad}$$

$$(g_C)_{xy} = -0.205 \text{ rad}$$

$$(g_D)_{xy} = -0.0262 \text{ rad}$$

2-7.

The pin-connected rigid rods AB and BC are inclined at $u = 30^\circ$ when they are unloaded. When the force P is applied u becomes 30.2° . Determine the average normal strain in wire AC .



Solution

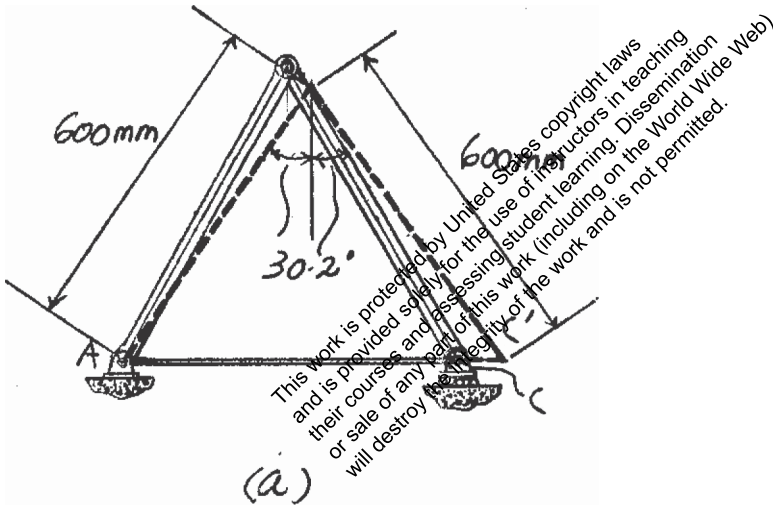
Geometry: Referring to Fig. a , the unstretched and stretched lengths of wire AD are

$$L_{AC} = 2(600 \sin 30^\circ) = 600 \text{ mm}$$

$$L_{AC} = 2(600 \sin 30.2^\circ) = 603.6239 \text{ mm}$$

Average Normal Strain:

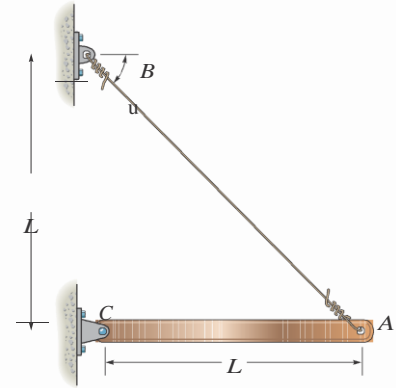
$$(\epsilon_{\text{avg}})_{AC} = \frac{L_{AC} - L_{AC}}{L_{AC}} = \frac{603.6239 - 600}{600} = 6.04(10^{-3}) \text{ mm/mm} \quad \text{Ans.}$$



Ans:
 $(P_{\text{avg}})_{AC} = 6.04(10^{-3}) \text{ mm}^2$

*2-8.

The wire AB is unstretched when $u = 45^\circ$. If a load is applied to the bar AC , which causes u to become 47° , determine the normal strain in the wire.



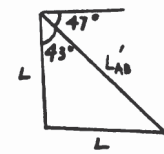
Solution

$$L^2 = L^2 + L_{AB}^2 - 2LL_A \cos 43$$

$$L_{AB} = 2L \cos 43$$

$$\begin{aligned} \epsilon_{AB} &= \frac{L_{AB} - L_{AB}}{L_{AB}} \\ &= \frac{2L \cos 43 - 2L}{2L} \\ &= 0.0343 \end{aligned}$$

Ans.

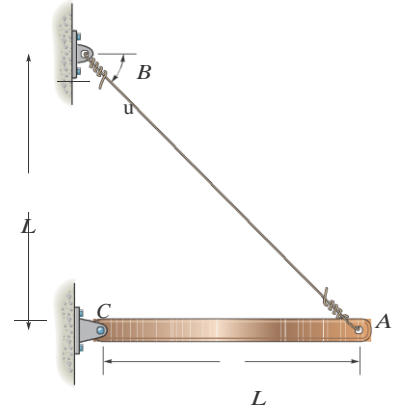


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Ans:
 $P_{AB} = 0.0343$

2-9.

If a horizontal load applied to the bar AC causes point A to be displaced to the right by an amount L , determine the normal strain in the wire AB. Originally, $u = 45^\circ$.



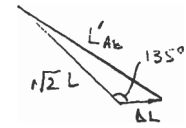
Solution

$$L_{AB} = \sqrt{(2L)^2 + L^2} = 2.236L$$

$$P_{AB} = \frac{L_{AB} - L_{AB_0}}{L_{AB_0}}$$

$$= \frac{2.236L + L - 2.236L}{2.236L}$$

$$= 1 + \frac{L}{2.236L} - 1$$



Neglecting the higher-order terms,

$$P_{AB} = 1 + \frac{L}{2L} - 1$$

$$= 1 + \frac{1}{2} - 1$$

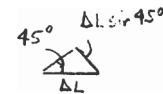
$$= 0.5$$

Also,

$$P_{AB} = \frac{L \sin 45^\circ}{2.236L} = \frac{0.707L}{2.236L}$$

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Ans.



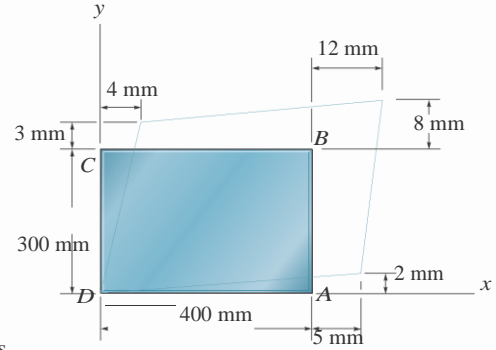
Ans.

Ans: $P_{AB} =$

0.5 *LL*

2-10.

Determine the shear strain g_{xy} at corners A and B if the plastic distorts as shown by the dashed lines.



Solution

Geometry: Referring to the geometry shown in Fig. a , the small-angle analysis gives

$$a = c = \frac{7}{306} = 0.022876 \text{ rad}$$

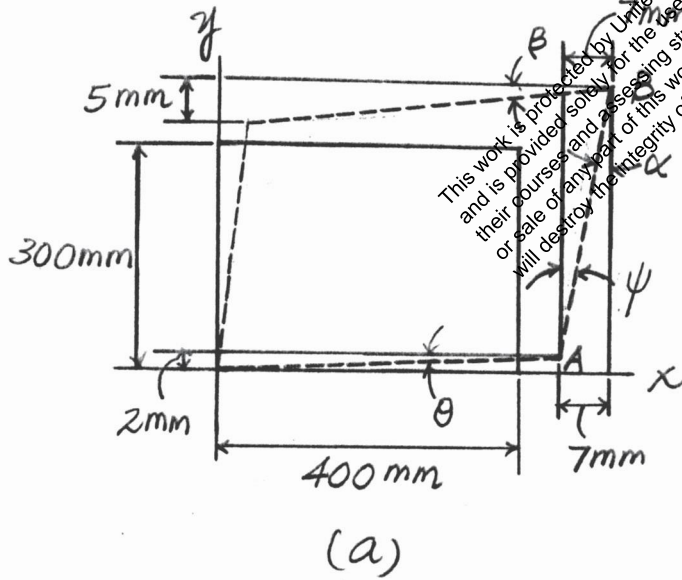
$$b = \frac{5}{408} = 0.012255 \text{ rad}$$

$$u = \frac{2}{405} = 0.0049383 \text{ rad}$$

Shear Strain: By definition,

$$(g_A)_{xy} = u + c = 0.02781 \text{ rad} = 27.8(10^{-3}) \text{ rad}$$

$$(g_B)_{xy} = a + b = 0.03513 \text{ rad} = 35.1(10^{-3}) \text{ rad}$$

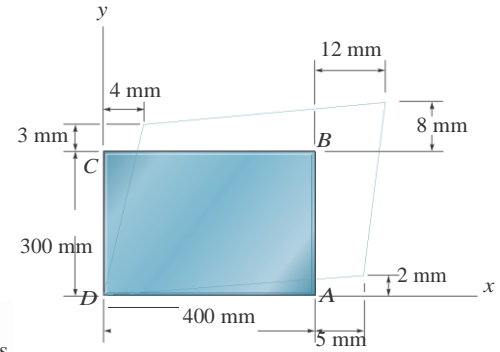


Ans:
 $(g_A)_{xy} = 27.8(10^{-3}) \text{ rad}$

$$(g_B)_{xy} = 35.1(10^{-3}) \text{ rad}$$

2-11.

Determine the shear strain g_{xy} at corners D and C if the plastic distorts as shown by the dashed lines.



Solution

Geometry: Referring to the geometry shown in Fig. *a*, the small-angle analysis gives

$$a = c = \frac{4}{303} = 0.013201 \text{ rad}$$

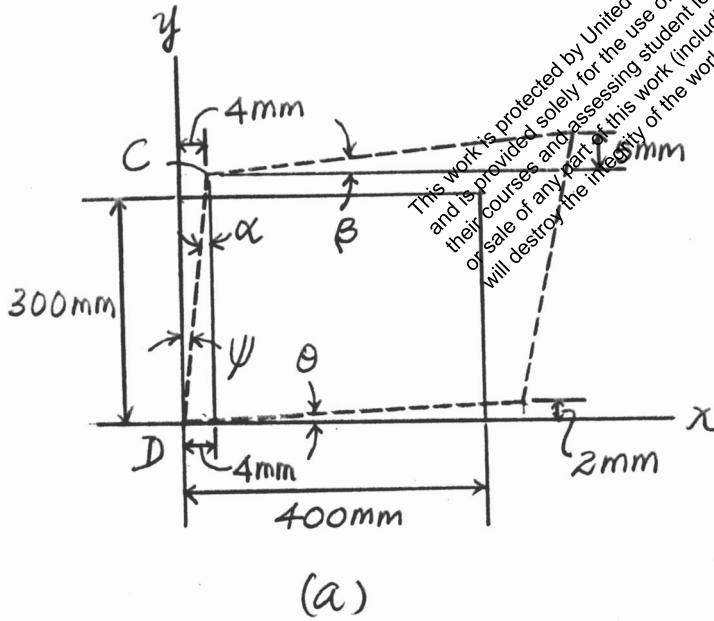
$$u = \frac{2}{405} = 0.0049383 \text{ rad}$$

$$b = \frac{5}{408} = 0.012255 \text{ rad}$$

Shear Strain: By definition,

$$(g_{xy})_C = a + b = 0.02546 \text{ rad} = 25.5(10^{-3}) \text{ rad}$$

$$(g_{xy})_D = u + c = 0.01814 \text{ rad} = 18.1(10^{-3}) \text{ rad}$$



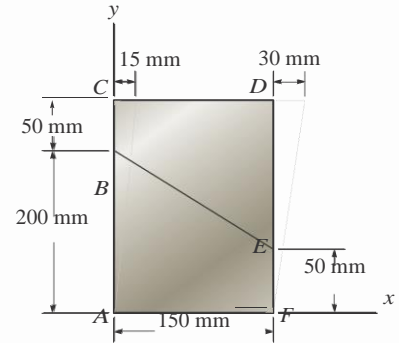
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Ans:
 $(g_{xy})_C = 25.5(10^{-3}) \text{ rad}$

$$(g_{xy})_D = 18.1(10^{-3}) \text{ rad}$$

*2-12.

The material distorts into the dashed position shown. Determine the average normal strains ϵ_x , ϵ_y and the shear strain γ_{xy} at A, and the average normal strain along line BE.



Solution

Geometry: Referring to the geometry shown in Fig. a,

$$\tan u = \frac{15}{250}; \quad u = (3.4336) a \frac{\pi}{180} \text{ rad} = 0.05993 \text{ rad}$$

$$L_{AC} = \sqrt{15^2 + 150^2} = 262.725 \text{ mm}$$

$$\frac{BB'}{15} = \frac{200}{250}; \quad BB' = 12 \text{ mm} \quad \frac{EE'}{30} = \frac{50}{250}; \quad EE' = 6 \text{ mm}$$

$$x = 150 + EE' - BB' = 150 + 6 - 12 = 144 \text{ mm}$$

$$L_{BE} = \sqrt{150^2 + 150^2} = 212.13 \text{ mm} \quad L_{B'E'} = \sqrt{144^2 + 150^2} = 207.8 \text{ mm}$$

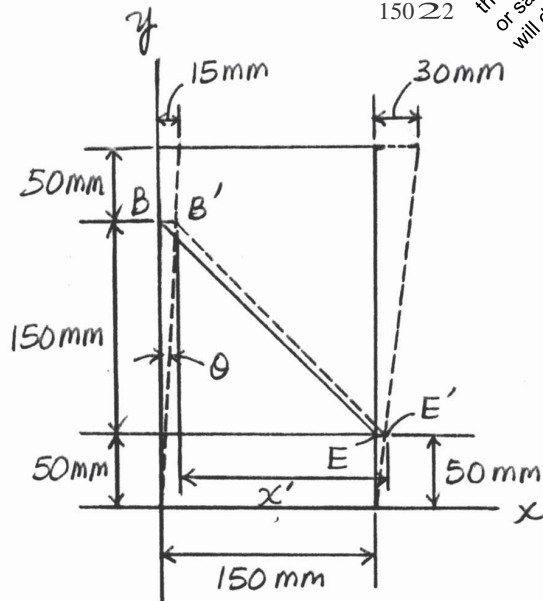
Average Normal and Shear Strain: Since no deformation occurs along y, $\epsilon_x = 0$.

$$(\epsilon_y)_A = \frac{L_{AC} - L_{AC}}{L_{AC}} = \frac{262.725 - 250}{250} = 1.80(10^{-3}) \text{ Ans.}$$

By definition,

$$(\gamma_{xy})_A = u = 0.0599 \text{ rad} \quad \text{Ans.}$$

$$P_{BE} = \frac{L_{B'E'} - L_{BE}}{L_{BE}} = \frac{207.8 - 212.13}{212.13} = -0.0204 \text{ Ans.}$$



(a)

Ans:
 $(\epsilon_x)_A = 0$

$$(P_y)_A = 1.80(10^{-3}) \text{ mm} > \text{mm}$$

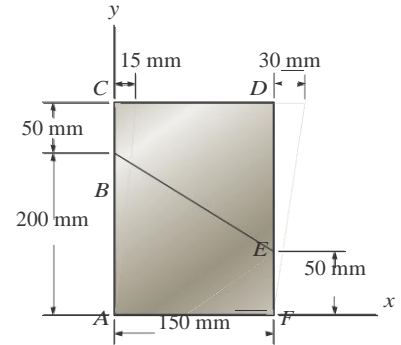
$$(g_{xy})_A = 0.0599 \text{ rad}$$

$$P_{BE} = -0.0198 \text{ mm} > \text{mm}$$

2-13.

The material distorts into the dashed position shown.

AD and CF .



Solution

Geometry: Referring to the geometry shown in Fig. a,

$$L_{AD} = L_{CF} = 2(150)^2 + 250^2 = 285000 \text{ mm}$$

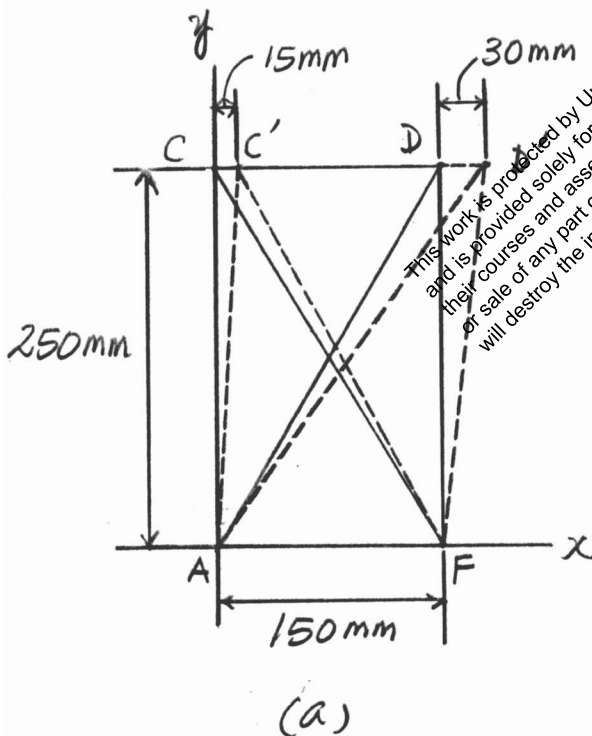
$$L_{AD} = 2(150 + 30)^2 + 250^2 = 294900 \text{ mm}$$

$$L_{CF} = 2(150 - 15)^2 + 250^2 = 280725 \text{ mm}$$

Average Normal Strain:

$$\epsilon_{AD} = \frac{L_{AD} - L_{AD}}{L_{AD}} = \frac{294900 - 285000}{285000} = 0.0347 \text{ mm/mm} \quad \text{Ans.}$$

$$\epsilon_{CF} = \frac{L_{CF} - L_{CF}}{L_{CF}} = \frac{280725 - 285000}{285000} = -0.0148 \text{ mm/mm}$$



Ans:
 $P_{AD} = 0.0566 \text{ mm} > \text{mm}$
 $P_{CF} = -0.0255 \text{ mm} > \text{mm}$

2-14.

Part of a control linkage for an airplane consists of a rigid member CB and a flexible cable AB . If a force is applied to the end B of the member and causes it to rotate by $u = 0.5^\circ$, determine the normal strain in the cable. Originally the cable is unstretched.

Solution

Geometry: Referring to the geometry shown in Fig. a , the unstretched and stretched lengths of cable AB are

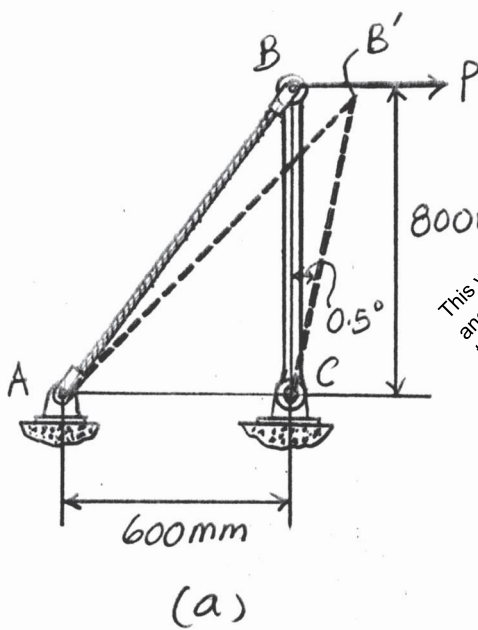
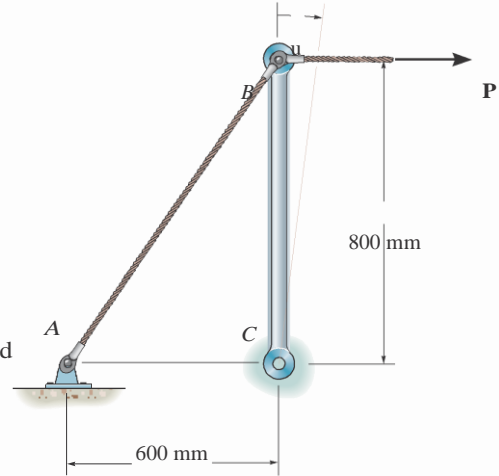
$$L_{AB} = \sqrt{600^2 + 800^2} = 1000 \text{ mm}$$

$$L_{AB} = \sqrt{600^2 + 800^2 - 2(600)(800) \cos 90.5^\circ} = 1004.18 \text{ mm}$$

Average Normal Strain:

$$\epsilon_{AB} = \frac{L_{AB} - L_{AB}}{L_{AB}} = \frac{1004.18 - 1000}{1000} = 0.00418 \text{ mm/mm}$$

Ans.



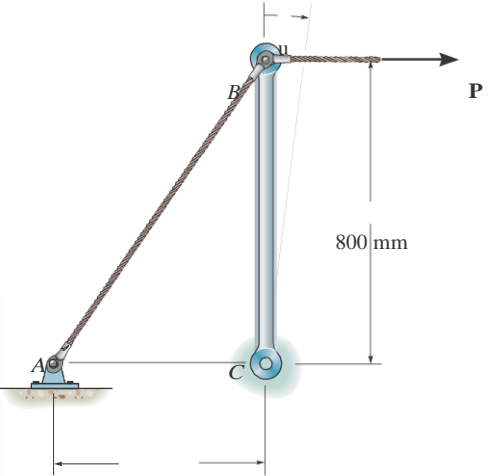
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Ans:

$$P_{AB} = 0.00418 \text{ mm} > \text{mm}$$

2-15.

Part of a control linkage for an airplane consists of a rigid member CB and a flexible cable AB . If a force is applied to the end B of the member and causes a normal strain in the cable of 0.004 mm/mm , determine the displacement of point B . Originally the cable is unstretched.



Solution

Geometry: Referring to the geometry shown in Fig. a , the unstretched and stretched lengths of cable AB are—

$$L_{AB} = \sqrt{600^2 + 800^2} = 1000 \text{ mm}$$

$$L_{AB} = \sqrt{600^2 + 800^2 - 2(600)(800) \cos(90^\circ + u)}$$

$$L_{AB} = \sqrt{10^6 - 0.960(10^6) \cos(90^\circ + u)}$$

Average Normal Strain:

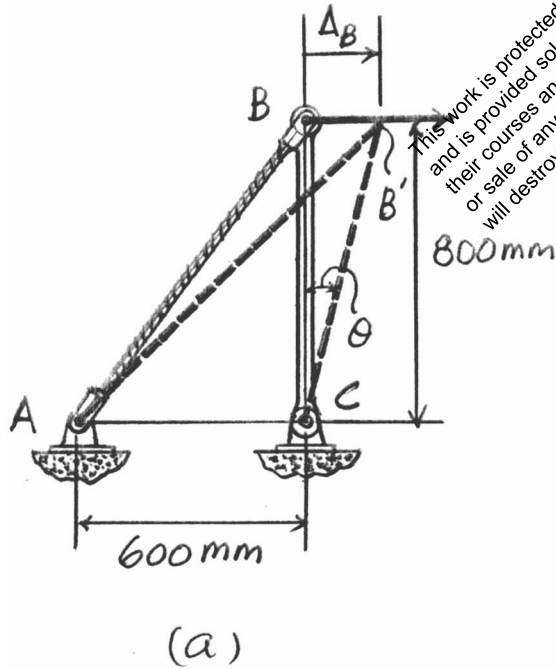
$$\epsilon_{AB} = \frac{L_{AB} - L_{AB}}{L_{AB}}; \quad 0.004 = \frac{\sqrt{10^6 - 0.960(10^6) \cos(90^\circ + u)} - 1000}{1000}$$

$$u = 0.4784 \text{ rad} \quad \theta = 0.008350 \text{ rad}$$

Thus,

$$\Delta_B = u L_{BC} = 0.008350(800) = 6.68 \text{ mm}$$

Ans.

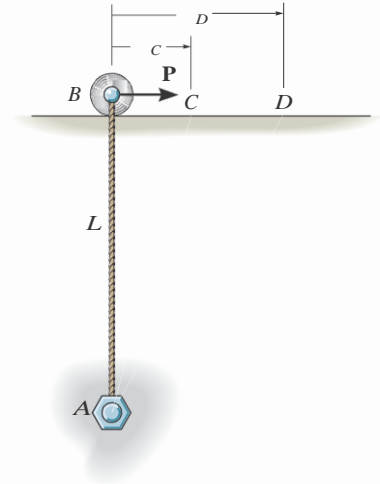


Ans:

$$B = 6.68 \text{ mm}$$

*2-16.

The nylon cord has an original length L and is tied to a bolt at A and a roller at B . If a force P is applied to the roller, determine the normal strain in the cord when the roller is at C , and at D . If the cord is originally unstrained when it is at C , determine the normal strain P_D when the roller moves to D . Show that if the displacements c and d are small, then $P_D = P_C - P_C$.



Solution

$$L_C = \sqrt{2L^2 + c^2}$$

$$P_C = \frac{\sqrt{2L^2 + c^2} - L}{L}$$

$$= \frac{L\sqrt{1 + \frac{c^2}{L^2}} - L}{L} = \sqrt{1 + a \frac{c^2}{L^2}} - 1$$

For small c ,

$$P_C = 1 + \frac{1}{2} a \frac{c^2}{L^2} - 1 = \frac{1}{2} \frac{c^2}{L^2}$$

In the same manner,

$$P_D = \frac{1}{2} \frac{d^2}{L^2}$$

$$P_D = \frac{\sqrt{2L^2 + d^2} - \sqrt{2L^2 + c^2}}{\sqrt{2L^2 + c^2}} = \frac{\sqrt{1 + \frac{d^2}{L^2}} - \sqrt{1 + \frac{c^2}{L^2}}}{\sqrt{1 + \frac{c^2}{L^2}}}$$

For small c and d ,

$$P_D = \frac{1 + \frac{1}{2} \frac{d^2}{L^2} - 1 - 1 + \frac{1}{2} \frac{c^2}{L^2}}{1 + \frac{1}{2} \frac{c^2}{L^2}} = \frac{\frac{1}{2} (\frac{d^2}{L^2} - \frac{c^2}{L^2})}{1 + \frac{1}{2} \frac{c^2}{L^2}} = \frac{1}{2} (\frac{d^2}{L^2} - \frac{c^2}{L^2}) (1 - \frac{1}{2} \frac{c^2}{L^2})$$

$$P_D = \frac{1}{2} (\frac{d^2}{L^2} - \frac{c^2}{L^2}) = P_C - P_C$$

QED

Also this problem can be solved as follows:

$$A_C = L \sec u_C; \quad A_D = L \sec u_D$$

$$P_C = \frac{L \sec u_C - L}{L} = \sec u_C - 1$$

$$P_D = \frac{L \sec u_D - L}{L} = \sec u_D - 1$$

Expanding $\sec u$

$$\sec u = 1 + \frac{u^2}{2!} + \frac{5u^4}{4!} + \dots$$

*2-16. Continued

For small u neglect the higher order terms

$$\sec u = 1 + \frac{u^2}{2}$$

Hence,

$$P_C = 1 + \frac{u_C^2}{2} - 1 = \frac{u_C^2}{2}$$

$$P_D = 1 + \frac{u_D^2}{2} - 1 = \frac{u_D^2}{2}$$

$$P_D = \frac{L \sec u_D - L \sec u_C}{L \sec u_C} = \frac{\sec u_D}{\sec u_C} - 1 = \sec u_D \cos u_C - 1$$

Since $\cos u = 1 - \frac{u^2}{2!} + \frac{u^4}{4!} \dots$

$$\begin{aligned} \sec u_D \cos u_C &= a \left(1 + \frac{u_D^2}{2} \dots \right) b \left(1 - \frac{u_C^2}{2} \dots \right) \\ &= 1 - \frac{u_C^2}{2} + \frac{u_D^2}{2} - \frac{u_C^2 u_D^2}{4} \end{aligned}$$

Neglecting the higher order terms

$$\sec u_D \cos u_C = 1 + \frac{u_D^2}{2} - \frac{u_C^2}{2}$$

$$P_D = \left(1 + \frac{u_D^2}{2} - \frac{u_C^2}{2} \right) - 1 = \frac{u_D^2}{2} - \frac{u_C^2}{2}$$

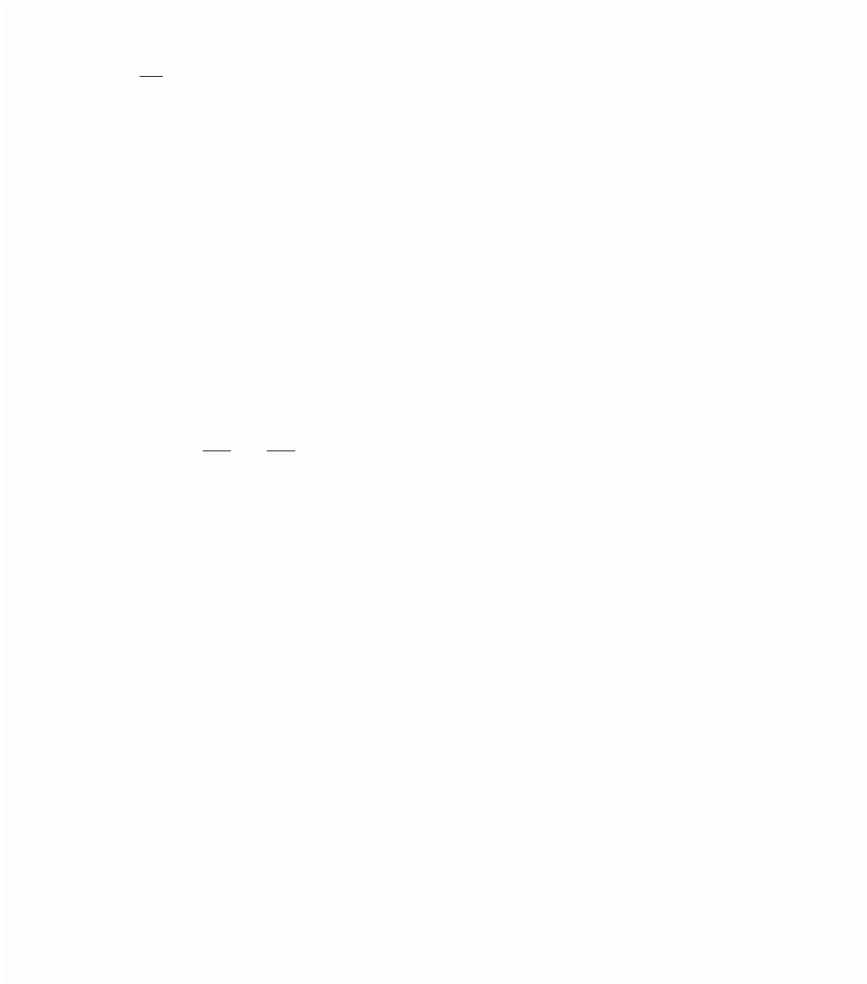
$$= P_D - P_C$$

QED

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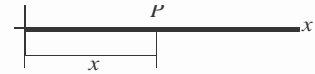
Ans: $1 - \frac{u_C^2}{2}$

$$P_C = 2 L^2$$
$$P_D = \frac{1}{2} \frac{D^2}{L^2}$$



2-17.

A thin wire, lying along the x axis, is strained such that each point on the wire is displaced $y = kx^2$ along the y axis. If k is constant, what is the normal strain at any point P along the wire?



Solution

$$\epsilon = \frac{d(y)}{dx} = 2kx$$

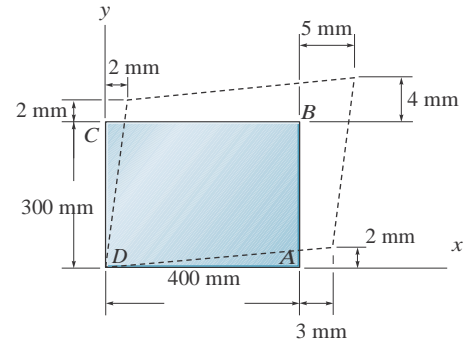
Ans.

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Ans:
 $P = 2kx$

2-18.

Determine the shear strain g_{xy} at corners A and B if the plate distorts as shown by the dashed lines.



Solution

Geometry: For small angles,

$$a = c = \frac{2}{302} = 0.00662252 \text{ rad}$$

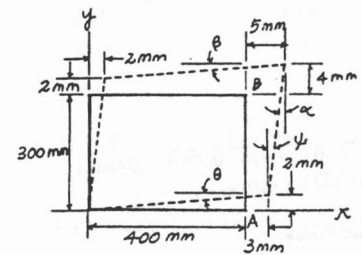
$$b = u = \frac{2}{403} = 0.00496278 \text{ rad}$$

Shear Strain:

$$(g_B)_{xy} = a + b = 0.0116 \text{ rad} = 11.6 \times 10^{-3} \text{ rad}$$

$$(g_A)_{xy} = u + c = 0.0116 \text{ rad} = 11.6 \times 10^{-3} \text{ rad}$$

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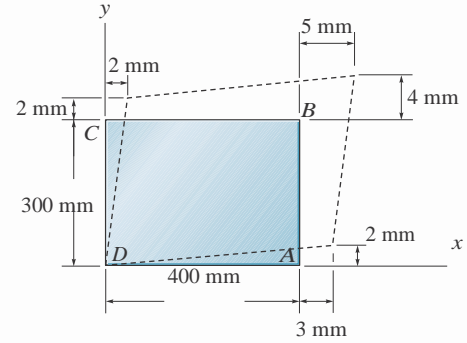


Ans:
 $(g_B)_{xy} = 11.6(10^{-3}) \text{ rad}$,

$$(g_A)_{xy} = 11.6(10^{-3}) \text{ rad}$$

2-19.

Determine the shear strain g_{xy} at corners D and C if the plate distorts as shown by the dashed lines.



Solution

Geometry: For small angles,

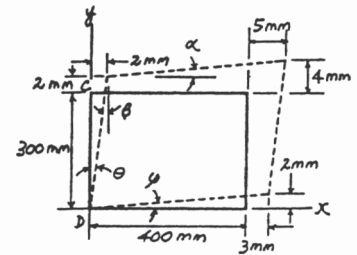
$$a = c = \frac{2}{403} = 0.00496278 \text{ rad}$$

$$b = u = \frac{2}{302} = 0.00662252 \text{ rad}$$

Shear Strain:

$$(g_C)_{xy} = a + b = 0.0116 \text{ rad} = 11.6 \cdot 10^{-3} \text{ rad}$$

$$(g_D)_{xy} = u + c = 0.0116 \text{ rad} = 11.6 \cdot 10^{-3} \text{ rad}$$



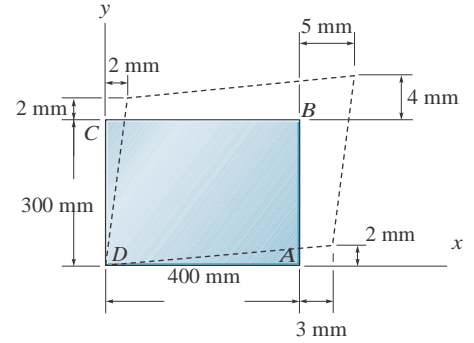
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Ans:
 $(g_C)_{xy} = 11.6(10^{-3}) \text{ rad}$,

$$(g_D)_{xy} = 11.6(10^{-3}) \text{ rad}$$

*2-20.

Determine the average normal strain that occurs along the diagonals AC and DB .



Solution

Geometry:

$$AC = DB = \sqrt{400^2 + 300^2} = 500 \text{ mm}$$

$$DB' = \sqrt{405^2 + 304^2} = 506.4 \text{ mm}$$

$$A'C' = \sqrt{401^2 + 300^2} = 500.8 \text{ mm}$$

Average Normal Strain:

$$\epsilon_{AC} = \frac{A'C' - AC}{AC} = \frac{500.8 - 500}{500}$$

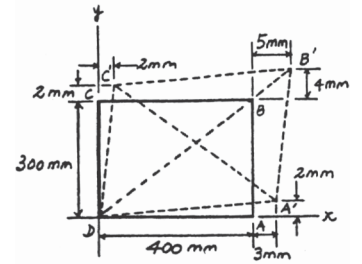
$$= 0.00160 \text{ mm/mm} = 1.60 \times 10^{-3} \text{ mm/mm}$$

$$\epsilon_{DB} = \frac{DB' - DB}{DB} = \frac{506.4 - 500}{500}$$

$$= 0.0128 \text{ mm/mm} = 12.8 \times 10^{-3} \text{ mm/mm}$$

Ans.

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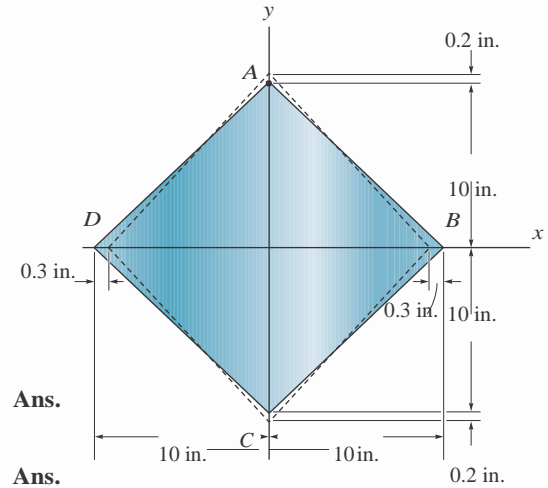
Ans:

$$P_{AC} = 1.60 \times 10^{-3} \text{ mm}^2$$

$$P_{DB} = 12.8 \times 10^{-3} \text{ mm}^2$$

2-21.

The corners of the square plate are given the displacements indicated. Determine the average normal strains P_x and P_y along the x and y axes.



Solution

$$P_x = \frac{-0.3}{10} = -0.03 \text{ in./in.}$$

$$P_y = \frac{0.2}{10} = 0.02 \text{ in./in.}$$

Ans.
Ans.

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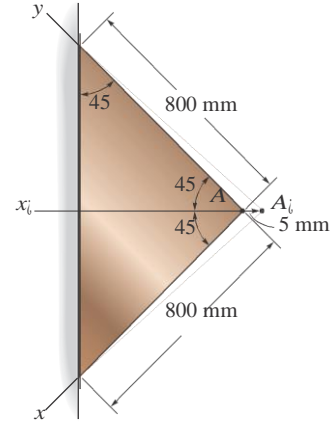
Ans:

$$P_x = -0.03 \text{ in.} > \text{in.}$$

$$P_y = 0.02 \text{ in.} > \text{in.}$$

2-22.

The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the shear strain, g_{xy} , at A .



Solution

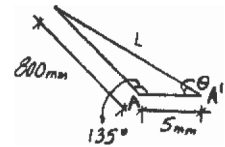
$$L = \sqrt{800^2 + 5^2} = 2(800)(5) \cos 135^\circ = 803.54 \text{ mm}$$

$$\frac{\sin 135^\circ}{803.54} = \frac{\sin u}{800}; \quad u = 44.75^\circ = 0.7810 \text{ rad}$$

$$g_{xy} = \frac{\pi}{2} - 2u = \frac{\pi}{2} - 2(0.7810)$$

$$= 0.00880 \text{ rad}$$

Ans.

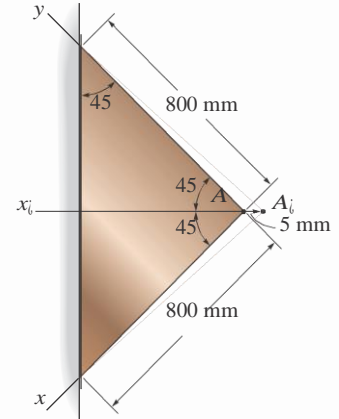


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Ans:
 $\xi_{xy} = 0.00880 \text{ rad}$

2-23.

The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the average normal strain P_x along the x axis.

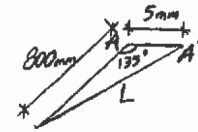


Solution

$$L = \sqrt{2(800)^2 + 5^2 - 2(800)(5) \cos 135^\circ} = 803.54 \text{ mm}$$

$$P_x = \frac{803.54 - 800}{800} = 0.00443 \text{ mm/mm}$$

Ans.



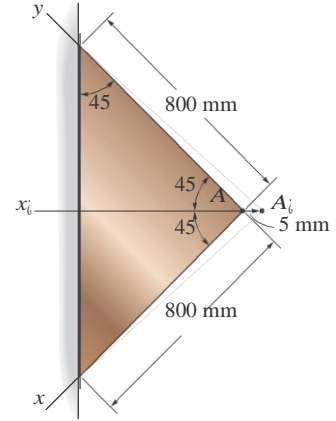
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Ans:

$$P_x = 0.00443 \text{ mm} > \text{mm}$$

***2-24.**

The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the average normal strain P_x along the x axis.

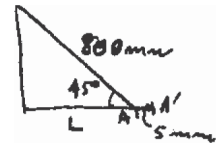


Solution

$$L = 800 \cos 45 = 565.69 \text{ mm}$$

$$P_x = \frac{5}{565.69} = 0.00884 \text{ mm/mm}$$

Ans.



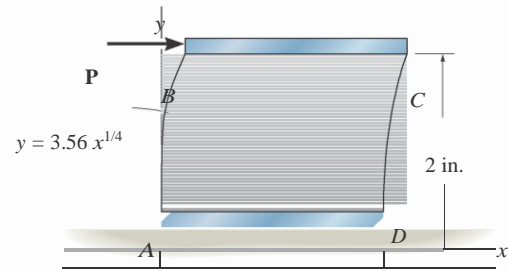
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Ans:

$$P_x = 0.0084 \text{ mm} > \text{mm}$$

2-25.

The polysulfone block is glued at its top and bottom to the
causes the material to deform so that its sides are described
by the equation $y = 3.56 x^{1/4}$, determine the shear strain at
the corners A and B .



Solution

$$y = 3.56 x^{1/4}$$

$$\frac{dy}{dx} = 0.890 x^{-3/4}$$

$$\frac{dx}{dy} = 1.123 x^{3/4}$$

At A , $x = 0$

$$g_A = \frac{dx}{dy} = 0$$

At B ,

$$2 = 3.56 x^{1/4}$$

$$x = 0.0996 \text{ in.}$$

$$g_B = \frac{dx}{dy} = 1.123(0.0996)^{3/4} = 0.199 \text{ rad}$$



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Ans.

Ans.

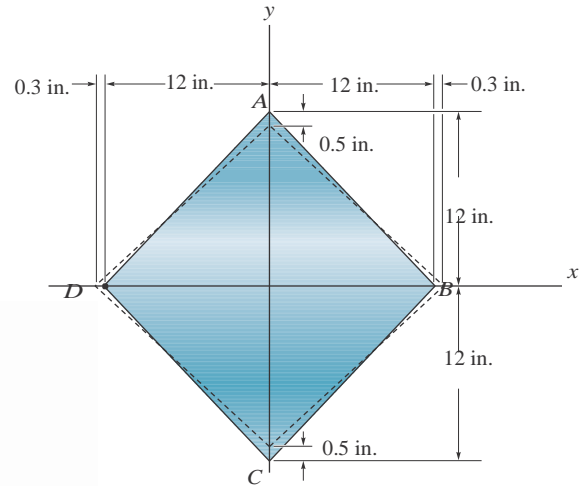
Ans:

$$g_A = 0$$

$$g_B = 0.199 \text{ rad}$$

2-26.

The corners of the square plate are given the displacements indicated. Determine the shear strain at A relative to axes that are directed along AB and AD , and the shear strain at B relative to axes that are directed along BC and BA .



Solution

Geometry: Referring to the geometry shown in Fig. a ,

$$\tan \frac{u}{2} = \frac{12.3}{11.5} \quad u = (93.85) a \frac{P}{180} \text{ rad} = 1.6380 \text{ rad}$$

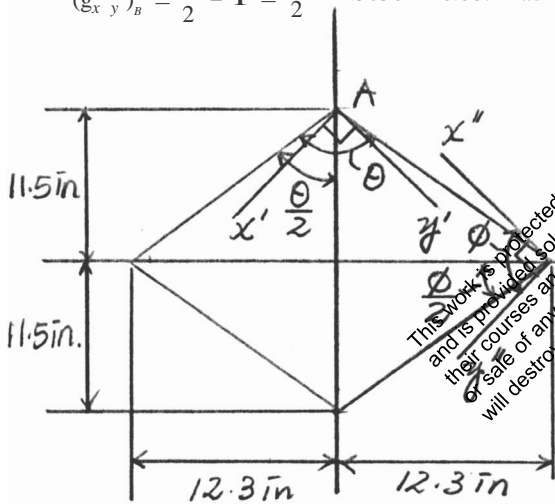
$$\tan \frac{f}{2} = \frac{11.5}{12.3} \quad f = (86.15) a \frac{P}{180} \text{ rad} = 1.5036 \text{ rad}$$

Shear Strain: By definition,

$$(g_{x y})_A = \frac{P}{2} - u = \frac{P}{2} - 1.6380 = -0.0672 \text{ rad}$$

$$(g_{x y})_B = \frac{P}{2} - f = \frac{P}{2} - 1.5036 = 0.0672 \text{ rad}$$

Ans.



(a)

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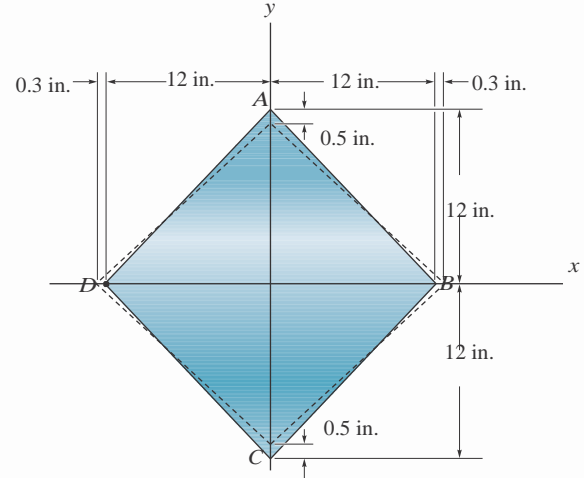
Ans:

$$(g_{x-y})_A = -0.0672 \text{ rad}$$

$$(g_{x-y})_B = 0.0672 \text{ rad}$$

2-27.

The corners of the square plate are given the displacements indicated. Determine the average normal strains along side AB and diagonals AC and BD .



Solution

Geometry: Referring to the geometry shown in Fig. a,

$$L_{AB} = 2(12)^2 + 12^2 = 12\sqrt{2} \text{ in.}$$

$$L_{A'B'} = 2(12.3)^2 + 11.5^2 = 2283.54 \text{ in.}$$

$$L_{BD} = 2(12) = 24 \text{ in.}$$

$$L_{B'D'} = 2(12 + 0.3) = 24.6 \text{ in.}$$

$$L_{AC} = 2(12) = 24 \text{ in.}$$

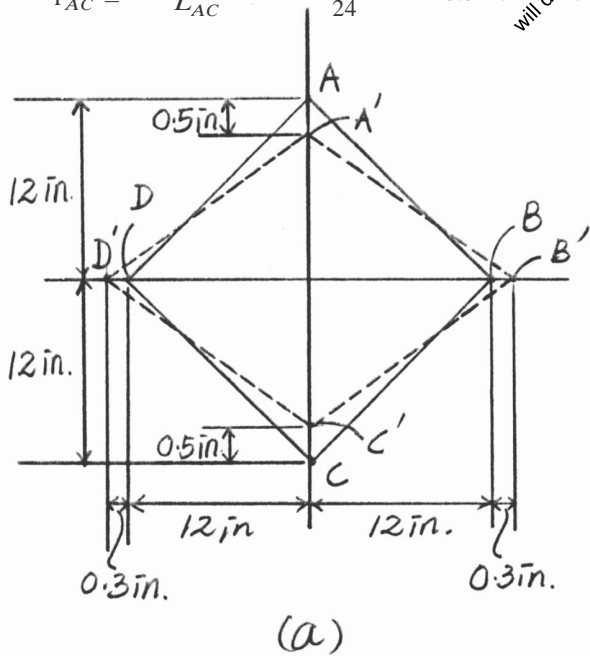
$$L_{A'C'} = 2(12 - 0.5) = 23 \text{ in.}$$

Average Normal Strain:

$$P_{AB} = \frac{L_{A'B'} - L_{AB}}{L_{AB}} = \frac{2283.54 - 12\sqrt{2}}{12\sqrt{2}} = -0.00501 \text{ in/in.} \quad \text{Ans.}$$

$$P_{BD} = \frac{L_{B'D'} - L_{BD}}{L_{BD}} = \frac{24.6 - 24}{24} = 0.025 \text{ in/in.} \quad \text{Ans.}$$

$$P_{AC} = \frac{L_{A'C'} - L_{AC}}{L_{AC}} = \frac{23 - 24}{24} = -0.0417 \text{ in/in.} \quad \text{Ans.}$$



Ans:

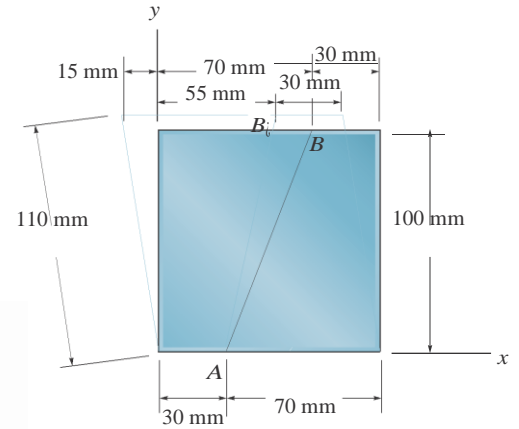
$$P_{AB} = -7.77(10^{-3}) \text{ in.} > \text{in.}$$

$$P_{BD} = 0.025 \text{ in.} > \text{in.}$$

$$P_{AC} = -0.0417 \text{ in.} > \text{in.}$$

*2-28.

The block is deformed into the position shown by the dashed lines. Determine the average normal strain along line AB .



Solution

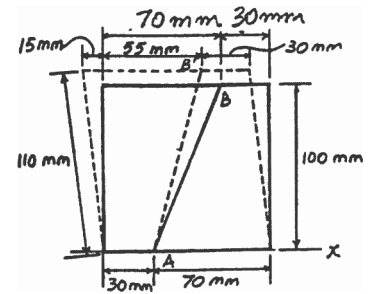
Geometry:

$$AB = \sqrt{100^2 + (70 - 30)^2} = 107.7033 \text{ mm}$$

$$AB = \sqrt{(70 - 30 - 15)^2 + (110^2 - 15^2)} = 111.8034 \text{ mm}$$

Average Normal Strain:

$$\begin{aligned} \epsilon_{AB} &= \frac{AB - AB}{AB} \\ &= \frac{111.8034 - 107.7033}{107.7033} \\ &= 0.0381 \text{ mm/mm} = 38.1 (10^{-3}) \text{ mm} \end{aligned}$$

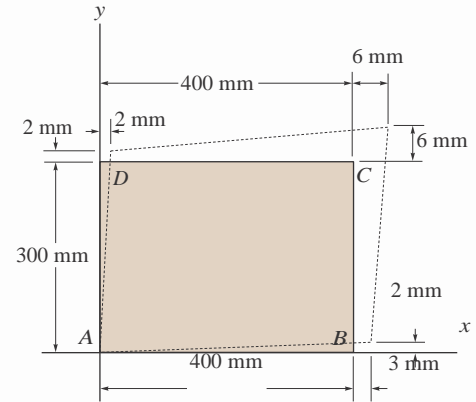


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Ans:
 $P_{AB} = 38.1 (10^{-3}) \text{ mm}$

2-29.

The rectangular plate is deformed into the shape shown by the dashed lines. Determine the average normal strain along diagonal AC, and the average shear strain at corner A relative to the x, y axes.



Solution

Geometry: The unstretched length of diagonal AC is

$$L_{AC} = \sqrt{300^2 + 400^2} = 500 \text{ mm}$$

Referring to Fig. a, the stretched length of diagonal AC is

$$L_{AC} = \sqrt{(400 + 6)^2 + (300 + 6)^2} = 508.4014 \text{ mm}$$

Referring to Fig. a and using small angle analysis,

$$f = \frac{2}{300 + 2} = 0.006623 \text{ rad}$$

$$a = \frac{2}{400 + 3} = 0.004963 \text{ rad}$$

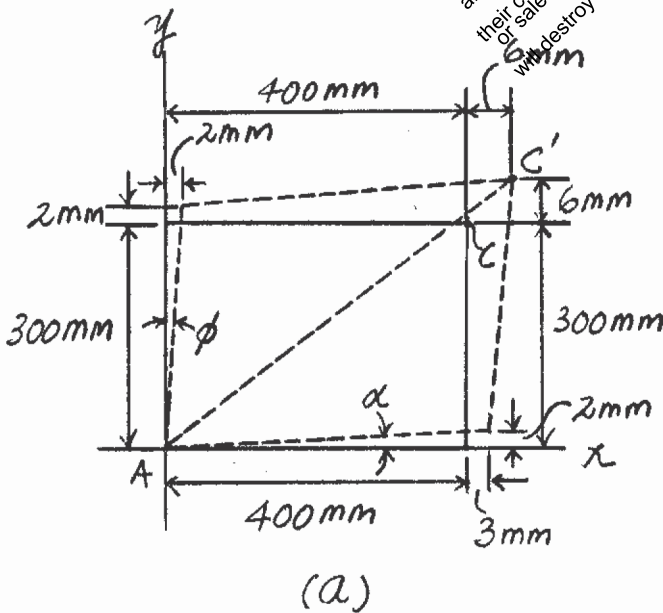
Average Normal Strain: Applying Eq. 2,

$$(P_{avg})_{AC} = \frac{L_{AC} - L_{AC}}{L_{AC}} = \frac{508.4014 - 500}{500} = 0.0168 \text{ mm/mm} \quad \text{Ans.}$$

Shear Strain: Referring to Fig. a,

$$(g_A)_{xy} = f + a = 0.006623 + 0.004963 = 0.011586 \text{ rad} \quad \text{Ans.}$$

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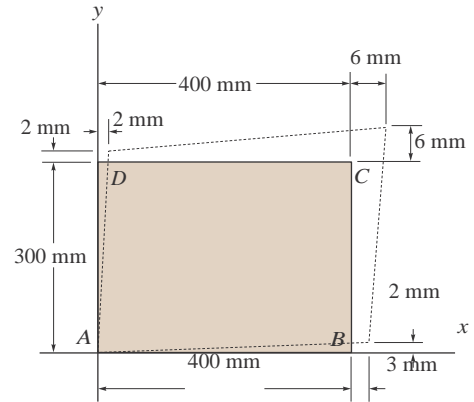


Ans:

$$(P_{\text{avg}})_{AC} = 0.0168 \text{ mm}^2/\text{mm}, (g_A)_{xy} = 0.0116 \text{ rad}$$

2-30.

The rectangular plate is deformed into the shape shown by the dashed lines. Determine the average normal strain along diagonal BD , and the average shear strain at corner B relative to the x, y axes.



Solution

Geometry: The unstretched length of diagonal BD is

$$L_{BD} = \sqrt{300^2 + 400^2} = 500 \text{ mm}$$

Referring to Fig. a , the stretched length of diagonal BD is

$$L_{BD} = \sqrt{(300 + 2 - 2)^2 + (400 + 3 - 2)^2} = 500.8004 \text{ mm}$$

Referring to Fig. a and using small angle analysis,

$$f = \frac{2}{403} = 0.004963 \text{ rad}$$

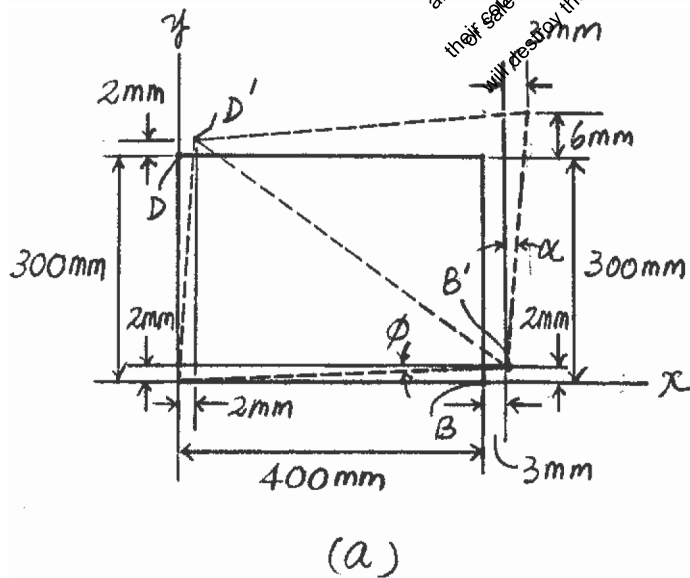
$$a = \frac{3}{300 + 6 - 2} = 0.009868 \text{ rad}$$

Average Normal Strain: Applying Eq. 2,

$$(P_{\text{avg}})_{BD} = \frac{L_{BD} - L_{BD}}{L_{BD}} = \frac{500.8004 - 500}{500} = 1.60(10^{-3}) \text{ mm/mm} \quad \text{Ans.}$$

Shear Strain: Referring to Fig. a ,

$$(\gamma_B)_{xy} = f + a = 0.004963 + 0.009868 = 0.014831 \text{ rad} \quad \text{Ans.}$$

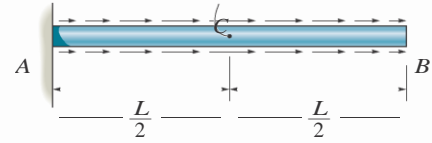


Ans:
 $(P_{\text{avg}})_{BD} = 1.60(10^{-3}) \text{ mm/mm}$,

$$(g_B)_{xy} = 0.0148 \text{ rad}$$

2-31.

The nonuniform loading causes a normal strain in the shaft that can be expressed as $P_x = k \sin a \frac{P}{L} x b$, where k is a constant. Determine the displacement of the center C and the average normal strain in the entire rod.



Solution

$$P_x = k \sin a \frac{P}{L} x b$$

$$\begin{aligned} (\delta x)_C &= \int_0^L P_x dx = \int_0^L k \sin a \frac{P}{L} x b dx \\ &= \frac{-k a}{P} b \cos a \frac{P}{L} x b \Big|_0^L = \frac{-k a}{P} b (\cos P - \cos 0) = \frac{2kL}{P} \end{aligned}$$

Ans.

$$\begin{aligned} (\delta x)_B &= \int_0^L k \sin a \frac{P}{L} x b dx \\ &= \frac{-k a}{P} b \cos a \frac{P}{L} x b \Big|_0^L = \frac{-k a}{P} b (\cos P - \cos 0) = \frac{2kL}{P} \end{aligned}$$

$$P_{avg} = \frac{(\delta x)_B}{L} = \frac{2k}{P}$$

Ans.

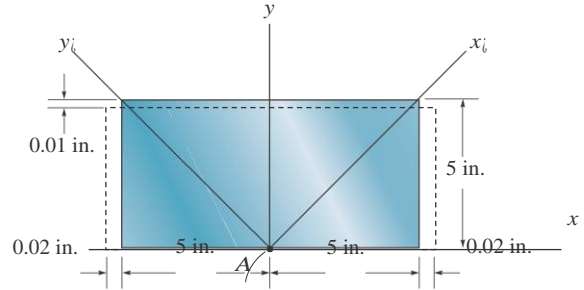
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Ans:

$$(x)_C = \frac{kL}{P}$$
$$P_{\text{avg}} = \frac{2k}{P}$$

*2-32.

The rectangular plate undergoes a deformation shown by the dashed lines. Determine the shear strain γ_{xy} and γ_{yx} at point A.



Solution

Since the right angle of an element along the x,y axes does not distort, then

$$\gamma_{xy} = 0$$

$$\tan u = \frac{5.02}{4.99}$$

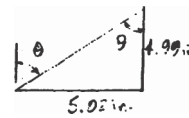
$$u = 45.17^\circ = 0.7884 \text{ rad}$$

$$\gamma_{x y} = \frac{P}{2} - 2u$$

$$= \frac{P}{2} - 2(0.7884)$$

$$= -0.00599 \text{ rad}$$

Ans.



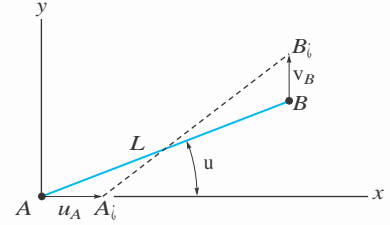
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Ans:

$$g_{xy} = 0$$
$$g_{x y} = -0.00599 \text{ rad}$$

2-33.

The fiber AB has a length L and orientation u . If its ends A and B undergo very small displacements u_A and v_B respectively, determine the normal strain in the fiber when it is in position $A_i B_i$.



Solution

Geometry:

$$L_{A_i B_i} = \sqrt{(L \cos u - u_A)^2 + (L \sin u + v_B)^2}$$

$$= \sqrt{L^2 + \frac{u_A^2}{2} + \frac{v_B^2}{2} + 2L(v_B \sin u - u_A \cos u)}$$

Average Normal Strain:

$$P_{AB} = \frac{L_{A_i B_i} - L}{L}$$

$$= \frac{\frac{u_A^2}{2} + \frac{v_B^2}{2} + 2L(v_B \sin u - u_A \cos u)}{L} - 1$$

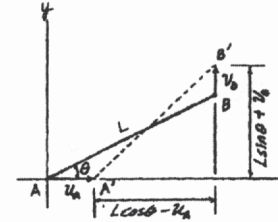
Neglecting higher terms u_A^2 and v_B^2 -

$$P_{AB} = 1 + \frac{2(v_B \sin u - u_A \cos u)}{L} - 1$$

Using the binomial theorem:

$$P_{AB} = 1 + \frac{1}{2} a \frac{2v_B \sin u}{L} - \frac{2u_A \cos u}{L} b + \dots - 1$$

$$= \frac{v_B \sin u}{L} - \frac{u_A \cos u}{L}$$



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Ans.

Ans:

$P_{AB} =$

$$\frac{y_B \sin u}{L}$$

$$\frac{u_A \cos u}{L}$$

2-34.

If the normal strain is defined in reference to the final length s , that is,

$$P = \lim_{s \rightarrow 0} a \frac{s - s_0}{s} b$$

instead of in reference to the original length, Eq. 2-2, show that the difference in these strains is represented as a second-order term, namely, $P - P^0 = PP^0$.

Solution

$$P = \frac{s - s_0}{s}$$

$$P - P^0 = \frac{s - s_0}{s} - \frac{s - s_0}{s_0}$$

$$= \frac{s^2 - s_0 s - s s_0 + s_0^2}{s s_0}$$

$$= \frac{s^2 + s_0^2 - 2 s s_0}{s s_0}$$

$$= \frac{(s - s_0)^2}{s s_0} = \epsilon \frac{s - s_0}{s} \leq \epsilon \frac{s - s_0}{s_0} \leq$$

$$= PP^0$$

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Ans:
N/A