# Prealgebra and Introductory Algebra 4th Edition Martin Gay 032195579X 9780321955791 Solution Manual <br> Full link download: <br> Test Bank: 

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## Solution Manual:

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## Chapter 2

## Section 2.1 Practice Exercises

1. a. If 0 represents the surface of the earth, then 3805 below the surface of the earth is -3805 .
b. If zero degrees Fahrenheit is represented by $0^{\circ} \mathrm{F}$, then 85 degrees below zero Fahrenheit is represented by $-85^{\circ} \mathrm{F}$.
2. 


3. a. $0>-5$ since 0 is to the right of -5 on a number line.
b. $-3<3$ since -3 is to the left of 3 on a number line.
c. $\quad-7>-12$ since -7 is to the right of -12 on a number line.
4. a. $|-6|=6$ because -6 is 6 units from 0 .
b. $\quad|4|=4$ because 4 is 4 units from 0 .
c. $|-12|=12$ because -12 is 12 units from 0 .
5. a. The opposite of 14 is -14 .
b. The opposite of -9 is $-(-9)$ or 9 .
6. a. $-|-7|=-7$
b. $\quad-|4|=-4$
c. $-(-12)=12$
7. $-|x|=-|-6|=-6$
8. The planet with the highest average daytime surface temperature is the one that corresponds to the bar that extends the furthest in the positive direction (upward). Venus has the highest average daytime surface temperature.

## Vocabulary, Readiness \& Video Check 2.1

1. The numbers $\ldots-3,-2,-1,0,1,2,3, \ldots$ are called integers.
2. Positive numbers, negative numbers, and zero together are called signed numbers.
3. The symbols "<" and " $>$ " are called inequality symbols.
4. Numbers greater than 0 are called positive numbers while numbers less than 0 are called negative numbers.
5. The sign " $<$ " means is less than and " $>$ " means is greater than.
6. On a number line, the greater number is to the right of the lesser number.
7. A number's distance from 0 on the number line is the number's absolute value.
8. The numbers -5 and 5 are called opposites.
9. number of feet a miner works underground
10. The tick marks are labeled with the integers.
11. 0 will always be greater than any of the negative integers.
12. $8 ;|8|=8$ also.
13. A negative sign can be translated into the phrase "opposite of."
14. Eyre

## Exercise Set 2.1

2. If 0 represents the surface of the water, then 25 feet below the surface of the water is -25 .
3. If 0 represents sea level, then 282 feet below sea level is -282 .
4. If 0 represents 0 degrees Fahrenheit, then 134 degrees above zero is +134 .
5. If 0 represents the surface of the ocean, then 14,040 below the surface of the ocean is $-14,040$.
6. If 0 represents a loss of $\$ 0$, then a loss of $\$ 555$ million is -555 million.
7. If 0 represents $0^{\circ}$ Celsius, then $10^{\circ}$ below $0^{\circ}$ Celsius is -10 . Since $5^{\circ}$ below $0^{\circ}$ Celsius is -5 and -10 is less than $-5,-10$ (or $10^{\circ}$ below $0^{\circ}$ Celsius) is cooler.
8. If 0 represents a decrease of $0 \%$, then a 23 percent decrease is -23 .
9. 


18.

20.

22.

24. $-8<0$ since -8 is to the left of 0 on a number line.
26. $-12<-10$ since -12 is to the left of -10 on a number line.
28. $-27>-29$ since -27 is to the right of -29 on a number line.
30. $13>-13$ since 13 is to the right of -13 on a number line.
32. $|7|=7$ since 7 is 7 units from 0 on a number line.
34. $|-19|=19$ since -19 is 19 units from 0 on a number line.
36. $|100|=100$ since 100 is 100 units from 0 on a number line.

38. $|-10|=10$ since -10 is 10 units from 0 on a number line.
40. The opposite of 8 is negative 8 .

$$
\begin{gathered}
-(8)= \\
-8
\end{gathered}
$$

42. The opposite of negative 6 is 6 .

$$
-(-6)=
$$

6
44. The opposite of 123 is negative 123 . $-(123)=-123$
46. The opposite of negative 13 is 13 .
$-(-13)=13$
48. $|-11|=11$
50. $-|43|=-43$
52. $-|-18|=-18$
54. $-(-27)=27$
56. $-(-14)=14$
58. $-|-29|=-29$
60. $-|x|=-|-8|=-8$
62. $-|-x|=-|-10|=-10$
64. $|x|=|32|=32$
66. $|-x|=|-1|=1$
68. $-4>-17$ since -4 is to the right of -17 on a number line.
70. $|-8|=8$
$|-4|=4$
Since $8>4,|-8|>$
$|-4|$.
72. $-|17|=-17$
$-(-17)=17$
Since $-17<17,-|17|<$
$-(-17)$.
74. $|-24|=24$
$-(-24)=24$
Since $24=24,|-24|=-(-24)$.
80. $-|-8|=-8$
$-|-4|=-4$
Since $-8<-4,-|-8|<-|-4|$.
82. $-(-38)=38$

Since $-22<38,-22<-(-38)$.
84. If the number is -13 , then the absolute value of -13 is 13 and the opposite of -13 is 13 .
86. If the opposite of a number is 90 , then the number is -90 and its absolute value is 90.
88. The 'bar' that is equal to 0 corresponds to Lake Maracaibo, so Lake Maracaibo has an elevation at sea level.
90. The bar that extends second to the farthest in the negative direction corresponds to Lake Eyre, so Lake Eyre has the second lowest elevation.
92. The smallest number on the graph is $-269^{\circ} \mathrm{C}$, which corresponds to helium.
94. The number on the graph closest to $+300^{\circ} \mathrm{C}$ is $280^{\circ} \mathrm{C}$, which corresponds to phosphorus.
96. $9+0=9$
98. 20
$\begin{array}{r}+15 \\ \hline 35\end{array}$

1
100. 362

37
$\begin{array}{r}+\quad 90 \\ \hline\end{array}$
489
102. $|10|=10,2^{3}=8,-|-5|=-5$, and $-(-4)=$ 4 , so the numbers in order from least to greatest are

$$
-|-5|,-(-4), 2^{3},|10|
$$

$7 \quad .-45<0$ since -45 is to the left of 0 on 6 a number line.

78. $|-45|=45$
$|0|=0$
Since $45>0,|-45|>|0|$.
104. $1^{4}=1,-(-3)=3,-|7|=-7$, and $|-20|=$ 20 , so the numbers in order from least to greatest are

$$
-|7|, 1^{4},-(-3),|-20| .
$$

106. 

$3^{3}=27,-|-11|=-11,-(-10)=10,-4=$ -4 ,
$-|2|=-2$, so the numbers in order from least to greatest are $-|-11|,-4,-|2|,-(-10)$, and $3^{3}$.
108. a. $|0|=0$; since $0<4$, then $|0|>4$ is false.

$$
2+(-18)=-16
$$

b. $|-4|=4$; since $4=4$, then $|-4|>4$ is false.
c. $|5|=5$; since $5>4$, then $|5|>4$ is true.
d. $|-100|=100$; since $100>4$, then $|-100|>$ 4 is true.
110. $(-|-(-7)|)=(-|7|)=-7$
112. False; consider 0 , where $|0|=0$ and 0 is not positive.
114. True; zero is always less than a positive number since it is to the left of it on a number line.
116. No; $b>a$ because $b$ is to the right of $a$ on the number line.
118. answers may vary
120. no; answers may vary

## Section 2.2 Practice Exercises


2.

3.

4. $|-3|+|-19|=3+19=22$

The common sign is negative, so
$(-3)+(-19)=-22$.
5. $-12+(-30)=-42$
6. $9+4=13$
7. $|-1|=1,|26|=26$, and $26-1=25$
$26>1$, so the answer is positive.
$-1+26=25$
8. $|2|=2,|-18|=18$, and $18-2=16$ $18>2$, so the answer is negative.

9. $-54+20=-34$
10. $7+(-2)=5$
11. $-3+0=-3$
12. $18+(-18)=0$
13. $-64+64=0$
14. $6+(-2)+(-15)=4+(-15)=-11$
15. $5+(-3)+12+(-14)=2+12+(-14)$

$$
=14+(-14)
$$

$=$
0
16. $x+3 y=-6+3(2)=-6+6=0$
17. $x+y=-13+(-9)=-22$
18. Temperature at 8 a.m. $=-7+(+4)+(+7)$
$=-3+(+7)$
=
4
The temperature was $4^{\circ} \mathrm{F}$ at 8 a.m.

## Calculator

Explorations

1. $-256+97=-159$
2. $811+(-1058)=-247$
3. $6(15)+(-46)=44$
4. $-129+10(48)=351$
5. $-108,650+(-786,205)=-894,855$
6. $-196,662+(-129,856)=-326,518$

## Vocabulary, Readiness \& Video Check

 2.21. If $n$ is a number, then $-n+n=\underline{0}$.
2. Since $x+n=n+x$, we say that addition is commutative.
3. If $a$ is a number, then $-(-a)=\underline{a}$.
4. Since $n+(x+a)=(n+x)+a$, we say that addition is associative.
5. Negative; the numbers have different signs and the sign of the sum is the same as the sign of the number with the larger absolute value, -6 .
6. Negative; the numbers have the same sign-both are negative-and we keep this common sign in the sum.
7. The diver's current depth is 231 feet below the surface.

## Exercise Set 2.2

2. 



$$
-6+(-5)=-11
$$

4. 


$10+(-3)=7$
6.

$9+(-4)=5$
8. $15+42=57$
10. $|-5|+|-4|=5+4=9$

The common sign is negative, so $-5+(-4)=-9$.
12. $-62+62=0$
14. $|8|-|-3|=8-3=5$
$8>3$, so the answer is positive.
$8+(-3)=5$
16. $-8+0=-8$
18. $|-9|-|5|=9-5=4$
$9>5$, so the answer is negative.
$5+(-9)=-4$
20. $|-6|+|-1|=6+1=7$

The common sign is negative, so $-6+(-1)=-7$.
22. $|-23|+|-23|=23+23=46$

The common sign is negative, so $-23+(-23)=-46$.
24. $|-400|+|-256|=400+256=656$

The common sign is negative, so $-400+(-256)=-656$.
26. $|24|-|-10|=24-10=14$
$24>10$, so the answer is positive.
$24+(-10)=14$
28. $|-8|-|4|=8-4=4$
$8>4$, so the answer is negative.
$-8+4=-4$
30. $|-89|-|37|=89-37=52$
$89>37$, so the answer is negative.
$-89+37=-52$
32. $|62|-|-32|=62-32=30$
$62>32$, so the answer is positive.
$-32+62=30$
34. $|-375|-|325|=375-325=50$ $375>325$, so the answer is negative. $325+(-375)=-50$
36. $|-56|+|-33|=56+33=89$

The common sign is negative, so $-56+(-33)=-89$.
38. $-1+5+(-8)=4+(-8)=-4$
40. $-103+(-32)+(-27)=-135+(-27)=$ $-162$
42. $18+(-9)+5+(-2)=9+5+(-2)$

$$
\begin{aligned}
& =14+(-2) \\
& =12
\end{aligned}
$$

44. $34+(-12)+(-11)+213=22+(-11)+213$

$$
\begin{aligned}
& =11+213 \\
& =224
\end{aligned}
$$

46. $-12+(-3)+(-5)=-15+(-5)=-20$
47. $-35+(-12)=-47$
48. $3+(-23)+6=-20+6=-14$
49. $-100+70=-30$
50. $(-45)+22+20=-23+20=-3$
51. $-87+0=-87$
52. $-16+6+(-14)+(-20)=-10+(-14)+$ (-20)

$$
\begin{aligned}
& =-24+(-20) \\
& = \\
& -44
\end{aligned}
$$

60. $x+y=-1+(-29)=-30$
61. The sum of $-49,-2$, and 40 is $-49+(-2)+40=-51+40=-11$.
62. $0+(-248)+8+(-16)+(-28)+32$
$=-248+8+(-16)+(-28)+32$
$=-240+(-16)+(-28)+32$
$=-256+(-28)+32$
$=-284+32$
$=-252$
The diver's final depth is 252 meters below the surface.
63. Since $-7<-2$, Dufner won Round 2 .
64. The bar for 2001 has a height of -25 , so the net income in 2001 was $-\$ 25,000,000$.
65. $3496+8240+25,922=37,658$ The total net income for the years 2007, 2009, and 2011 was $\$ 37,658,000,000$.
66. $14+(-5)+(-8)+7=9+(-8)+7=1+7=8$ Her total score was 8 .
67. $-10,412+(-1786)+15,395+31,418$
$=-12,198+15,395+31,418$
$=3197+31,418$
$=34,615$
The net income for all the years shown is $\$ 34,615$.
68. $-45+3=-42$

Pennsylvania's all-time record low temperature is $-42^{\circ} \mathrm{F}$.
84. $-10,924+3245=-7679$

The depth of the Aleutian Trench is -7679 meters.
86. $91-0=91$
88. 400
$\frac{-18}{-382}$
90. answers may vary
92. $-4+14=10$
62. $3 x+y=3(7)+(-11)=21+(-11)=10$

64. $3 x+y=3(13)+(-17)=39+(-17)=$ 22
66. The sum of -30 and 15 is $-30+15=$ -15 .
94. $-15+(-17)=-32$
96. True
98. True
100. answers may vary
5. additive inverse

## Section 2.3 Practice Exercises

1. $13-4=13+(-4)=9$
2. $-8-2=-8+(-2)=-10$
3. $11-(-15)=11+15=26$
4. $-9-(-1)=-9+1=-8$
5. $6-9=6+(-9)=-3$
6. $-14-5=-14+(-5)=-19$
7. $-3-(-4)=-3+4=1$
8. $-15-6=-15+(-6)=-21$
9. $-6-5-2-(-3)=-6+(-5)+(-2)+3$
$=-11+(-2)+3$
$=-13+$
3
=
$-10$
10. $8+(-2)-9-(-7)=8+(-2)+(-9)+7$

$$
\begin{aligned}
& =6+(-9)+7 \\
& =-3+7 \\
& =4
\end{aligned}
$$

11. $x-y=-5-13=-5+(-13)=-18$
12. $3 y-z=3(9)-(-4)=27+4=31$
13. $29,028-(-1312)=29,028+1312=$ 30,340
Mount Everest is 30,340 feet higher than the Dead Sea.

## Vocabulary, Readiness \& Video Check 2.3

1. It is true that $a-b=\underline{a+(-b)}$. b
2. The opposite of $n$ is $-n$. a
3. To evaluate $x-y$ for $x=-10$ and $y=-14$, we replace $x$ with -10 and $y$ with -14 and evaluate $-10-(-14)$. d
4. The expression $-5-10$ equals $-5+(-10)$. c

## 

7. to follow the order of operations
8. The warmest temperature is $265^{\circ} \mathrm{F}$ warmer than the coldest temperature.

## Exercise Set 2.3

2. $-6-(-6)=-6+$ $6=0$
3. $-12-(-5)=-12+5=-7$
4. $16-45=16+(-45)=-29$
5. $-22-10=-22+(-10)=-32$
6. $-8-(-13)=-8+13=5$
7. $-50-(-50)=-50+50=0$
8. $15-12=15+(-12)$

$$
=3
$$

6. $2-5=2+(-5)=-3$
7. $12-(-12)=12+12=$ 24
8. $-25-(-25)=-25+25=0$
9. $-2-42=-2+(-42)=-44$
10. $8-9=8+(-9)=-1$
11. $17-63=17+(-63)=-46$
12. $844-(-20)=844+20=864$
13. $-5-8=-5+(-8)=-13$
14. $-3+4+(23)+(-10)$; all the subtraction operations are rewritten as additions in one step rather than changing one operation at a time as you work from left to right.
15. $23-(-17)+(-9)=23+17+$ $(-9)$

$$
\begin{aligned}
& =40+(-9) \\
& =31
\end{aligned}
$$

50. $-(-9)-14+(-23)=9+(-14)+(-23)$

$$
\begin{aligned}
& =-5+ \\
& (-23) \\
& =
\end{aligned}
$$

52. 

$$
-28
$$

$$
\begin{gathered}
-6-(-8)+(-12)-7=-6+8+(-12) \\
+(-7) \\
=2+(-12)+(-7) \\
=-10+(-7) \\
= \\
-17
\end{gathered}
$$

54. $5+(-18)-(-21)-2=5+(-18)+21+$ (-2)

$$
\begin{aligned}
& =-13+21+(-2) \\
& =8+(-2) \\
& =6
\end{aligned}
$$

56. $x-y=-7-1=-7+(-1)=-8$
57. $x-y=9-(-2)=9+2=11$
58. $2 x-y=2(8)-(-10)=16+10=26$
59. $2 x-y=2(14)-(-12)=28+12=40$
60. The temperature in November is $3^{\circ} \mathrm{F}$ and in December is $-4^{\circ} \mathrm{F}$.
$3-(-4)=3+4=7$
The difference is $7^{\circ} \mathrm{F}$.
61. The month with the warmest temperature is July, $63^{\circ} \mathrm{F}$, and the month with the coldest temperature is January, $-8^{\circ} \mathrm{F}$.
$63-(-8)=63+8=71$
The difference is $71^{\circ} \mathrm{F}$.
62. $134-(-80)=134+80=214$

Therefore, $134^{\circ} \mathrm{F}$ is $214^{\circ} \mathrm{F}$ warmer than $-80^{\circ} \mathrm{F}$.
70. $93-18-26=93+(-18)+(-26)$

$$
\begin{aligned}
& =75+(-26) \\
& =49
\end{aligned}
$$

She owes $\$ 49$ on her account.
78. $512-(-92)=512+92=604$ The difference in elevation is 604 feet.
80. $-52-(-92)=-52+92=40$

The difference in elevation is 40 feet.
82. $845-(-162)=845+162=1007$ The difference in temperature is $1007^{\circ} \mathrm{F}$.
84. $1165-3878=1165+(-3878)=-2713$ The trade balance was -2713 million barrels.
86. The difference of -3 and a number is $-3-x$.
88. Add a number and -36 is $x+(-36)$.
90. $\frac{96}{3}=32$
72. $13,796-(-21,857)=13,796+21,857=$ 35,653

The difference in elevation is 35,653 feet.
74. $-384-(-505)=-384+505=121$

The difference in elevation is 121 feet.
76. $-236-(-505)=-236+505=269$

The difference in elevation is 269 feet.

32
396
$\Gamma$
$\overline{\overline{9}}$
06
$\overline{\bar{\sigma}}$
0
92. 51
$\times 89$
459
4080
4539
94. answers may vary
96. $-4-8=-4+(-8)=-12$
98. $-3-(-10)=-3+10=7$
100. $|-12|-|-5|=12-5=12+(-5)=7$
102. $|-8|-|8|=8-8=0$
104. $|-23|-|-42|=23-42=23+(-42)=-19$
106. $|-2-(-6)|=|-2+6|=|4|=4$
$|-2|-|-6|=2-6=2+(-6)=-4$
Since $4 \neq-4$, the statement is false.
108. no; answers may vary

## Section 2.4 Practice Exercises

1. $-3 \cdot 8=$
$-24$
2. $-5(-2)=$

10
3. $0 \cdot(-20)=0$
4. $10(-5)=-50$
5. $8(-6)(-2)=-48(-2)=96$
6. $(-9)(-2)(-1)=18(-1)=-18$
7. $(-3)(-4)(-5)(-1)=12(-5)(-1)=$ $-60(-1)=60$
8. $(-2)^{4}=(-2)(-2)(-2)(-2)$

$$
\begin{aligned}
& =4(-2)(-2) \\
& =-8(-2) \\
& =16
\end{aligned}
$$

9. $-8^{2}=-(8 \cdot 8)=-64$
10. $\frac{42}{\overline{7}}=-6$
11. $-16 \div(-2)=$

8
12. $\frac{-80}{10}=-8$
13. -6 is
$\underset{0}{\text { undefined. }}$
14. $\frac{0}{\overline{7}}=0$
15. $x y=5 \cdot(-8)=$ $-40$
16. $\underline{x}=\frac{-12}{}=4$
$y \quad-3$
17. total score $=4 \cdot(-13)=-52$

The card player's total score was -52 .

## Vocabulary, Readiness \& Video Check 2.4

1. The product of a negative number and a positive number is a negative number.
2. The product of a negative number and zero is $\underline{0}$.
3. The quotient of 0 and a negative number is $\underline{0}$.
4. The quotient of a negative number and 0 is undefined.
5. When a negative sign is involved in an expression with an exponent, parentheses tell you whether or not the exponent applies to the negative sign. In Example 3, $(-3)^{2}$, the exponent applies to everything within the parentheses, so -3 is squared; in Example 4, $-3^{2}$, the exponent does not apply to the sign and only 3 is squared.
6. We can find out about sign rules for division because we know sign rules for multiplication.
7. That $a b$ means $a \cdot b$.
8. The phrase "lost four yards" in the example translates to the negative number -4 .

## Exercise Set 2.4

2. $5(-3)=-15$
3. $-7(-2)=14$
4. $-9(7)=-63$
5. $-6(0)=0$
6. $-2(3)(-7)=-6(-7)=42$
7. $-8(-3)(-3)=24(-3)=-72$
8. $2(-5)(-4)=-10(-4)=40$
9. $3(0)(-4)(-8)=0$
10. $-2(-1)(3)(-2)=2(3)(-2)=6(-2)=-12$
11. The product of two negative numbers is a positive number.

12. The quotient of two negative numbers is a positive number.
13. The quotient of a negative number and a positive number is a negative number.
14. $-2^{4}=-(2)(2)(2)(2)=-4(2)(2)=-8(2)=-16$
15. $(-1)^{4}=(-1)(-1)(-1)(-1)$

$$
=1(-1)(-1)
$$

$=-1(-1)$
$=1$
24. $-4^{3}=-(4 \cdot 4 \cdot 4)=$ $-64$
26. $(-3)^{2}=(-3)(-3)$
$=9$
66. $480 \div(-8)=\frac{480}{-8}=-60$
28. $90 \div(-9)=$ $-10$
68. $\frac{-36}{-3}=12$
30. $\frac{56}{-}=-7$
70. $-2^{3}=-(2 \cdot 2 \cdot 2)=-8$
32. $-32=$
$-8$
72. $(-11)^{2}=(-11)(-11)=121$
34. $\frac{-1}{\underline{3}}$ is undefined.

0
36. $\frac{0}{-1}=0$
38. $-24=$
$\stackrel{2}{-12}$
40. $0(-100)=0$
42. $-6 \cdot 2=-12$
44. $-12(13)=-156$
46. $-9(-5)=45$
48. $-7(-5)(-3)=35(-3)=$ $-105$
50. $(-5)^{2}=(-5)(-5)=$ 25
84. $a b=5(-1)=-5$
52.

$$
-\frac{30}{5}=-6
$$

86. $a b=(-8)(8)=-64$
87. $a b=(-9)(-6)=54$
88. 

$-\frac{49}{}=-7$
7
56. $-15 \div 3=-5$

## 

90. 
91. 

$$
(-3)
$$

60. $-20 \cdot 5 \cdot(-5) \cdot(-3)=-100 \cdot(-5)$

$$
\begin{aligned}
& =500 \cdot(-3) \\
= & -1500
\end{aligned}
$$

62. $-\frac{0}{-}=0$
$-1$
4
63. $\underline{63}=-7$
$\overline{9}$
$x$
$=$
9
$=$

- 

3
$\frac{y}{3}$
$\underline{x}$
$\overline{\overline{0}}$
$\underline{0}$
$=$
0

$$
y \quad-5
$$

$$
\underline{x} \quad-10
$$

$$
\text { 94. } y=-10=1
$$

96. $x y=20 \cdot(-5)=-100$
$\begin{aligned} & x \\ & y\end{aligned}=\begin{aligned} & 20 \\ & -5\end{aligned}=-4$
97. $x y=-3 \cdot 0=0$
$\frac{x}{y}=\frac{-3}{0}$ is undefined.
98. $-63 \div(-3)=21$

The quotient of -63 and -3 is 21 .
102. 49
$\begin{array}{r} \\ \times \quad 5 \\ \hline\end{array}$
245
$-49(5)=-245$
The product of -49 and 5 is -245 .
104. The quotient of -8 and a number is $\frac{-8}{x}$ or $-8 \div x$.
106. The sum of a number and -12 is $x+(-12)$.
108. The difference of a number and -10 is $x-$ $(-10)$.
110. Multiply a number by -17 is $x \cdot(-17)$ or $-17 x$.
112. A loss of $\$ 400$ is represented by -400 .
$7 \cdot(-400)=-2800$
His total loss was $\$ 2800$.
114. A drop of 5 degrees is represented by -5 .
$6 \cdot(-5)=$
$-30$

The total drop in temperature was 30 degrees.
116. $-1 \cdot(-39)=39$

The melting point of rubidium is $39^{\circ} \mathrm{C}$.
118. $-11 \cdot(-70)=770$

The melting point of strontium is $770^{\circ} \mathrm{C}$.
120. $-30,000=$
$-10,000$
3
The expected loss for each month would be
b. This is a period of 25 years.


The average change was 15 California Condors per year.
124. $3 \cdot(7-4)+2 \cdot 5^{2}=3 \cdot 3+2 \cdot 5^{2}$

$$
=3 \cdot 3+2 \cdot 25
$$

$$
=9+2 \cdot 25
$$

$$
=9+50
$$

$$
=59
$$

126. $12 \div(4-2)+7=12 \div 2+7=6+7=13$
127. $-9(-11)=99$
128. $-4+(-3)+21=-7+21=14$
129. $-16-(-2)=-16+2=-14$
130. The product of an even number of negative numbers is positive, so the product of ten negative numbers is positive.
131. $(-1)^{50}$ and are positive since there are $(-7)^{20}$
an even number of factors. Note that $(-7)^{20}>(-1)^{50}$ since $(-1)^{50}=1$.
$(-1)^{55}$ and $(-7)^{23}$ are negative since there are an odd number of factors. Note that $(-7)^{23}<(-1)^{55}$ since $(-1)^{55}=-1$. $0^{15}=0$
The numbers from least to greatest are
$(-7)^{23}, \quad 0^{15},(-1)^{50},(-7)^{20}$. $(-1)^{55}$,


10,000 shipments or $-10,000$ shipments per month.
122. a. $405-30=375$

There were about 375 more California Condors in 2012 than in 1987. This is a change of 375 condors.
138. answers may vary

## Integrated Review

1. Let 0 represent $0^{\circ} \mathrm{F}$. Then 50 degrees below zero is represented by -50 and 122 degrees above zero is represented by +122 or 122 .
2. 


3. $0>-10$ since 0 is to the right of -10 on a number line.
4. $-4<4$ since -4 is to the left of 4 on a number line.
5. $-15<-5$ since -15 is to the left of -5 on a number line.
6. $-2>-7$ since -2 is to the right of -7 on a number line.
7. $|-3|=3$ because -3 is 3 units from 0 .
8. $|-9|=9$ because -9 is 9 units from
0.
9. $-|-4|=-4$
10. $-(-5)=5$
11. The opposite of 11 is -11 .
12. The opposite of -3 is $-(-3)=3$.
13. The opposite of 64 is -64 .
14. The opposite of 0 is $-0=$
0.
15. $-3+15=$

12
16. $-9+(-11)=-20$
17. $-8(-6)(-1)=48(-1)=-48$
18. $-18 \div 2=-9$
19. $65+(-55)=10$
20. $1000-1002=1000+(-1002)=$ -2
21. $53-(-53)=53+53=106$
22. $-2-1=-2+(-1)=-3$
23. $\frac{0}{7^{4}}=0$
29. $-12-6-(-6)=-12+(-6)+6=-18+6=$ $-12$
30. $-4+(-8)-16-(-9)=-4+(-8)+(-16)+$

$$
=-12+(-16)+9
$$

$$
=-28+
$$

$$
9
$$

31. 

$$
-19
$$

$\frac{-105}{0}$ is undefined.
32. $7(-16)(0)(-3)=0($ since one factor is 0$)$
33. Subtract -8 from -12 is $-12-(-8)=-12+8=-4$.
34. The sum of -17 and -27 is $-17+(-27)=$ -44 .
35. The product of -5 and -25 is $-5(-25)=125$.
36. The quotient of -100 and $-5 \frac{-100}{-5}=20$.
$\begin{array}{ll}\text { 37. Divide a number by }-17 & \frac{x}{-1} \\ \text { is } & \text { or } x \div(-17) \text {. } \\ \frac{7}{7}\end{array}$
38. The sum of -3 and a number is $-3+x$.
39. A number decreased by -18 is $x-(-18)$.
40. The product of -7 and a number is $-7 \cdot x$ or $-7 x$.
41. $x+y=-3+12=9$
42. $x-y=-3-12=-3+(-12)=-15$
43. $2 y-x=2(12)-(-3)=24-(-3)=24+3=$ 27
44. $3 y+x=3(12)+(-3)=36+(-3)=33$
45. $5 x=5(-3)=-15$
46. $\underline{y}=\underline{12}=-4$

24. $-\frac{36}{=}$
$x \quad-3$
4
$-9$
25. $-17-(-59)=-17+59=$ 42
26. $-8+(-6)+20=-14+20$ $=6$
27. $-95=$
$\xrightarrow{19} 5$

## Section 2.5 Practice Exercises

1. $(-2)^{4}=(-2)(-2)(-2)(-2)=16$
2. $-2^{4}=-(2)(2)(2)(2)=-16$
3. $3 \cdot 6^{2}=3 \cdot(6 \cdot 6)=3 \cdot 36=108$
4. $-9(100)=-900$
5. $-25=\frac{-25}{}=$

5

$$
\begin{aligned}
& 5(-1) \\
& -5
\end{aligned}
$$

5. $\frac{-18+6}{-3-1}=\frac{-12}{-4}=3$
6. $30+50+(-4)^{3}=30+50+(-64)$

$$
\begin{aligned}
& =80+(-64) \\
& =16
\end{aligned}
$$

7. $-2^{3}+(-4)^{2}+1^{5}=-8+16+1=8+1=$ 9
8. $2(2-9)+(-12)-3=2(-7)+(-12)$ $-3$

$$
\begin{aligned}
& =-14+(-12)-3 \\
& =-26-3 \\
& =-29
\end{aligned}
$$

9. $(-5) \cdot-18+(-3)+2^{3}=(-5) \cdot 8+(-3)$ $+2^{3}$

$$
\begin{aligned}
& =(-5) \cdot 8+(-3)+ \\
& 8 \\
& =-40+(-3)+8 \\
& =-43+8 \\
& =-35
\end{aligned}
$$

10. $-4[-6+5(-3+5)]-7=-4[-6+$ 5(2)] -7

$$
\frac{\overline{7}}{}-4[-6+10]-
$$

14. 

$$
\begin{aligned}
& =-4(4)-7 \\
& =-16-7 \\
& =-23
\end{aligned}
$$

$x^{2}=(-15)^{2}=(-15)(-15)=225$
$-x^{2}=-(-15)^{2}=-(-15)(-15)=-225$
12.
13.
11.
$5 y^{2}=5(4)^{2}=5(16)=80$
$5 y^{2}=5(-4)^{2}=5(16)=80$
$x^{2}+y=(-6)^{2}+(-3)=36+(-3)=33$

4. To simplify $5[-9+(-3)] \div 4$,

4-
$x^{2}=$
4-
(-8)
${ }^{2}=4$

- 64
$=$
which operation
should be performed first?
addition

5. To simplify $-2+3(10-12)$. $(-8)$, which operation should be performed first? subtraction
6. To evaluate $x-3 y$ for $x=-7$ and $y=-1$, replace $x$ with -7 and $y$ with -1 and evaluate $-7-3(-1)$.
7. A fraction bar means divided by and it is a grouping symbol.
8. To make sure that the entire value of -2 , including the sign, is squared.
9. Finding the average is a good application of both order of operations and adding and dividing integers.
10. average
$=\frac{\text { sum of numbers }}{\text { number of numbers }}$
$=\frac{17+(-1)+(-11)+(-13)+(-16)+(-13)}{}$
$\pm \underline{2}$
7

$$
\begin{aligned}
& =\frac{-35}{7} \\
& =-5
\end{aligned}
$$

The average of the temperatures is $-5^{\circ} \mathrm{F}$.
8. $10-23-12=-13-12=$
-25
10. $-8+4(3)=-8+12=4$
12. $7(-6)+3=-42+3=-39$
14. $-12+6 \div 3=-12+2=$ $-10$
16. $5+9 \cdot 4-20=5+36-20$

$$
\begin{aligned}
& =41-20 \\
& =21
\end{aligned}
$$

52. $\left(11-3^{2}\right)^{3}=(11-9)^{3}=2^{3}=8$
53. $\underline{20-15}=\frac{5}{}=-5$

$$
\begin{aligned}
& -1 \\
& -1
\end{aligned}
$$

20. $-88=\underline{88}=-8$

$$
\begin{aligned}
& -8-1 \\
& { }_{3}^{-8-1}
\end{aligned}
$$

22. $7(-4)-(-6)=-28+6=$ $-22$
23. $[9+(-2)]^{3}=[7]^{3}=$ 343
24. $7 \cdot 6-6 \cdot 5+(-10)=42-6 \cdot 5+$ (-10)

$$
\begin{aligned}
& =42-30+ \\
& (-10) \\
& =12+(-10) \\
& =2
\end{aligned}
$$

28. $7-(-5)^{2}=7-25=-18$
29. $\left|-3+7 \cdot 7^{2}=\right| 4 \cdot 7^{2}=4 \cdot 7^{2}=4 \cdot 49=$ 196
30. 

$10 \cdot 5^{3}+7=10 \cdot 125+7=1250+7=1257$
34.
$8^{2}-(5-2)^{4}=8^{2}-3^{4}=64-81=$ $-17$
36. $|12-19| \div 7=|-7| \div 7=7 \div 7=$
46. $3 \cdot(8-3)+(-4)-10=3 \cdot(5)+(-4)-10$

$$
\begin{aligned}
& =15+(-4)-10 \\
& \quad= \\
& 11-10 \\
& =1
\end{aligned}
$$

48. $(4-12) \cdot(8-17)=(-8) \cdot(-9)=72$
49. $(-4 \div 4)-(8 \div 8)=(-1)-(1)=-2$
50. $-3(4-8)^{2}+5(14-16)^{3}=-3(-4)^{2}+5(-2)^{3}$
51. $12-[7-(3-6)]+(2-3)^{3}$
$=12-[7-(-3)]+(2-3)^{3}$
$=12-(7+3)+(-1)^{3}$
$=12-10+(-1)$
$=2+(-1)$
$=1$
52. $\frac{10(-1)-(-2)(-3)}{2[-8 \div(-2-2)]}=\frac{-10-6}{2[-8 \div(-4)]}$

$$
\begin{gathered}
=\frac{-16}{2(2)} \\
=\frac{-16}{4} \\
= \\
-4
\end{gathered}
$$

60. 

$-2[6+4(2-8)]-25=-2[6+4(-6)]$ - 25 $=-2[6+(-24)]-25$ $=-2(-18)-25$ $=36-25$ $=11$

$$
\begin{aligned}
& =-3(16)+5(-8) \\
& =-48+(-40) \\
& =-88
\end{aligned}
$$


38. $-(-2)^{3}=-(-8)=8$
40. $(2-7)^{2} \div(4-3)^{4}=(-5)^{2} \div 1^{4}=25 \div 1=$ 25
42. $|3-15 \cdot(-4) \div(-16)|=+12 \cdot(-4) \div(-16)$

$$
\begin{aligned}
& =12 \cdot(-4) \div(-16) \\
& =-48 \div(-16) \\
& =3
\end{aligned}
$$

44. $(-20-5) \div 5-15=(-25) \div 5-15=-5-15$

$$
=-20
$$

62. $x-y-z=-2-4-$

$$
(-1)
$$

$$
=-2-4+1
$$

$$
=-6+1
$$

$$
=-5
$$

64. $5 x-y+4 z=5(-2)-4+4(-1)$

$$
\begin{aligned}
& =-10-4+(-4) \\
& =-14+(-4) \\
& =-18
\end{aligned}
$$

66. $x^{2}+z=(-2)^{2}+(-1)=4+(-1)=3$
67. $\underline{4 x}=\frac{4(-2)}{}=\frac{-8}{=}=-2$

## $\begin{array}{lll}y & 4 & 4\end{array}$

70. $z^{2}=(-4)^{2}=16$
71. $-x^{2}=-(-3)^{2}=-9$
72. $3 x^{2}=3(-3)^{2}=3(9)=27$
73. $3-z^{2}=3-(-4)^{2}=3-16=-13$
74. $3 z^{2}-x=3(-4)^{2}-(-3)=3(16)+3=48+3=51$
75. average $=\frac{-18+(-8)+(-1)+(-1)+0+4}{6}$

$$
\begin{aligned}
& =\frac{-24}{6} \\
& =-4
\end{aligned}
$$

82. average $=\frac{-40+(-20)+(-10)+(-15)+(-5)}{5}$

$$
\begin{aligned}
& =\frac{-90}{5} \\
& =-18
\end{aligned}
$$

84. The two lowest scores are -12 and -5 .
$-5-(-12)=-5+12=7$
The difference between the two lowest scores is 7.
85. average $=\frac{-12+(-5)+(-1)+6}{=}=-3$

## 4

4
The average of the scores is -3 .
88. no; answers may vary
90. $90 \div 45=2$
92. $45+90=135$
94. $3+5+3+5=16$
104. answers may vary
106. $(-17)^{6}=(-17)(-17)(-17)(-17)(-17)(-17)$

$$
=24,137,569
$$

108. $3 x^{2}+2 x-y=3(-18)^{2}+2(-18)-2868$

$$
\begin{aligned}
& =3(324)+(-36)-2868 \\
& =972+(-36)-2868 \\
& =936-2868 \\
& =-1932
\end{aligned}
$$

110. $5(a b+3)^{b}=5(-2 \cdot 3+3)^{3}$

$$
\begin{aligned}
& =5(-6+3)^{3} \\
& =5(-3)^{3} \\
& =5(-27) \\
& =-135
\end{aligned}
$$

## Section 2.6 Practice Exercises

1. $-4 x-3=5$
$-4(-2)-325$
$8-325$
8-325 $5=5 \quad$ True
Since $5=5$ is true, -2 is a solution of the equation.
2. $y-6=-2$
$y-6+6=-2+6$
$y=4$

Check: $y-6=-2$
4-62-2 $-2=-2$ True

The solution is 4 .
3. $-2=z+8$
$-2-8=z+8-8$
$-10=z$
Check: $-2=z+8$

$$
-22-10+8
$$

$$
-2=-2 \quad \text { True }
$$

The perimeter is 16 centimeters.

96. $17+23+32=72$

The perimeter is 72 meters.
98. $(7 \cdot 3-4) \cdot 2=(21-4) \cdot 2=17 \cdot 2=34$
100. $2 \cdot(8 \div 4-20)=2 \cdot(2-20)=2 \cdot(-18)=-36$
102. answers may vary

The solution is -10 .
4. $x=-2+90+(-100)$
$x=88+(-100)$
$x=-12$
The solution is -12 .
5. $3 y=-18$
$\frac{3 y}{3}=\frac{-18}{3}$
$\frac{3}{3} \cdot y=\frac{-18}{3}$
$y=-6$
Check: $\quad 3 y=-18$
3(-6) $2-18$
$-18=-18$ True
The solution is -6 .
6. $-32=8 x$
$\frac{-32}{8}=\frac{8 x}{8}$
$\frac{-32}{8}=\frac{8}{8} \cdot x$
$-4=x$

$$
\text { Check: } \begin{aligned}
& -32=8 x \\
& -3228(-4) \\
& -32=-32 \text { True }
\end{aligned}
$$

The solution is -4 .
7. $-3 y=-27$
$\frac{-3 y}{-3}=\frac{-27}{-3}$
$\frac{-3}{-3} \cdot y=\frac{-27}{-3}$
$y=9$

$$
\text { Check: } \begin{array}{rl}
-3 y & =-27 \\
-3 \cdot 9 & 2-27 \\
-27 & =-27 \quad \text { True }
\end{array}
$$

The solution is 9 .
8. $\quad \frac{x}{-4}=7$

$$
\begin{aligned}
-4 \cdot \frac{x}{-4} & =-4 \cdot 7 \\
\frac{-4}{-4} \cdot x & =-4 \cdot 7 \\
x & =-28
\end{aligned}
$$

Check: $\begin{aligned} \quad \frac{x}{-4} & =7 \\ \frac{-28}{-4} & 27 \\ 7 & =7 \quad \text { True }\end{aligned}$
2. A statement of the form
"expression = expression" is called an equation.
3. An equation contains an equal sign (=) while an expression does not.
4. An expression may be simplified and evaluated while an equation may be solved.
5. A solution of an equation is a number that when substituted for a variable makes the equation a true statement.
6. Equivalent equations have the same solution.
7. By the addition property of equality, the same number may be added to or subtracted from both sides of an equation without changing the solution of the equation.
8. By the multiplication property of equality, both sides of an equation may be multiplied or
divided by the same nonzero number without changing the solution of the equation.
9. an equal sign
10. We can add the same number to both sides of an equation and we'll have an equivalent equation. Also, we can subtract the same number from both sides of an equation and have an equivalent equation.
11. To check a solution, we go back to the original equation, replace the variable with the proposed solution, and see if we get a true statement.

## Exercise Set 2.6

2. $y-16=-7$

9-162-7

$$
-7=-7 \quad \text { True }
$$

Since $-7=-7$ is true, 9 is a solution of the equation.
4. $a+23=-16$
$-7+232-16$ $16=-16$ False
Since $16=-16$ is false, -7 is not a solution of

The solution is -28 .
the equation.

## Vocabulary, Readiness \& Video Check 2.6

1. A combination of operations on variables and numbers is called an expression.
2. $\begin{array}{rl}-3 k & =12-k \\ -3(-6) & 212-(-6) \\ 18 & 212+6 \\ 18 & =18 \quad \text { True }\end{array}$

Since $18=18$ is true, -6 is a solution of the equation.
8. $2(b-3)=10$
$2(1-3) 210$
2(-2) 210

$$
-4=10 \quad \text { False }
$$

Since $-4=10$ is false, 1 is not a solution of the equation.
10. $\begin{aligned} f+4 & =-6 \\ f+4-4 & =-6-4\end{aligned}$

$$
f=-10
$$

Check: $\quad f+4=-6$

$$
\begin{array}{rl}
-10+4 & 2-6 \\
-6 & =-6 \text { True }
\end{array}
$$

The solution is -10 .
12. $s-7=-15$
$s-7+7=-15+7$

$$
s=-8
$$

Check: $s-7=-15$

$$
\begin{array}{r}
-8-72-15 \\
-15=-15 \quad \text { True }
\end{array}
$$

The solution is -8 .
14. $1=y+7$
$1-7=y+7-7$

$$
-6=y
$$

Check: $1=y+7$

$$
12-6+7
$$

$$
1=1 \quad \text { True }
$$

The solution is -6 .
16. $-50+40-5=z$

$$
\begin{array}{r}
-10-5=z \\
-15=z
\end{array}
$$

Check: $-50+40-5=z$
18. $6 y=48$
$\frac{6 y}{6}=\frac{48}{6}$
$\frac{6}{6} \cdot y=\frac{48}{6}$

$$
y=8
$$

Check: $6 y=48$

$$
\begin{array}{r}
6(8) 248 \\
48=48 \quad \text { True }
\end{array}
$$

The solution is 8 .
20. $-2 x=26$

$$
\begin{aligned}
& \overline{-2 x}=\overline{26} \\
&-2-2 \\
& \overline{-2} \cdot x=\begin{array}{c}
26 \\
-2 \\
-2
\end{array} \\
&-2 \\
& x=-13
\end{aligned}
$$

$$
\text { Check: } \begin{aligned}
-2 x & =26 \\
-2(-13) & 226 \\
26 & =26 \quad \text { True }
\end{aligned}
$$

The solution is -13 .
22. ${ }^{n}=-5$
$11 \cdot \frac{n}{11}=11 \cdot(-5)$
$\frac{11}{11} \cdot n=11 \cdot(-5)$
$n=-55$
Check: $\begin{array}{r}\frac{n}{11}=-5 \\ \frac{-55}{11} 2-5\end{array}$
$-5=-5$ True
The solution is -55 .
24. $7 y=-21$
$\frac{7 y}{7}=\frac{-21}{7}$
$\frac{7}{7} \cdot y=\frac{-21}{7}$
$-50+40-52-15$
 $-10-52 y=-3$
-15 Check: $7 y=-21$
$-15=7 \cdot(-3) 2-21$
$-15 \quad-21=-21$
True True
The solution is -15 .
The solution is -3 .
26. $-9 x=0$
$\underline{-9 x}=\underline{0}$
$-9 \quad-9$
$\underline{-9} \cdot x=\underline{0}$
$-9 x=0{ }^{-9}$
Check: $-9 x=0$

$$
-9 \cdot 020
$$

$$
0=0 \quad \text { True }
$$

The solution is 0 .
28. $-31 x=-31$
$\underline{-31 x}=\underline{-31}$
$\begin{array}{ll}-31 & -31\end{array}$
$\underline{-31} \cdot x=\underline{-31}$
$-31 x=1^{-31}$
Check: $-31 x=-31$
$-31 \cdot 12-31$
$-31=-31$ True
The solution is 1 .
30. $3 y=-27$
$\frac{3 y}{3}=\frac{-27}{3}$
$\frac{3}{3} \cdot y=\frac{-27}{3}$

$$
y=-9
$$

The solution is -9 .
32. $n-4=-48$
$n-4+4=-48+4$ $n=-44$
The solution is -44 .
36.
34.

40. $-11 x=-121$
$\underline{-11 x}=\underline{-121}$
$-11 \quad-11$
$\underline{-11} \cdot x=\underline{-121}$
${ }^{-11} x=11^{-11}$
The solution is 11 .
41. $\quad \underline{n}=-20$
$5 \cdot \frac{n}{5}=5 \cdot(-20)$
$\underline{5} \cdot n=5 \cdot(-20)$
5

$$
n=-100
$$

The solution is -100 .
44. $-81=27 x$
$\frac{-81}{27}=\frac{27 x}{27}$
$\frac{-81}{27}=\frac{27}{27} \cdot x$ $-3=x$
The solution is -3 .
46. A number increased by -5 is $x+(-5)$.
48. The quotient of a number and -20 is $x \div(-20)$ or $\frac{x}{-20}$.
50. -32 multiplied by a number is $-32 \cdot x$ or $-32 x$.
52. Subtract a number from -18 is $-18-x$.
$\left.\begin{array}{lc} & 12 \\ =36-12=y+12-12 \\ 3 & -48=y \\ 6 & \\ = & \text { The solution is }-48 . \\ y & \\ + & \\ & \\ & -9\end{array}\right)$

## 



The
solu
solu
tion is
81.

9
ニ
$\underline{9}$
$x$
$=$

9
(

9
$-9$
$x$
$=$
1
54.
56.
$n$
$+\quad-18$
$-98 \cdot \frac{y}{-18}=-18 \cdot 1098$
6
$1 \frac{-18}{-18} \cdot y=-18 \cdot 1098$
$=-\quad y=-19,764$
1
The solution is $-19,764$.
0
$+$
9
6
1
-

9
6
1
$=$

1

2
0
-

9
6
1
$n$
=
-
4
1
Th
e
sol
uti
on
is

84
1.
$y$ $\qquad$

38. $z=-28+36$ $z=8$
The solution is 8 .
58. answers may vary
60. answers may vary

## Chapter 2 Vocabulary Check

1. Two numbers that are the same distance from 0 on the number line but are on opposite sides of 0 are called opposites.
2. The absolute value of a number is that number's distance from 0 on a number line.
3. The integers are $\ldots,-3,-2,-1,0,1,2,3, \ldots$.
4. The negative numbers are numbers less than zero.
5. The positive numbers are numbers greater than zero.
6. The symbols "<" and ">" are called inequality symbols.
7. A solution of an equation is a number that when substituted for a variable makes the equation a true statement.
8. The average of a list of numbers is $\frac{\text { sum of numbers }}{\text { number of numbers }}$.
9. A combination of operations on variables and numbers is called an expression.
10. A statement of the form "expression $=$ expression" is called an equation.
11. The sign " $<$ " means is less than and " $>$ " means is greater than.
12. By the addition property of equality, the same number may be added to or subtracted from both sides of an equation without changing the solution of the equation.
13. By the multiplication property of equality, both sides of an equation may be multiplied or divided by the same nonzero number without changing the solution of the equation.

## Chapter 2 Review

1. If 0 represents ground level, then 1572 feet below the ground is -1572 .
2. If 0 represents sea level, then an elevation of 11,239 feet is $+11,239$.
3. 


4.

5. $|-11|=11$ since -11 is 11 units from 0 on a number line.
6. $|0|=0$ since 0 is 0 units from 0 on a number line.
7. $-|8|=-8$
8. $-(-9)=9$
9. $-|-16|=-16$
10. $-(-2)=2$

11. $-18>-20$ since -18 is to the right of -20 on a number line.
12. $-5<5$ since -5 is to the left of 5 on a number line.
13. $|-123|=123$
$-|-198|=-198$
Since $123>-198,|-123|>-|-198|$.
14. $|-12|=12$
$-|-16|=-16$
Since $12>-16,|-12|>-|-16|$.
15. The opposite of -18 is 18 .
$-(-18)=18$
16. The opposite of 42 is negative 42 .
$-(42)=-42$
17. False; consider $a=1$ and $b=2$, then $1<2$.
18. True
19. True
20. True
21. $|y|=|-2|=2$
22. $|-x|=|-(-3)|=|3|=3$
23. $-|-z|=-|-(-5)|=-|5|=-5$
24. $-|-n|=-|-(-10)|=-|10|=-10$
25. The bar that extends the farthest in the negative direction corresponds to Elevator D, so Elevator D extends the farthest below ground.
26. The bar that extends the farthest in the positive direction corresponds to Elevator B, so Elevator $B$ extends the highest above ground.
27. $|5|-|-3|=5-3=2$
$5>3$, so the answer is positive.
$5+(-3)=2$
28. $|18|-|-4|=18-4=14$
$18>4$, so the answer is positive.
$18+(-4)=14$
29. $|16|-|-12|=16-12=4$
$16>12$, so the answer is positive.
$-12+16=4$
31. $|-8|+|-15|=8+15=23$

The common sign is negative, so $-8+(-15)=-23$.
32. $|-5|+|-17|=5+17=22$

The common sign is negative, so $-5+(-17)=-22$.
33. $|-24|-|3|=24-3=21$
$24>3$, so the answer is negative.
$-24+3=-21$
34. $|-89|-|19|=89-19=70$
$89>19$, so the answer is negative.
$-89+19=-70$
35. $15+(-15)=0$
36. $-24+24=0$
37. $|-43|+|-108|=43+108=151$

The common sign is negative, so $-43+(-108)=-151$.
38. $|-100|+|-506|=100+506=606$

The common sign is negative, so $-100+(-506)=-606$.
39. $-15+(-5)=-20$

The temperature at $6 \mathrm{a} . \mathrm{m}$. is $-20^{\circ} \mathrm{C}$.
40. $-127+(-23)=-150$

The diver's current depth is -150 feet.
41. $-6+(-9)+(-4)+(-2)=-15+(-4)+(-2)$

$$
\begin{aligned}
& =-19+(-2) \\
& =-21
\end{aligned}
$$

His total score was -21 .
30. $|40|-|-23|=40-23=17$
$40>23$, so the answer is positive. $-23+40=17$

42. $16-4=16+(-4)=12$

The team's
score was
12.
43. $12-4=12+(-4)=8$
44. $-12-4=-12+(-4)=-16$
45. $-7-17=-7+(-17)=-24$
46. $7-17=7+(-17)=-10$
47. $7-(-13)=7+13=20$
48. $-6-(-14)=-6+14=8$
49. $16-16=16+(-16)=0$
50. $-16-16=-16+(-16)=-32$
51. $-12-(-12)=-12+12=0$
52. $-5-(-12)=-5+12=7$
53. $-(-5)-12+(-3)=5+(-12)+(-3)$

$$
\begin{aligned}
& =-7+(-3) \\
& =-10
\end{aligned}
$$

54. $-8+(-12)-10-(-3)=-8+(-12)+(-10)+3$

$$
\begin{aligned}
& =-20+(-10)+3 \\
& =-30+3 \\
& =-27
\end{aligned}
$$

55. $600-(-92)=600+92=692$

The difference in elevations is 692 feet.
56. $142-125+43-85=142+(-125)+43+(-85)$

$$
\begin{aligned}
& =17+43+(-85) \\
& =60+(-85) \\
& =-25
\end{aligned}
$$

The balance in his account is -25 .
57. $85-99=85+(-99)=-14$

You are -14 feet or 14 feet below ground at the end of the drop.
58. $66-(-16)=66+16=82$

The total length of the elevator shaft for Elevator C is 82 feet.
59. $|-5|-|-6|=5-6=5+(-6)=-1$
$5-6=5+(-6)=-1$
$|-5|-|-6|=5-6$ is true.
60. $|-5-(-6)|=|-5+6|=|1|=1$
$5+6=11$
Since $1 \neq 11$, the statement is false.
61. $-3(-7)=21$
62. $-6(3)=-18$
63. $-4(16)=-64$
64. $-5(-12)=60$
68. $-1(6)(2)(-2)=-6(2)(-2)=-12(-2)=24$
69. $-15 \div 3=-5$
70. $\frac{-24}{-8}=3$
71. $\frac{0}{-3}=0$
72. $\frac{-46}{0}$ is undefined.
73. $\frac{100}{-5}=-20$
74. $\frac{-72}{8}=-9$
75. $\frac{-38}{-1}=38$
76. $\frac{45}{-9}=-5$
77. A loss of 5 yards is represented by -5 .
$(-5)(2)=-10$
The total loss is 10 yards.
78. A loss of $\$ 50$ is represented by -50 .
$(-50)(4)=-200$
The total loss is $\$ 200$.
79. $A$ debt of $\$ 1024$ is represented by -1024 .
$-1024 \div 4=-256$
Each payment is $\$ 256$.
80. A drop of 45 degrees is represented by -45 .
$\frac{-45}{9}=-5$ or $-45 \div 9=-5$
The average drop each hour is $5^{\circ} \mathrm{F}$.
82.
81.

$(-7)^{2}=(-7)(-7)=$
49
65. $(-5)^{2}=(-5)(-5)=25$
66. $(-1)^{5}=(-1)(-1)(-1)(-1)(-1)=-1$
67. $12(-3)(0)=0$

$$
=-(7 \cdot 7)=-49
$$

$$
-
$$

$$
7^{2}
$$

83. $5-8+3=-3+3=0$
84. $-3+12+(-7)-10=9+(-7)-10=2-10=-8$
85. $-10+3 \cdot(-2)=-10+(-6)=-16$
86. $5-10 \cdot(-3)=5-(-30)=5+30=35$
87. $16 \div(-2) \cdot 4=-8 \cdot 4=-32$
88. $-20 \div 5 \cdot 2=-4 \cdot 2=-8$
89. $16+(-3) \cdot 12 \div 4=16+(-36) \div 4$

$$
\begin{aligned}
& =16+(-9) \\
& =7
\end{aligned}
$$

90. $-12+10 \div(-5)=-12+(-2)=-14$
91. $4^{3}-(8-3)^{2}=4^{3}-(5)^{2}=64-25=$
92. $39(-3)^{3}-90=-27-90=-117$
93. $(-4)(-3)-(-2)(-1)=\frac{12-2}{=}=-2$

$$
\begin{array}{lll}
-10+5 & -5 & -5
\end{array}
$$

94. $\frac{4(12-18)}{-10 \div(-2-3)}=\frac{4(-6)}{-10 \div(-5)}=\frac{-24}{2}=-12$
95. average $=\frac{-18+25+(-30)+7+0+(-2)}{6}$

$$
=\frac{-18}{6}
$$

$$
=-3
$$

96. average $=\frac{-45+(-40)+(-30)+(-25)}{4}$

$$
\begin{aligned}
& =\frac{-140}{4} \\
& =-35
\end{aligned}
$$

97. $2 x-y=2(-2)-1=-4-1=-5$
98. $y^{2}+x^{2}=1^{2}+(-2)^{2}=1+4=5$
99. $\frac{3 x}{6}=\frac{3(-2)}{6}=\frac{-6}{6}=-1$
100. $\underline{5 y-x}=\underline{5(1)-(-2)}=\frac{5+2}{}=\frac{7}{=-7}$
101. $2(c-8)=-20$
$2(-2-8) 2-20$
$2(-10) 2-20$

$$
-20=-20 \quad \text { True }
$$

Since $-20=-20$ is true, -2 is a solution of the equation.
103. $n-7=-20$
$n-7+7=-20+7$ $n=-13$
The solution is -13 .
104. $-5=n+15$
$-5-15=n+15-15$

$$
-20=n
$$

The solution is -20 .
105. $10 x=-30$

$$
10 x==30
$$

$$
\begin{gathered}
\underline{10}_{10}^{10} \cdot x=\begin{array}{l}
10 \\
\underline{-30} \\
10
\end{array} \\
x=-3
\end{gathered}
$$

The solution is -3 .
106. $-8 x=72$
$\underline{-8 x}=\underline{72}$
$\begin{array}{ll}-8 & -8\end{array}$
$\begin{aligned} \frac{-8}{-8} \cdot x & =\frac{72}{-8} \\ x & =-9\end{aligned}$
The solution is -9 .
107. $-20+7=y$

$$
-13=y
$$

The solution is -13 .
108. $x-31=-62$
$x-31+31=-62+31$
$x=-31$
The solution is -31 .
109. $\frac{n}{-4}=-11$


| $-y$ | -1 | -1 | -1 |
| :--- | :--- | :--- | :--- |

101. $2 n-6=16$
$2(-5)-6216$
$-10-6216$
$-16=16$ False
Since $-16=16$ is false, -5 is not a solution of the equation.

$$
\begin{aligned}
-4 \cdot^{n} & =-4 \cdot(-11) \\
\frac{-4}{-4} \cdot n & =-4 \cdot(-11) \\
n & =44
\end{aligned}
$$

The solution is 44 .
110. $\quad \frac{x}{-2}=13$

$$
-2 \frac{x}{-2}=-2 \cdot 13
$$

$$
=\stackrel{2}{2} \cdot x=-2 \cdot 13
$$

$$
-2
$$

$$
x=-26
$$

The solution is -26 .
111. $n+12=-7$
$n+12-12=-7-12$

$$
n=-19
$$

The solution is -19 .
112. $n-40=-2$
$n-40+40=-2+40$

$$
n=38
$$

The solution is 38 .
113. $-36=-6 x$
$\underline{-36}=\underline{-6 x}$
$-6 \quad-6$
$\underline{-36}=\underline{-6} \cdot x$
$-6 \quad-6$

$$
6=x
$$

The solution is 6 .
114. $-40=8 y$
$\frac{-40}{8}=\frac{8 y}{8}$
$\frac{-40}{8}=\frac{8}{8} \cdot y$
$-5=y$
The solution is -5 .
115. $-6+(-9)=-15$
116. $-16-3=-16+(-3)=-19$
117. $-4(-12)=48$
118. $\underline{84}=-21$
123. $12,923-(-195)=12,923+195=13,118$

The difference in elevations is 13,118 feet.
124. $-32+23=-9$

His financial situation can be represented by -9 .
125. $(3-7)^{2} \div(6-4)^{3}=(-4)^{2} \div(2)^{3}=16 \div 8=2$
126. $3(4+2)+(-6)-3^{2}=3(6)+(-6)-3^{2}$

$$
\begin{aligned}
& =3(6)+(-6)-9 \\
& =18+(-6)-9 \\
& =12-9 \\
& =3
\end{aligned}
$$

127. $2-4 \cdot 3+5=2-12+5=-10+5=-5$
128. $4-6 \cdot 5+1=4-30+1=-26+1=-25$
129. $\frac{-|-14|-6}{7+2(-3)}=\frac{-14-6}{7+(-6)}=\frac{-20}{1}=-20$
130. $5(7-6)^{3}-4(2-3)^{2}+2^{4}=5(1)^{3}-4(-1)^{2}+2^{4}$

$$
\begin{aligned}
& =5(1)-4(1)+16 \\
& =5-4+16 \\
& =1+16 \\
& =17
\end{aligned}
$$

131. $n-9=-30$
$\begin{aligned} n-9+9 & =-30+9 \\ n & =-21\end{aligned}$

$$
n=-21
$$

The solution is -21 .
132. $n+18=1$
$n+18-18=1-18$

$$
n=-17
$$

The solution is -17 .
133. $-4 x=-48$

$$
\begin{gathered}
\overline{-4 x}=\overline{-48} \\
-4
\end{gathered}=\begin{gathered}
-4
\end{gathered}
$$

$\underline{-4} \cdot x=\underline{-48}$
 -4
119. $-76-(-97)=-76+97=21$
$-4 \quad \begin{array}{ll}-4 \\ x & =12\end{array}$
The solution is 12 .
120. $-9+4=-5$
121. $-18-9=-27$

The temperature on Friday was $-27^{\circ} \mathrm{C}$.
122. $-11+17=6$

The temperature at noon on Tuesday was $6^{\circ} \mathrm{C}$.
134. $9 x=-81$
$\underline{9 x}=\underline{-81}$

$$
\begin{array}{r}
9 \\
\frac{9}{9} \cdot x=\frac{9}{9} \\
x=-9
\end{array}
$$

The solution is -9 .
135. $\frac{n}{-2}=100$

$$
-2 \cdot \frac{n}{-2}=-2 \cdot 100
$$

$$
\frac{-2}{-2} \cdot n=-2 \cdot 100
$$

$$
n=-200
$$

The solution is -200 .
136. $\frac{y}{-1}=-3$
$-1 \cdot \frac{y}{-1}=-1(-3)$ $\underline{-1} \cdot y=-1 \cdot(-3)$

$$
\begin{aligned}
& -1 \\
& y=3
\end{aligned}
$$

The solution is 3 .

## Chapter 2 Test

1. $-5+8=3$
2. $18-24=18+(-24)=-6$
3. $5 \cdot(-20)=-100$
4. $-16 \div(-4)=4$
5. $-18+(-12)=-30$
6. $-7-(-19)=-7+19=12$
7. $-5 \cdot(-13)=65$
8. $\frac{-25}{-5}=5$
9. $-8+9 \div(-3)=-8+(-3)=-11$
10. $-7+(-32)-12+5=-7+(-32)+(-12)+5$

$$
=-39+(-12)+5
$$

$$
=-51+5
$$

$$
=-46
$$

15. $(-5)^{3}-24 \div(-3)=-125-24 \div(-3)$

$$
\begin{aligned}
& =-125-(-8) \\
& =-125+8 \\
& =-117
\end{aligned}
$$

16. $(5-9)^{2} \cdot(8-2)^{3}=(-4)^{2} \cdot(6)^{3}=16 \cdot 216=3456$
17. $-(-7)^{2} \div 7 \cdot(-4)=-49 \div 7 \cdot(-4)=-7 \cdot(-4)=28$
18. $3-(8-2)^{3}=3-6^{3}$

$$
\begin{aligned}
& =3-216 \\
& =3+(-216) \\
& =-213
\end{aligned}
$$

$\underline{4} \quad \underline{8}^{\underline{2}} \quad \underline{4} \quad \underline{64}$
19. $2^{-}{ }_{16}={ }_{2}{ }^{-}{ }_{16}=2-4=2+(-4)=-2$
20. $\frac{-3(-2)+12}{-1(-4-5)}=\frac{6+12}{-1(-9)}=\frac{18}{9}=2$
21. $\frac{|25-30|^{2}}{2(-6)+7}=\frac{| |}{-12+7}=\frac{-5^{2}}{-5}=\frac{(5)^{2}}{-5}=-5$
22. $5(-8)-[6-(2-4)]+(12-16)^{2}$
$=5(-8)-[6-(-2)]+(12-16)^{2}$
$=5(-8)-(6+2)+(-4)^{2}$
$=5(-8)-8+(-4)^{2}$
$=5(-8)-8+16$
$=-40-8+16$
$=-48+16$

$$
=-32
$$

23. $7 x+3 y-4 z=7(0)+3(-3)-4(2)$
24. $|-25|+(-13)=25+(-13)=12$

25. $14-|-20|=14-20=14+(-20)=-6$
26. $|5| \cdot|-10|=5 \cdot 10=50$

$$
\begin{aligned}
& =0+(-9)-8 \\
& =-9-8 \\
& =-17
\end{aligned}
$$

24. $10-y^{2}=10-(-3)^{2}=10-9=1$
25. $\frac{|-10|}{-|-5|}=\frac{10}{-5}=-2$
26. $\frac{3 z}{}=\frac{3(2)}{2(-3)}=-6=-1$
27. A descent of 22 feet is represented by -22 . $4(-22)=-88$
Mary is 88 feet below sea level.
28. $129+(-79)+(-40)+35=50+(-40)+35$

$$
\begin{aligned}
& =10+35 \\
& =45
\end{aligned}
$$

His new balance can be represented by 45 .
28. Subtract the elevation of the Romanche Gap from the elevation of Mt. Washington. $6288-(-25,354)=6288+25,354=31,642$
The difference in elevations is 31,642 feet.
29. Subtract the depth of the lake from the elevation of the surface.
$1495-5315=1495+(-5315)=-3820$
The deepest point of the lake is 3820 feet below sea level.
30. average $=\frac{-12+(-13)+0+9}{4}=\frac{-16}{4}=-4$
31. a. The product of a number and 17 is $17 \cdot x$ or $17 x$.
b. A number subtracted from 20 is $20-x$.
32. $-9 n=-45$

$$
\underline{-9 n}=\frac{-45}{}
$$

$$
\begin{gathered}
\frac{-9}{-9} \cdot n=\frac{-45}{-9} \\
n=5
\end{gathered}
$$

The solution is 5 .
33. $\frac{n}{-7}=4$
$-7 \cdot \frac{n}{-7}=-7 \cdot 4$

$$
\frac{-7}{-7} \cdot n=-7 \cdot 4
$$

$$
n=-28
$$

The solution is -28 .
34. $x-16=-36$
$x-16+16=-36+16$

$$
x=-20
$$

35. $-20+8+8=x$

$$
-12+8=x
$$

$$
-4=x
$$

The solution is -4 .

## Cumulative Review Chapters 1-2

1. The place value of 3 in 396,418 is hundredthousands.
2. The place value of 3 in 4308 is hundreds.
3. The place value of 3 in 93,192 is thousands.
4. The place value of 3 is 693,298 is thousands.
5. The place value of 3 in $534,275,866$ is tenmillions.
6. The place value of 3 in $267,301,818$ is hundredthousands.
7. a. $-7<7$ since -7 is to the left of 7 on a number line.
b. $0>-4$ since 0 is to the right of -4 on a number line.
c. $-9>-11$ since -9 is to the right of -11 on a number line.
8. a. $12>-4$ since 12 is to the right of -4 on a number line.
b. $-13>-31$ since -13 is to the right of -31 on a number line.
c. $-82<79$ since -82 is to the left of 79 on a number line.
9. $\begin{aligned} 13+2+7+8+9 & =(13+7)+(2+8)+9 \\ & =20+10+9 \\ & =39\end{aligned}$
10. $11+3+9+16=(11+9)+(3+16)=20+19=39$
11. 7826
$\begin{array}{r}-\quad 505 \\ \hline 7321\end{array}$
 The solution is -20 .

Check: 7321

| +505 |
| :--- |

7826
12. 3285

| -272 |
| ---: | ---: |
| 3013 |
| Check: $\begin{array}{r}3013 \\ +\quad 272 \\ \hline\end{array} \quad 3285$ |

13. Subtract 7257 from the radius of Jupiter.

43,441

- 1201

36,184
The radius of Saturn is 36,184 miles.
14. Subtract the cost of the camera from the amount in her account.

762
$-237$ 525
She will have $\$ 525$ left in her account after buying the camera.
15. To round 568 to the nearest ten, observe that the digit in the ones place is 8 . Since this digit is at least 5 , we add 1 to the digit in the tens place. The number 568 rounded to the nearest ten is 570.
16. To round 568 to the nearest hundred, observe that the digit in the tens place is 6 . Since this digit is at least 5 , we add 1 to the digit in the hundreds place. The number 568 rounded to the nearest hundred is 600 .
17. 4725 rounds to 4700
-2879 rounds to -2900
1800
18. 8394 rounds to 8000
-2913 rounds to $\frac{-3000}{5000}$
19. a. $5(6+5)=5 \cdot 6+5 \cdot 5$
b. $20(4+7)=20 \cdot 4+20 \cdot 7$
c. $2(7+9)=2 \cdot 7+2 \cdot 9$
21. 631
$\begin{array}{r}\times \quad 125 \\ \hline 3155\end{array}$
12620
$\begin{array}{r}63100 \\ \hline 78,875\end{array}$
22. 299
$\begin{array}{r}\times \quad 104 \\ \hline 1196\end{array}$
29900
31,096
23. a. $42 \div 7=6$ because $6 \cdot 7=42$.
b. $\frac{64}{8}=8$ because $8 \cdot 8=64$.
c. $\quad 3 \longdiv { 7 }$ 年
24. a. $\frac{35}{5}=7$ because $7 \cdot 5=35$.
b. $64 \div 8=8$ because $8 \cdot 8=64$.
c. $4 \longdiv { 1 2 }$ because $12 \cdot 4=48$.

741
25. $5 \longdiv { 3 7 0 5 }$

$$
\underline{-35}
$$

$$
20
$$

$$
\frac{-20}{05}
$$

$$
\frac{-5}{0}
$$

Check: 741
2

$$
2+12)=5 \cdot 2+5 \cdot 12
$$

0
b. $9(3+6)=9 \cdot 3+9 \cdot 6$
c. $\quad 4(8+1)=4 \cdot 8+4 \cdot 1$


26.

Check: 456

$$
\begin{array}{r}
\times \quad 8 \\
\hline 3648
\end{array}
$$

27. number of cards number of number of for each person $=$ cards $\quad \div$ friends $=238 \div 19$
$19 \begin{array}{r}12 \\ 238 \\ -19 \\ 48 \\ \frac{-38}{10}\end{array}$

Each friend will receive 12 cards. There will be 10 cards left over.
28. $\begin{gathered}\text { Cost of each } \\ \text { ticket }\end{gathered}=\begin{gathered}\text { total } \\ \text { cost }\end{gathered} \div$ number of tickets $=324 \div 36$
$3 6 \longdiv { 9 2 4 }$
-324
0

Each ticket cost \$9.
37. $x+6=8+6=14$
38. $5+x=5+9=14$
39. a. $|-9|=9$ because -9 is 9 units from 0 .
b. $\quad|8|=8$ because 8 is 8 units from 0 .
c. $\quad|0|=0$ because 0 is 0 units from 0 .
40. a. $|4|=4$ because 4 is 4 units from 0 .
b. $|-7|=7$ because -7 is 7 units from 0 .
41. $-2+25=23$
42. $8+(-3)=5$
43. $2 a-b=2(8)-(-6)=16-(-6)=16+6=22$
44. $x-y=-2-(-7)=-2+7=5$
45. $-7 \cdot 3=-21$
46. $5(-2)=-10$
47. $0 \cdot(-4)=0$
29. $9^{2}=9 \cdot 9=81$
30. $5^{3}=5 \cdot 5 \cdot 5=125$
31. $6^{1}=6$
32. $4^{1}=4$
33. $5 \cdot 6^{2}=5 \cdot 6 \cdot 6=180$
34. $2^{3} \cdot 7=2 \cdot 2 \cdot 2 \cdot 7=56$
35. $3^{7-2 \cdot 3+}=7-2 \cdot 3+9=7=7$
$5(2-1) \quad 5(1) \quad 5 \quad 5$
36. $6^{2}+4 \cdot 4+2^{3}$
48. $-6 \cdot 9=-54$
49. $3(4-7)+(-2)-5=3(-3)+(-2)-5$

$$
\begin{aligned}
& =-9+(-2)-5 \\
& =-11-5 \\
& =-16
\end{aligned}
$$

50. $4-8(7-3)-(-1)=4-8(4)-(-1)$

$$
\begin{aligned}
& =4-32-(-1) \\
& =4-32+1 \\
& =-28+1 \\
& =-27
\end{aligned}
$$



|  | 3 | $+4 \cdot 4+8$ |
| :---: | :---: | :---: |
|  | 6 | 37-25 |
|  |  | $\underline{36+16+8}$ |
|  |  | $\begin{aligned} & =\frac{60}{12} \\ & =5 \end{aligned}$ |

