## Solution Manual for Algebra and Trigonometry Graphs and Models 5th Edition Bittinger Beecher Ellenbogen Penna 9780321783974 0321783972

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## **Chapter 2**

# **More on Functions**

#### Exercise Set 2.1

- a) Forx-values from -5 to 1, they-values increase from -3 to 3. Thus the function is increasing on the interval (-5, 1).
  - b) Forx-values from 3 to 5, the y-values decrease from 3 to 1. Thus the function is decreasing on the inter- val (3, 5).
  - c) Forx-values from 1 to 3, y is 3. Thus the function is constant on (1, 3).
- **2.** a) Forx-values from 1 to3, they-values increase from 1 to2. Thus, the function is increasing on the interval (1, 3).
  - b) For *x*-values from 5 to -1, the *y*-values decrease from 4 to 1. Thus the function is decreasing on the interval (-5, 1).
  - c) For *x*-values from 3 to 5, *y* is 2. Thus the function is constant on (3, 5).
- **3.** a) For *x*-values from 3 to-1, the *y*-values increase from 4 to 4. Also, f-or*x*-values from 3 to 5, the *y*-values increase from 2 to 6. Thus the function is increasing on (-3, -1) and on (3, 5).
  - b) Forx-values from 1 to 3, the y-values decrease from 3 to 2. Thus the function is decreasing on the inter-val (1, 3).
  - c) For x-values from -5 to -3, y is 1. Thus the function is constant on (-5, -3).
- **4.** a) Forx-values from 1 to 2, the *y*-values increase from 1 to 2. Thus the function is increasing on the interval (1, 2).
  - b) For x-values from 5 to-2, the y-values decrease from 3 to 1. For x-values from 2 to 1, the y-values decrease from 3 to 1. And for x-values from 3 to 5, the y-values decrease from 2 to 1. Thus the function is decreasing on (-5, -2), on (-2, 1), and on (3, 5).
  - c) For*x*-values from 2 to 3, *y* is 2. Thus the function is constant on (2, 3).

- 5. a) Forx-values from-∞ to-8, the y-values increase from-∞ to2. Also, for x-values from-3 to -2, the y-values increase from -2 to 3. Thus the function is increasing on (-∞, -8) and on (-3, -2).
  - b) For x-values from -8 to -6, the y-values decrease from 2 to -2. Thus the function is decreasing on the interval (-8, -6).
  - c) For x-values from -6 to -3, y is -2. Also, for x- values from -2 to  $\infty$ , y is 3. Thus the function is constant on (-6, -3) and on (-2,  $\infty$ ).

- 6. a) Forx-valuesfrom1to4,they-valuesincreasefrom2 to11.Thusthe functionisincreasingontheinterval (1, 4).
  - b) For x-values from -1 to 1, the y-values decrease from 6 to 2. Also, for x-values from 4 to ∞, the y-values decrease from 11 to -∞. Thus the function is decreasing on (-1, 1) and on (4, ∞).
  - c) For x-values from  $-\infty$  to -1, y is 3. Thus the function is constant on  $(-\infty, -1)$ .
- 7. The x-values extend from -5 to 5, so the domain is [-5, 5]. The y-values extend from -3 to 3, so the range is [-3, 3].
- 8. Domain: [-5, 5]; range: [1, 4]
- 9. The *x*-values extend from -5 to -1 and from 1 to 5, so the domain is [-5, -1] ∪ [1, 5].
  The *y*-values extend from -4 to 6, so the range is [-4, 6].

They-valuesextenditorin 4 to 0, somerangers

- **10.** Domain: [-5, 5]; range: [1, 3]
- **11.** The *x*-values extend from  $-\infty$  to  $\infty$ , so the domain is

```
(−∞, ∞). They-
```

values extendfrom- $\infty$ to3,sotherangeis(- $\infty$ ,3].

- **12.** Domain: (-∞,∞); range: (-∞,11]
- **13.** From the graph we see that a relative maximum value of the function is

3.25. It occurs at x = 2.5. There is no relative minimum value.

The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point, the graph decreases. Thus the function is increasing on  $(-\infty, 2.5)$  and is decreasing on  $(2.5, \infty)$ .

14. From the graph we see that a relative minimum value of 2 occurs atx=1. There is no relative maximum value.

The graph starts falling, or decreasing, from the left and stops decreasing at the relative minimum. From this point, the graph increases. Thus the function is increasing on  $(1, \infty)$  and is decreasing on  $(-\infty, 1)$ .

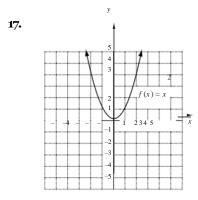
**15.** From the graph we see that a relative maximum value of the function is

2.370. It occurs at x = 0.667. We also see that **a** relative minimum value of 0 occursat x = 2.

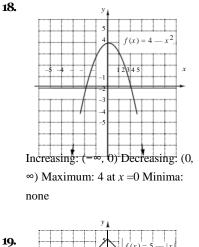
The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point it decreases to the relative minimum and then increases again. Thus the function is increasing on  $(-\infty, -0.667)$  and on  $(2, \infty)$ . It is decreasing on (-0.667, 2).

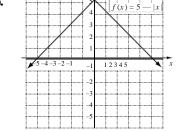
**16.** From the graph we see that a relative maximum value of 2.921 occurs at x = 3.601. A relative minimum value of 0.995 occurs at x = 0.103.

The graph starts decreasing from the left and stops de- creasing at the relativeminimum. From this point itin- creases to the relative maximum and then decreases again. Thus the function is increasing on (0.103, 3.601) and is de- creasing on  $(-\infty, 0.103)$  and on  $(3.601, \infty)$ .

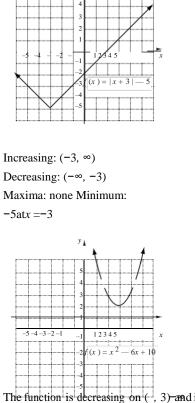


The function is increasing on (0, ) and decreasing on (, 0). We





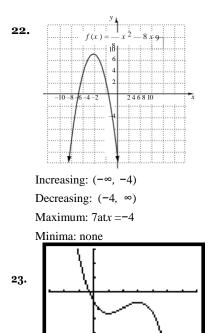
The function is increasing on (, 0)—and decreasing on (0, ). We estimate that the maximum is 5 at x = 0. There are no minima.



20.

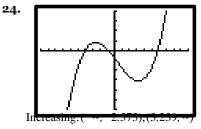
21.

The function is decreasing on (1, 3) and increasing on (3, ). We estimate that the minimum is 1 at x = 3. There are no maxima.

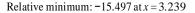


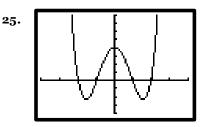
Beginning at the left side of the window, the graph first drops as we move to the right. We see that the function is

decreasing on (, Herewitzer the find that the function is increasing on (1, 3) and decreasing again on (3, ). The MAXIMPUM and MINIMUM features also show that the relative maximum x=4 at x=3 and the relative minimum is -8 at x=1.



Decreasing: (-2.573, 3.239) Relativemaximum: 4.134atx =-2.573

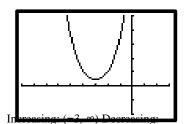




We find that the function is increasing on (1.552, 0) and on (1.552, ) and decreasing on (, 1.552) and on ( $\theta_{10}$  1-552). The relative maximum is 4.07 at x = 0 and the relative minima are 2.314 at x =

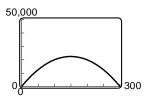
1.552 and 2.314 at x = 1.552.

26.



 $(-\infty, -3)$  Relative maxima: none Relative minimum: 9.78 at x = -3

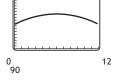
**27.** a) 
$$y = -x^2 + 300x + 6$$



b) 22, 506 at *a* = 150

c) The greatest number of baskets will be sold when \$150 thousand is spent on advertising. For that amount,

**28.** a)  $y = -0.1x^2 + 1.2x + 98.6$ 



- b) Using the MAXIMUM feature we find that the rel- ative maximum is 102.2 at t=6. Thus, we know that the patient's temperature was the highest at t=6, or 6 days after the onset of the illness and that the highest temperature was  $102.2^{\circ}$  F.
- **29.** Graph  $y = \frac{8x}{x^2 + 1}$ Increasing: (-1, 1) Decreasing: (- $\infty$ , -1), (1,  $\infty$ ) <u>-4</u> **30.** Graph  $y = \frac{-4}{x^2 + 1}$ Increasing: (0,  $\infty$ ) Decreasing: (- $\infty$ , 0) **31.** Graph y = x 4 -  $x^2$ , for -2  $\le x \le 2$ . Increasing: (-1.414, 1.414) Decreasing: (-2, -1.414), (1.414, 2) **32.** Graph y = -0.8x 9 -  $x^2$ , for -3  $\le x \le 3$ .
- **32.** Graph  $y = -0.8x \ 9 x^2$ , for  $-3 \le x \le 3$ . Increasing: (-3, -2.121), (2.121, 3)Decreasing: (-2.121, 2.121)
- **33.** If x = the length of the rectangle, in meters, then the  $\frac{480-2x}{2}$  width is  $2^{-1}$ , or 240-x. We use the formula Area=

length  $\times$  width:

$$A(x) = x(240 - x)$$
, or  
 $A(x) = 240x - x^2$ 

**34.** Let h=theheight of the scarf, in inches. Then the length of the base = 2h - 7.

$$A(h) = \frac{1}{2}(2h - 7)(h)$$
$$A(h) = h^2 - \frac{7}{2}h$$

**35.** After*t* minutes, the balloon has risen 120*t* ft. We use the Pythagorean theorem.

 $[d(t)]^2 = (120t)^2 + 400^2$ 

 $d(t) = (120t)^2 + 400^2$ 

We considered only the positive square root since distance must be nonnegative.

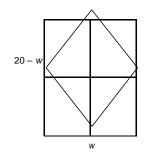
**36.** Use the Pythagorean theorem.  $[h(d)]^2$ +  $(3700)^2 = d^2$ 

$$[h(d)]^2 = d^2 - 3700^2$$
  
22,506 baskets will be sold

$$h(d) = \sqrt[4]{d^23700}$$
 Taking the positive square root

**37.** Let w = the width of the rectangle. Then the

length= $\frac{40-2w}{2}$  or 20-w. Divide the rectangle into quadrants as shown below.



In each quadrant there are two congruent triangles. One triangle is part of the rhombus and both are part of the rectangle. Thus, in each quadrant the area of the rhombus is one-half the area of the rectangle. Then, in total, the area of the rhombus is one-half the area of the rectangle.

$$A(w) = \frac{1}{2}(20 - w)(w)$$
$$A(w) = 10w - \frac{w^2}{2}$$

**38.** Let w = the width, in feet. Then the length =  $\frac{46-2w}{2}$ ,

or 23 – *w*.

$$A(w) = (23 - w)w$$
$$A(w) = 23w - w^2$$

**39.** We will use similar triangles, expressing all distations in feet. 6 in  $=^{-1}$  ft, s in  $=^{-5}$  ft, and d vd = 3d ft We

1

have

$$\frac{3d}{3d} = 2 \frac{1}{2}$$

$$7 \frac{s}{12}$$

$$\frac{1}{12} \cdot 3d = 7 \cdot 2$$

$$\frac{sd}{-4} = \frac{7}{2}$$

$$d = \frac{4}{2} \cdot \frac{7}{2}$$
so
$$\frac{14}{4}$$

$$d(s) = \frac{1}{2}$$

**40.** The volume of the tank is the sum of the volume of a sphere with radius *r* and aright circular cylinder with radius *r* and height 6 ft.

$$V(r) = \frac{4}{3}\pi r^3 + 6\pi r^2$$

**41.** a) If the length = x feet, then the width = 30 - x feet.

$$A(x) = x(30 - x)$$

- $A(x) = 30x x^2$
- b)The length of the rectangle mustbe positive and less than 30 ft, so the domain of the function is  $\{x|0 < x < 30\}$ , or (0, 30).

c) We see from the graph that the maximum value of the area function on the interval (0, 30) appears to be 225 when x = 15. Then the dimensions that yield the maximum area are length = 15 ft and width = 30 - 15, or 15 ft.

**42.** a) 
$$A(x)=x(360 - 3x)$$
, or  $360x - 3x^2$ 

c) The maximum value occurs when x = 60 so the width of each corral should be 60 yd and the total lengt-h-of the two corralsshouldbe 360 3 60, or 180 yd.

Σ

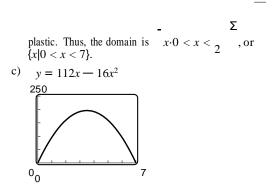
 $\overline{3}$ , or

**43.** a) If the height of the file is x inches, then the width is 14 2xinches-and the length is 8 in. We use the formula Volume = length width height to find the **x**olume of the file. V(x) = 8(14 - 2x)x or

$$V(x) = 8(14 - 2x)x,$$

$$V(x) = 112x - 16x^2$$

b) The height of the file must be positive and less than half of the measure of the long side of the piece of 14



- d) Using the MAXIMUM feature, we find that the maximum value of the volume function occurs when x = 3.5, so the file should be 3.5 in. tall.
- **44.** a) When a square with sides of length x is cut from each corner, the length of each of the remaining sides of the piece of cardboard is 12 - 2x. Then the di-mensions of the box are x by 12 - 2x by 12 - 2x. We use the formula Volume = length × width × height

to find the volume of the box:  

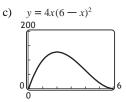
$$V(x) = (12-2x)(12-2x)(x) V(x)$$
  
 $= (144-48x+4x^2)(x) V(x) =$   
 $144x-48x^2+4x^3$ 

This can also be expressed as  $V(x)=4x(x-6)^2$ , or  $V(x)=4x(6-x)^2$ .

b) The length of the sides of the square corners that are cut out must be positive and less than half the length of a side of the piece of cardboard. Thus, the domain of the function is  $\{x|0 < x < 6\}$ , or (0, 6).

2

#### **Exercise Set 2.1**



d)Using the MAXIMUM feature, we find that the maximum valueofthevolumeoccurswhen x = 2.

When x = 2, 12, 2x = 12, 22 = 8, so the dimensionsthatyieldthemaximumvolumeare 8cmby 8 cm by 2 cm.

45. a) The length of a diameter of the circle (and a di- agonal of the rectangle) is  $2 \cdot 8$ , or 16 ft. Let l =the length of the rectangle. Use the Pythagorean theorem to write *l* as a function of *x*.

$$x^2 + l^2 = 16^2$$

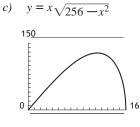
$$x^{2} + l^{2} = 256$$
$$l^{2} = 256 - x^{2}$$
$$l = 256 - x^{2}$$

Since the length must be positive, we considered only the positive square root.

UsetheformulaArea=length **x** widthtofindthe area of the restangle:

$$A(x) = x \ 256 - x^2$$

b) The width of the rectangle must be positive and less than the diameter of the circle. Thus, the domain of the function is  $\{x | 0 < x < 16\}, \text{ or } (0, 16).$ 



0

d) Using the MAXIMUM feature, we find that the max- imum area\_ ∞<u>ccurs</u> <u>when x</u> <u>is about 11.314</u>. When x ≈ 11.314.

Thus the dimensions that maximize the area are about 11.314 ft by 11.313 ft. (Answers may vary slightly due to rounding differences.)

х

**46.** a)Let
$$h(x)$$
=theheightofthebox. 320 =  $x$ 

b)Thelengthofthebasemustbepositive, so the do- main of the function is  $\{x | x > 0\}$ , or  $(0, \infty)$ .

c) 
$$y = 2.5x^2 + \frac{3200}{x}$$
  
1000 20

d) Using the MIMIMUM feature, we find that the minimum cost occurs when x 8.618. Thus,  $\approx$  the dimensions that minimize the cost areabout 320

 $(\overline{8.618})^2$ , or about 4.309 ft. 8.618ftby8.618ftby

47. x + 4, for  $x \le 1, 8 -$ 

$$g(x) = x, \text{ for } x > 1$$
  
Since  $-4 \le 1, g(-4) = -4+4 = 0.$   
Since  $0 \le 1, g(0) = 0+4 = 4.$   
Since  $1 \le 1, g(1) = 1+4 = 5.$   
Since  $3 > 1, g(3) = 8-3 = 5.$ 

**48.** 
$$f(x) = \begin{bmatrix} 3, & \text{for } x \le -2, \\ & \Box \ \frac{1}{2} x + 6, \text{ for } x > -2 \\ f(-5) = 3 \end{bmatrix}$$
  
 $f(-2) = 3$   
 $f(-2) = 3$   
 $f(0) = 2 \cdot \frac{1}{0} + 6 = 6$   
 $f(2) = 2 \cdot 2 + 6 = 7$   
 $- 3x - 18, \text{ for } x < -5,$   
**49.**  $h(x) = 1, \qquad \text{for } -5 \le x < 1, \\ x + 2, \qquad \text{for } x \ge 1$   
Since -5 is in the interval  $[-5, 1), h(-5) = 1$ . Since 0 is in the interval  $[-5, 1), h(0) = 1$ .  
Since  $1 \ge 1, h(1) = 1 + 2 = 3$ .  
Since  $4 \ge 1, h(4) = 4 + 2 = 6$ .  
 $\Box -5x - 8, \text{ for } x < -2,$   
**50.**  $f(x) = \Box -x + 5, \qquad \text{for } -2 \le x \le 4,$   
 $\Box 2$   
 $10 - 2x, \qquad \text{for } x > 4$   
Since  $-4 < -2, f(-4) = -5(-4) - 8 = 12$ .

1[**-**2,4],*f*(-

Since 
$$-2$$
 is in the interval  $[-2, 4]$ .  $f(-$ 

 $2) = \frac{1}{2}(-2) + 5 = 4.$ 

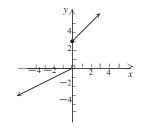
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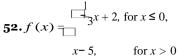
$$C(x) = 1.5x^{2} + +4(2.5) \quad \frac{320}{x} + 1 \cdot x^{2}$$
$$C(x) = 2.5x^{2} + \frac{3200}{x}$$

Since 4 is in the interval[-2,4],  $f(4) = {1 \choose 4} \cdot 4 + 5 = 7$ . Since 6 > 4, f (6) = 10 - 2 \cdot 6 = -2.

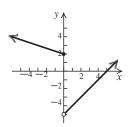
**51.** 
$$f(x) = \frac{2}{2}x$$
, for  $x < 0$ ,  
 $(x + 3)$ , for  $x \ge 0$ 

We create the graph intwo parts. Graph f(x) = x for 2 inputs *x* less than 0. Then graph f(x) = x+3 for inputs *x* greater than or equal to 0.





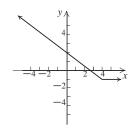




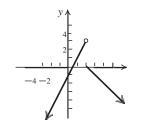
**53.** 
$$f(x) = \frac{\Box_4 x + 2}{\Box_1}$$
, for  $x < 4$ ,  
 $\Box_1$ , for  $x \ge 4$ 

We create the graph in two parts. Graph  $\frac{3}{3}$ f(x) = -x + 2 for inputs x less than 4. Then graph

f(x) = -1 for inputs x greater than or equal to 4.



2x - 1, for x < 2.254. for  $x \ge 2$ - x. h(x) =

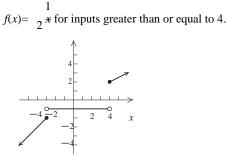


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$$x + 1$$
, for  $x \le -3$ ,

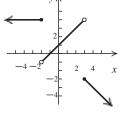
**55.** 
$$f(x) = -1$$
, for  $-3 < x < 4$   
 $1 = -3$ , for  $x \ge 4$ 

We create the graph in three parts. Graph f(x) = x + 1- 3. Graph f(x) =- 1 forinputs*x* lessthanorequalto



$$4, \quad \text{for } x \leq -2,$$

**56.** 
$$f(x) = -x$$
 for  $x \ge 3^+ 1$ , for



$$\Box$$

$$\frac{1}{2}x - 1, \text{ for } x < 0,$$

$$\Box$$
for  $0 \le x \le 1$ 

**57.** g(x) =3

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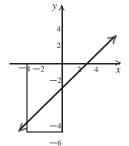
$$2x, \qquad \text{for } x > 1$$

1 We create the graph in three parts. Graph g(x) = x - 12 for inputs less than 0. Graph g(x) = 3 for inputs greater than or equal to 0 and less than or equal to 1. Then graph g(x) = -2x for inputs greater than 1.

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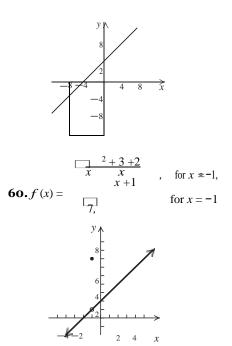
2 4 x --4

**58.** 
$$f(x) = \bigcup_{\substack{x = -3, \\ y = -3}}^{2} \text{ for } x = -3, \text{ for } x = -3$$



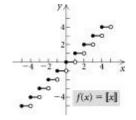
2, for 
$$x=5$$
,  
59.  $f(x) = \frac{2}{x^2-25}$   
When  $x \approx 5$ , for  $x \approx 5$   
When  $x \approx 5$ , the denominator of  $(x^2 - 25)/(x - 5)$  is  
nonzerosowecansimplify:  
 $\frac{x^2-25}{x} (x+5)(x-5) +5$ .  
 $x = x + 5$ , for  $x \approx 5$   
Thus,  $f(x) = x + 5$ , for  $x \approx 5$ .

The graph of this part of the function consists of a line with a "hole" at the point (5, 10), indicated by an open dot. At x = 5, we have f(5) = 2, so the point (5, 2) is plotted below the open dot.



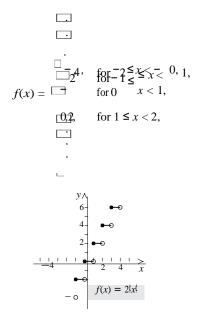


See Example 9.



#### **62.** f(x) = 2[[x]]

This function can be defined by a piecewise function with an infinite number of statements:



**63.** f(x) = 1 + [[x]]

This function can be defined by a piecewise function with an infinite number of statements:



 $-4 g(x) = 1 + \xi x \xi$ 

**64.**  $f(x) = \frac{1}{2}[[x]] - 2$ 

This function can be defined by a piecewise function with an infinite number of statements:

$$f(x) = \begin{array}{c} 2 \\ -2^{1}, \text{ for } -1 \le x < 0, \\ f(x) = \begin{array}{c} -2^{1}, \text{ for } 0 \le x < 1, \\ -1^{1}, \text{ for } 1 \le x < 2, \\ \\ 1, \text{ for } 2 \le x < 3, \\ \\ \end{array}$$

65. From the graph we see that the domain is ( ) and <u>−∞</u>∞ the range is  $\begin{pmatrix} 0 & 0 \\ -\infty & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ .

**66.** Domain: (-∞, ∞); range: (-5, ∞)

- **67.** From the graph we see that the domain is  $(-\infty, \infty)$  and the range is [−1, ∞).
- **68.** Domain:  $(\infty, \infty)$ ; range:  $(-\infty, 3)$

 $-\infty, \infty$  ) and 69. From the graph we see that the domain is (

therangeis{ $y | y \leq -2 \text{ or } y = -1 \text{ or } y \geq 2$ }.

**70.** Domain: (-∞,∞);range: (-∞,-3]U (-1,4] 71. From the graph we see that the domain is ( ) and <u>−∞</u>∞ therangeis 5 24

$$\{-, -, \}.$$
 An equation for the function is:  

$$- 2, \text{ for } x < 2,$$

$$f(x) = 5, \text{ for } x$$

$$4, \text{ for } x > 2$$

**72.** Domain:  $(-\infty, \infty)$ ; range:  $\{y | y = -3 \text{ or } y \ge 0\}$ 

$$\begin{array}{c} -3, \text{ for } x < 0, x, \\ g(x) = & \text{ for } x \ge 0 \end{array}$$

73. From the graph we see that the domain is (, ) and the range is (, 1] [2, ). Finding the slope of each segment and using the slope-intercept orpoint-slope for- mula, we find that an equation for the function is:

 $\{y|y = -2 \text{ or } y \ge \}0$ . An **74.** Domain:  $(-\infty, \infty)$ ; range: equation for the functionis:

$$\begin{array}{c} -(x) = -(x), & \text{for } x < 3, \\ h x = -2, & \text{for } x \ge 3 \\ \end{array}$$
 This can also be expressed as follows:

$$for x \le 0,$$
  
()= 3,  
h x x, for  $0 < x <$   
-2, for  $x \ge 3$   
It can also be expressed as follows:  
for  $x < 0$ .

$$h(x) = -x,$$
  
 $h(x) = x, \text{ for } 0 \le x < 3,$   
 $-2, \text{ for } x \ge 3$ 

**75.** From the graph we see that the domain is [5,3] and the range is (3,5). Finding the slope of each segment and using the slope-intercept or point-slope formula, we find that an equation for the function is:

$$\begin{array}{rrrr} x+8, & \text{for } -5 \leq x < -3, \\ & -\leq & \leq \\ h(x) = & 3x-6, & \text{for } \hat{p} < x \frac{\log 7}{3} \end{array}$$

**76.** Domain: [−4, ∞); range: [−2, 4]

$$f(x) = \begin{array}{c} -2x - 4, \text{ for } -4 \leq x \leq -1 \\ 2, & \text{ for } x \geq 2 \end{array}$$

This can also be expressed as:

$$f(x) = \begin{cases} 2x - 4, \text{ for } -4 \le x < -1 \\ -5 \le 2, & \text{for } x \ge 12 \end{cases}$$

**77.** 
$$f(x) = 5x^2 - 7$$

-

a) 
$$f(-3) = 5(-3)^2 - 7 = 5 \cdot 9 - 7 = 45 - 7 = 38$$
  
b)  $f(3) = 5 \cdot 3^2 - 7 = 5 \cdot 9 - 7 = 45 - 7 = 38$   
c)  $f(a) = 5a^2 - 7$   
d)  $f(-a) = 5(-a)^2 - 7 = 5a^2 - 7$ 

**78.** 
$$f(x) = 4x - 5x$$
  
a)  $f(2) = 4 \cdot 2^3 - 5 \cdot 2 = 4 \cdot 8 - 5 \cdot 2 = 32 - 10 = 22$   
b)  $f(-2) = 4(-2)^3 - 5(-2) = 4(-8) - 5(-2) = -32 + 10 = -22$   
c)  $f(a) = 4a^3 - 5a$   
d)  $f(-a) = 4(-a)^3 - 5(-a) = 4(-a^3) - 5(-a) = -4a^3 + 5a$ 

- **79.** First find the slope of the given line. 8x y =10
- x, for  $x \leq -1$ , Copyright © 2013 Pearson Education, Inc.

g(x) =

-

8x = y + 10

*x*, for  $x > 2^{2}$ , for -1

-

8x - 10 = yThe slope of the given line is 8. The slope of a line per-pendicular to

This can also be expressed as follows:

$$x$$
, for  $x \leq -1$ ,

 $g(x) = x, \text{ for } x \ge 22, \text{ for } 1$ 

this line is the opposite of the reciprocal of 8, or  $\frac{1}{2}$ .

 $y - y_{1} = m(x - x_{1})$   $y - 1 = -\frac{1}{[x - (-1)]}$  8  $y - 1 = -(x_{8}^{1} + 1)$  1  $y - 1 = -\frac{1}{8}x = \frac{1}{8} - \frac{1}{9}x - \frac{1}{8}x = \frac{1}{8}$  $y = -\frac{1}{8}x + \frac{7}{8} - \frac{1}{8}x - \frac{7}{8}x - \frac{1}{8}x = \frac{1}{8}x - \frac{1}{8}x - \frac{1}{8}x = \frac{1}{8}x - \frac$ 

**61.** Graph  $y = x^{2} + 4x^{2} - 50x^{2} - 100x + 400$  increasing: (-. -2), (4,  $\infty$ )

Decreasing:  $(-\infty, -5)$ , (-2, 4) Relative

maximum: 560 atx = -2

Relativeminima: 425atx = -5, -304atx = 4

**82.** Graph  $y = 3.22x^5 - 5.208x^3 - 11$ 

Increasing:  $(-\infty, -0.985), (0.985, \infty)$ Decreasing: (-0.985, 0.985)Relativemaximum: -9.008atx = -0.985Relative minimum: -12.992 at x = 0.985

**83.** a) The function C(t) can be defined piecewise.

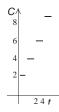
$$2, \text{ for } 0 < t < 1,$$

$$\Box_{4}^{4}, \text{ for } 1 \le t < 2,$$

$$G_{6}, \text{ for } 2 \le t < 3,$$

$$C(t) = \frac{1}{2}$$

We graph this function.



b)Fromthedefinition of the function in part (a), we see that it can be written as

**84.** If[[x + 2]]=-3,then-3 $\leq x+2 < -2$ ,or -5  $\leq x < -4$ . The possible inputs for *x* are  $\{x|-5 \leq x < -4\}$ .

C(t) = 2[[t]] + 1, t > 0.

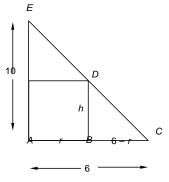
**85.** If  $[[x]]^2 = 25$ , then [[x]] = 5 or [-[x]] = 5. For

**86.** a) The distance from A to S is 4 - x. Using the Pythagorean  $t \not\!\!/ e orem$ , we find that the

> distance from S to C is Then C(x) = 3000(4-x) + 5000  $\sqrt{1 + x^2}$ . 3000x + 5000  $1 + x^2$ .

b) Use a graphing calculator to graph y = 12,000 - 3000x + 5000  $1 + x^2$  in a window such as [0, 5, 10, 000, 20, 000], Xscl = 1, Yscl = 1000. Using the MINIMUM feature, we findthat costismini- mized when x = 0.75, so the line should come to shore 0.75 mi from *B*.

**87.** a) We add labels to the drawing in thetext.



We write a proportion involving the lengths of the sides of the similar triangles BCD and ACE. Then we solve it for h.

$$\frac{h}{6-r} = \frac{10}{6}$$

$$\frac{10}{5}$$

$$h = \frac{10}{6}(6-r) = \frac{10}{3}(6-r)$$

$$h = \frac{30-5r}{3}$$
Thus,  $h(r) = \frac{30-5r}{3}$ .

b) 
$$V = \pi r^{2} h \frac{1}{30 - 5r} \Sigma$$

$$V(r) = \pi r^{2} \frac{1}{30 - 5r} V(r) = \pi r^{2} \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r} V(r) = \frac{1}{30 - 5r} V(r) + \frac{1}{30 - 5r$$

c) We first express r interms of h. 
$$h = \frac{30}{100}$$

$$\frac{-5r}{3}$$

$$3h = 30-5r$$

$$5r = 30-3h$$

$$r = \frac{30-3h}{5}$$

$$V = \pi r^{2}h$$

$$\frac{\Sigma}{30} = \frac{-3h}{V} 5h \pi$$
Substituting for r
$$\frac{30-3h}{V} = 3h$$

5

We can also write  $V(h) = \pi h$ 

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 $-5 \le x < -4$ , [[x]] = 5.-For  $5 \le x < 6$ , [[x]] = 5. Thus, the possible inputs for x are  $\{x|-5 \le x < -4 \text{ or } 5 \le x < 6\}$ .

#### **9.** (g - f)(-1) = g(-1) - f(-1)Exercise Set 2.2 $= [2(-1) + 1] - [(-1)^2 - 3]$ =(-2+1)-(1-3)**1.** (f + g)(5) = f(5) + g(5)= -1 - (-2) $=(5^2 - 3) + (2 \cdot 5 + 1)$ = -1+2= 25 - 3+ 10+1 = 1 = 33 1 **2.** $(fg)(0) = f(0) \cdot g(0)$ 10. ( g/f) $-\frac{1}{2}\sum_{g=0}^{2} \frac{\sum_{g=0}^{2}}{2}$ $=(0^2-3)(2\cdot 0+1)$ $= \frac{1 \Sigma}{\frac{f}{2 - f} + \frac{\Sigma}{12}}$ $= \frac{2 \frac{1}{2} \frac{1}{2}}{\Sigma}$ = -3(1) = -3**3.** (f - g)(-1) = f(-1) - g(-1) $=((-1)^2-3)-(2(-1)+1)$ $= -\frac{\overline{0}_{2}}{1\Gamma} - 3$ =-2-(-1)=-2+1 =-1 $\overline{4}$ **4.** $(fg)(2) = f(2) \cdot g(2)$ = 0 $=(2^2 - 3)(2 \cdot 2 + 1)$ **11.** $(h - g)(-4) = h(-4) - g(-4)_{\sqrt{2}}$ $= 1 \cdot 5 = 5$ $= (-4 + \sqrt{4}) = -4 - 1$ = 0 - -5 $-\frac{1}{1}\sum f_{-2}$ **5.** ( f/g) $-2 = \overline{1}$ -5isnotarealnumber,(h-g)(-4)doesnotexist. **12.** $(gh)(10) = g(10) \cdot h(10)$ $=\frac{10^{9}-1(10+4)}{10}$ = 9(14)2 - 2 + 1 $\frac{1}{2} - 3$ = 3 14= 42 **13.** $(g/h)(1) = \frac{g(1)}{2}$ $=\frac{4}{-1+1}$ k(1) <u>\_ 11</u> 4 = 1+40 $\sqrt{}$ 1 0 Since division by 0 is not defined, (f/g) - 2doesnot 5 exist. $=\frac{0}{5}=0$ **6.** (f - g)(0) = f(0) - g(0)**14.** $(h/g)(1) = {h(1)}$ $= (0^2 - 3) - (2 \cdot 0 + 1)$ $\Sigma^{= -3 - 1 = -4} \sum_{\Sigma = -\infty} \Sigma$ g(1) $7 \cdot (fg) - {1 \over 2} = f - {1 \over 2} \cdot g - {1 \over 2} - f - {1 \over 2} - {1 \over 2} \cdot g - {1 \over 2} - {1 \over 2}$ 2 $= \frac{\Sigma}{2} - \frac{1}{2} \frac{\Sigma}{2} - \frac{\Sigma}{32} - \frac{1}{2} \frac{\Sigma}{2} - \frac{1}{32} \frac{\Sigma}{2} - \frac{1}{1} \frac{\Sigma}{1} \frac{\Sigma}{1$ 5 Since division $b^0 y 0$ is not defined, (h/g)(1) does not exist.

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-2

**15.** 
$$(g+h)(1) = g(1) + h(1)$$

**8.** (f/g)(-

$$\begin{array}{c} \sqrt{1} & -\frac{4}{3}, \\ 3 & = \frac{f(-3)}{2}, \\ g(3) & \sqrt{3}, \\ (\sqrt{3})^2, 3 \\ -\sqrt{2}, \\ -\sqrt{2}, \\ \end{array}$$

$$\begin{array}{rcl}
-2 \ 3+1 &=& 0+5 \\ &=& 0+ \\ 5 &=& 5 \\ g(3) \\ &=& \\ &(3+ \\ 4) \ 3 & 1 \\ &=& 7 \ 2 \end{array}$$

**17.** f(x) = 2x + 3, g(x) = 3 - 5xa) The domain of *f* and of *g* is the set of all real numbers, or  $(-\infty, \infty)$ . Then the domain of f + g, f - g, ff, 3 and  $fg \text{ isalso}(-\infty,\infty)$ . For f/g we must exclude 5since g = 0. Then the domain of f/g is  $\begin{array}{c} -2 \operatorname{since}_{\Sigma} f_{2}^{3} = 0.3 \operatorname{The domain of } g/f \text{ is} \\ \text{b)} \quad -\infty, -2 \quad \cup \quad -2, \infty \end{array}$  $(f+g)(3x_x) = f(x)+g(x)=(2x+3)+(3-$ 5x) =(f-g)(x)=f(x)-g(x)=(2x+3)-(3-5x)=2x + 3 - 3 + 5x = 7x $(fg)(x) = f(x) \cdot g(x) = (2x + 3)(3 - 5x) =$  $6x - 10x^2 + 9 - 15x = -10x^2 - 9x + 9$ (ff)(x) = f(x) f(x) = (2x+3)(2x+3) = $4x^{2} + 12x + 9 = 4x^{2} + 3x^{2} +$  $(g/f)(x) = \frac{g(x)}{g(x)} = \frac{3-5x}{3-5x}$ f(x) = 2x+3**18.** f(x) = -x + 1, g(x) = 4x - 2a) The domain of f, g, f + g, f - g, fg, and ff is - Σ2  $(-\infty, \infty)$ <u>1</u>. Since <u>1</u> $g^{-1} = 0$ , the domain of f/g is Σ. Σ b)  $g \not f$  is  $(f \rightarrow 0, 1) \ge 0$  (1, Since f(1) = 0, the domain of (f+g)(x) = (-x+1) + (4x-2) = 3x - 1(f - g)(x) = (-x + 1) - (4x - 2) =-x + 1 - 4x + 2 = -5x + 3 (fg)(x  $=(-x+1)(4x-2)=4x^{2}$ +6x-2 $(ff)(x) = (-x+1)(-x+1) = x^2 - 2x + 1$  $(f/g)(x) = \frac{-x+1}{2}$ 4x - 2 $(g/f)(x) = \frac{4x - 2}{2}$ *−x* +1

**19.** f(x) = x - 3, g(x) = x + 4

a) Any number can be an input in f, so the domain of

*f* is the set of all real numbers, or  $(-\infty, \infty)$ .

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The domain of f/g is the set of all numbers in the domains of f and g, excluding those for which g(x)=0. Since g(-4)=0, the domain of f/g is  $(-4, \infty)$ .

The domain of g/f is the set of all numbers in the domains of g and f, excluding those for which f(x) = 0. Since f(3) = 0, the domain of g/f is  $[-4, 3) \cup (3, \infty)$ .

b) 
$$(f+g)(x)=f(x)+g(x)=x-3+x\sqrt{44} \sqrt{2}$$
  
 $(f-g)(x)=f(x)-g(x)=x-\sqrt{3}-x+4$   
 $(fg)(x)=f(x) \cdot g(x)=(x-3)x+4$   
 $(ff x \sum f(x)^2 = (x-3)^2 = x^2 - 6x + 9$   
 $x-3$   
 $\Sigma$   
 $(f/g)(x)=g(x) = \sqrt{x+4} \sqrt{2}$   
 $(g/f)(x)=g(x) = \sqrt{x+4} \sqrt{2}$   
 $(g/f)(x)=g(x) = \sqrt{x+4} \sqrt{2}$   
 $\sqrt{2}$ 

**20.** f(x) = x + 2, g(x) = x - 1

a) The domain of *f* is (-∞, ∞). The domain of *g* consists of all the values of *x* for which *x* − 1 is nonnegative, or [1, ∞). Thenthedomainof

$$f + g$$
,  $f - g$ , and  $fg$  is  $[1, \infty)$ . The domain of  $ff$  is  $(-\infty, \infty)$ . Since  $g(1) = 0$ , the domain of  $f/g$  is  $(1, \infty)$ . Since  $f(-2) = 0$  and  $-2$  is not in the domain of

g, the domain of 
$$g/f$$
 is  $[1, \infty)$ .  
b)  $(f+g)(x)=x+2+\sqrt{x-1}(f-g)(x)=x+2-\sqrt{x+1}$   
 $fg x x \sqrt{x-1}(f-g)(x)=(x+2)(x+2)=x^2+4x+4$   
 $(ff)(x)=(x+2)(x+2)=x^2+4x+4$ 

$$(f/g)(x) = \sqrt[]{\frac{x-1}{x-1}}$$

$$(g/f)(x) = \frac{\sqrt{x-1}}{x-1}$$

**21.**  $f(x) = 2x - 1, g(x) \stackrel{x}{=} \frac{1}{2} 2x^2$ 

a) The domain of f and of g is (, ). Then the domain of f + g, f g, fg, and ff is (, ). For f/g, we must-exclude 0 since g(0) = 0. The domain of f/g is  $(-\infty, 0) \cup (0, \infty)$ . For g/f, we

must exclude 
$$\frac{1}{\operatorname{since} f}$$
  $\frac{1}{2} = 0$ . The domain of  
 $\frac{1^2}{2} = \frac{1}{2} = \frac{1}{2}$   
 $g/f$  is  $\frac{1}{2} = \frac{1}{2} = \frac{1}{2}$ 

The domain of g consists of all values of x for which x+4 is nonnegative, so we have  $x+4 \ge 0$ , or  $x \ge -4$ . Thus, the domain of g is  $[-4, \infty)$ .

The domain of f + g, f g, an-df g is the set of all numbers in the domain sofboth f and g. This is  $[-4, \infty)$ .

The domain of *ff* is the domain of *f*, or  $(-\infty, \infty)$ .

b) 
$$(f + g)(x) = f(x) + g(x) = (2x - 1) + (-2x^2) = -2x^2 + 2x - 1(f - g)(x) = f(x) - g(x) = (2x - 1) - (-2x^2) = 2x^2 + 2x-1(fg)(x) = f(x) \cdot g(x) = (2x - 1)(-2x^2) = -4x^3 + 2x^2(ff)(x) = f(x) \cdot f(x) = (2x - 1)(2x - 1) = 4x^2 - 4x + 1(f/g)(x) = \frac{f(x)}{x} = \frac{2x - 1}{g(x)} = \frac{g(x)}{-2x^2}$$
  
( )( ) =  $g(x) = \frac{-2x^2}{-2x^2}$ 

g/f x = f(x) = 2x - 1

**22.**  $f(x) = x^2 - 1$ , g(x) = 2x + 5

a) The domain of f and of g is the set of all real num-bers, or  $(-\infty,\infty)$ . Then the domain of  $f+g, f-g, \Sigma$ 

$$fg \text{ and } ff \text{ is } (-\infty, \infty).$$
 Since  $g - \frac{5}{5} = 0$ , the  $\frac{2}{5}$ . Since domain of  $f/g$  is  $-\infty, -\frac{5}{5} = 0$ , the  $\frac{2}{5}$ . Since  $2 = 2$ 

f(1) = 0 and f(-

-

$$(1) (11) (1, x) = 0, \text{ the domain of } g/f \text{ is}$$
  

$$-\infty, - U - , U (1, \infty).$$
  
b)  $(f + g)(x) = x^2 - 1 + 2x + 5 = x^2 + 2x + 4 (f - g)(x) = x^2 - 1 - (2x + 5) = x^2 - 2x - 6 (fg)(x) = (x^2 - 1)(2x + 5) = 2x^3 + 5x^2 - 2x - 5 (ff)(x) = (x^2 - 1)^2$   

$$= x^4 - 2x^2 + 1$$
  

$$(1) (x) = x^2 - 1$$

$$f/g \quad x \quad 2x + 5 \\ (g/f)(x) = \frac{2x + 5}{x^2 - 1} \\ \sqrt{\frac{x^2 - 1}{x^2 - 3}} \\ \mathbf{23.} f(x) = \frac{x - 3}{x - 3} \\ g(x) = \frac{x + 3}{x - 3}$$

a) Since f(x) is nonnegative for values of x in [3, ), this is the domain of f. Since g(x) is nonnegative for values of x in [-3,  $\infty$ ), this is the domain of g. The domain of f+g, f-g, and fg is the intersection of the domains of f and g, or  $[3, \infty)$ . The domain

of *ff* is the same as the domain of f, or  $[3, \infty)$ . For f/g, we must exclude -3 since g(-3) = 0. This is not in [3,  $\infty$  ), so the domain of f/g is [3, ∞ ). For g/f, we must exclude  $3 \operatorname{since} f(3) = 0$ . The domain

of g/f is 
$$(3, \infty)$$
.  
b)  $(f + g)(x) = f(x) + g(x) = \underline{x - 3} + x + 3$   
 $(f - g)(x) = f(x) - g(x) = \frac{\sqrt{x - 3}}{\sqrt{x - 3}} + \frac{\sqrt{x - 3}}{\sqrt{x + 3}}$   
 $(fg)(x) = f(x) \cdot g(x) = \frac{\sqrt{x - 3}}{\sqrt{x + 3}} + \frac{\sqrt{x - 9}}{\sqrt{x - 3}}$   
 $(ff)(x) = f(x) \cdot f(x) = x - 3 \cdot x - 3 = |x - 3|$   
 $(f/g)(x) = \sqrt{\frac{x - 3}{x + 3}}$   
 $(g/f)(x) = \sqrt{\sqrt{x - 3}} + \frac{x + 3}{x + 3}$   
**24.**  $f(x) = x, g(x) = x + 23 x$   
a) The domain of is [0]. The domain of is

g  $(-\infty, 2]$ . Then the domain of f + g, f-g, and  $\hat{fg}$  is [0,2]. The domain of ff is thesame as the domainof  $f, [0, \infty)$ . Since g(2)=0, the domain of Copyright © 2013 Pearson Education, Inc.

**25.** f(x) = x + 1, g(x) = |x|

a) The domain of f and of g is ( , ). There the domain of f+g, f g, fg, and ff is (, ). For f/g, we must-exclude 0

since  $g(0) \neq 0$ . The g(-1) = 0. The domain of f we must exclude g(-1) = 0. The domain of f we

g/f is  $(-\infty, -1) \cup (-1, \infty)$ .

b) 
$$(f + g)(x) = f(x) + g(x) = x + 1 + |x|$$
  
 $(f - g)(x) = f(x) - g(x) = x + 1 - |x|$   
 $(fg)(x) = f(x) \cdot g(x) = (x + 1)|x|$   
 $(ff)(x) = f(x) \cdot f(x) = (x+1)(x+1) = x^2 + 2x + 1)$   
 $x + 1$   
 $(f/g)(x) = |x|$   
 $|x|$   
 $|x|$ 

(g/f)(x) =x + 1**26.** f(x) = 4|x|, g(x) = 1 - x

> a) The domain of f and of g is (, ). There the domain of f+g, f, g, fg, and ff is (, ). Since g(1) = 0, the domain

of 
$$f/g$$
 is (, 1) (1, ).  $-\infty \cup \infty$   
Sincef(0)=0,the domain of  $g/f$  is  $(-\infty, 0) \cup (0, \infty)$ .  
b)  $(f+g)(x)=4|x|+1-x + (f-g)(x)=4|x|-(1-x)=4|x|-1+x$   
()()=4 (1)=4 4

$$fg' x |x| - x |x| - |x|| - |x||$$

$$(ff)(x) = 4|x| \cdot 4|x| = 16x^{2}$$

$$(f/g)(x) = 1 - x$$

$$1 - x$$

$$(g/f)(x) = 4|x|$$

**27.**  $f(x) = x^3$ ,  $g(x) = 2x^2 + 5x - 3$ 

(-∞, 0) ∪ (0, ∞).

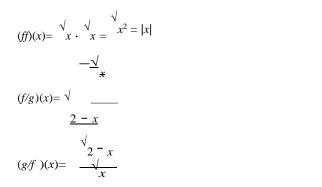
a) Since any number can be an input for either for g, the domain of f, g, f + g, f - g, fg, and ff is the set of all real numbers, or (−∞, ∞). or  $(-\infty, \infty)$ . Since g(-3) = 0 and  $g = \frac{1}{2} \sum_{\substack{n=0\\2}} \frac{1}{2} \sum_{\substack{n=0}} \frac{1}{2} \sum_{\substack{n=0}} \frac{1}{2} \sum_{\substack{n=0\\2}} \frac{1}{2} \sum_{\substack{$ is  $(-\infty, -3)$   $\cup$  -3,  $\frac{1}{2}$   $\cup$   $\frac{1}{2}$   $\infty$ . Since f(0) = 0, the domain of g/f is is(-∞,-3)∪

f/g is [0,2). Since f(0)=0, the domain of g/f is (0,2].

b) 
$$(f + g)(x) = f(x) + g(x) = x^3 + 2x^2 + 5x - 3$$
  
b)  $\sqrt[4]{y} \frac{\sqrt{y}}{\sqrt{y}} \frac{\sqrt{y}$ 

 $(f - g)(x) = f(x) - g(x) = x^{-3}(2x + 5x - 3) = x^{3} - 2x^{2} - 5x + 3$  $(fg)(x) = f(x) \cdot g(x) = x(x^{3} + 5x - 3) = 2x + 5x^{-4} + 3x^{-3}$ 

 $(ff)(x) = f(x) \cdot f(x) = x^3 \cdot x^3 = x^6$ 



$$( )( \underbrace{f(x)}_{g(x)} = x^{3} \\ f/g(x) = \frac{g(x)}{g(x)} = \frac{x^{3}}{2x^{2} + 5x - 3}$$
$$( )( \underbrace{g(x)}_{g=1} = 2x + 5x - 3 \\ g/f(x) = f(x) + 5x - 3 \\ g/f(x) = x^{3}$$

**28.**  $f(x) = x^2 - 4$ ,  $g(x) = x^3$ a) The domain of and of is ( ). Then the domain of + , f , g  $-\infty, \infty$  ). Since f g f - g f g, and f f is  $(-\infty, \infty)$ g(0) = 0, the domain of f/g is  $(-\infty, 0) \cup (0, \infty)$ .

Since 
$$f(-2)=0$$
 and  $f(2)=0$ , the domain of  $g/f$   
is  $(-\infty, -2)\cup (-2, 2)\cup (2, \infty)$ .  
b)  $(f+g)(x)=x^2-4+x^3$ , or  $x^3+x^2-4$   
 $(f-g)(x)=x^2-4-x^3$ , or  $-x^3+x^2-4$ 

$$(fg)(x) = (x^{2} - 4)(x^{3}) = x^{5} - 4x^{3}$$

$$(ff)(x) = (x^{2} - 4)(x^{2} - 4) = x^{4} - 8x^{2} + 16$$

$$x^{2} - 4$$

$$(f/g)(x) =$$

$$(f/g)(x) =$$

$$(f/g)(x) =$$

$$g/f x = \frac{x^{33}}{x^{2} - 4}$$
**29.**  $f(x) = \frac{4}{x}, g(x) = \frac{1}{x}$ 

+1 6-xa) Since x+1=0 when x=-1, we must exclude -1 from the domain of f. It is  $(-\infty, -1) \cup (-1, \infty)$ . Since 6-x=0 when x=6, we must exclude 6 from the domain of g. It is  $(-\infty, 6) \cup (6, \infty)$ . The domain of f+g, f-g, and fg is the intersection of the domain so ff and g, or  $(-\infty, -1) \cup (-1, 6)$  (6  $\infty$ ). The domain of ff is the same as the domain of f, or (, 1) (1, -1) = 8 ince there are no values of x for which g(x)=0 or

(x) = 0, the domain of f/g and g/f is  $(-\infty, -1) \cup (-1, 6)$ 

∪ (6, ∞).

f

b) 
$$(f+g)(x) = f(x) + g(x) = \frac{4}{x+1} + \frac{1}{6-x}$$

$$(f - g)(x) = f(x) - g(x) = \frac{4}{x + 1} - \frac{1}{6 - x}$$

$$(fg)(x) = f(x) \cdot g(x) = \frac{4}{x + 1} - \frac{4}{6 - x}$$

$$(fg)(x) = f(x) \cdot g(x) = \frac{4}{x + 1} - \frac{4}{6 - x} - \frac{4}{(x + 1)(6 - x)}$$

$$(ff)(x) = f(x) \cdot f(x) = \frac{4}{x + 1} \cdot \frac{4}{x} - \frac{4}{1 - 1} = \frac{16}{(x + 1)^2}, \text{ or }$$

$$\frac{16}{-x^2 + 2x + 1}$$

$$(f/g)(x) = \begin{array}{c} \underline{x+1} & \underline{4} & \underline{6-x} & \underline{4(6-x)} \\ = & \underline{-1} & x+1 & 1 & x+1 \\ & \underline{6-x} & 1 & 1 \end{array}$$

b) 
$$(f+g)(x) = 2x^2 + \frac{2}{x-5}$$
  
 $(f-g)(x) = 2x^2 - \frac{2}{x-5}$   
 $(g)(x) = 2x \cdot x - 5 = x - 5$   
 $(f)(x) = 2x^2 \cdot 2x^2 = 4x^4$   
 $\frac{x^{2-2} \cdot x - 5}{(f'g)(x)} = \frac{x-5}{2}$   
 $(g/f)(x) = \frac{x-5}{2} = \frac{1}{x-5}$   
 $(g/f)(x) = \frac{x-5}{2} = \frac{1}{x-5}$   
 $2x^2x-5 - 2x^2x^2(x-5) - x^3 - 5x^2$   
**31.**  $f(x) = \frac{1}{x}, g(x) = x - 3$   
 $x$ 

a) Since f (0) is not defined, the domain of f is (-∞, 0) U (0, ∞). The domain of g is (-∞, ∞).

Then the domain of f + g, f - g, fg, and ff is  $(\neg \Theta)$  (0, U). Since g(3) = 0, the domain of f/g is (, 0) (0, 3) (3, 3). There are no values of x for which f(x) = 0, so the domain of g/f is  $(-\infty, 0) \cup (0, \infty)$ .

b) 
$$(f + g)(x) = f(x) + g(x) = \frac{1}{x} + x - \frac{1}{3}$$
  
 $(f - g)(x) = f(x) - g(x) = \frac{1}{x} - \overline{(x-3)} = \frac{1}{x} - x + 3$   
 $\frac{1}{x} - \frac{x-3}{x} - \frac{x}{3}$ 

$$(fg)(x) = f(x) \cdot g(x) = \cdot (x-3) =$$
, or 1 –

$$(ff)(x) = f(x) \cdot f(x) = \frac{x}{1} \cdot \frac{1}{1} = \frac{1}{1}$$
 x x

**32.** 
$$f(x) = x + 6, g(x) =$$

a) The domain of f(x) is  $[-6, \infty)$ . The domain of g(x)

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is  $(-\infty, 0) \cup (0, \infty)$ . Then the domain of f + g, f - g, and fg is  $[-6, 0) \cup (0, \infty)$ . The domain of ff is  $[-6, \infty)$ . Since

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$$(g/f)(x) = \frac{6-x}{4-\frac{x}{6-x}} \cdot \frac{x+1}{6-x} = \frac{x+1}{4(6-x)}$$
$$x+1 = \frac{x+1}{2}$$

**30.**  $f(x) = 2x^2$ ,  $g(x) = \frac{1}{x-5}$ 

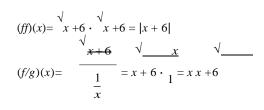
a) The  
domain of 
$$f$$
 is  $(-\infty, \infty)$ . Since  $x-5=0$  when  $x=5$ ,  
the domain of  $g$  is  $(-\infty,5)\cup(5,\infty)$ . Then the

domain of f+g, f-g, and fg is  $(-\infty, 5) \cup (5, \infty)$ . The domain of ff is (, )-Since there are no values of x there are no values of x for which g(x)=0, the domain of f/g is  $[-6,0) \cup (0, \infty)$ . Since

for which g(x)=0, the domain of f/g is  $(-\infty, 5) \cup (5, \infty)$ . Since f

(0)=0, the domain of

g/f is  $(-\infty, 0) \cup (0, 5) \cup (5, \infty)$ .



$$(g/f)(x) = \frac{\sqrt{x}}{\sqrt{x}} \quad \frac{1}{\sqrt{x}} \quad \frac{$$

**33**• f(x) = , g(x) = x - 1

a) Since f (2) is not defined, the domain of f is (, 2) (2, ). Since g(xt) is nonnegative for val- ues of x in [1, ), this is the domain of g. The domain of f + g, f g, and fg is the intersection of the-domains of f and g, or [1, 2) (2, ). The domain of ff is the same as the doumain∞of f, or (, 2) (2, ). For f/g, we must exclude 1 since g(1) = 0, so the domain of fs/g is (1, 2) (2, ). There are no values of x for which f(x)=0, so the domain of g/f is [1, 2) ∪ (2, ∞).

b) 
$$(f+g)(x) = f(x) + g(x) = \frac{3}{2} + \frac{\sqrt{3}}{x-1}$$
  
 $(f-g)(x) = f(x) - g(x) = \frac{3}{2} \sqrt{\frac{3}{x-2}} - \frac{\sqrt{-1}}{3\sqrt{x-1}}$   
 $()() = () \qquad () = ($   
 $fg(x) - f(x) + g(x) = \frac{3}{2} + \frac{3}{x-2} - \frac{1}{x-1})$  or  $\frac{1}{x-2}$   
 $(ff)(x) = f(x) + f(x) = \frac{3}{2} + \frac{3}{2} + \frac{9}{2}$ 

**34.** 
$$f(x) = \frac{2}{4-x}, g(x) = \frac{5}{x-1}$$

 $(-\infty, 1) \cup (1, \infty)$ . The domain of f+g, f-g, and fg is  $(-\infty, 1) \cup (1, 4) \cup (4, \infty)$ . The domain of ff is  $(-\infty, 4) \cup (4, \infty)$ . The domain of f/g and of g/f is  $(-\infty, 1) \cup (1, 4) \cup (4, \infty)$ .

**35.** From the graph we see that the domain of F is [2, 11] and the domain of G is [1, 9]. The domain of F + G is the set of numbers in the domains

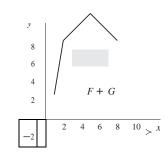
ofbothF andG. Thisis[2,9].

**36.** The domain of F *G*-and FG is the set of numbers in the domains of both F and G. (See Exercise 33.) This is [2,9].

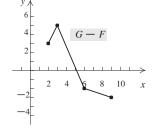
The domain of F/G is the set of numbers in the domains of both F and G, excluding those for which G=0. Since G > 0 for all values of x in its domain, the domain of F/G is [2, 9].

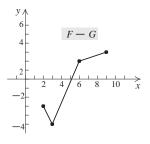
- **37.** The domain of G/F is the set of numbers in the domains of both *F* and *G* (See Exercise 33.), excluding those for which F=0. Since F(3)=0, the domain of G/F is  $[2,3)\cup(3,9]$ .
- 38.

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**41.** From the graph, we see that the domain of *F* is [0,9] and the domain of

*G* is [3, 10]. The domain of F + G is the set

of numbers in the domains of both F and G. This is [3,9].

**42.** The domain of *F* – *G* and *FG* is the set of numbers in the domain sofboth *F* and *G*. (See Exercise 39.) This is [3,9].

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$$\frac{5}{x-1} = 5(4-x)$$

$$\frac{5}{x-1} = \frac{5}{5(4-x)}$$

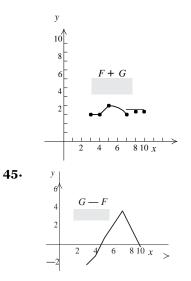
$$(g/f)(x) = \frac{2}{4-x} = 2(x-1)$$

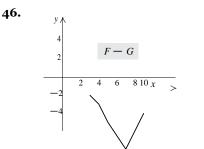
The domain of F/G is the set of numbers in the domains of both F and G, excluding those for which G=0. Since G>0 for all values of x in

its domain, the domain of F/G is [3, 9].

**43.** The domain of G/F is the set of numbers in the domains of both F and G (See Exercise 39.), excluding those for which F = 0. Since F(6) = 0 and F(8) = 0, the domain of G/F is  $[3, 6) \cup (6, 8) \cup (8, 9]$ .

**44.** (F + G)(x) = F(x) + G(x)





**47.** a) 
$$P(x) = R(x) - C(x) = 60x - 0.4x^2 - (3x + 13) =$$

$$60x - 0.4x^2 - 3x - 13 = -0.4x^2 + 57x - 13$$

b)  $R(100) = 60 \cdot 100 - 0.4(100)^2 = 6000 - 0.4(10, 000) = 6000 - 4000$ = 2000  $C(100) = 3 \cdot 100 + 13 = 300 + 13 = 313$ P(100) = R(100) - C(100) = 2000 - 313 = 1687

**48.** a)  $P(x) = 200x - x^2 - (5000 + 8x) =$ 

 $200x - x^{2} - 5000 - 8x = -x^{2} + 192x - 5000$ b)  $R(175) = 200(175) - 175^{2} = 4375$  $C(175) = 5000 + 8 \cdot 175 = 6400$ P(175) = R(175) - C(175) = 4375 - 6400 = -2025(We could also use the function found in part (a) to find P (175).)

49. 
$$f(x) = 3x - 5$$
  
 $f(x+h) = 3(x+h) - 5 = 3x + 3h - 5$   
 $h = \frac{3x + 3h - 5 - 3x + 5}{h}$   
 $= \frac{3x + 3h - 5 - 3x + 5}{h}$   
 $= \frac{-3}{h}$   
 $\frac{f(x+h) - f(x)}{h} = \frac{4(x+h) - 1 - (4x - 1)}{h} =$   
 $\frac{4x + 4h - \frac{1 - 4x + 1}{h}}{h} = \frac{4h}{4h} = 4\frac{4h}{h}$   
51.  $f(x) = 6x + 2$   
 $f(x+h) = 6(x+h) + 2 = 6x + 6h + 2$   
 $\frac{f(x+h) - f(x)}{h} = \frac{6x + 6h + 2 - (6x + 2)}{h}$   
 $= \frac{6x + 6h + 2 - 6x - 2}{h}$   
 $= \frac{6h}{h} = 6$   
52.  $f(x) = 5x + 3$   
 $\frac{f(x+h) - f(x)}{h} = \frac{5(x+h) + 3 - (5x + 3)}{h} =$   
 $\frac{5x + 5h + 3 - 5x - 3}{h} = 5h = 5h$   
53.  $f(x) = \frac{1}{x} + 1$ 

$$\frac{3}{1} \underbrace{\frac{1}{x+h} + \frac{1}{3} \underbrace{\frac{1}{x+h} + 1}_{3} + \frac{1}{3} \underbrace{\frac{1}{x+1} + \frac{1}{3}}_{3} + \frac{1}{3} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h} - \frac{1}{3} \underbrace{\frac{x+1}{x+1} - \frac{1}{3}}_{h} - \frac{1}{3} \underbrace{\frac{x+1}{h} - \frac{1}{3} \underbrace{\frac{x+1}{h} - \frac{1}{3}}_{h}}_{= 3 \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h} - \frac{1}{3}}_{h} - \frac{1}{3} \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{= 3 \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h} - \frac{1}{3}}_{h} - \frac{1}{3} \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{= 3 \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h} - \frac{1}{3} \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h} - \frac{1}{3} \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h} - \frac{1}{2} \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h}}_{h}}_{h} - \underbrace{\frac{1}{2} \underbrace{\frac{1}{x+1} + \frac{1}{3} + \frac{1}{3}}_{h}}_{h}}_{h}}_{h}}_{h}}$$

$$55 \cdot f(x) = \frac{1}{3x} \frac{1}{1 - 1}$$

$$f(x+h) = \frac{1}{3(x+h)} = \frac{3(x+h) \cdot 3x - 1}{3(x+h) \cdot 3x - 1}$$

$$h = \frac{1}{x} \frac{1}{x - 1} \frac{x+h}{x - 1}$$

$$= \frac{3(x+h) \cdot x}{h} \frac{h}{h} \frac{x + h}{h}$$

$$= \frac{3x(x+h)}{h} \frac{h}{h} \frac{x - x + h}{h}$$

$$= \frac{3x(x+h)}{h} \frac{3x(x+h)}{h} \frac{x - x - h}{h}$$

$$= \frac{3x(x+h)}{h} \frac{3x(x+h)}{h} \frac{x - x - h}{h}$$

$$= \frac{-h}{3x(x+h)} \frac{-h}{h} \frac{3x(x+h) \cdot h}{h}$$

$$= \frac{-h}{3x(x+h) \cdot h} \frac{-h}{3x(x+h) \cdot h}$$

$$= \frac{-1}{3x(x+h) \cdot h} \frac{1}{x - 1} \frac{1}{x + 1} \frac{x + 1}{x + 1}$$

$$f(x+h) - f(x) = \frac{1}{2(x+h)} \frac{2}{x} \frac{1}{x - 1} \frac{1}{x} \frac{1}{x + h}$$

$$f(x+h) = -\frac{1}{4x} \frac{1}{x + 1} \frac{1}{x + 1} \frac{1}{x + 1} \frac{1}{x + 1}$$

$$f(x+h) = -\frac{1}{4(x+h)} \frac{1}{x} \frac{1}{x + 1} \frac{1}{x + 1}$$

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$$58. f(x) = -\frac{1}{x} \qquad 1 \qquad 1$$

$$\frac{f(x+h) - f(x)}{h} = -\frac{1}{x+h} - \frac{1}{x}$$

$$\frac{f(x+h) - f(x)}{h} = -\frac{1}{x+h} - \frac{1}{x}$$

$$\frac{1}{x} \qquad 1 \qquad \frac{x+h}{h} - \frac{1}{x}$$

$$\frac{1}{x} \qquad \frac{1}{x+h} \qquad \frac{x+h}{h} - \frac{1}{x}$$

$$\frac{x+h}{x} \qquad \frac{x}{x+h} - \frac{1}{x}$$

$$\frac{x+h}{x} \qquad \frac{x}{x+h} - \frac{1}{x}$$

$$\frac{x(x+h)}{h} = -\frac{1}{x(x+h)}$$

59. 
$$f(x) = x^2 + 1$$
  
 $f(x+h) = (x+h)^2 + 1 = x^2 + 2xh + h^2 + 1$   
 $\frac{f(x+h) - f(x)}{h} = \frac{x^2 + 2xh + h^2 + 1 - (x^2 + 1)}{h}$   
 $= \frac{x^2 + 2xh + h^2 + 1 - x^2 - 1}{h}$   
 $= \frac{2xh + h^2}{h}$   
 $= \frac{h(2x+h)}{h}$   
 $= \frac{h(2x+h)}{h}$   
 $= \frac{h(2x+h)}{h}$   
 $= 2x + h$ 

$$\frac{x^{2} + 2xh + h^{2} - 3 - x^{2} + 3 2xh + h^{2} h(2x + h)}{=} =$$

$$\frac{h}{h} =$$

$$h$$

$$h$$

$$h$$

$$h$$

$$h$$

61. 
$$f(x) = 4 - x^2$$
  
 $f(x+h) = 4 - (x+h)^2 = 4 - (x^2 + 2xh + h^2) = 4 - x^2 - 2xh - h^2$   
 $\frac{f(x+h) - f(x)}{h} = 4 - \frac{x^2 - 2xh - h^2 - (4 - x^2)}{h}$   
 $h = 4 - \frac{x^2 - 2xh - h^2 - 4 + x^2}{h}$ 

 $=\frac{-2xh-h^2}{h} \frac{h}{h}$ 

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=

$$-4(x+h) \cdot x - 4x \cdot x+h$$

$$= -2x - h$$

$= \frac{h}{4x(x+h)} + \frac{h}{4x(x+h)}$	<b>62.</b> $f(x) = 2 -x^2$ $\frac{f(x+h) - f(x)}{f(x+h) - f(x)} = 2 - \frac{(x+h)^2 - (2-x)^2}{(x+h)^2 - (2-x)^2}$
$= h \\ \underline{-x + x + h} \qquad \underline{-h}$	$\frac{h}{2 - x^2 - 2xh - h^2 - 2 + x^2} - 2xh - h^2$
$=\frac{4x(x+h)}{h} = \frac{4x(x+h)}{h}$ $=\frac{h}{h} \cdot \frac{1}{h} = \frac{h \cdot 1}{h} = \frac{1}{h}$	$\frac{h}{h(-2x-h)} = -2x - h$

4x(x+h) h  $4x(x+h)\cdot h$  4x(x+h)

**63.**  $f(x) = 3x^2 - 2x + 1$  $f(x+h) = 3(x+h)^2 - 2(x+h) + 1 = 3(x^2 + 2xh + h^2) - 2(x+h) + 1 =$ 

$$3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1$$

$$f(x) = 3x^{2} - 2x + 1$$

$$f(x) = 3x^{2} - 2x + 1$$

$$\frac{1}{f(x) = 3x^{2} - 2x + 1}$$

$$\frac{1}{f(x) = 3x^{2} - 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x + 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x + 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$=$$

$$\frac{1}{(3x^{2} + 6xh + 3h^{2} - 2x - 2h + 1) - (3x^{2} - 2x - 1)}$$

$$\frac{1}{(x^{2} + h^{2} - x)^{2} - (x^{2} - x^{2} - x$$

x+h-4 $x-4$				
$ \frac{x+h+3}{h} \frac{x+3}{(x+h+3)(x+3)} = $				
$\frac{(x+h-4)(x+3) - (x-4)(x+h+3)}{h(x+h+3)(x+3)} =$				
$\frac{x^2 + hx - 4x + 3x + 3h - 12 - (x^2 + hx + 3x - 4x - 4h - 12)}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)} = \frac{x^2 + hx - x + 3h - 12 - x^2 - hx + x + 4h + 12}{h(x + h + 3)(x + 3)}$				
<u>h</u>				
$\frac{n}{h(x+h+3)(x+3)} = \frac{h}{h(x+h+3)(x+3)} =$				
$ \frac{7}{(x+h+3)(x+3)} = \frac{7}{n(x+n+3)(x+3)} $ 70. ()= $ \frac{f x}{2-x} $				
2 - x $x + h$ $x$				
$\frac{f(x+h) - f(x)}{h} = \frac{2 - (x+h)^{-2} - x}{h} =$				
$\frac{(x+h)(2-x) - x(2-x-h)}{(2-x-h)(2-x)} = \frac{h}{h}$				
$\frac{2x - x^2 + 2h - hx - 2x + x^2 + hx}{2x - x^2 + hx}$				
(2-x-h)(2-x) =				
h				
$\frac{\frac{2h}{(2-x-h)(2-x)}}{h} =$				
<u>2h 1</u> 2				
(2-x-h)(2-x) $h$ $(2-x-h)(2-x)$				
<b>71.</b> Graph $y = 3x - 1$ . Wefindsomeorderedpairsthataresolutionsoftheequa- tion, plot these points, and draw the graph. When $x = -1$ , $y = 3(-1) - 1 = -3 - 1 = -4$ .				
When $x = 0$ , $y = 3 \cdot 0 - 1 = 0 - 1 = -1$ .				
When $x = 2$ , $y = 3 \cdot 2 - 1 = 6 - 1 = 5$ .				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				

$$\begin{array}{c} -2 & x \\ & -2 & x \\ & -4 & y = 3x - 1 \\ \hline & 3x^2h + 3xh^2 + h^3 - 2h \\ & h & \equiv & \frac{h(3x^2 + 3xh + h^2 - 2)}{h} \\ \hline & 3x^2 + 3xh + h^2 - 2 \end{array}$$

**69.** 
$$f(x) = \frac{x-4}{x+3}$$
  $\frac{x+h-4}{x-4}$ 

.

 ++++++4 ++++++++++++++++++++++++++++++	2x + y = 4
	242

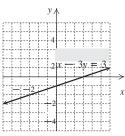
 $\frac{f(x+h) - f(x)}{h} = \frac{x+h+3}{h} = \frac{x+3}{h}$ 

73. Graph x - 3y = 3. First we find the *x*- and *y*-intercepts.  $x - 3 \cdot 0$  = 3 x = 3The *x*-intercept is (3, 0).

$$0 - 3y = 3$$
$$-3y = 3$$
$$y = -1$$

- They-interceptis(0,-1).
- We find a third point as a check. We let x = 3 and solve for y. -3 - 3y = 3
  - -3y = 6y = -2

anddrawthegraph.



74.

У
11111 <b>A</b> 14 <b>A</b> 11 <b>A</b> 11311
<b>A</b> 12
·····
<u>-4</u> <u>-2</u> <u>24</u> <u>x</u>
22
$\mathbf{y}_{1} = \mathbf{y}_{2} + \mathbf{y}_{2} + \mathbf{y}_{3} $

**75.** Answersmayvary; f(x) =

$$\underline{1}_{\underline{g}(x)=}$$
  $\underline{1}_{\underline{g}(x)=}$ 

*x* +7 *x* - 3

**76.** The domain of h+f, h-f, and hf consists of all numbers that are in the domain of both h and f, or  $\{-4, 0, 3\}$ .

The domain of *h*/*f* consists of all numbers that are in the domain of both *h* and *f*, excluding any for which the value of *f* is 0, or  $\{-4, 0\}$ .

**77.** The domain of h(x) is x x

, and the domain of 
$$g(x)$$

is{x|x f=3}, so  $\frac{1}{a}$  and 3a renotinthe domain of (h/g)(x). We must also exclude the value of x for which g(x)=0.  $\frac{x^4 - 1}{5x - 15} = 0$  $x^4 - 1 = 0$ Multiplying by 5x - 15

$$x^4 = 1$$

 $x = \pm 1$ 

## Exercise Set 2.3

 $g(-3) = (-3)^2 - 2(-3) - 6 = 9 + 6 - 6 = 9$ **11.**  $(h \circ h)(2) = h(h(2)) = h(2^3) = h(8) = 8^3 = 512$ **12.**  $(h \circ h)(-1) = h(h(-1)) = h((-1)) = h(-1) = (-1) = -1$ 

- **13.**  $(f \circ f)(-4) = f(f(-4)) = f(3(-4) + 1) = f(-12 + 1) = f(-11) = 3(-11) + 1 = -33 + 1 = -32$
- **14.**  $(f \circ f)(1) = f(f(1)) = f(3 \cdot 1 + 1) = f(3 + 1) = f(4) = 3 \cdot 4 + 1 = 12 + 1 = 13$

**15.** 
$$(h \circ h)(x) = h(h(x)) = h(x^3) = (x^3)^3 = x^9$$

**16.**  $(f \circ f)(x) = f(f(x)) = f(3x + 1) = 3(3x + 1) + 1 = 9x + 3 + 1 = 9x + 4$ 

**17.** 
$$(f \circ g)(x) = f(g(x)) = f(x - 3) = x - 3 + 3 = x$$
  
 $(g \circ f)(x) = g(f(x)) = g(x + 3) = x + 3 - 3 = x$   
The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**18.** 
$$(f \circ g)(x) = f \cdot \frac{5}{2}x^{2} = \frac{4}{2} \cdot \frac{5}{2}x = x$$
  
**4** 54

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Then the domain of (h/g)(x) is

$$(g \circ f)(x) = g \overset{4}{x} \overset{\Sigma}{x} = \overset{5}{\cdot} \overset{4}{x} = x$$

 $\frac{7}{3}$  3

 $x x f = \frac{7}{3}$  and x = 3 and x = -1 and x = 1, or The domain of x = 1, or  $f = \frac{5}{3}$  and  $f = \frac{4}{3}$  (matrix), so the domain of  $f = \frac{5}{3}$  (

 $\begin{array}{ccc} f & g & -\infty, \ \infty \\ f \circ g \text{ and of } g \circ f \text{ is } (-\infty, \ \infty). \end{array}$ 

. Σ. Σ

 $(-\infty, -1) \cup (-1, 1) \cup 1, \qquad \cup \quad , 3 \cup (3, \infty).$ 

### **Exercise Set 2.3**

**19.** 
$$(f \circ g)(x) = f(g(x)) = f(3x^2 - 2x - 1) = 3x^2 - 2x - 1 + 1 =$$
  
 $3x^2 - 2x$   
 $(g \circ f)(x) = g(f(x)) = g(x+1) = 3(x+1)^2 - 2(x+1) - 1 =$   
 $3(x^2 + 2x + 1) 2(x+1) 1 = 3x^2 + 6x + 3 2x 2 1 = - - 3x^2 + 4x$   
The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**20.** 
$$(f \circ g)(x) = f(x^2 + 5) = 3(x^2 + 5) - 2 = 3x^2 + 15 - 2 =$$
  
 $3x^2 + 13$   
 $(g \circ f)(x) = g(3x - 2) = (3x - 2)^2 + 5 = 9x^2 - 12x + 4 + 5 =$   
 $9x^2 - 12x + 9$ 

The domain of f and of g is  $(-\infty, \infty)$ , so the domain of

**21.** 
$$(f \circ g)(x) = f(g(x)) = f(4x-3) = (4x-3)^2 - 3 =$$

$$16x^{2} - 24x + 9 - 3 = 16x^{2} - 24x + 6$$
  
(g of)(x)=g(f(x))=g(x^{2}-3)=4(x^{2}-3)-3=

 $4x^2 - 12 - 3 = 4x^2 - 15$ . The domain of f and of g is  $(-\infty, \infty)$ , so the domain of

 $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**22.** 
$$(f \circ g)(x) = f(2x - 7) = 4(2x - 7)^2 - (2x - 7) + 10 = 4(4x^2 - 28x + 49) - (2x - 7) + 10 = 16x^2 - 112x + 196 - 2x + 7 + 10 = 16x^2 - 114x + 213 (g \circ f)(x) = g(4x^2 - x + 10) = 2(4x^2 - x + 10) - 7 = 8x^2 - 2x + 20 - 7 = 8x^2 - 2x + 13$$

The domain of *f* and of *g* is  $(-\infty, \infty)$ , so the domain of

$$f \circ g$$
 and of  $g \circ f$  is  $(-\infty, \infty)$ .

(g

 $\sum_{1} 4 4$  **23.**  $(f \circ g)(x) = f(g(x)) = f_x = - \frac{1}{1-5 \cdot 1} = \frac{5}{1-5} =$ 

f 5. Since the shortain of g is The domain of f is  $x \cdot x$  $Consider the domain of_{\!\circ}$ {| 1

the domain of g, 0 is not in the domain of f, we know that g(x

24. 
$$(f \circ g)(x) = f' \frac{\Sigma_{1=1}}{2 + \frac{1}{x}} \frac{6}{2x + 1} = \frac{1}{1}$$
  
 $6(2x + \frac{X}{2}), \text{ or } 12x + 6$   
 $(g \circ f)(x) = g \quad 6 = \frac{1}{x} \frac{6}{2 \cdot x + 1} = \frac{1}{2x + 1} = \frac{12^{1}}{x} = \frac{1}{12^{1} + x} = \frac{1}{x}$   
 $1\frac{x}{x} = \frac{12 + x}{1 \cdot x} = \frac{12 + x}{1 \cdot x}$   
The domain of  $f$  is  $\{x | x = 0\}$  and the domain of  $g$   
is  $x \cdot x \cdot f = -\frac{1}{2}$ . Consider the domain of  $f \circ g$ . Since  
 $\frac{1}{2}$  is not in the domain of  $g$ ,  $-\frac{1}{2}$  is not in the domain of  $f \circ g$ . Now  
0 is not in the domain of  $f$  but  $g(x)$   
is never 0, so the domain of  $f \circ x$ .  $f = -4$ , or  $1$   
 $g = x \cdot x$ .

6 = 6.

-2 U  $-\infty$ . Now consider the domain of g f. Since 0 is not in the domain of f, then 0 is not in the domain of g f. Also,  $\infty$ since isnotinthedomainofg, we find the value (s) of 2

x for which 
$$f(x) = -\frac{1}{2}$$
.  
 $\frac{6}{x} = -\frac{1}{2}$   
 $-12 = x$ 

Then the domain of g f is x = 12 and x = 0, or  $(-\infty, -12) \cup$ 

$$(-12, 0) \cup (0, \infty). \qquad f = -x + 7$$

$$25. (f \circ g)(x) = f(g(x)) = f_{\sum} = -3 = -3$$

$$3 = -3 = -7 = x + 7 - 7 = x$$

$$(g \circ f)(x) = g(f(x)) = g(3x - 7) = -\frac{(3x - 7) + 7}{3} = -3$$

3 The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

 $\underline{3x} = x$ 

26.  

$$(f \circ g)(x) = f(1.5x + 1.2) = \frac{2}{3}(1.5x + 1.2) - \frac{4}{5}$$

$$\frac{x + 0.8 - \frac{4}{5}}{5} = x$$

$$(g \circ f)(x) = g^{-2}x - 4 - \Sigma = 1.5 - \frac{2x - 4}{5} + 1.2 = 1.5$$

117

 $\overset{2x+1}{1} =$ 

 $_1$  ) cannot be .

ł

Wefindthevalue(s)ofx forwhichg(x

$$\frac{1}{x} = \frac{1}{5}$$

$$x = 5$$

$$5 = x$$
Multiplying by 5x

Thus 5 is also not in the domain of  $f \circ g$  is  $\{x | x \in \mathbb{N}\}$ 

$$f=0$$
 and  $x f=5$ , or  $(-\infty, 0) \cup (0, 5) \cup (5, \infty)$ . Now consider the

domain of  $g \circ f$ . Recall that is not in

\_

the domain of f, so it isnot in the domain of g f. Now  $\circ$  0 is not in the domain of g but f(x) is never 0, so the domain 1  $\begin{array}{cccc} & & & \Sigma \\ 3 & 5 & & 3 & 5 \\ x - 1.2 + 1.2 = x & & & \end{array}$ 

The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**27.** 
$$(f \circ g)(x) = f(g(x)) = f(x) = 2 + 1$$

$$(g \circ f)(x) = g(f(x)) = g(2x + 1) = \sqrt[n]{2x + 1}$$

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5

)=<sub>5</sub>.

, , , 
$$\Sigma = \Sigma$$
  
of  $g \circ f$  is  $x \cdot x = 5$ , or  $-\infty$ ,  $5 \cup 5$ ,  $\infty$ .

Now consider the domain of  $g \circ f$ . There are no restrictions onthe domain of *f*, butthe domain of *g* is  $\{x | x \ge 0\}$ . Since

$$f(x) \ge 0 \text{ for } x \ge -2, \text{ the } \frac{1}{2} \text{ domain of } g \circ f \text{ is } x x \qquad \ge -2^{1},$$
  
or  $-\frac{1}{2} \infty$ .  
 $\Sigma \qquad \Sigma$ 

**28.**  $(f \circ g)(x) = f(2 - 3x) = 2 - 3x$ 

 $(g \circ f)(x) = g(x) = 2 - 3x$ 

The domain of f is  $\{x | x \ge 0\}$  and the domain of g is  $(-\infty, \infty)$ . Since  $g(x)\ge 0$  when  $x\le \frac{2}{2}$ , the domain of  $f\circ g$ 

3

is 
$$-\infty, \frac{2\Sigma}{3}$$

Now consider the domain of  $g \circ f$ . Since the domain of f

is  $\{x | x \ge 0\}$  and the domain of g is  $(-\infty, \infty)$ , the domain

of 
$$g \circ f$$
 is  $\{x | x \ge 0\}$ , or  $[0, \infty)$ .  
**29.**  $(f \circ g)(x) = f(g(x)) = f(0.05) = 20$ 

 $(g \circ f)(x) = g(f(x)) = g(20) = 0.05$ The domain of f and of g is  $(-\infty, \infty)$ , so the domain of

 $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**30.** 
$$(f \circ 4^{4})^{-1}$$
  
 $(g)(x) = (x) = x$   
 $\sqrt{-1}$   
 $(g \circ f)(x) = 4^{4}x^{4} = |x|$ 

The domain of f is  $(-\infty, \infty)$  and the domain of g is  $\{x|x \ge 0\}$ , so the domain of  $f \circ g$  is  $\{x|x \ge 0\}$ , or  $[0, \infty)$ . Now consider the domain of  $g \circ f$ . There are no restrictions on the domain of f and  $f(x) \ge 0$  for all values of x, so the domain is  $(-\infty, \infty)$ .

**31.** 
$$(f \circ g)(x) = f(g(x)) = f(x^2 - 5) =$$

$$\sqrt[n]{x^2 - 5 + 5} = \frac{\sqrt[n]{x^2 - 5}}{x^2 - 5 + 5} = \frac{\sqrt[n]{x^2 - 5}}{x^2 - 5} = \frac{\sqrt[$$

The domain of *f* is  $\{x | x \ge -5\}$  and the domain of *g* is

 $(-\infty,\infty)$ . Since  $x^2 \ge 0$  for all values of x, then  $x^2-5 \ge -5$  for all values of x and the domain of  $g \circ f$  is  $(-\infty, \infty)$ .

Now consider the domain of  $f \circ g$ . There are no restrictions on the domain of g, so the domain of  $f \circ g$  is the same as the domain of  $f \cdot \{x | x \ge -5\}$ , or  $[-5, \infty)$ .

**32.** 
$$(f \circ g)(x) = ({\stackrel{\checkmark}{5}}_{x+2})^5 - 2 = x + 2 - 2 = x$$

$$(g \circ f)(x) = {}^{5}x^{5} - 2 + 2 = {}^{5}x^{5} = x$$

**34.**  $(f \circ g)(x) = f(x^2 - 25) = 1 - (x^2 - 25)^2 =$   $1 - (x^2 - 25) = 1 - x^2 + 25 = 26 - x^2$  $(g \circ f)(x) = \frac{g(1 - x)}{1 - 2x^2 + x^4 - 25} = \frac{2}{x^4 - 2x^2 - 24}$ 

The domain of f is  $(-\infty, \infty)$  and the domain of g is  $\{x | x \le -5 \text{ or } x \ge 5\}$ , so the domain of  $f \circ g$  is  $\{x | x \le -5 \text{ or } x \ge 5\}$ , or  $(-\infty, -5] \cup [5, \infty)$ .

Now consider the domain of g of f. There are no restrictions on the domain of f and the domain of g is  $\{x|x \le -5 \text{ or } x \ge 5\}$ , so we find the values of x for

which  $f(x) \leq -5$  or  $f(x) \geq 5$ . We see that  $1 \leq x^2 \leq -5$ 

when  $x \le -6$  or  $x \ge 6$  and  $1-x \ge 5$  has no solution, so the domain of  $g \circ f$  is  $\{x | x \le -6 \text{ or } x \ge -6\}$ , or  $(-\infty, -6] \cup [6, \infty)$ .

$$35. (f \circ g)(x) = f(g(x)) = f^{-1} + x^{-1} = 1 + x = 1 + x = 1 + x = \frac{1}{1 + x} = \frac{1 + x}{1 + x} = \frac{1}{1 - x}$$

 $\frac{1}{r}$ 

1

The domain of f is  $\{x|x = 0\}$  and the domain of g is  $\{x|x f = -1\}$ , so we know that -1 is not in the **dom** of  $f \circ g$ . Since 0 is not in the domain of f, values of x for which g(x) = 0 are not in the domain of  $f \circ g$ . But g(x) is never 0, so the domain of  $f \circ g$  is  $\{x|x f = -1\}$ , or  $(-\infty, -1) \cup (-1, \infty)$ .

Now consider the domain of  $g \circ f$ . Recall that 0 is not in the domain of f. Since -1 is not in the domain of g, we know that g(x) cannot be

-1. We find the value (s) of x for which 
$$f(x) = -1$$
.  

$$\frac{1-x}{x} = 1 - \frac{1-x}{x} = 1 - \frac{1-x$$

The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ . Copyright © 2

Copyright © 2013 Pearson Education, xInc. x Multiplying by x

**33.**  $(f \circ g)(x) = f(g(x)) = f(3 - x) = (3 - x)^2 + 2 =$ 3-x+2=5-x $(gf(x))=g(f(x))=g(x^2+2)=3(x^2+2)=$ °  $\sqrt[n]{\frac{1}{3-x^2-2=1}} \sqrt[n]{\sqrt{1-x^2-2=1}}$ The domain of f is (-∞,∞) and the domain of g is

1 = 0False equation

We see that there are no values of x for which f(x) = -1, so the domain of  $g \circ f$  is { $x \mid x f = 0$ }, or( $-\infty$ , 0)U (0,  $\infty$ ).

*x*+2 1

 $\{x | x \le 3\}$ , so the domain of  $f \circ g$  is  $\{x | x \le 3\}$ , or  $(-\infty, 3]$ . Now consider the domain of  $g \circ f$ . There are no restrictions

onthe domain of *f* and the domain of *g* is  $\{x | x \le 3\}$ , so we find the values of *x* for which  $f(x) \le 3$ . We see that  $x^2 + 2 \le 3$  for  $-1 \le x \le 1$ , so the domain of  $g \circ f$  is

 $\{x|{-}1{\leq}x{\leq}1\}, {\rm or}[{-}1,1].$ 

**36.** 
$$(f \circ g)(x) = f$$
  
$$x = \frac{x+2}{x} - 2$$
$$= \frac{1}{\frac{x+2-2x}{x}} = \frac{\frac{x}{-x}}{\frac{-x+2}{x}}$$
$$= 1 \cdot \frac{x}{-x+2} = \frac{x}{-x+2}, \text{ or } \frac{x}{2-x}$$

$$(g \circ f)(x) = g \qquad \frac{1}{x-2} = \frac{x-2}{\frac{1}{x-2}}$$
$$= \frac{\frac{1+2x-4}{x-2}}{\frac{1-2}{x-2}} = \frac{2x-3}{\frac{1-2}{x-2}}$$
$$= \frac{2x-3}{x-2} = 2x-3$$
$$x-2 \qquad 1$$

The domain of f is  $\{x|x=2\}$  and the domain of g is  $\{x|x=0, s\}$  of is not in the domain of f g. We fine dthe value of x for which g(x)=2.

1

$$\frac{x+2}{x} = 2$$

$$x + 2 = 2x$$

$$2 = x$$

Then the domain of  $f \circ g$  is  $(-\infty, 0) \cup (0, 2) \cup (2, \infty)$ . Now consider the domain of g f. Since the domain of f

is  $\{x \nmid = f2, y\}$  know that 2 is not in the domain of g f. Since the domain of g is xx = 0, we find the falle of x for which f(x) = 0.

$$\frac{1}{x-2} = 0$$
$$1 = 0$$

We get a false equation, so there are no such values. Then the domain of  $g \circ f$  is  $(-\infty, 2) \cup (2, \infty)$ .

**37.** 
$$(f \circ g)(x) = f(g(x)) = f(x + 1) = (x + 1)^3 - 5(x+1)^2 + 3(x+1) + 7 = x^3 + 3x^2 + 3x + 1 - 5x^2 - 10x - 5 + 3x + 3 + 7 = x^3 - 2x^2 - 4x + 6$$
  
 $(g \circ f)(x) = g(f(x)) = g(x^3 - 5x^2 + 3x + 7) = 3x^3 - 3x^2 + 3x + 7 = 3x^3 - 3x^2 + 3x + 7 = 3x^3 - 3x^2 + 3x + 7 = 3x^3 - 3x^2 + 3x^2 +$ 

 $x^3 - 5x^2 + 3x + 7 + 1 = x^3 - 5x^2 + 3x + 8$ 

The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

**38.**  $(g \circ f)(x) = x^3 + 2x^2 - 3x - 9 - 1 =$  $x^3 + 2x^2 - 3x - 10$  $(g \circ f)(x) = (x - 1)^3 + 2(x - 1)^2 - 3(x - 1) - 9 =$  $x^3 - 3x^2 + 3x - 1 + 2x^2 - 4x + 2 - 3x + 3 - 9 =$ 

$$x^3 - x^2 - 4x - 5$$

The domain of f and of g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and of  $g \circ f$  is  $(-\infty, \infty)$ .

## **39.** $h(x) = (4 + 3x)^5$

This is 4+3x to the 5th power. The most obvious answer is  $f(x) = x^5$ and  $g(x) = \frac{1}{\sqrt{2}} 4 + 3x$ .

**40.** 
$$f(x) = {}^{3}x, g(x) = x^{2} - 8$$

**41.** *h*(*x*)=

 $(x - 2)^4$ Thisis1dividedby(x-2)tothe4thpower. Oneobvious

42. 
$$f(x) = \frac{1}{\sqrt{x}}, g(x) = 3x + 7$$
  
 $\stackrel{\times}{\underline{x}}$   
43.  $f(x) = \frac{x-1}{x+1}, g(x) = x^3$   
44.  $f(x) = |x|, g(x) = 9x^2 - 4$   
45.  $() = \frac{6}{x}, () = \frac{2+x^3}{2\sqrt{2}-x^3}$   
46.  $f(x) = \frac{x^4}{\sqrt{x}}, g(x) = x - 3$   
 $\sqrt{x-5}$ 

**48.** 
$$f(x) = 1 + x, g(x) = 1 + x$$

**49.** 
$$f(x) = x^3 - 5x^2 + 3x - 1$$
,  $g(x) = x + 2$ 

**50.** 
$$f(x) = 2x^{5/3} + 5x^{2/3}$$
,  $g(x) = x - 1$ , or  
 $f(x) = 2x^5 + 5x^2$ ,  $g(x) = (x - 1)^{1/3}$ 

- **51.** a) Use the distance formula, distance = rate time. Substitute3fortherateandt fortime. r(t)=3t
  - b) Use the formula for the area of a circle.  $A(r) = \pi r^2$
  - c)  $(A \circ r)(t) = A(r(t)) = A(3t) = \pi(3t)^2 = 9\pi t^2$ Thisfunctiongives the area of the ripple interms of time t.

52. a) 
$$h = 2r$$
  
 $S(r) = 2\pi r(2r) + 2\pi r^2$   
 $S(r) = 4\pi r^2 + 2\pi r^2 S(r) =$   
 $6\pi r^2$   
b)  $r = \frac{h}{2}$   
 $S(h) = 2\pi - h \frac{\Sigma}{h + 2\pi} - h \frac{\Sigma}{2}$   
 $S(h) = \pi h^2 + \frac{\pi h^2}{2}$ 

2

**53.** The manufacturer charges m + 2 per drill. The chain store sells each drill for 150%(m+2), or 1.5(m+2), or 1.5m+3. Thus, we have P(m) = 1.5m+3.

2

- **54.**  $f(x) = (t \circ s)(x) = t(s(x)) = t(x 3) = x 3 + 4 = x + 1$  We have f(x) = x + 1.
- **55.** Equations (a) (f) are in the form y = mx + b, so we can read the yintercepts directly from the equations. Equa- tions (g) and (h) can be

writteninthisformas y = x - 2

and y = -2x +3, respectively. We see that only equa-tion (c) has y-intercept (0, 1).

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Tansweris f(x) =and g(x) = x - 2.Another possibility

$$\frac{1}{x^4} = \frac{1}{x^4} = \frac{1}$$

**56.** None (See Exercise 55.)

**57.** If a line slopes downfrom left to right, its slope is negative. The equations y=mx+b for which *m* is negative are (b),

(d), (f), and (h). (See Exercise 55.)

- **58.** The equation for which *m* is g|r|eatestisthe equation with thesteepest slant. This is equation(b). (See Exercise 55.)
- **59.** The only equation that has (0, 0) as a solution is (a).
- **60.** Equations(c)and(g)have the same slope. (See Exer-cise 55.)
- **61.** Only equations (c) and (g) have the same slope and differ- ent *y*-intercepts. They represent parallel lines.
- **62.** Theonlyequations for which the product of the slopes is -1 are (a) and (f).
- **63.** Only the composition (c p)(a) makes sense. It represents the cost of the
- **64.** Answers may vary. One example is f(x) = 2x + 5 and  $g(x) = \frac{x-5}{2}$ . Otherexamples are found in Exercises 17, 2 18, 25, 26, 32 and 35.

## **Chapter 2 Mid-Chapter Mixed Review**

- 1. The statement is true. See page 162 in the text.
- 2. The statement is false. See page 177 in the text.
- **3.** The statement is true. See Example 2 on page 185 in the text, for instance.
- **4.** a) Forx-values from 2 to 4, the *y*-values increase from 2 to 4. Thus the function is increasing on the interval (2, 4).
  - b) Forx-values from -5 to -3, they-values decrease from 5 to 1. Also, for x-values from 4 to 5, the y-

values decrease from 4 to -3. Thus the function is decreasing on (-5, -3) and on (4, 5).

- c) Forx-values from -3 to -1, y is 3. Thus the function is constant on (-3, -1).
- **5.** From the graph we see that a relative maximum value of 6.30 occurs at x = -1.29. We also see that a relative

minimum value of -2.30 occurs at x = 1.29.

The graph starts rising, or increasing, from the left and stops increasing at the relative maximum. From this point it decreases to the

relative minimum and then increases again. Thus the function is increasing on  $(-\infty, -1.29)$  and on  $(1.29, \infty)$ . It is decreasing on (-1.29, 1.29).

6. The *x*-values extend from -5 to -1 and from 2 to 5, so the domain is  $[-5, -1] \cup [2, 5]$ . The *y*-values extend from -3 to 5, so the range is [-3, 5].

$$7 \cdot A(h) = \frac{1}{2} (h_2 - 2)h$$

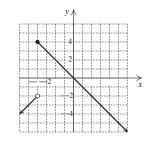
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 $\begin{array}{rcl}
x - 5, & \text{for } x \leq -3, \, 2x + \\
& & \Box_{3, \ \text{for } -3 < x \leq 0,} \\
& & f x \\
& & J = \frac{1}{2} & \text{for } x > 0, \\
\end{array}$ 

Since  $-5 \le -3$ , f(-5) = -5 - 5 = -10. Since  $-3 \le -3$ , f(-3) = -3 - 5 = -8. Since  $-3 < -1 \le 0$ , f(-1) = 2(-1)+3 = -2 + 3 = 1.  $\underline{1}$ Since 6 > 0, f(6) = -6 = 3.

$$x+2, \text{ for } x < -4,$$
  
**9.**  $g(x) = -x, \text{ for } x \ge -4$ 

We create the graph in two parts. Graph g(x) = x+2 for inputs less than -4. Then graph g(x) = -x for inputs greater than or equal to -4.



**10.** 
$$(f + g)(-1) = f(-1) + g(-1)$$
  
=  $[3(-1) - 1] + [(-1)^2 + 4]$   
=  $-3 - 1 + 1 + 4$   
= 1

**11.** 
$$(fg)(0) = f(0) \cdot g(0)$$

$$= (3 \cdot 0 - 1) \cdot (0^2 + 4) = -1 \cdot 4$$

= -4

12. 
$$(g - f)(3) = g(3) - f(3)$$
  
 $= (3^{2} + 4) - (3 \cdot 3 - 1)$   
 $= 9 + 4 - (9 - 1)$   
 $= 9 + 4 - 9 + 1$   
 $= 5$   
13.  $(g/f)$   
 $3_{1}^{\Sigma} = \frac{g}{5} \cdot \frac{1}{3} \sum_{\substack{f = -\frac{1}{3}, \frac{1}{3} \\ f = \frac{1}{3} \cdot \frac{1}{3} - 1}}{\frac{1}{3} \cdot \frac{1}{3} - 1}$   
 $= \frac{\frac{1}{3} \cdot \frac{1}{3} - 1}{\frac{1}{3} + 4}$   
 $= \frac{\frac{1}{9} + 4}{\frac{1}{1} - 1}$   
 $37$ 

 $\frac{1}{h^2 - h}$  $= \frac{9}{2}0$ 

121

Since division by 0 is not defined, (g/f) does not exist.

**14.** f(x) = 2x + 5, g(x) = -x - 4

a) The domain of *f* and of *g* is the set of all real numbers, or (-∞,∞). Thenthedomain of *f* +*g*, *f* −*g*, *fg*, and *ff* is also (-∞,∞).

For f/g we must exclude  $-4 \operatorname{since} g(-4)=0$ . Then the domain of f/g is  $(-\infty, -4) \cup (-4, \infty)$ . For we must exclude  $\frac{5}{2} \operatorname{since} = 5 = 0$ .

Then the domain of g/f is -2 f-2 $-\infty, -\frac{5}{2}\sum_{i=0}^{\infty} \sum_{j=-\frac{5}{2}} \sum_{i=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{i=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{i=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{i=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{i=-\frac{5}{2}} \sum_{j=-\frac{5}{2}} \sum_{j=-\frac{5}{2}}$ 

b)
$$(f+g)(x)=f(x)+g(x)=(2x+5)+(-x-4)=x+1$$

$$(f - g)(x) = f(x) - g(x) = (2x + 5) - (4) = (2x + 5 + x + 4) = 3x + 9$$

$$(fg)(x) = f(x) \cdot g(x) = (2x + 5)(-x - 4) = (2x + 5)(-x - 4)(-x - 4) = (2x + 5)(-x - 4)(-x - 4) = (2x + 5)(-x - 4)(-x -$$

 $(g)(x) - f(x) \cdot g(x) - (2x + 3)(-x - 4) =$  $-2x^2 - 8x - 5x - 20 = -2x^2 - 13x - 20$  $(ff)(x) = f(x) \cdot f(x) = (2x + 5) \cdot (2x + 5) =$ 

$$4x^{2}+10x+10x+25=4x^{2}+20x+25$$

$$(f/g)(x) = \frac{f(x)}{f(x)} = \frac{2x+5}{-x-4}$$

$$(g/f)(x) = \frac{g(x)}{-x-4} = \frac{-x-4}{-x-4}$$

$$f(x) = 2x+5$$
**15.**  $f(x) = x - 1, g(x) = \sqrt[7]{x+2}$ 

a) Anynumbercan bean input for *f*, so the domain of *f* is the set of all real numbers, or (-∞, ∞).

The domain of *g* consists of all values for which *x*+2 is nonnegative, so we have  $x+2 \ge 0$ , or  $x \ge -2$ , or  $[-2, \infty)$ . Then the domain of f + g, f - g, and fg

is [−2, ∞).

The domain of *ff* is  $(-\infty, \infty)$ . Since g(-2)=0, the domain of f/g is  $(-2, \infty)$ .

Since f(1)=0, the domain of g/f is  $[-2,1)\cup(1,\infty)$ . b) (f + g)(x) = f(x) + g(x) = x - 1 + x + 2 (f - g)(x) = f(x) - g(x) = x - 1 - x + 2  $(f\overline{g})(\overline{x}) = f(x) \cdot g(x) = (x - 1) + 2$   $(ff)(x) = f(x) \cdot f(x) = (x - 1)(x - 1) = x^2 - x - x + 1 = x^2 - 2x + 1$   $(f/g)(x) = \frac{f(x)}{g(x)} = \sqrt{x + 2}$  $(g/f)(x) = \frac{g(x)}{g(x)} = \sqrt{x + 2}$ 

$$\frac{f(x+h) - f(x)}{h} = 6 - \frac{(x+h)^2 - (6 - x^2)}{h} = \frac{1}{h}$$

$$\frac{6 - (x^2 + 2xh + h^2) - 6 + x^2}{h} = \frac{6 - x^2 - 2xh - h^2 - 6 + x^2}{h} = \frac{1}{h}$$

$$\frac{-2xh - h^2}{k} = \frac{h(-2x - h)}{h} = 2$$

$$h \qquad h \cdot 1 \qquad -x - h$$

$$18 \cdot (f \circ g)(1) = f(g(1)) = f(1^3 + 1) = f(1 + 1) = f(2) = \frac{1}{2}$$

$$19 \cdot (g - h)(2) = g(h(2)) = g(2^2 - 2 - 2 + 3) = g(4 - 4 + 3) = g(3) = 3^3 + 1 = 27 + 1 = 28$$

$$20 \cdot (f \circ f)(0) = f(f(0)) = f(5 \cdot 0 - 4) = f(-4) = 5(-4) - 4 = -20 - 4 = -24$$

$$21 \cdot (h \circ f)(-1) = h(f(-1)) = h(5(-1) - 4) = h(-5 - 4) = \frac{1}{2}$$

**17.**  $f(x) = 6 - x^2$ 

$$h(-9) = (-9)^2 - 2(-9) + 3 = 81 + 18 + 3 = 102$$
  
**22.** (f g)(x) = f(g(x)) = f(6x+4) =  $\frac{1}{2}(6x+4) = 3x+2$ 

$$(g \circ f)(x) = g(f(x)) = g^{-1} x^{-1} x^{-1$$

The domain of f and g is  $(-\infty, \infty)$ , so the domain of  $f \circ g$  and  $g \circ f$  is  $(-\infty, \infty)$ .

**23.** ( )( ) = (()) = (<sup>N</sup>) = 3<sup>N</sup> +2  

$$f \circ g \ x \ f \ g \ x \ f \ x \ x \ x = 3^{N} +2$$
  
 $(g \circ f)(x) = g(f(x)) = g(3x + 2) = 3^{N} +2$ 

The domain of f is  $(-\infty, \infty)$  and the domain of g is  $[0, \infty)$ . Consider the domain of  $f^{\circ}g$ . Since any number can be an input for f, the domain of  $f^{\circ}g$  is the same as the domain of g,  $[0, \infty)$ . Now consider the domain of g of f. Since the input so fg

must be nonnegative, we must have  $3x+2 \ge 0$ , or x  $\Sigma$ Thus the domain of  $g \circ f$  is  $-\frac{2}{2} \propto \frac{2}{3}$  2 . 3

≥-

**24.** The graph of  $y = (h \ g)(x)$  will be the same as the graph of y = h(x) moved down *b* units.

- **25.** Under the given conditions, (f + g)(x) and (f/g)(x) have different domains if g(x) = 0 for one or more real numbers *x*.
- **26.** If *f* and *g* are linear functions, then any real number can be an input foreach function. Thus, the domain of  $f \circ g =$

the domain of  $g \circ f = (-\infty, \infty)$ .

**27.** This approach is not valid. Consider Exercise 23 on page 188 in the text, for example. Since  $(f \circ g)(x) = 4x$ ,

x - 5

$$\frac{f(x+h) - f(x)}{h} = \frac{4(x+h) - 3 - (4x - 3)}{h} = \frac{4x + 4h - 3 - 4x + 3}{h} = \frac{4h}{h} = 4$$

an examination of only this composed function would lead to the incorrect conclusion that the domain of  $f \circ g$  is  $(-\infty,5) \cup (5,\infty)$ . However, we must also exclude from the domain of  $f \circ g$  those values of x that are not in the domain of g. Thus, the domain of  $f \circ g$  is  $(-\infty, 0) \cup (0, 5) \cup (5, \infty)$ .

## Exercise Set 2.4

1. If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would not coincide, so the graph is not symmetric with respect to the *x*-axis.

If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would coincide, so the graph is symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

2. If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would not coincide, so the graph is not symmetric with respect to the *x*-axis.

If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would coincide, so the graph is symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

**3.** If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would coincide, so the graph is symmetric with respect to the *x*-axis.

If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would not coincide, so the graph is not symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would not coincide with the original graph, so it is not symmetric with respect to the origin.

**4.** If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would not coincide, so the graph is not symmetric with respect to the *x*-axis.

If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would not coincide, so the graph is not symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

**5.** If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would not coincide, so the graph is not symmetric with respect to the *x*-axis.

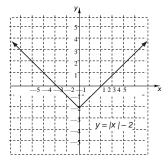
If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would not coincide, so the graph is not symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

**6.** If the graph were folded on the *x*-axis, the parts above and below the *x*-axis would coincide, so the graph is symmetric with respect to the *x*-axis.

If the graph were folded on the *y*-axis, the parts to the left and right of the *y*-axis would coincide, so the graph is symmetric with respect to the *y*-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.



The graph is symmetric with respect to the *y*-axis. It is not symmetric with respect to the *x*-axis or the origin.

Testalgebraicallyforsymmetrywithrespecttothex-axis: y = |x| - 2

# Original equation

$$-y = |x| - 2$$
 Replacing y by  $-y = y = y$ 

-|x| + 2 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Testalgebraicallyforsymmetrywithrespecttothey-axis: y = |x| - 2

Original equation

$$y = |-x| - 2$$
 Replacing x by  $-x y =$ 

|x|-2 Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the *y*-axis.

Testalgebraically forsymmetry with respect to the origin:

$$y = |x| - 2$$
 Original equation  

$$-y = |-x| - 2$$
 Replacing x by -x and  
y by -y  

$$-y = |x| - 2$$
 Simplifying

$$y = -|x| + 2$$

8.

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

У	
×+-+-+-+ 6	
	y =  x + 5   _
-10 +8 -6 +4 -2	$\begin{array}{c}$
+-+-+-+-+-+	
	$\begin{array}{c} & & & \\ & & & \\ & & & \\ \hline \\ \hline \\ \hline \\ \hline \\$
	1.1.1.1.1.1.

Thegraphisnotsymmetric with respect to the *x*-axis, the *y*-axis, or the origin.

Testalgebraicallyforsymmetrywithrespecttothex-axis: y = |x + 5|

Original equation

-y = |x+5| Replacing y by -y y = -|x+5| Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Testalgebraicallyforsymmetrywithrespecttothey-axis: y = |x + 5|Original equation

y = |-x + 5| Replacing x by -x

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

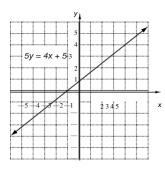
Testalgebraicallyforsymmetrywithrespecttotheorigin:

y = |x+5| Original equation

-y = |-x+5| Replacing x by-x and y by-y y = -|-x|

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

9.



The graph is not symmetric with respect to the *x*-axis, the *y*-axis, or the origin.

Testalgebraicallyforsymmetrywith respect to the x-axis: 5y = 4x + 5

	Original equation
5(-y) = 4x + 5	Replacing y by -y
-5y = 4x + 5	Simplifying
5y = -4x - 5	

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Testalgebraically for symmetry with respect to the y-axis: 5y = 4x + 5

Original equation

$$5y = 4(-x) + 5$$
 Replacing x by  $-x$   
 $5y = -4x + 5$  Simplifying

5y = -4x + 5 Simplifying

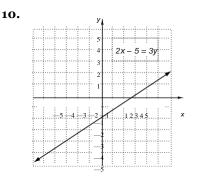
The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Testalgebraically for symmetry with respect to the origin: 5y = 4x + 5

Original equation  

$$5(-y) = 4(x) - 5$$
 Replacing x by  $-x$   
and  
y by  $-y$   
 $-5y = -4x + 5$  Simplifying  
 $5y = 4x - 5$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.



Thegraphisnotsymmetric with respect to the *x*-axis, the *y*-axis, or the origin.

Testalgebraicallyforsymmetrywithrespecttothex-axis: 2x - 5 = 3y

Original equation

$$2x - 5 = 3(-y)$$
 Replacing y by  $-y$ 

-2x + 5 = 3y Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Testalgebraically for symmetry with respect to the y-axis: 2x - 5 = 3y

Original  
equation  
$$2(-x) - 5 = 3y$$
 Replacing x by  $-x$ 

-2x - 5 = 3y Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

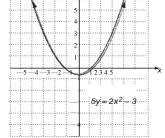
Testalgebraicallyforsymmetrywithrespecttotheorigin: 2x - 5 = 3y

Original equation

$$2(-x) - 5 = 3(-y) \text{ Replacing } x \text{ by } -x \text{ and}$$
  
y by -y  
$$-2x - 5 = -3y \qquad \text{Simplifying}$$
  
$$2x + 5 = 3y$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

11.



The graph is symmetric with respect to the y-axis. It is notsymmetric with respect to the x-axis or the origin. Test

algebraically for symmetry with respect to the x-axis:

 $5y = 2x^2 - 3$  Original equation  $5(-y) = 2x^2 - 3$  Replacing y by -y  $-5y = 2x^2 - 3$  Simplifying  $5y = -2x^2 + 3$ 

The last equation is not equivalent to the original equation, so the graph is Copyright © 2013 Pearson Education, Inc.

Testalgebraically for symmetry with respect to the y-axis:  $5y = 2x^2 - 3$ 

Original equation

$$5y = 2(-x)^2 - 3$$
 Replacing x by  $-x$ 

$$5y = 2x^2 - 3$$

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the y-axis.

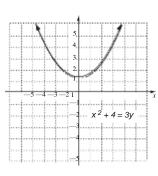
Testalgebraicallyforsymmetrywithrespecttotheorigin:  $5y=2x^2-3$ 

Original equation

$$5(-y) = 2(-x)^2 - 3$$
 Replacing x by  $-x$  and  
y by  $-y$ 

$$5y = 2x^2 - 3$$
  
Simplifying  
$$5y = -2x^2 + 3$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.



The graph is symmetric with respect to the y-axis. It is notsymmetric withrespect to the x-axis or the origin.

Testalgebraicallyforsymmetrywithrespecttothex-axis:  $x^2 + 4 = 3y$ 

Original equation  $x^2 + 4 = 3(-y)$  Replacing y by -y

 $-x^2 - 4 = 3y$ Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the x-axis.

Testalgebraically forsymmetrywithrespecttothey-axis:

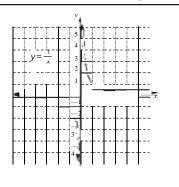
 $x^2 + 4 = 3y$  Original equation  $(-x)^2$ +4 = 3y Replacing x by -x $x^2 + 4 = 3y$ 

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the y-axis.

Testalgebraicallyforsymmetrywithrespecttotheorigin:

$$x^{2} + 4 = 3y$$
 Original equation  $(-x)^{2} + 4 = 3(-y)$  Replacing x by  $-x$  and  
y by  $-y$   
 $x^{2} + 4 = -3y$  Simplifying  
 $-x^{2} - 4 - 3y$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.



13.



x-axis:

$$-y = x$$
 Replacing y by-y  
1  
 $y = -x -$  Simplifying

The graph is not symmetric with respect to the the

y-axis. It is symmetric with respect to the origin. Testal gebraically for symmetry with respect to the 1 y = - Original equation

x

1

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the x-axis.

Testalgebraicallyforsymmetrywithrespecttothey-axis: 1

$$y =$$
Original equation  

$$x =$$

$$y =$$
Replacing x by x-x  

$$y =$$

$$y =$$
Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

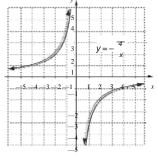
Testalgebraically forsymmetry with respect to the origin:

$$y = \frac{1}{x}$$
Original equation
$$-y = \frac{1}{\frac{1}{x}}$$
Replacing x by -x and y by -y

Simplifying *y* =  $\overline{x}$ 

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.





The graphisnot symmetric with respect to the x-axis or the y-axis. It is copyright © 2013 Pearson Education, Inc.

Testalgebraicallyforsymmetrywithrespecttothex-axis: 4  $y = -_{x}$  Original equation

4  

$$-y = -\frac{1}{x}$$
 Replacing y by  $-y$   
4  
 $y = \frac{1}{x}$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Testalgebraicallyforsymmetrywithrespecttothey-axis: 4

$$y = -\frac{4}{x}$$
 Original equation  
 $y = -\frac{4}{x}$  Replacing  $x$  by  $-x$   
 $y = \frac{-x}{x}$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis. Test algebraically for symmetry with respect to the origin:

$$y = -\frac{4}{x}$$
 Original equation  

$$-y = -\frac{4}{x}$$
 Replacing x by -x and y by -y  

$$y = -\frac{4}{x}$$
 Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the origin.

**15.** Testfor symmetry with respect to the x-axis: 5x - 5y =

0 Original equation

5x - 5(-y) = 0 Replacing y by -y

5x + 5y = 0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the y-axis: 5x - 5y =

0 Original equation

$$5(-x) - 5y = 0$$
 Replacing x by  $-x$   
 $-5x-5y = 0$  Simplifying  $5x + 1$ 

$$5y = 0$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Testforsymmetry with respect to the origin: 5x - 5y = 0

Original equation = 5(-x) = 0 Replacing

$$5(-x) - 5(-y) = 0$$
 Replacing x by  $-x$  and y by  $-y$ 

-5x+5y = 0 Simplifying 5x -

$$5v = 0$$

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**16.** Testfor symmetry with respect to the x-axis: 6x + 7y =

0 Original equation

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The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the y-axis:

6x + 7y = 0 Original equation 6(-x) +

7y = 0 Replacing x by -x

6x - 7y = 0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *y*-axis.

Testforsymmetry with respect to the origin: 6x + 7y = 0

Original equation 6(-x)+7(-y) = 0 Replacing x by -x and y by -y

$$6x + 7y = 0$$
 Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is

symmetric with respect to the origin.

**17.** Testforsymmetrywithrespecttothe *x*-axis:  $3x^2 - 2y^2 = 3$  Original equation

 $3x^2 - 2(-y)^2 = 3$  Replacing y by -y

$$6x + 7(-y) = 0$$
 Replacing y by  $-y$   
 $6x - 7y = 0$  Simplifying

$$3x^2 - 2y^2 = 3$$
  
Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis:  $3x^2 - 2y^2$ 

= 3 Original equation  

$$3(-x)^2 - 2y^2 = 3$$
 Replacing x by  
 $-x$   
 $3x^2 - 2y^2 = 3$   
Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *y*-axis.

Testfor symmetry with respect to the origin:  $3x^2 - 2y^2 =$ 

3 Original equation  $3(-x)^2 - 2(-y)^2 = 3$  Replacing x by -xand y by -y

$$3x^2 - 2y^2 = 3$$
  
Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**18.** Test for symmetry with respect to the x-axis: 5y =

 $7x^2$ - 2xOriginal equation

 $5(-y) = 7x^2 - 2x$  Replacing y by-y

 $5y = -7x^2 + 2x$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis:  $5y = 7x^2 - 7x^$ 

2*x* Original equation

 $5y = 7(-x)^2 - 2(-x)$  Replacing *x* by -x

 $5y = 7x^2 + 2x$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:  $5y = 7x^2 - 2x$ Original equation  $5(-y) = 7(-x)^2 - 2(-x)$  Replacing x by -x

 $-5y = 7x^2 + 2x$   $5y = -7x^2 - 2x$ Simplifying  $5y = -7x^2 - 2x$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**19.** Test for symmetry with respect to the *x*-axis: y = |2x|

Original equation

-y = |2x| Replacing y by -y y =

-|2x| Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis: y = |2x|

Original equation

$$y = |2(-x)|$$
 Replacing x by  $-x y =$ 

|-2x| Simplifying

y = |2x|

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:

$$y = |2x|$$
 Original equation  

$$-y = |2(-x)|$$
 Replacing x by -x and y by -y  

$$-y = |-2x|$$
 Simplifying  

$$-y = |2x|$$
  

$$y = -|2x|$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**20.** Test for symmetry with respect to the x-axis:  $y^3 = 2x^2$ 

Originalequation

 $(-y)^3 = 2x^2$  Replacing y by-y  $-y^3 = 2x^2$  Simplifying  $y^3 = -2x^2$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis:  $y^3 = 2x^2$ 

Original equation

$$y^3 = 2(-x)^2$$
 Replacing x by  $-x y^3 = 2x^2$  Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:

$$y^3 = 2x^2$$
 Original equation  $(-y)^3 = 2(-x)^2$  Replacing x by -x and  
y by -y  
 $-y^3 = 2x^2$  Simplifying  
 $y^3 = -2x^2$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**21.** Test for symmetry with respect to the x-axis:  $2x^4 + 3 =$ 

$$y^2$$
 Original equation  $2x^4$ 

+ 3 =  $(-y)^2$  Replacing y by  $-y 2x^4 + 3 = y^2$ 

Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *x*-axis.

Test for symmetry with respect to the y-axis:  $2x^4 + 3 =$ 

 $y^2$  Original equation

$$2(-x)^4 + 3 = y^2$$
 Replacing x by  $-x$ 

 $2x^4 + 3 = y^2$  Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:  $2x^4 + 3 =$ 

Original equation

 $2(-x)^4 + 3 = (-y)^2 \text{ Replacing } x \text{ by } -x$ and y by -y

 $v^2$ 

12

 $2x^4 + 3 = y^2$  Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**22.** Test for symmetry with respect to the *x*-axis:  $2y^2 = 5x^2$ 

+ 12 Original equation

$$2(-y)^2 = 5x^2 + 12$$
 Replacing y by  $-y$ 

 $2y^2 = 5x^2 + 12$  Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the *x*-axis.

Testfor symmetry with respect to the y-axis:  $2y^2 = 5x^2$ 

+12 Original equation 
$$2y^2$$
  
= 5(-x)<sup>2</sup> +12 Replacing x by -x  $2y^2$  =5x<sup>2</sup> +  
12 Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:  $2y^2 = 5x^2 +$ 

Original equation

 $2(-y)^{2} = 5(-x)^{2} + 12 \text{ Replacing } x \text{ by } -x$ and y by -y  $2y^{2} = 5x^{2} + 12 \text{ Simplifying}$ 

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**23.** Test for symmetry with respect to the x-axis:  $3y^3 = 4x^3$ 

+2 Original equation  $3(-y)^3 = 4x^3+2$  Replacing y by -y  $-3y^3 = 4x^3+2$  Simplifying  $3y^3 = -4x^3-2$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis:  $3y^3 = 4x^3$ 

+2 Original equation 
$$3y^3$$

$$= 4(-x)^3 + 2 \text{ Replacing } x \text{ by } -x 3y^3 = -4x^3 + 2 \text{ Simplifying}$$

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:  $3y^3 = 4x^3 +$ 

2 Original equation  

$$3(-y)^3 = 4(-x)^3 + 2$$
 Replacing x by  $-x$   
and y by  $-y$ 

 $-3y^3 = -4x^3 + 2$  Simplifying

 $3y^3 = 4x^3 - 2$ 

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**24.** Test for symmetry with respect to the x-axis: 
$$3x = |y|$$

Original equation

$$3x = |-y|$$
 Replacing y by  $-y$ 

3x = |y| Simplifying

The last equation is equivalent to the original equation, so the graph is symmetric with respect to the *x*-axis.

Test for symmetry with respect to the *y*-axis: 3x = |y|

Original equation

3(-x) = |y| Replacing x by -x

-3x = |y| Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Testforsymmetry with respect to the origin: 3x = |y|

Original equation

3(-x) = |-y| Replacing *x* by -x and *y* by -y

-3x = |y| Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**25.** Test for symmetry with respect to the *x*-axis: xy = 12

Original equation

x(-y) = 12	Replacing <i>y</i> by- <i>y</i>
-xy = 12	Simplifying

xy = -12

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Test for symmetry with respect to the y-axis: xy = 12

Original equation

$$-xy = 12$$
 Replacing x by  $-xxy$ 

= -12 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the origin.

**26.** Testforsymmetrywithrespecttothex-axis:  $xy - x^2 =$ 

 $x(-y) - x^2 = 3$  Replacing y by -y xy

 $+x^2 = -3$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the x-axis.

Test for symmetry with respect to the y-axis:  $xy - x^2 =$ 

3 Original equation

$$-xy - (-x) = 3$$
 Replacing x by  $-x$   
 $xy + x^2 = -3$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:

$$xy - x^2 = 3$$
 Original equation

$$-x(-y) - (-x)^2 = 3$$
 Replacing x by  $-x$  and y by  $-y$ 

$$xy - x^2 = 3$$
 Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**27.** *x*-axis: Replace *y* with -*y*; (-5,-6)

*y*-axis: Replace *x* with -x; (5, 6) Origin: Replace *x* with -x and *y* with -y; (5, -6)

**28.** x-axis: Replace y with -y;  $\frac{7}{7}$ ,

y-axis: Replace x with 
$$-x$$
;  $-\frac{7}{2}$ ,  $0$ 

Origin: Replace x with -x and y with -y; -, 0

**29.** *x*-axis: Replace *y* with -y; (-10,7) *y*-axis: Replace *x* with -x; (10, -7)

Origin: Replace x with -x and y with -y; (10, 7) **30.** x-axis: Replace y with -y; 1,  $-\frac{3}{\pi}$ 

y-axis: Replace x with 
$$-x$$
;  $-1$ ,  $\frac{3}{2}\Sigma$ 

Origin: Replace x with -x and y with -y; -1, -1

**31.** *x*-axis: Replace *y* with -*y*; (0,4) *y*-axis: Replace *x* with -*x*; (0, -4)

xy = 12 Original equation

$$x(-y) = 12$$
 Replacing x by  $-x$  and y by  $-y$   $xy = 12$ 

<sup>8</sup>. <u>3</u>Σ

8

# Simplifying

Test for symmetry with respect to the origin opyright © 2013 Pearson Education, Inc.

Origin: Replace x with -x and y with -y; (0, 4)

- 32. *x*-axis: Replace *y* with -*y*; (8, 3) *y*-axis: Replace *x* with -*x*; (-8, -3)
  Origin: Replace *x* with -*x* and *y* with -*y*; (-8, 3)
- **33.** The graph is symmetric with respect to the *y*-axis, so the function is even.

- **34.** The graph is symmetric with respect to the *y*-axis, so the function is even.
- **35.** The graph is symmetric with respect to the origin, so the function is odd.
- **36.** The graphisnot symmetric with respect to either the y- axis or the origin, so the function is neither even norodd.
- **37.** Thegraphisnotsymmetric with respect to either the y- axis or the origin, so the function is neither even no rodd.
- **38.** Thegraphisnotsymmetric with respect to either the y- axis or the

origin, so the function is neither even norodd.

**39.** 
$$f(x) = -3x^3 + 2x$$
  
 $f(-x) = -3(-x)^3 + 2(-x) = 3x^3 - 2x$   
 $-f(x) = -(-3x^3 + 2x) = 3x^3 - 2x$   
 $f(-x) = -f(x)$ , so f is odd.

**40.** 
$$f(x) = 7x^3 + 4x - 2$$
  
 $f(-x) = 7(-x)^3 + 4(-x) - 2 = -7x^3 - 4x - 2$   
 $-f(x) = -(7x^3 + 4x - 2) = -7x^3 - 4x + 2$ 

 $f(x) \neq f(-x)$ , so f is not even. f(-x) = -f(x), so f is not odd.

Thus,  $f(x) = 7x^3 + 4x - 2$  is neither even no rodd.

**41.** 
$$f(x) = 5x^2 + 2x^4 - 1$$
  
 $f(-x) = 5(-x)^2 + 2(-x)^4 - 1 = 5x^2 + 2x^4 - 1$   
 $f(x) = f(-x)$ , so f is even.

1

х

**42.**  $f(x) = x + \frac{1}{x}$ 

f(-x) = -f(x), so f is odd.

**43.**  $f(x) = x^{17}$  $f(-x) = (-x)^{17} = -x^{17}$  $-f(x) = -x^{17}$ 

f(-x) = -f(x), so f is odd.

**44.** 
$$f(x) = {}^{3}x$$

**46.** 
$$f(x) = \frac{1}{x^2}$$
  
 $f(-x) = \frac{x^2}{(-x)^2} x^2$ 

$$f(x) = f(-x)$$
, so f is even.

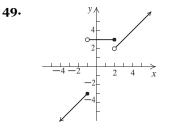
f(x) = 8  

$$f(-x)=8$$
  
 $f(x)=f(-x)$ , so f is even.

**48.** 
$$f(x) = x_{2+1} \sqrt{2}$$

$$f(-x) = (-x)^2 + 1 = x^2 + 1$$

$$f(x) = f(-x)$$
, so f is even.



**50.** *Familiarize*. Let t = the price of a ticket to the closing ceremonies. Then t+325 = the price of a ticket to the opening ceremonies. Together, thetwo tickets cost t + (t + 325) = 2t + 325.

*Translate*. Thetotalcostofthetwoticketsis\$1875, so we have the following equation.

$$2t + 325 = 1875$$

*Carry out*. We solve the equation. 2t + 325 = 1875

$$2t = 1550$$

*t* = 775

Then t + 325 = 775 + 325 = 1100.

*Check*. \$1100is\$325morethan\$775and\$775+\$1100 = \$1875, so the answer checks.

**State**. Atickettotheopeningceremoniescost\$1100,and a ticket to the closing ceremonies cost \$775.

1

**51.** 
$$f(x) = x \cdot 10 - \frac{1}{x^2}$$

$$f(\sqrt{x}) = x \quad 10 \quad (x)^2 = x^{-1} 10 \qquad x^2$$
  
-  $f(x) = -x^{-1} 10 - x_{-1}$ 

2

Since 
$$f(-x) = -f(x)$$
,  $f$  is odd.  
52.  
 $f(x) = \frac{x^2 + 1}{x^3 + 1}$   
 $f(-x)^2 + 1$   
 $f(-x)^2 + 1$   
 $f(-x) = -x - |x|$   
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f(-x) =

$$-f(x) = -(x - |x|) = -x + |x| f(x)$$
  

$$f = f(-x), \text{ so } f \text{ is not even. } f(-x) f =$$
  

$$-f(x), \text{ so } f \text{ is not odd.}$$
  
Thus,  $f(x) = x - |x|$  is neither even no rodd.

$$(-x)^{3} + 1^{=} -x^{3}$$

$$x^{2} + 1 + 1$$

$$-f(x) = -x^{3} + 1$$
Since  $f(x) f = f(-x), f$  is not even. Since
$$f(-x) f = -f(x), f$$
 is not odd.
$$x^{2} + 1$$
Thus,  $f(x) = \frac{x^{3} + 1}{x^{3} + 1}$  is neither even nor odd.

53. If the graph were folded on the x-axis, the parts above and below the x-axis wouldcoincide, so the graphissymmetric with respect to the x-axis.

If the graph were folded on the y-axis, the parts to the left and right of the y-axis would not coincide, so the graph is not symmetric with respect

with the original graph, so it is not symmetric with respect to the origin.

**54.** If the graph were folded on the x-axis, the parts above and below the x-

to the *x*-axis.

If the graph were folded on the y-axis, the parts to the left and right of the y-axis would not coincide, so the graph is not symmetric with respect to they-axis.

If the graph were rotated 180°, the resulting graph would coincide with the original graph, so it is symmetric with respect to the origin.

55. See the answer section in the text.

**56.** 
$$O(-x) = \frac{f(-x) - f(-(-x))}{2} = \frac{f(-x) - f(x)}{2}, 2^2$$
  
 $-O(x) = -\frac{f(x) - f(-x)}{2} = \frac{f(-x) - f(x)}{2}.$  Thus,  
 $O(-x) = -O(x)$  and  $O$  is odd.

- 57. a), b) See the answer section in the text.
- **58.** Let f(x) = g(x) = x. Now f and g are odd functions, but  $(fg)(x) = x^2$ = (fg)(x). Thus, the product is even, so the statement is false.

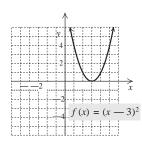
$$(-x)$$
 and  $g(x) = g(-x)$ . Thus,  $(f + g)(x) = f(x) + g(x) = f(-x) + g(-x) = (f + g)(-x)$  and  $f + g$  is

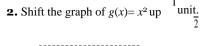
even. The statement is true.

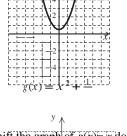
definition f(x) = f(x) and g(x) = g(x), or g(x) =- g(

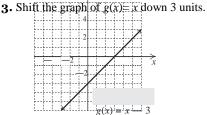
-fg(\*), and fg is odd. The f(-x) g(x) =statement is true.

### Exercise Set 2.5







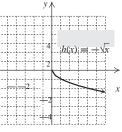


**4.** Reflect the graph of g(x) = x across the x-axis and then shift it down 2 units.

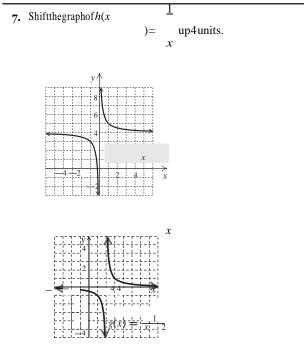
2 2	
g(x) =	-x-2



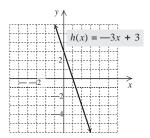
**5.** Reflect the graph of h(x) = x across the *x*-axis.



				4						
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[ "				4				_	[ "	
	g(,	x)	=	4	x	_	_			
	1									



**9.** First stretch the graph of h(x) = x vertically by multiplying each *y*-coordinate by 3. Then reflect it across the *x*-axis and shift it up 3 units.



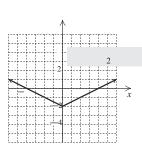
**10.** Firststretchthegraphof f(x) = x vertically by multiply- ingeach *y*-coordinate by 2. Thenshiftitup 1 unit.

 /

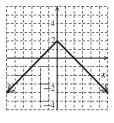
$$f(x) = 2x + 1$$

**11.** First shrink the graph of h(x) = |x| vertically by multiply-

1

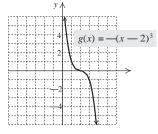


**12.** Reflect the graph of  $g(x) = x \operatorname{acros} |s|$  the *x*-axis and shift it up 2 units.



g(x) = -|x| + 2

**13.** Shiftthegraphof  $g(x) = x^3$  right 2 units and reflect it across the *x*-axis.

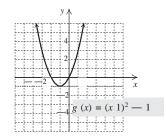


**14.** Shift the graph of  $f(x) = x^3$  left 1 unit.

|--|

 $f(x) = (x + 1)^3$ 

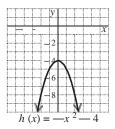
**15.** Shiftthegraphof  $g(x) = x^2 \operatorname{left} 1$  unit and down 1 unit.



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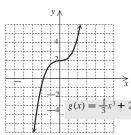
#### Exercise Set 2.5

**16.** Reflect the graph of  $h(x) = x^2$  across the x-axis and down 4 units.



**17.** Firstshrinkthegraphof $g(x) = x^3$  verticallyby multiply- 1 -coordinate by  $_3$ . Then shift it up 2 units.

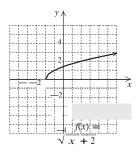
ing eachy



**18.** Reflect the graph of  $h(x) = x^3$  across the y-axis.

	1 <u>y</u>		K - L - L - L - L - L - J
h(x)	4	$(-x)^3$	1-1-2-2-2-1-1

**19.** Shiftthe graph of  $f(x) = x \operatorname{left} 2 \operatorname{units}$ .



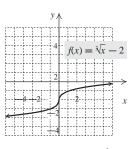
**20.** Firstshiftthegraphof f(x) = x right 1 unit. Shrinkit vertically by

multiplying each *y*-coordinate by and then reflect it across the *x*-axis.

 $V(\mathbf{k}) = \frac{1}{2} \sqrt{2} \sqrt{2}$ 

**21.** Shift the graph of  $f(x) = {}^{3}x$  down 2 units.

 $\sqrt{}$ 



**22.** Shift the graph of  $h(x) = {}^{3}x$  left 1 unit.

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	hi	r	-	- 1	K/ 3	2.1	L.	1	

23. Think of the graph of f(x) = |x|. Since g(x) = f(3x), the graph of g(x) = |3x| is the graph of f(x) = |x| shrunk horizontally by dividing each *x*- $\Sigma \qquad 1$ 

coordinate by 3 or multiplying each x-coordinate by  $_3$ .

 $\sqrt{1}$ graph of  $f(x) = \frac{3}{2} \frac{x}{2}$  is the graph of  $g(x) = \frac{3}{2} x$  shrunk  $\frac{2}{-1}$ vertically by multiplying each y-coordinate by  $\frac{1}{2}$ .

$$f(x) = x$$
. Since  $h(x) = f(x)$ 

the graph of  $h(x = 2 \qquad f(x = 1)$ ) = isthegraph of -

= x stretched

x y - x vertically by multiplying each *y*-coordinate by 2.

**26.** Think of the graph of g(x) = |x|. Since f(x) = g(x-3)-4, the graph of

f(x) = |x - 3| - 4 is the graph of g(x) = |x|

shifted right 3 units and down 4 units. **27.** Think of the graph of () =  $\therefore$  Sin<u>c</u>xe () =  $\Im(x) = g x - 5$ ,

the graph of 
$$f(x) = 3x^{\sqrt{g X}} - 5$$
 is the graph of  $g(x) = \sqrt[\gamma]{x}$  -

stretched vertically by multiplying each *y*-coordinate by 3 and then shifted down 5 units.

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2

**28.** Thinkofthegraphof
$$g(x) = \frac{1}{x}$$
. Since  $f(x) = 5 - g(x)$ , or   
 $x = 1$ 

1

$$f(x) = -g(x)+5$$
, the graph of  $f(x) = 5 - \frac{1}{x}$  is the graph  
of  $g(x) = \frac{1}{x}$  reflected across the x-axis and then shifted up 5

units.

х

**29.** Think of the graph of 
$$f(x) = |x|$$
. Since  $g(x) = \sum_{\substack{x \\ x \\ 3}} - 4$ , the graph of  $g(x) = \frac{1}{x} - 4$  is the graph of  $g(x) = \frac{1}{x} - \frac{1}{x}$ 

f(x) = x stretchedhorizontallybymultiplyingeachx- coordinate

by3 and then shifted down 4 units. **30.** Think of the graph of () = 3. Since

$$f(x) = \frac{2}{g}(x) - 4$$
, the graph of  $f(x) = \frac{2}{x^3} - 4$  is the

3 graphof  $g(x) = x^3$  shrunkvertically by multiplyingeach 2 y-coordinate by 3 and then shifted down 4 units.

- **31.** Thinkofthegraphof  $g(x) = x^2$ . Since  $f(x) = -\frac{1}{g(x-5)}$ , the graph of  $f(x) = -\frac{1}{4}(x-5)^2$  is the graph of  $g(x) = x^2$ shiftedright5units, shrunkverticallybymultiplyingeach 1 y-coordinate by  $_{\Delta}$ , and reflected across the x-axis.
- **32.** Think of the graph of  $g(x) = x^3$ . Since f(x) = g(x) = 5, the graph of  $f(x) = (x)^3 5$  is the graph of  $g(x) = x^3$  reflected across the yaxisandshifteddown5units.

**33.** Think of the graph of (  

$$g(x) = .$$
 Since  $f(x) = \frac{1}{x+3} + 2$ , the graph of  $f(x) = \frac{1}{x+3} + 2$  is the graph

of g(x) = shifted left 3 units and up 2 units.

**34.** Think of the graph of  $(f = x^{\gamma})$ . Since  $(f = (g x_{\gamma} - f - x) + 5$ . the graph of g(x) =

x+5 is the graph of f(x) = xreflected across the y-axis and shifted up 5 units.

- **35.** Think of the graph of  $f(x) = x^2$ . Since h(x) = f(x 3) + 5, the graph of  $h(x) = (x \ 3)^2 + 5$  is the graph of  $f(x) = x^2$  shifted right 3 units, reflected across the x-axis, and shifted up 5 units.
- **36.** Thinkofthegraphof  $g(x) = x^2$ . Since f(x) = 3g(x+4) 3, the graph $off(x)=3(x+4)^2$  3isthegraphof $g(x-)=x^2$  shifted left 4 units, stretched vertically by multiplying each y-coordinate by 3, and then shifted down 3units.
- **37.** The graph of y = g(x) is the graph of y = f(x) shrunk

vertically by a factor of  $\frac{1}{2}$ . Multiply the *y*-coordinate by  $\frac{1}{2}^2$  (-12, 2).

**40.** The graph of 
$$y = g(x)$$
 is the graph of  $y = f(x)$  shrunk  
horizontally. The *x*-coordinates of  $y = g(x)$  are <sup>1</sup> – the  
corresponding *x*-coordinates of  $y = f(x)$ , so we div <sup>4</sup>  
the  
-  $\Sigma$  1 ide

*x*-coordinate by 4 or multiply it by  $_4$  : (-3,-4).

- **41.** The graph of y = g(x) is the graph of y = f(x) shifted down 2 units. Subtract 2 from the *y*-coordinate: (-12, 2).
- **42.** The graph of y = g(x) is the graph of y = f(x) stretched horizontally. The x-coordinates of y = g(x) are twice the corresponding xcoordinates of y = f(x), so we multiply

the *x*-coordinate by 2<sup>-</sup> ordivide it by 1 : (-24, 4).

**43.** The graph of y = g(x) is the graph of y = f(x) stretched

verticallybyafactorof4. Multiplythey-coordinateby4: (-12, 16).

- **44.** The graph of y = g(x) is the graph y = f(x) reflected across the xaxis. Reflect the point across the x-axis: (-12, -4).
- **45.**  $g(x) = x^2 + 4$  is the function  $f(x) = x^2 + 3$  shifted up 1 unit, so g(x)=f(x)+1. Answer B is correct.
- **46.** If we substitute 3x for x in f, we get  $9x^2+3$ , so g(x) = f(3x). Answer D is correct.
- 47. If we substitute x-2 for x in f, we get  $(x-2)^3+3$ , so g(x)=f(x-2). Answer A is correct.
- **48.** If we multiply  $x^2 + 3$  by 2, we get  $2x^2 + 6$ , so g(x) = 2f(x).

Answer C is correct.

**49.** Shape:  $h(x) = x^2$ 

Turn h(x) upside-down (that is, reflect it across the x- axis): g(x) = $-h(x) = -x^2$ 

**50.** Shafteg(x) right  $\sqrt{8}$  units:  $f(x) = g(x - 8) = -(x - 8)^2$ 

$$h x \qquad x$$
  
Shift  $h(x)$  left 6 units:  $g(x) = h(x+6) = \sqrt[\gamma]{x+6}$   
down 5 units:  $f(x) = g(x) - 5 = x+6 - 5$ 

**51.** Shape: h(x) = |x|

Shift h(x) left 7 units: g(x) = h(x + 7) = |x + 7| Shift g(x) up 2 units: f(x) = g(x) + 2 = |x + 7| + 2

**52.** Shape:  $h(x) = x^3$ 

Turn h(x) upside-down (that is, reflect it across the x- axis): g(x) =

$$-h(x) = -x^3$$
  
Shift  $g(x)$  right 5 units:  $f(x) = g(x - 5) = -(x - 5)^3$ 

х

**53.** Shape: 
$$h(x) = -$$

**38.** The graph of y = g(x) is the graph of y = f(x) chifted right 2013 Pearson Education. Inc. Shrink h(x) Vertically by a factor of 2 that is,

units. Add 2 to the *x*-coordinate: (-10,4).

**39.** The graph of y = g(x) is the graph of y = f(x) reflected across the y-axis, so wereflect the point across the y-axis:

(12,4).

multiply each function value by 2: 1 g(x)=h(x)=2  $2 \cdot x \text{ or } 2x$ Shift g(x) down 3 units: f(x)=g(x) - 3=1 - 3 2x

#### Exercise Set 2.5

- **54.** Shape:  $h(x) = x^2$ Shift h(x) right 6 units:  $g(x) = h(x-6) = (x-6)^2$  Shift g(x) up 2 units:  $f(x) = g(x) + 2 = (x-6)^2 + 2$
- **55.** Shape:  $m(x) = x^2$ 
  - Turn m(x) upside-down (that is, reflect it across the x- axis):  $h(x) = -m(x) = -x^2$

Shift h(x) right 3 units:  $g(x) = h(x-3) = -(x-3)^2$  Shift g(x) up 4 units:  $f(x) = g(x) + 4 = -(x-3)^2 + 4$ 

**56.** Shape: h(x) = |x|

Stretch h(x) horizontally by a factor of 2 that is, multiply  $\sum_{1} - \sum_{1} \frac{1}{1}$ each x-value by 2:  $\frac{g(x)}{2} = h_2 x = \frac{1}{2} x - \frac{1}{2}$ 

- Shift g(x) down 5 units:  $f(x) = g(x) 5 = \frac{1}{2}x 5$ .
- **57.** Shape:  $m(x) = \sqrt[\gamma]{x}$

Reflect m(x) across the y-axis:  $h(x) = m(-x) = \sqrt[\gamma]{-x}$ Shift h(x) left 2 units:  $g(x) = h(x+2) = \sqrt[\gamma]{-(x+2)}$ Shift g(x) down 1 unit: f(x) = g(x) - 1 =

$$-(x+2) - 1$$

**58.** Shape: h(x) =

Reflect h(x) across the *x*-axis: g(x) = -h(x) = -

x

1 = \_\_\_+1

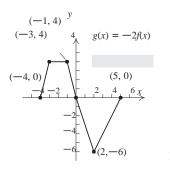
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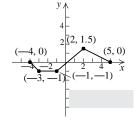
Shift g(x) up 1 unit: f(x)=g(x)+1=

59. Each y-coordinate is multiplied by-2. We plot and con-

nect (-4, 0), (-3, 4), (-1, 4), (2, -6), and (5, 0).

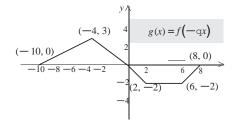


**60.** Each y -coordinate is multiplied by  $_2$ . We plot and connect



**61.** Thegraphisreflectedacrossthe*y*-axisandstretchedhor- izontally by a factor of 2. That is, each *x*-coordinate is

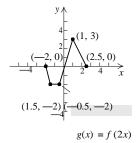
multiplied by -2 or divided by  $-\frac{1}{2}$ . We <del>p</del>lot and connect (8, 0), (6, -2), (2, -2), (-4, 3), and (-10, 0).



**62.** The graph is shrunk horizontally by a factor of 2. That is, each xcoordinate is divided by  $2 - \sum_{\text{or multiplied by}} \frac{1}{2}$ 

We plot and connect ( 2, 0), ( 1.5, 2), ( 0.5, 2), (1, 3), -

and (2.5, 0).



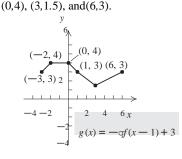
**63.** The graph is shifted right 1 unit so each *x*-coordinate is increased by 1.

The graph is also reflected across the x- axis, shrunk vertically by a factor of 2, and shifted up 3

units. Thus, each y-coordinate is multiplied by- and then increased

by 3. We plot and connect (-3, 3), (2, 4),

1

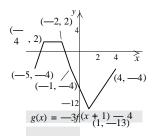


**64.** The graph is shifted left 1 unit so each x-coordinate is decreased by

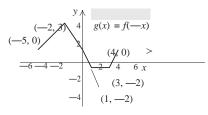
*I*. The graph is also reflected across the *x*-axis, stretched vertically by a factor of 3, and shifted down 4 units. Thus, each *y*-coordinate is multiplied by -3 and then decreased by 4. We plot and connect (-5, -4), (-4, 2), (-2, 2), (1, -13), and (4, -4).

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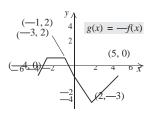
 $-4 \quad g(x) = \operatorname{q} f(x)$ 



**65.** The graph is reflected across the y-axis so each x-coordinate is replaced by its opposite.

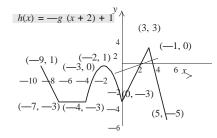


**66.** The graph is reflected across the *x*-axis soeach *y*-coordinate is replaced by its opposite.



**67.** The graph is shifted left 2 units so each *x*-coordinate is decreased by 2.

Itisalsoreflectedacrossthe*x*-axissoeach *y*-coordinateisreplacedwithits opposite. In addition, the graph is shifted up 1 unit, so each *y*-coordinate is then increased by 1.



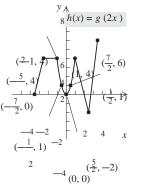
68. The graphis reflected across the y-axis so each x-coordinate is replaced with its opposite. It is also shrunk vertically by a 1

factorof ,soeachy-coordinateismulti-

plied by 2 (or divided by 2).

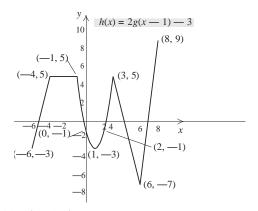
 $(-7.3) (-2,2)^{4} (0,0) (2,2) (5.2) (7.0) (-5,-1) (-1,\frac{1}{2}) (-1,\frac$ 

**69.** The graph is shrunk horizontally. The *x*-coordinates of y = h(x) are one-half the corresponding *x*-coordinates of y = g(x).



- **70.** Thegraphisshifted right 1 unit, soeach *x*-coordinate is increased by 1. It is also stretched vertically by afactor
  - of 2, so each y-coordinate is multiplied by 2 or divided

by <sub>21</sub>. In addition, the graphiss hifted down 3 units, so each y-coordinate is decreased by 3.



**71.** 
$$g(x) = f(-x) + 3$$

The graph of g(x) is the graph of f(x) reflected across the *y*-axis and shifted up 3 units. This is graph (f).

**72.** g(x)=f(x)+3

The graph of g(x) is the graph of f(x) shifted up 3 units. This is graph (h).

**73.** g(x) = -f(x) + 3

The graph of g(x) is the graph of f(x) reflected across the *x*-axis and shifted up 3 units. This is graph (f).

**74.** g(x) = -f(-x)

The graph of g(x) is the graph of f(x) reflected across the

x-axis and the y-axis. This is graph (a).

75. 
$$g(x) = \frac{1}{3}f_3(x-2)$$

Thegraphof*g*(*x*)isthegraphof*f*(*x*)shrunkvertically by a factor of

3 that is, each y-coordinate is multiplied  $1\Sigma$ 

by and then shifted right 2 units. This is graph (d). Copyright © 2013 Pearson Education, Inc.

**76.**  $g(x) = \frac{1}{2}f_2(x) - 3$ 

The graph of g(x) is the graph of f(x) shrunk vertically by a factor of

 $\frac{3}{1\Sigma}$  that is, each y-coordinate is multiplied

by  $\tau$ -andthenshifteddown 3 units. This is graph(e).

77. 
$$g(x) = \frac{1}{5} \frac{f_{-1}(x+2)}{3}$$

The graph of g(x) is the graph of f(x) shrunk vertically by a factor of 3 that is, each y-coordinate is multiplied  $1\Sigma$ 

by  $3^{-}$  and then shifted left 2 units. This is graph (c).

78. g(x) = -f(x+2)

The graph of g(x) is the graph f(x) reflected across the *x*-axis and shifted left 2 units. This is graph (b).

**79.** 
$$f(-x) = 2(-x)^4 - 35(-x)^3 + 3(-x) - 5 = 2x^4 + 35x^3 - 3x - 5 = g(x)$$

**80.** 
$$f(-x \quad \underline{1} \quad -x \quad 4 \quad \underline{1} \quad -x) \quad -81(-x) \quad -17 = 1$$
  
 $1 \quad \underline{1}_{x^4} - \underline{1}_{x^3} - 81x^2 - 17 \quad g(x)$   
 $4 \quad 5$ 

- **81.** The graph of  $f(x) = x^3 3x^2$  is shifted up 2 units. A formula for the transformed function is g(x) = f(x) + 2, or  $g(x) = x^3 3x^2 + 2$ .
- 82. Eachy-coordinate of the graph of  $f(x) = x^3 3x^2$  is multiplied by <sup>1</sup>. A formula for-the transformed function is  $h(x) = \frac{1}{f} f(x)$ , or  $h(x) = \frac{1}{x^3 - 3x^2}$ .
- **83.** The graph of  $f(x) = x^3 3x^2$  –isshifted left 1 unit. A formula for the transformed function is k(x) = f(x+1), or  $k(x) = (x+1)^3 3(x+1)^2$ .
- 84. The graph of  $f(x) = x^3 3x^2$  is shifted right 2 units and up 1 unit. A formula for the transformed function is t(x) = f(x-2)+1, or  $t(x) = (x-2)^3 3(x-2)^2 + 1$ .

 $(x) = \int (x - 2) + 1, \text{ of } l(x) = (x - 2)^{\circ} - 3(x - 2) + 1$ 

**85.** Test for symmetry with respect to the x-axis.  $y = 3x^4 - x^4$ 

3 Original equation

$$-y = 3x^4 - 3$$
 Replacing y by  $-y = 3x^4 - 3$ 

 $-3x^4 + 3$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the x-axis. Test for

symmetry with respect to the y-axis.

$$y = 3x^4 - 3$$
 Original equation  $y = 3(-x)^4 - 3$  Replacing x by  $-x y = 3x^4 - 3x^4$ 

Simplifying

Thelastequationisequivalenttotheoriginal equation, so the graph is symmetric with respect to the *y*-axis.

Test for symmetry with respect to the origin:

$$y = 3x^4 - 3$$
  
-y = 3(-x)^4 - 3 Replacing x by -x and  
y by -y

 $-y = 3x^4 - 3$ 

3

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

**86.** Testforsymmetrywithrespecttothex-axis.  $y^2 = x$ Original equation

 $(-y)^2 = x$  Replacing y by  $-y y^2 = x$ 

Simplifying

9

Thelastequationisequivalenttotheoriginalequation, so the graph is

symmetric with respect to the *x*-axis. Test for symmetry with respect to the *y*-axis:  $y^2 = x$ Original equation

y = -x Replacing x by -x

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Test for symmetry with respect to the origin:

 $y^2 = x$  Original equation  $(-y)^2 = -x$  Replacing x by-x and

y by -y

 $y^2 = -x$  Simplifying Thelastequationisnotequivalenttotheoriginalequation, sothegraphisnotsymmetric with respect to the origin.

**87.** Testforsymmetry with respect to the *x*-axis: 2x - 5y = 0

$$2x - 5(-y) = 0$$
 Replacing y by  $-y$   
 $2x + 5y = 0$  Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis. Test for symmetry with respect to the *y*-axis:

2x-5y = 0 Original equation 2(-x)-

5y = 0 Replacing *x* by-*x* 

-2x - 5y = 0 Simplifying

The last equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Testfor symmetry with respect to the origin: 2x-5y=0

Original equation

$$2(-x) - 5(-y) = 0$$
 Replacing x by  $-x$  and  
y by  $-y$ 

$$y$$
 by  $2x + 5y = 0$ 

$$2x - 5y = 0$$
 Simplifying

Thelastequationisequivalenttotheoriginalequation, so the graph is symmetric with respect to the origin.

**88.** Let m = the number of Madden games sold, in millions. Then 3m-1 = the number of Wii Fit games sold.

Solve: 3m - 1 = 3.5

m = 1.5 million games

**89.** *Familiarize*. Let *g* = the total amount spenton giftcards, in billions of dollars.

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 $y = -3x^4 + 3$  Simplifying

 $5 = 0.06 \cdot g$ 

Carry out. We solve the equation.

 $5 = 0.06 \cdot g$  5 = g 0.06  $83.3 \approx g$ 

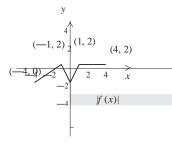
**Check.** 6% of \$83.3 billion is 0.06(\$83.3 billion) =\$4.998billion  $\approx$  \$5 billion. (Remember that werounded the value of *g*.) The answer checks.

State. About \$83.3 billion was spent on gift cards.

**90.** Let *n* = the number of tax returns e-filed in 2005, in mil-lions.

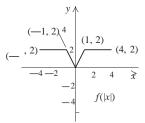
Solve: n + 0.439n = 98.3 $n \approx 68.3$  mllion returns

**91.** Each point for which f(x) < 0 is reflected across the x-axis.

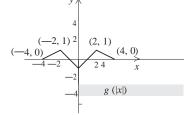


**92.** The graph of y = f(|x|) consists of the points of y = f(x) for which  $x \ge 0$  along with their reflections across the

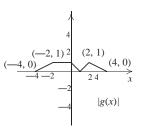
y-axis.

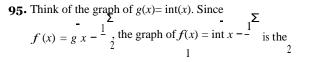


**93.** The graph of y=g(x) c|o|nsists of the points of y=g(x) for which x 0 along with the  $\geq$  ir reflections across the y-axis.

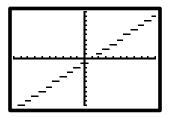


**94.** Eachpointforwhich g(x) < 0 is reflected across the x-axis.





graph of g(x) = int(x) shifted right unit. The domain is the set of all real numbers; the range is the set of all integers.

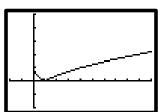


**96.** This function can be defined piecewise as follows:

$$f(x) = \begin{array}{c} (x-1), \text{ for } 0 \le x < 1, \\ \Box \checkmark \\ x-1, \qquad \text{ for } x \ge 1, \end{array}$$

Think of the graph of g(x) = x. First shift it down

1 unit. Then reflect across the *x*-axis the portion of the graph for which 0 < x < 1. The domain and range are both the set of nonnegativereal numbers, or  $[0, \infty)$ .



**97.** On the graph of y = 2f(x) each y-coordinate of y = f(x) is multiplied by 2, so(3, 4, 2), or(3, 8) is south etransformed graph.

On the graph of y = 2 + f(x), each y-coordinate of y = f(x) is increased by 2 (shifted up 2 units), so (3, 4+2), or (3, 6) is on the transformed graph.

On the graph of y = f(2x), each x-coordinate of  $\Sigma = f(x)$  ismultiplied by (ordivided by 2), so  $\frac{1}{2} \cdot 3,4$ , or

$$\frac{\Sigma}{2}$$
,  $\frac{\Sigma}{4}$  is on the transformed graph. 2

#### Exercise Set 2.6

**98.** Using a graphing calculator we find that the zeros are -2.582, 0, and 2.582.

The graph of  $y = f(x \ 3)$  is the graph of y = f(x) shifted right 3 units. Thus we shift each of the zeros of f(x) 3 units

righttofindthezerosof*f*(*x*-3). Theyare-2.582+3, or 0.418; 0 + 3, or 3; and 2.582+3, or 5.582.

The graph of y = f(x+8) is the graph of y = f(x) shifted 8 units left. Thus we shift each of the zeros of f(x) 8 units left to find the zeros of f(x+8). They are -2.582-8, or -10.582; 0-8, or -8; and 2.582-8, or -5.418.

### **Exercise Set 2.6**

1. y = kx  $54 = k \cdot 12$  $\frac{54}{2} = k$ , or  $k = \frac{9}{12}$ 

2

ation is 
$$y = 9 \frac{x}{x}$$
, or  $y = 4.5x$ .

**2.** y = kx

0.1 = k(0.2)  $\frac{1}{2} = k \text{ Variation constant}$ 

Equationofvariation: 
$$y = \frac{1}{x}$$
, or  $y = 0.5x$ .  
**3.**  $y = \frac{k}{3}$   
 $3 = \frac{k^2}{12}$ 

$$36 = k$$

The variation constant is 36. The equation of variation is 36  $y = \frac{1}{x}$ . 4.  $y = \frac{k}{k}$ 

12 = 5 60 = k Variation constantEquation of variation: y = 60

**5.** y = kx

 $1 = k \cdot \frac{1}{2}$ 

= k

The variation constantis4. The equation of variation is y = 4x.

**6.**  $y = {k \atop x} 0.1 = {k \atop 0.5}$ 

7. 
$$y = \frac{k}{x}$$
$$32 = \frac{k}{1}$$
$$\frac{1}{8} \cdot 32 = k$$
$$4 = k$$
The variation constant is 4. The equation of variation
$$y = \frac{4}{x}$$
$$y = kx$$
$$3 = k \cdot 33$$
$$+ \frac{1}{2} k \text{ Variation constant 11}$$
Equation of variation:  $y = \frac{1}{11}x$   
9. 
$$y = kx$$
$$\frac{3}{2} = k$$
$$\frac{3}{2$$

ŀ

The variation constant is 0.54. The equation of variation is  $y = \frac{x}{2}$ 

**12.** 
$$y = kx$$
  
 $0.9 = k(0.4)$ 

 $\frac{9}{4} = k \text{ Variation constant 4}$ Equation of variation:  $y = \frac{9}{4}x$ , or y = 2.25x0.05 = k Variation constant

Equation of variation:  $y = \frac{0.05}{1000}$ 

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0.54

is

**13.** Let *S* = the sales tax and *p* = the purchase price. S = kp *S* varies directly as *p*.  $17.50 = k \cdot 260$  Substituting  $0.067 \approx k$  Variation constant 138

$$4.50 = k \cdot 6$$
$$0.75 = k$$

$$W = 0.75a$$
  
 $W = 0.75(11)$   
 $W = $8.25$ 

<u>k</u>

$$W = W \text{ varies inversely as } L.L$$

$$1200 = \frac{k}{8} \text{ Substituting}$$

$$9600 = k \text{ Variation constant}$$

$$W = \frac{9600}{L} \text{ Equation of variation}$$

$$W = \frac{9600}{8} \text{ Substituting } 14$$

$$W \approx 686$$

A14-mbeamcansupportabout686kg.

16. 
$$t = \frac{k}{r}$$

$$5 = \frac{k}{80}$$

$$400 = r$$

$$t = \frac{400}{70}$$

$$t = \frac{40}{7}, \text{ or } 5\frac{5}{7} \text{ hr}$$

**17.** Let *F* = thenumber of grams of fat and *w* = the weight.

F = kw F varies directly asw. $60 = k \cdot 120 \text{ Substituting}$ 

$$\frac{60}{120} = k, \text{ or } Solvingfork}$$

$$\frac{1}{20} = k \quad \text{Variation constant 2}$$

$$F = \frac{1}{2^{w}}$$
 Equation of variation  

$$F = \frac{1}{2^{*}} 180$$
 Substituting  

$$F = 90$$

The maximum daily fatintake for a person weighing 180 lb is 90 g.

**18.** 
$$N = kP$$
  
 $29 = k \cdot 19,011,000$  Substituting  
 $\frac{29}{19,011,000} = k$  Variation constant 29  
 $N = \frac{29}{19,011,000}P$   
 $29$   
 $N = \frac{29}{19,011,000} \cdot 4,418,000$  Substituting  
 $N \approx 7$   
Colorado has 7 representatives.  
**19.**  $T = \frac{k}{P}$  T varies inversely as P.  
 $5 = \frac{k}{7}$  Substituting  
 $35 = k$  Variation constant  
 $T = \frac{35}{P}$  Equation of variation  
 $T = \frac{35}{10}$  Substituting  
 $T = 3.5$ 

It will take 10 bricklayers 3.5 hr to complete the job.

20. 
$$t = {k \atop r} \\ 45 = {k \atop 600} \\ 27,000 = k \\ t = {27,000 \atop 1000} \\ t = {27,000 \atop 1000} \\ t = 27 \text{ min}$$

**21.**  $d = km \ d$  varies directly as  $m. 40 = k \cdot 3$  Substituting

$$\frac{40}{k} = k$$
 Variation constant 3

$$d = \frac{40}{3^{-m}}$$
 Equation of variation  
$$d = \frac{40}{3} \cdot 5 = \frac{200}{3}$$
 Substituting  
$$d = 66\frac{2}{3^{-}}$$

A 5-kg mass will stretch the spring 66 cm.  $\frac{3}{3}$ 

**22.** 
$$f = kF$$
  
 $6.3 = k \cdot 150$   
 $0.042 = k$   
 $f = 0.042F$   
 $f = 0.042(80)$   
 $f = 3.36$ 

Exercise Set 2.6	
<b>23.</b> $P = \frac{k}{W}$ <i>P</i> varies inversely as <i>W</i> .	<b>28.</b> $y = kx^2$ 6 = k · 3 <sup>2</sup>
$330 = \frac{\kappa}{3.2}$ Substituting	$\begin{array}{c} 6 = k \cdot 3^2 \\ \frac{2}{3} = k \end{array}$
1056 = k Variation constant	$y = \frac{2}{x^2} 3$
$P = \frac{1056}{2}$ Equation of variation	$y = -x^2 3$
W	<b>29.</b> $y = kxz$
$550 = \frac{1056}{W}$ Substituting	$56=k \cdot 7 \cdot 8$ Substituting $56=56k$
550W = 1056 Multiplying by W	1 = k
$W = \frac{1056}{550}$ Dividing by 550	The equation of variation is $y = xz$ . <b>30.</b> $y = \frac{k\underline{x}}{2}$
W = 1.92 Simplifying	
Atone with a pitch of 550 vibrations persecond has a wavelength of 1.92 ft.	$4 = \frac{k \cdot 12}{15}$ 5 = k
<b>24.</b> $M = kE$ <i>M</i> varies directlyas <i>E</i> . 38	$y = \frac{5x}{z}$
$= k \cdot 95$ Substituting	$\begin{array}{ll}z\\ 31. & y = kxz^2\end{array}$
$\frac{2}{2} = k$ Variation constant 5	$105=k \cdot 14 \cdot 5^2$ Substituting $105 =$
$M = 5 \frac{E}{2}$ Equation of variation	350k
$M = \frac{2}{5} \cdot 100$ Substituting	$\frac{105}{350} = k$
M = 40	$\frac{3}{10} = k$
A 100-lb person would weigh 40 lb on Mars.	10 The equation of variation is $y = \frac{3}{xz_{\perp}^2}$
<b>25.</b> $y = k^{k}$	xz 10
$\overline{X^2}$	$y = k \cdot$
$0.15 = \frac{k}{2}$	<b>32.</b> <u>w</u>
Substituting	$\frac{3}{2} = k \cdot \frac{2 \cdot 3}{4}$
$0.15 = \frac{k \frac{(0.1)^2}{0.01}}{0.01}$	$\begin{array}{ccc} 2 & 4 \\ 1 = k \end{array}$
0.01	xz
0.15(0.01) = k	y = -w
0.0015 = k The equation of variation is $y = \frac{0.0015}{k}$ .	33. $y = k \frac{3}{wp}$ $\frac{3}{28} = k \frac{3 \cdot 10}{7 \cdot 8}$ Substituting
$\chi^2$	$\frac{3}{28} = k_{7} \frac{3 \cdot 10}{8}$ Substituting
<b>26.</b> $y = k^{-1}$	$3_{k}$
<b>26.</b> $y = \frac{k^{-1}}{k^{2}}$	28 56
32	<u>3</u> <u>56</u>
54 = k	$\frac{3}{28} \cdot \frac{56}{30} = k$
$^{54}y \equiv$	$\frac{1}{5} = k$
$y \equiv x^2$	
<b>27.</b> $y = kx^2$	The equation of variation is $y = \frac{1}{5} \frac{xz}{wp}$ , or $\frac{xz}{.5} wp$
$0.15 = k(0.1)^2$ Substituting $0.15 =$	$34. \qquad y = k \cdot \frac{1}{w^2}$
0.01k	$\frac{12}{5} = k \frac{16 \cdot 3}{5^2}$
0.15	
$\underline{\qquad} = k$ Copyright © 2013 Pearson Education, Inc.	

0.01 15 = k	$\frac{5}{4} = k$
The equation of variation is $y = 15x^2$ .	$y = \frac{5 xz}{0}$ or $\frac{5xz}{0}$
	$4 w^2 \qquad 4 w^2$

**35.** 
$$I = \frac{k}{d^2}$$
  

$$90 = \frac{k}{25}$$
Substituting  

$$90 = \frac{k^{52}}{25}$$

$$2250 = k$$

Theequationofvariationis I =

Substitute40for*I* and find*d*.

$$40 = \frac{d^2}{d^2}$$
$$40d^2 = 2250$$
$$d^2 = 56.25$$

*d* = 7.5

Thedistancefrom5mto7.5mis7.5-5,or2.5m,soitis 2.5mfurthertoapointwheretheintensityis40W/m<sup>2</sup>.

2250

 $d^2$ .

18

36. D = kAv $222 = k \cdot 37.8 \cdot 40$  $\frac{37}{252} = k$  $D = \frac{37}{25\underline{37}}Av$  $430 = 252 \cdot 51v$  $v \approx 57.4 \text{ mph}$ **3**7.  $d = kr^2$  $200 = k \cdot 60^2$  Substituting 200 = 3600k200  $\frac{1}{3600} = k$ 1  $\overline{18} = k$ The equation of variation is  $d = \frac{1}{r^2}$ . Substitute 72 for *d* and find *r*.  $72 = \frac{2}{r}$ 18  $1296 = r^2$ 

> 36 = rAcarcantravel 36 mphandstillstopin72 ft.

> > $W = \frac{k}{2}$

38.

$$\frac{d^{2}_{k}}{220 = \frac{}{(3978)^{2}}}$$
3, 481, 386, 480 = k  

$$W = \frac{3, 481, 386, 480}{\frac{d^{2}_{3}}{3, 481_{386}}}$$
, 480

**39.** 
$$E = \frac{kR_{-}}{I}$$
  
We first find k.  
 $3.89 = \frac{k \cdot 93}{215.2}$  Substituting  
 $215.2$   $215.2$   
 $389_{-} \Sigma = Multiplying by$   
 $93_{-} 9 \approx k^{k}$   $9R$   
The equation of variation is  $E =$   
Substitute 3.89 for  $F_{R}$  and 238 for  $I_{and}^{I}$  solve for  $R$ .  
 $3.89 = \frac{218}{238}$   
 $\frac{3.89(238)}{9} = R$  Multiplying by  $\frac{238}{9}$   
 $103 \approx R$ 

Bronson Arroyo would have given up about 103 earned runs if he had pitched 238 innings.

40. 
$$V = \frac{kT}{P}$$
  

$$231 = \frac{k \cdot 42}{20}$$
  

$$110 = k$$
  

$$V = \frac{110T}{P}$$
  

$$V = \frac{110 \cdot 30}{15}$$
  

$$V = 220 \text{ cm}^{3}$$
  
41. parallel  
42. zero  
43. relative minimum  
44. odd function  
45. inverse variation  
46. a)  $7xy = 14$   

$$2$$
  

$$y = x$$
  
Inversely  
b)  $x - 2y = 12$   

$$y = \frac{x}{2} - 6$$
  

$$W = (3978 + 200)^{2}$$
  

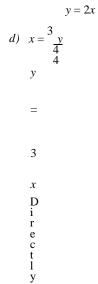
$$W \approx 199 \text{ lb}$$

N e i t h e r c )

 $\frac{-}{2}$ 

- x  $^+$
- y
- =
- 0

y = 2x Directly



\_

$$\frac{x}{y} = 2$$

$$\frac{y}{2x} = 1$$

$$\frac{1}{2x}$$
Directly

**47.** Let *V* represent the volume and *p* represent the price of a jar of peanut butter.

V = kp V varies directly as p.

Substituting

$$-\underline{3}_{\pi 2}^{\Sigma}$$
<sup>2</sup>(5)=(289) Substituting

$3.89\pi = k \; .$	Variation constant
$V = 3.89\pi p$	Equationofvariation

 $\pi(1.625)^2(5.5)=3.89\pi p$ 

If cost is directly proportional to volume, the larger jar should cost \$3.73.

Now let *W* represent the weight and *p* represent the price of a jar of peanut butter.

W = kp		
18 = k(2.89) Substituting		
$6.23 \approx k$	Variation constant $W =$	
6.23 <i>p</i>	Equationofvariation 28=	
$6.23p$ $4.49 \approx p$	Substituting	

If cost is directly proportional to weight, the larger jar should cost \$4.49. (Answers may vary slightly due to rounding differences.)

**48.**  $Q = \frac{kp^2}{q^3}$ 

Q varies directly as the square of p and inversely as the cube of q.

**49.** Weare told  $A = kd^2$ , and we know  $A = \pi r^2$  so we have:

 $kd^2 = \pi r^2$ 

$$d^{2}\Sigma^{2} = r = \frac{d}{2}$$

$$kd^{2} = \frac{\pi d^{2}}{4}$$

$$k = \frac{\pi}{4}$$
Variation constant

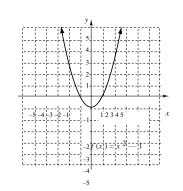
## **Chapter 2 Review Exercises**

- 1. This statement is true by the definition of the greatest integer function.
- **2.** Thes statement is false. See Example 2(b) in Section 2.3 in the text.
- **3.** The graph of  $y = f(x \ d)$  is the graph of y = f(x) shifted right d units, so the statement is true.
- **4.** The graph of y = -f(x) is the reflection of the graph of y = f(x) across the *x*-axis, so the statement is true.

- **5.** a) For x-values from -4 to -2, the y-values increase from 1 to 4. Thus the function is increasing on the interval (-4, -2).
  - b) Forx-values from 2 to 5, the y-values decrease from 4 to 3. Thus the function is decreasing on the inter-val (2, 5).
  - c) Forx-values from -2 to 2, y is 4. Thus the function is constant on the interval (-2, 2).
- 6. a)Forx-values from −1 to 0, the y-values increase from 3 to 4. Also, for x-values from 2 to ∞, the y-values increase from 0 to ∞.

Thus the function is increas- ing on the intervals (-1, 0), and  $(2, \infty)$ .

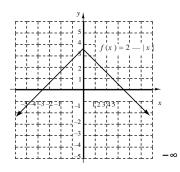
- b) Forx-values from 0 to 2, the y-values decrease from 4 to 0. Thus, the function is decreasing on the in- terval (0, 2).
- c) For x-values from  $-\infty$  to -1, y is 3. Thus the func- tion is constant on the interval  $(-\infty, -1)$ .



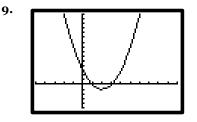
The function is increasing on (0, ) and decreasing on ( , 0 ). We estimate that the minimum value is 1 at x = 0. There are no maxima.



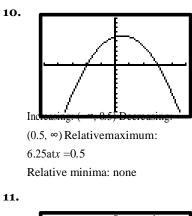
7.

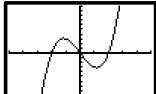


The  $\infty$  function is increasing on (, 0) and decreasing on (0, ). We estimate that the maximum value is 2 at x = 0. There are no minima.

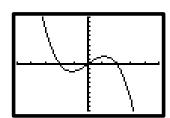


We find that the function is increasing on (2, ) and de- energy on ( , 2). The relative main immum is 1 at x = 2. There are no maxima.





We find that the function is increasing on  $(-\infty, -1.155)$  and on  $(1.155, \infty)$  and decreasing on (-1.155, 1.155). The relative maximum is 3.079 at x = -1.155 and the relative minimum is -3.079 at x = 1.155.



We find that the function is increasing on (1.1-55, 1.155) and decreasing on (, 1.155) and on (1.155). The relative maximum

is 1.540 at x = 1.155 and the relative minimum is -1.540 at x =

-1.155.

12.

**13.** If d = 2l he length of the tablecloth, then the width is , or 10-l. We use the formula Area = length × 2

width.

A(l) = l(10 - l), or  $A(l) = 10l - l^2$ 

**14.** Thelengthoftherectangleis2

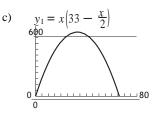
*x* coordinateofthepoint(*x*, *y*) onthe circle. The circle has center  $(0\sqrt{0})$  and radius 2, so its equation is  $x^2 + y^2 = 4$ and  $y = 4\pi x^2$ . Thus the area of the rectangle is given

. The width is the second

by A(x)= 2x 4 - x<sup>2</sup>.
15. a) If the length of the side parallel to the garage is x feet long, 6th6e\_nxthe lengt h of each of the other

twosidesis \_\_\_\_\_, or 33- . We use the formula  
Area = length 
$${}^{2}w_{x}$$
 idth. 2  
 $A(x) = x 33 - \frac{x}{33 - x}$ , or  
2  
Conv

b) The length of the side parallel to the garage must be positive and less than 66 ft, so the domain of the function is  $\{x|0 < x < 66\}$ , or (0, 66).



d) By observing the graph or using the MAXIMUM feature, we see that the maximum value of the function occurs when x = 33. When x = 33, then  $33 - \frac{x}{2} = 33 - \frac{33}{2} = 33 - 16.5 = 16.5$ . Thus the di-

mensions that yield the maximum area are 33 ft by 16.5 ft.

**16.** a) Let h = the height of the box. Since the volume is 108 in<sup>3</sup>, we have:

$$108 = x \cdot x \cdot h$$

$$108 = x^{2}h$$

$$\frac{108}{x^{2}} = h$$
Now find the surface area.
$$S = x^{2} + 4 \cdot x \cdot h$$

$$S(x) = x^{2} + 4x \frac{108}{2}$$

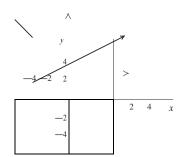
$$S(x) = x^{2} + \frac{432}{2}$$

$$x^{2}$$

- b) x must be positive, so the domain is  $(0, \infty)$ .
- c) From the graph, we see that the minimum value of the function occurs when x = 6 in. For this value of x, 108

$$h = \frac{108}{x^2} = \frac{108}{6^2} = \frac{-3 \text{ in.}}{36}$$
  
for  $x \le -4$ ,  
$$\Box_{-x},$$
  
**17.**  $f(x) = \frac{-12}{-x+1}$ , for  $x > -4$ 

We create the graph in two parts. Graph f(x) = -x for inputsless than or equal to -4. Then graph f(x) = x+1for inputs greater than -4.



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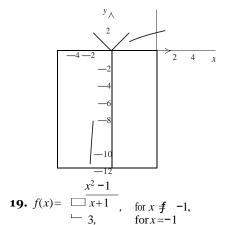
 $x^2$ 

A(x) = 33x - 2 —

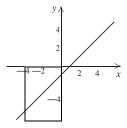
#### **Chapter 2 Review Exercises**

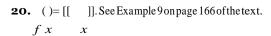
**18.** 
$$f(x) = |x|$$
, for  $x < -2$ ,  
 $x - 1$ , for  $x > 2$ 

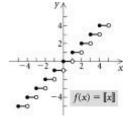
We create the graph in three parts. Graph  $f(x) = x^3$  for inputs less than -2. Then graph f(x) = |x| for inputs greater than or equal to  $\frac{b-2}{x-1}$  and less than or equal to 2. Finally graph f(x) = x-1 for inputs greater than 2.



We create the graph in two parts. Graph  $f(x) = x^2 - 1$ for all inputs except -1. Then graph f(x) = 3 for x = -1.







## **21.** f(x) = [[x - 3]]

This function could be defined by a piecewise function with an infinite number of statements.

 $f(x) = \frac{4}{-2}, \text{ for } 1 = 0,$   $f(x) = \frac{-2}{-2}, \text{ for } 1 \le x < 2,$   $f(x) = -1, \text{ for } 2 \le x < 3,$   $\frac{1}{-1}, \text{ for } 2 \le x < 3,$   $\frac{1}{-1}, \text{ for } 2 \le x < 3,$   $\frac{1}{-1}, \text{ for } 3 = \frac{1}{-2},$   $\frac{1}{-2}, \text{ for } x < -2,$   $22. \quad f(x) = \sqrt{x}, \text{ for } x < 2,$  x = 1, for x > 2, x = 1, for x > 2

Since -1 is in the interval [-2,2], f(-1)=|-1|=1. Since 5 > 2, f(5) = 5 - 1 = 4 = 2. Since -2 is in the interval [-2,2], f(-2)=|-2|=2. Since -3 < -2,  $f(-3) = (-3)^3 = -27$ .

**23.** 
$$f(x) = \frac{x^2 - 1}{x + 1}$$
 for  $x f = -1$ ,

$$\Box_{3, for x = -1}$$
Since  $2 = 1, -f(2) = (-2)^2 - 1 = 4 - 1 = 3$   

$$= -2 + 1 - 1 - 1 - 1$$
Since  $x = -1$ , we have  $f(-1) = 3$ .  
Since  $0 = 1, (0) = 0 - 1 = -1 = 1$ .  
Since  $4 = 1, (4) = 4^{2} - 1 = 16 - 1 = 15 = 3$ .  

$$- f = 4 - 16 - 1 = 15 = 3$$
.  

$$- f = 4 - 16 - 1 = 15 = 3$$
.  

$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
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$$- f = 4 - 16 - 1 = 15 = 3$$
.  

$$- f = 4 - 16 - 1 = 15 = 3$$
.  

$$- f = 4 - 16 - 1 = 10$$
.  

$$= 2 - 35 = -33$$
.  

$$25. (fg)(2) = f(2) \cdot g(2) = -35 = -33$$
.  

$$= 2 - 2 \cdot (2^{-2} - 1) = 0 \cdot (4 - 1)$$
.

**26.** (f+g)(-1) = f(-1) + g(-1)=  $\frac{-1}{\sqrt{-1} - 2 + ((-1) - 1)}^2$  $\sqrt{-1} = -3 + (1 - 1)$ 

Since -3 is not a real number, (f+g)(-1) does not exist.

**27.**  $f(x) = \frac{4}{3}, g(x) = 3 - 2x$ a) Divisionby zeroisundefined, so the domain of f is  $\{x|x f=0\}, or(-\infty,0) \cup (0,\infty)$ . The domain of g sitheset of all real numbers, or  $(-\infty, \infty)$ . The domain of f+g, f-g and fg is  $\{x|x f=0\}$ , or (-20),  $(0, \infty)$ . Since  $\frac{3}{2} = 0$ , the domain of f/g is  $x \cdot x = 0$  and  $x = f = \frac{1}{2}$ , or  $(-\infty,0) \cup \begin{array}{c} \mathbf{0}, \underline{3} \\ \mathbf{2} \\ \underline{4} \\ \underline{4} \\ \mathbf{0}, \infty \end{array}, \underline{2} \\ \mathbf{\Sigma} \\ \underline{5} \\ \underline{5}$ b)  $(f+g)(x) = \frac{1}{x^2} + (3-2x) = \frac{1}{x^2} + 3 - \frac{2x}{4}$  $(f - g)(x) = \frac{\mathbf{A}}{x^2} \sum_{-(3 - 2x)=x^2}^{-(3 - 2x)=x^2} \frac{4}{x^2 - 3 + 2x}$  $\overline{12}$   $\overline{8}$ 4 . <del>Σ</del>  $(fg)(x) = x^2 (3-2x) = x^2 - x$ ()() =  $\frac{-x^2}{4} = \frac{2}{f/g} = \frac{4}{x^2(3-2x)}$ **28.** a) The domain of f, g, f + g, f - g, and fg is all real numbers, or  $(-\infty, \infty)$ . Since  $g = \frac{1}{1} = 0$ , the domain  $2_1$ 1 Σ\_ >\_ Σ

of 
$$f/g$$
 is  $x x = 2$ , or  $-\infty, 2 \cup 2, \infty$ 

b) 
$$(f + g)(x) = (3x^2 + 4x) + (2x - 1) = 3x^2 + 6x - 1$$

 $(f - g)(x) = (3x^{2} + 4x) - (2x - 1) = 3x^{2} + 2x + 1 \quad (fg)(x) =$  $(3x^{2} + 4x)(2x - 1) = 6x^{3} + 5x^{2} - 4x$  $(f/g)(x) = \frac{3x^{2} + 4x}{2x - 1}$ **29.**  $P(x) = R(x) - C(x) = (120x - 0.5x^{2}) - (15x + 6) = 120x - 0.5x^{2} - 15x - 6$ 

$$= -0.5x^2 + 105x - 6$$

**30.** 
$$f(x) = 2x + 7$$
  
$$\frac{f(x+h) - f(x)}{h} = \frac{2(x+h) + 7 - (2x+7)}{h} =$$

$$\frac{f(x+h) - f(x)}{h} = \frac{3 - \frac{x^2 - 2xh - h^2 - (3 - x^2)}{h}}{h}$$

$$= \frac{3 - \frac{x^2 - 2xh - h^2 - 3 + x^2}{h}}{h}$$

$$= \frac{-2xh - h^2 \frac{h(-2x - h)}{h}}{h}$$

$$= \frac{h - 2x - h}{h} = -2x - h$$
**32.**  $f(x) = \frac{4}{x}$ 

$$\frac{4 - 4 - 4 - x - 4h}{h} = -2x - h$$

$$\frac{4 - 4 - 4 - x - 4h}{h} = -2x - h$$

$$= \frac{4x - 4(x+h)}{h} = \frac{x(x+h)}{h} = \frac{x(x+h)}{h} = \frac{-4h}{h}$$

$$= \frac{4x - 4(x+h)}{h} = \frac{x(x+h)}{h} = \frac{x(x+h)}{h} = \frac{-4}{h}$$
**33.**  $(f \circ g)(1) = f(g(1)) = f(1^2 + 4) = f(1 + 4) = f(5) = 2 \cdot 5 - 1 = 10 - 1 = 9$ 

**34.** 
$$(g \circ f)(1) = g(f(1)) = g(2 \cdot 1 - 1) = g(2 - 1) = g(1) =$$

$$1^2 + 4 = 1 + 4 = 5$$
  
**35.**  $(h \circ f)(-2) = h(f(-2)) = h(2(-2) - 1) =$ 

$$h(-4 - 1) = h(-5) = 3 - (-5)^3 = 3 - (-125) =$$

3 + 125 = 128

**36.**  $(g \circ h)(3) = g(h(3)) = g(3 - 3^3) = g(3 - 27) =$  $g(-24) = (-24)^2 + 4 = 576 + 4 = 580$ 

**37.** 
$$(f \circ h)(-1) = f(h(-1)) = f(3 - (-1)^3) =$$

$$f(3-(-1)) = f(3+1) = f(4) = 2 \cdot 4 - 1 = 8 - 1 = 7$$
2
38. (h \circ g)(2) = h(g(2)) = h(2 + 4) = h(4+4)

$$h(8) = 3 - 8^3 = 3 - 512 = -509$$

**39.** 
$$(f \circ f)(x) = f(f(x)) = f(2x - 1) = 2(2x - 1) - 1 = 4x - 2 - 1 = 4x - 3$$
  
**40.**  $(h \circ h)(x) = h(h(x)) = h(3 - x^3) = 3 - (3 - x^3)^3 = 3 - (27 - 27x^3 + 9x^6 - x^9) = 3 - 27 + 27x^3 - 9x^6 + x^9 = -24 + 27x^3 - 9x^6 + x^9$ 

**41.** a) 
$$f \circ g(x) = G - 2x = \frac{4}{(3 - 2x)^2}$$
  
 $g \circ f(x) = g - \frac{4}{x^2} = 3 - 2 - \frac{4}{x^2} = 3 - \frac{8}{x^2}$ 

$$\frac{2x+2h+7-2x-7}{h} = {}^{2h} = 2\frac{}{h}$$
**31.**  $f(x)=3-x^2$ 
 $f(x+h)=3-(x+h)^2=3-(x^2+2xh+h^2)=$ 

 $3 - x^2 - 2xh - h^2$ 

b) The domain of f is  $\{x | x f = 0\}$  and the domain of gis the set of all real numbers. To find the domain of  $f \circ g$ , we find the values of x fogwhich g(x)=0. Since 3-2x=0 when x3= the domain of  $f \circ g$ 



is x x, or  $-\infty$ ,  $2 \cup 2, \infty$ . Since any real number can be an input for g, the domain of  $g \circ f$  is the same as the domain of f,  $\{x | x f=0\}$ , or  $(-\infty, 0) \cup$ 

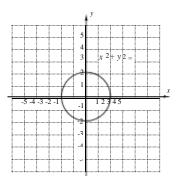
(0, ∞).

42. a) 
$$f \circ g(x) = f(2x - 1)$$
  
 $= 3(2x - 1)^{2} + 4(2x - 1)$   
 $= 3(4x^{2} - 4x + 1) + 4(2x - 1)$   
 $= 12x^{2} - 12x + 3 + 8x - 4$   
 $= 12x^{2} - 4x - 1$   
 $(g \circ f)(x) = g(3x^{2} + 4x)$   
 $= 2(3x^{2} + 4x) - 1$   
 $= 6x^{2} + 8x - 1$   
b) Domain of f=domain of g = all real numbers, so domain of f  
 $\circ g = \text{domain of } g \circ f = \text{all real numbers}, \text{ or } (-\infty, \infty).$ 

**43.** f(x) = x, g(x) = 5x + 2. Answers may vary.

**44.** 
$$f(x) = 4x^2 + 9$$
,  $g(x) = 5x - 1$ . Answers may vary.

**45.**  $x^2 + y^2 = 4$ 



The graph is symmetric with respect to the *x*-axis, the *y*-axis, and the origin.

Replace *y* with *y* to-testalgebraically for symmetry with respect to the *x*-axis.

$$x^{2} + (-y)^{2} = 4$$
$$x^{2} + y^{2} = 4$$

The resulting equation is equivalent to the original equa-tion, so the

Replace x with -x to test algebraically for symmetry with respect to the y-axis.

$$+y^2 = 4$$

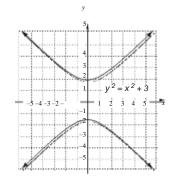
The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the *y*-axis.

Replace x and -x and y with -y to test forsymmetry with respect to theorigin.

$$(-x)^2 + (-y)^2 = 4$$
  
 $x^2 + y^2 = 4$ 

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the origin.

**46.**  $y^2 = x^2 + 3$ 



The graph is symmetric with respect to the x-axis, the

y-axis, and the origin.

(

Replace y with y to-testal gebraically for symmetry with respect to the x-axis.

$$-y)^2 = x^2 + 3$$
$$y^2 = x^2 + 3$$

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the *x*-axis.

Replace x with x to testalgebraically for symmetry with respect to the y-axis.

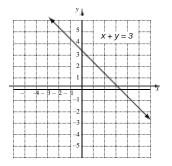
$$y^2 = (-x)^2 + 3$$
  
 $y^2 = x^2 + 3$ 

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the *y*-axis.

Replace x and -x and y with -y to test forsymmetry with respect to theorigin.

$$(-y)^2 = (-x)^2 + 3$$
  
 $y^2 = x^2 + 3$ 

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the origin.



Thegraphisnotsymmetric with respect to the *x*-axis, the *y*-axis, or the origin.

Replace y with y totest algebraically for symmetry with respect to the x-axis.

x - y = 3

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Replace x with x to test algebraically for symmetry with respect to the *y*-axis.

```
-x + y = 3
```

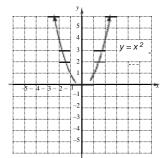
The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *y*-axis.

Replace x and x and y with y to test-for symmetry with respect

$$-x - y = 3$$
$$x + y = -3$$

The resulting equation is not equivalent to the original equation, so

**48.** 
$$y = x^2$$



The graph is symmetric with respect to the *y*-axis. It is not symmetric with respect to the *x*-axis or the origin.

Replace y with y totest algebraically for symmetry with respect to the x-axis.

 $-y = x^2$  $y = -x^2$ 

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Replace x with x to test algebraically for symmetry with respect to the *y*-axis.

$$y = (-x)^2$$
$$y = x^2$$

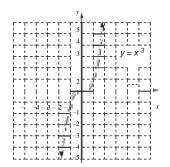
The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the *y*-axis.

Replace x and x and y with y to test-for symmetry with respect to the origin.

$$-y = (-x)^2$$
$$-y = x^2$$
$$y = -x^2$$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.





The graph is symmetric with respect to the origin. It is not symmetric with respect to the *x*-axis or the *y*-axis.

Replace *y* with *y* t-otest algebraically for symmetry with respect to the *x*-axis.

$$-y = x$$
$$y = -x^3$$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Replace x with x to test algebraically for symmetry with respect to the *y*-axis.

$$y = (-x)^3$$
$$y = -x^3$$

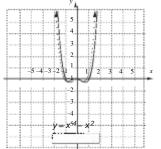
The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the y-axis.

Replace x and x and y with y to test-for symmetry with respect to the origin.

$$-y = (-x)^3$$
$$-y = -x^3$$
$$y = x^3$$

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the origin.

**50.** 
$$y = x^4 - x^2$$



The graph is symmetric with respect to the *y*-axis. It is not symmetric with respect to the *x*-axis or the origin.

Replace y with y to-testal gebraically for symmetry with respect to the x-axis.

$$-y = x^4 - x^2$$
$$y = -x^4 + x^2$$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis. Replace x with – to test algebraically for symmetry with

respect to the y-axis.  $y = (-x)^4 - (-x)^2$ 

 $y = x^4 - x^2$ 

The resulting equation is equivalent to the original equa- tion, so the graph is symmetric with respect to the *y*-axis.

Replace x and -x and y with -y to test for symmetry with respect to the origin.

 $-y = (-x)^4 - (-x)^2$  $-y = x^4 - x^2$ 

$$y = -x^4 + x^2$$

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the origin.

- **51.** The graph is symmetric with respect to the *y*-axis, so the function is even.
- **52.** The graph issymmetric with respect to the *y*-axis, so the function is even.
- **53.** The graph is symmetric with respect to the origin, so the function is odd.
- **54.** The graph issymmetric with respect to the *y*-axis, so the function is even.
- **55.**  $f(x)=9 x^2$

$$f(-x) = 9 - (-x^2) = 9 - x^2$$
  
 $f(x) = f(-x)$ , so f is even.

- **56.**  $f(x) = x^3 2x + 4$  $f(-x) = (-x)^3 - 2(-x) + 4 = -x^3 + 2x + 4$ 
  - f(x) = f(-x), so f is not even.

$$-f(x) = -(x^3 - 2x + 4) = -x^3 + 2x - 4$$
  
f(-x) f = -f(x), so f is not odd.

Thus,  $f(x) = x^3 - 2x + 4$  is neither even or odd.

**57.** 
$$f(x) = x^7 - x^5$$
  
 $f(-x) = (-x)^7 - (-x)^5 = -x^7 + x^5$   
 $f(x) \quad f(-x)$ , so  $f$  is noteven.  
 $-f(x) = -(x^7 - x^5) = -x^7 + x^5$   
 $f(-x) = -f(x)$ , so  $f$  is odd.  
**58.**  $f(x) = |x|$   
 $f(-x) = |-x| - |x|$ 

f(-x) = |-x| = |x|  $f(x) = \sqrt{(-x)}, \text{ so } f \text{ is even.}$   $59 \cdot f(x) = 16 - x^{2} - \sqrt{16 - (-x^{2})} = 16 - x^{2}$ f(-x) = f(-x), so f is even.

**60.** 
$$f(x) = \frac{10x}{x^2 + 1}$$
$$f(-x) = \frac{10(-x)}{10(-x)} = -\frac{10x}{x^2 + 1}$$
$$f(x) \qquad f(-x), \text{ so } f(x) \text{ is not even}$$
$$10x$$
$$-f(x) = -\frac{10x}{x^2 + 1}$$
$$f(-x) = -f(x), \text{ so } f \text{ is odd.}$$

10

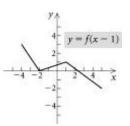
- **61.** Shape:  $g(x) = x^2$ Shift g(x) left 3 units:  $f(x) = g(x + 3) = (x + 3)^2$
- **62.** Shape: t(x) = xTurnt(x)upsidedown(thatis,reflectitacrossthex-axis):  $\sqrt{-}$  h(x) = -t(x) = -x. Shift h(x) right 3 units: g(x) = h(x-3) = -x-3.

Shift g(x) up 4 units: f(x) = g(x) + 4 = -x - 3 + 4.

**63.** Shape: h(x) = |x|

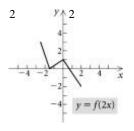
Stretch h(x) vertically by a factor of 2 (that is, multiply each function value by 2): g(x)=2h(x)=2|x|. Shift g(x) right 3 units: f(x)=g(x-3)=2|x-3|.

**64.** The graph is shifted right 1 unit so each *x*-coordinate is increased by 1. We plot and connect (-4, 3), (-2, 0), (1, 1) and (5, -2).



**65.** The graph is shrunk horizontally by a factor of 2. That is, each *x*-coordinates ivided by 2. We plot and connect

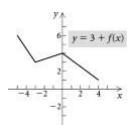
$$-\frac{5}{2}$$
, 3,  $-\frac{3}{2}$ , 0, (0, 1) and (2, -2).



**66.** Each y-coordinate is multiplied by -2. We plot and con-nect ( $\neg 5$ , -6), (-3, 0), (0, -2) and (4, 4).



**67.** Each *y*-coordinate is increased by 3. We plot and connect (-5, 6), (-3, 3), (0, 4) and (4, 1).



**68.** y = kx100 = 25x

4 = x

Equationofvariation: y = 4x

**69.** *y* =*kx* 

$$6 = 9x$$
  

$$\frac{2}{3} = x$$
 Variation constant

Equation of variation:  $y = \frac{2}{x}$ 

$$y = \frac{k}{x_k}$$

$$100 = \frac{k}{25}$$

$$2500 = k$$
  
Equation of variation:  $y = \frac{2500}{x}$ 

71.  $y = \frac{k}{6}$   $6 = \frac{k^{2}}{9}$ 54 = k Variation constant

Equationof variation: y = 54

х

72. 
$$y = \frac{k}{x^2}$$
$$12 = \frac{k}{48}$$
$$48 = k^{22}$$
$$\frac{48}{y} = \frac{48}{x}$$

*x*<sup>2</sup>

73. 
$$y = \frac{kxz^{2}}{w}$$

$$z = \frac{k(16)^{\frac{1}{2}}}{0.2}$$

$$2 = \frac{4k}{0.2}$$

$$2 = \frac{4k}{0.2}$$

$$2 = \frac{4k}{0.2}$$

$$\frac{4}{0.2}$$

$$\frac{2 = 20k}{1-w}$$

$$\frac{1}{w}$$

**78.** For b > 0, the graph of y = f(x) + b is the graph of y = f(x) shifted up b

units. Answer C is correct.

#### Chapter 2 Test

79. The graph of  $g(x) = -\frac{1}{f(x)} + 1$  is the graph of y = f(x)

shrunkverticallybyafactor of  $\frac{1}{x}$ , then reflected across the 2 *x*-axis, and shifted up 1 unit. The correct graph is B.

- **80.** Let f(x) and g(x) be odd functions. Then by definition,  $f(-x) = f^{-}(x)$ , or f(x) = f(-x), and g(x) = -g(x), or g(x) = -g(x). Thus (f + g)(x) = f(x) + g(x) = -f(x) + [g(x)] = [f(-x) + g(x)] = (f + g)(-x) and f + g is odd.
- **81.** Reflect the graph of y = f(x) across the *x*-axis and then

across the y-axis.

**82.** 
$$f(x) = 4x^3 - 2x + 7$$
  
a)  $f(x) + 2 = 4x^3 - 2x + 7 + 2 = 4x^3 - 2x + 9$  b)  $f(x + 2) = 4(x + 2)^3 - 2(x + 2) + 7$   
 $= 4(x^3 + 6x^2 + 12x + 8) - 2(x + 2) + 7$   
 $= 4x^3 + 24x^2 + 48x + 32 - 2x - 4 + 7$   
 $= 4x^3 + 24x^2 + 46x + 35$   
c)  $f(x) + f(2) = 4x^3 - 2x + 7 + 4 \cdot 2^3 - 2 \cdot 2 + 7$   
 $= 4x^3 - 2x + 7 + 32 - 4 + 7$   
 $= 4x^3 - 2x + 42$ 

f(x)+2 adds 2 to each function value; f(x+2) adds 2 to each input before the function value is found; f(x)+f(2) adds the output for 2 to the output for *x*.

- **83.** In the graph of y = f(cx), the constant *c* stretches or shrinks the graphof y=f(x) horizontally. The constant *c* in y=cf(x) stretchesor shrinks the graph of y = f(x) vertically. For y = f(cx), the *x*-coordinates of y = f(x) are divided by *c*; for y = cf(x), the *y*-coordinates of y=f(x) are multiplied by *c*.
- **84.** The graph of f(x)=0 is symmetric with respect to the x-axis, the y- axis, and the origin. This function is both even and odd.
- **85.** If all of the exponents are even numbers, then f(x) is an even function. If  $a_0 = 0$  and all of the exponents are odd numbers, then f(x) is an

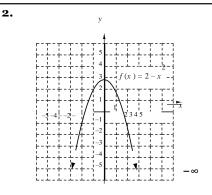




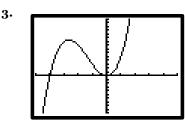
**1.** a) For *x*-values from -5 to -2, the *y*-values increase from-4to3. Thus the function is increasing on the interval

(-5, -2).

- b) Forx-values from 2 to 5, the y-values decrease from 2 to -1. Thus the function is decreasing on the interval (2, 5).
- c) Forx-valuesfrom-2to2, *y* is 2. Thus the function is constant on the interval (-2, 2).



The function is increasing on (, 0) and decreasing on (0, ). The relative maximum is 2 at x = 0. There are no minima.



- We find that the function is increasing on (, 2.667) and on (0, ) and decreasing on (2.667, 0). The relative maximum is 9.481 at 2.667 and the relative minimum is 0 at x = 0.
- **4.** If b = the length of the base, in inches, then the height = 4b 6. We use the formula for the area of a triangle,

$$= 2^{\frac{1}{bh}}.$$

$$A(b) = 2^{\frac{1}{b}}(4b - 6), \text{ or }$$

$$A(b) = 2b^{2} - 3b$$

$$\Box_{x^{2}}, \quad \text{ for } x < -1,$$

A

$$|x|_{,} = \lim_{x \to 1} f(x) = \frac{1}{x - 1} \le x \le 1, \mathbf{5} \cdot f(x) = \frac{1}{x - 1}$$

Since 
$$-4 < -1$$
,  $f(-4) = (-4)^2 = 16$ .  
7.  $(f + g)(-6) = f(-6) + g(-6) =$   
(6)  $4(-6) + 3 + \sqrt{3} \sqrt{(6)} =$   
 $3\overline{6} + 2\overline{4} + \overline{3} + \frac{\sqrt{3}}{3 + 6 - 63} + 9\overline{-63} + \overline{3} = 66$ 

8. 
$$(f - g)(-1) = f(-1) - g(-1) =$$
  
 $(\sqrt{y})^2 - 4(-1) + 3 \qquad 3 = (1) =$   
 $1 - + 4 + 3 - 3 + 1 = 8 - 4 = 82 = 6$   
 $1 - + 4 + 3 - - \sqrt{y}$   
9.  $(fg)(2) = f(2) \cdot g(2) = (2^2 - 4 \cdot 2 + 3)(3 - 2) =$   
 $(4 - 8 + 3)(1) = -1 \cdot 1 = -1$   
 $f(1) - \frac{2}{-4 \cdot 1 + 3} - \frac{4 + 3}{\sqrt{y}} = 0 = 0$   
10.  $(f/g)(1) = g(\overline{1}) - \frac{1}{\sqrt{y}} = \sqrt{y} = \sqrt{y}$   
 $-1 - 2 - 2$ 

- 11. Anyreal number can be an input for  $f(x) = x^2$ , so the domain is the set of real numbers, or  $(-\infty, \infty)$ .
- **12.** The domain of g(x) = x 3 is the set of real numbers for which  $x 3 \ge x 3$

0,or*x* ≥3. Thus the domain is{ $x | x \ge 3$ }, or [3, ∞).

- 13. The domain of f+g is the intersection of the domains of f and g. This is {x|x ≥ 3}, or [3, ∞).
- 14. The domain of f-g is the intersection of the domains of f and g. This is {x|x ≥ 3}, or [3, ∞).
- **15.** The domain of fg is the intersection of the domains of f and g. This is  $\{x|x \ge 3\}$ , or  $[3, \infty)$ .
- **16.** The domain of f/g is the intersection of the domains of f and g, excluding those x-values for which g(x)=0. Since x-3=0 when x=3, the domain is  $(3, \infty)$ .

3, the domain is (3,  $\infty$ ). **17.**  $(f + g)(x) = f(x) + g(x) = x^2 + \sqrt[7]{x - 3} = \sqrt[7]{x}$ 

**18.** 
$$(f - g)(x) = f(x) - g(x) = x^2 - \overline{x - 3}$$

**19.** 
$$(fg)(x) = f(x) \cdot g(x) = x^2 x - 3^-$$
  
 $f(x) x^2$ 

**20.** 
$$(f/g)(\chi = \underline{=} \sqrt{}$$

$$g(x)$$
  $x$ 

21

$$f(x) = \frac{1}{2} \frac{x}{2} + 4$$

$$f(x+h) = \frac{1}{2}(x+h) + 4 = \frac{1}{2}$$

$$\frac{f(x+h)-f(x)}{h} = \frac{2 \frac{x+2}{2} \frac{h+4}{2} \frac{x+4}{2}}{h}$$

$$=\frac{2^{x+2}h+4-2^{x-4}}{h}$$

$$=\frac{2}{-\frac{1}{2}}\frac{1}{2}\frac{1}{2}=\frac{1}{2}\frac{1}{2}\frac{1}{2}=\frac{1}{2}\frac{1}$$

 $+2^{h+4}$ 

**22.**  $f(x) = 2x^2 - x + 3$  $f(x+h) = 2(x+h)^2 - (x+h) + 3 = 2(x^2 + 2xh + h^2) - x - h + 3 = 2x^2 + 4xh + 2h^2 - x - h + 3$ 

$$f(x+h)-f(x) = 2x^2+4xh+2h^2-x-h+3-(2x^2-x+3)$$

h  

$$= \frac{2x^{2}+4xh+2h^{2}-x-h+3-2x^{2}+x-3}{h}$$

$$= \frac{4xh+2h^{2}-h}{h}$$

$$= \frac{h(4x+2h-1)}{h}$$

$$= 4x+2h-1$$

23. 
$$(g \circ h)(2) = g(h(2)) = g(3 \cdot 2^2 + 2 \cdot 2 + 4) =$$
  
 $g(3 \cdot 4 + 4 + 4) = g(12 + 4 + 4) = g(20) = 4 \cdot 20 + 3 =$   
 $80 + 3 = 8 3$   
24.  $(f \circ g)(-1) = f(g(-1)) = f(4(-1) + 3) = f(-4 + 3) =$   
 $f(-1) = (-1)^2 - 1 = 1 - 1 = 0$   
25.  $(h \circ f)(1) = h(f(1)) = h(1^2 - 1) = h(1 - 1) = h(0) =$   
 $3 \cdot 0^2 + 2 \cdot 0 + 4 = 0 + 0 + 4 = 4$   
26.  $(g \circ g)(x) = g(g(x)) = g(4x + 3) = 4(4x + 3) + 3 =$   
 $16x + 12 + 3 = 16x + 15 \qquad \sqrt{}$   
27.  $(f \circ g \cdot x) = f(x + 15) \qquad \sqrt{}$   
 $(f \circ g \cdot x) = f(x + 15) \qquad \sqrt{}$   
 $f \circ g \cdot x \qquad f \cdot x \qquad x^2 - 4$   
 $(g \circ f)(x) = g(f(x)) = g((x - 5)) = (x - 5)^2 + 1 =$ 

**28.** The inputs for f(x) must be such that  $x - 5 \ge 0$ , or  $x \ge 5$ . Then for  $(f \circ g)(x)$  we must have  $g(x) \ge 5$ , or  $x + 1 \ge 5$ , or  $x \ge 4$ . Then the domain of  $(f \circ g)(x)$  is  $(-\infty, -2] \cup [2, \infty)$ .

Since we can substitute any real number for x in g, the domain of  $(g \circ f)(x)$  is the same as the domain of f(x), [5,  $\infty$ ).

**29.** Answers may vary.  $f(x) = x^4$ , g(x) = 2x - 7

**30.** 
$$y = x^4 - 2x^2$$

x - 5 + 1 = x - 4

Replacey with y to test for symmetry with respect to the x-

axis.  $-y = x^4 - 2x^2$   $y = -x^4 + 2x^2$ 

The resulting equation is not equivalent to the original equation, so the graph is not symmetric with respect to the *x*-axis.

Replace*x* with *x* to-testforsymmetrywit hrespectto the *y*-axis.

у = (  $\frac{-}{x}$ ) 4 -2 ( x ) 2 y = *x* 4 -2 *x* 2 The resulting equation

is equivalent to the original equa- tion, so the graph is symmetric with respect to the yaxis. Replace x with -x and y with -y to test for symmetry with respect to theorigin.

$$-y = (-x)^4 - 2(-x)^2$$
$$-y = x^4 - 2x^2$$
$$y = -x^4 + 2x^2$$

The resulting equation is not equivalent to the original

equation, so the graph is not symmetric with respect to the origin.

**31.** 
$$f(x) = \frac{2x}{x^2 + 1}$$
  
 $f(-x) = \frac{-2x}{(-x)^2 + 1} - \frac{-2x}{x^2 + 1}$   
 $f(x) f = f(-x)$ , so f is not even.

$$-f(x) = -\frac{2x}{x^2+1}$$

f(-x) = -f(x), so f is odd.

- **32.** Shape:  $h(x) = x^2$ Shift h(x) right 2 units:  $g(x) = h(x-2) = (x-2)^2$  Shift g(x)down 1 unit:  $f(x) = (x-2)^2 - 1$
- **33.** Shape:  $h(x)=x^2$ Shift h(x) left 2 units:  $g(x)=h(x+2)=(x+2)^2$  Shift g(x)down 3 units:  $f(x)=(x+2)^2-3$
- **34.** Eachy-coordinate is multiplied by . We plot an  $\frac{1}{2}$  connect (-5, 1), (-3, -2), (1, 2) and (4, -1).

y = k y = k  $y = -\frac{1}{2}f(x)$ 35. y = k  $5 = k^{x}$  6 30 = k Variation constant Equation of variation : y = 30 x36. y = kx

 $60 = k \cdot 12$  5 = k Variation constant Equationof variation: y=5x

**37.** 
$$y = \frac{kxz^2}{w}$$

$$100 = \frac{k(0.1)(10)^2}{5}$$

$$100 = 2k$$

$$50 = k \text{ Variation constant } 50xz^2$$

$$y = \underline{\qquad} \qquad \text{Equation of variation}$$

38.

$$200 = k \cdot 60^{2}$$

$$\frac{1}{2} = k$$

$$d = \frac{1}{2}r^{2}$$

$$\frac{1}{2}$$
Equation of variation 18
$$\frac{1}{2}$$

$$d = \frac{1}{18} \cdot 30^{2}$$

$$d = 50 \text{ ft}$$

**39.** The graph of 
$$g(x) = 2f(x) - 1$$
 is the graph of  $y = f(x)$ 

stretchedverticallybyafactorof2andshifteddown1unit. The correct graph is C.

**40.** Each x-coordinate on the graph of y = f(x) is divided by 3 on the

graphofy = 
$$f(3x)$$
. Thus the point  $-3$  **x** , 1 , or 3

$$(-1, 1)$$
 is on the graph of  $f(3x)$ .

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