# Solution Manual for Microeconomics An Intuitive Approach with Calculus 2nd Edition Thomas Nechyba 13056504689781305650466 Link full download Test Bank: <br> https://testbankpack.com/p/test-bank-for-microeconomics-an-intuitive-approach-with-calculus-2nd-edition-thomas-nechyba-13056504689781305650466/ <br> Solution Manual: <br> https://testbankpack.com/p/solution-manual-for-microeconomics-an-intuitive-approach-with-calculus-2nd-edition-thomas-nechyba-1305650468-9781305650466/ 

CHAPTER



## Choice Sets and Budget Constraints


#### Abstract

The even-numbered solutions to end-of-chapter exercises are provided for use by instructors. (Solutions to odd-numbered end-of-chapter exercises are pro-vided here as well as in the Study Guide that is available to students.)


Solutions may be shared by an instructor with his or her students at the in-structor's discretion.

They may not be made publicly available.

If posted on a course web-site, the site must be password protected and for use only by the students in the course.

Reproduction and/or distribution of the solutions beyond classroom use is strictly prohibited.

- Each end-of-chapter exercise begins on a new page. This is to facilitate max-imum flexibility for instructors who may wish to share answers to some but not all exercises with their students.
- If you are assigning only the A-parts of exercises in Microeconomics: An In-tuitive Approach with Calculus, you may wish to instead use the solution set created for the companion book Microeconomics: An Intuitive Approach.
- Solutions to Within-Chapter Exercises are provided in the student Study Guide.


## Exercise 2.1

Any good Southern breakfast includes grits (which my wife loves) and bacon (which I love). Suppose we allocate $\$ 60$ per week to consumption of grits and bacon, that grits cost $\$ 2$ per box and bacon costs $\$ 3$ per package.

A: Use a graph with boxes of grits on the horizontal axis and packages of bacon on the vertical to answer the following:
(a) Illustrate my family's weekly budget constraint and choice set.

Answer: The graph is drawn in panel (a) of Exercise Graph 2.1.


Exercise Graph 2.1 : (a) Answer to (a); (b) Answer to (c); (c) Answer to (d)
(b) Identify the opportunity cost of bacon and grits and relate these to concepts on your graph.
Answer: The opportunity cost of grits is equal to $2 / 3$ of a package of bacon (which is equal to the negative slope of the budget since grits appear on the horizontal axis). The opportunity cost of a package of bacon is $3 / 2$ of a box of grits (which is equal to the inverse of the negative slope of the budget since bacon appears on the vertical axis).
(c) How would your graph change if a sudden appearance of a rare hog dis-ease caused the price of bacon to rise to $\$ 6$ per package, and how does this change the opportunity cost of bacon and grits?

Answer: This change is illustrated in panel (b) of Exercise Graph 2.1. This changes the opportunity cost of grits to $1 / 3$ of a package of bacon, and it changes the opportunity cost of bacon to 3 boxes of grits. This makes sense: Bacon is now 3 times as expensive as grits - so you have to give up 3 boxes of grits for one package of bacon, or $1 / 3$ of a package of bacon for 1 box of grits.
(d) What happens in your graph if (instead of the change in (c)) the loss of my job caused us to decrease our weekly budget for Southern breakfasts from $\$ 60$ to $\$ 30$ ? How does this change the opportunity cost of bacon and grits?

Answer: The change is illustrated in panel (c) of Exercise Graph 2.1. Since relative prices have not changed, opportunity costs have not changed. This is reflected in the fact that the slope stays unchanged.

B: In the following, compare a mathematical approach to the graphical ap-proach used in part $A$, using $x_{1}$ to represent boxes of grits and $x_{2}$ to represent packages of bacon:
(a) Write down the mathematical formulation of the budget line and choice set and identify elements in the budget equation that correspond to key features of your graph from part 2.1A(a).
Answer: The budget equation is $p_{1} x_{1}+p_{2} x_{2}=I$ can also be written as

$$
\begin{equation*}
x_{2}=\frac{I}{p_{2}}-\frac{p_{1}}{p_{2}} x_{1} . \tag{2.1.i}
\end{equation*}
$$

With $I=60, p_{1}=2$ and $p_{2}=3$, this becomes $x_{2}=20-(2 / 3) x_{1}-$ an equa-tion with intercept of 20 and slope of $-2 / 3$ as drawn in Exercise Graph 2.1(a).
(b) How can you identify the opportunity cost of bacon and grits in your equation of a budget line, and how does this relate to your answer in 2.1A(b). Answer: The opportunity cost of $x_{1}$ (grits) is simply the negative of the slope term (in terms of units of $x_{2}$ ). The opportunity cost of $x_{2}$ (bacon) is the inverse of that.
(c) Illustrate how the budget line equation changes under the scenario of 2.1A(c) and identify the change in opportunity costs.
Answer: Substituting the new price $p_{2}=6$ into equation (2.1.i), we get $x_{2}=10-$ (1/3) $x_{1}$ - an equation with intercept of 10 and slope of $-1 / 3$ as depicted in panel (b) of Exercise Graph 2.1.
(d) Repeat (c) for the scenario in 2.1A(d).

Answer: Substituting the new income $I=30$ into equation (2.1.i) (hold-ing prices at $p_{1}=2$ and $p_{2}=3$, we get $x_{2}=10-(2 / 3) x_{1}-$ an equation with intercept of 10 and slope of $-2 / 3$ as depicted in panel (c) of Exercise Graph 2.1.

## Exercise 2.2

Suppose the only two goods in the world are peanut butter and jelly.
A: You have no exogenous income but you do own 6 jars of peanut butter and 2 jars of jelly. The price of peanut butter is $\$ 4$ per jar, and the price of jelly is $\$ 6$ per jar.
(a) On a graph with jars of peanut butter on the horizontal and jars of jelly on the vertical axis, illustrate your budget constraint.
Answer: This is depicted in panel (a) of Exercise Graph 2.2. The point $E$ is the endowment point of 2 jars of jelly and 6 jars of peanut butter (PB). If you sold your 2 jars of jelly (at a price of $\$ 6$ per jar), you could make $\$ 12$, and with that you could buy an additional 3 jars of PB (at the price of $\$ 4$ per jar). Thus, the most PB you could have is 9 , the intercept on the horizontal axis. Similarly, you could sell your 6 jars of PB for $\$ 24$, and with that you could buy 4 additional jars of jelly to get you to a maximum total of 6 jars of jelly - the intercept on the vertical axis. The resulting budget line has slope $-2 / 3$, which makes sense since the price of $\mathrm{PB}(\$ 4)$ divided by the price of jelly (\$6) is in fact $2 / 3$.


Exercise Graph 2.2 : (a) Answer to (a); (b) Answer to (b)
(b) How does your constraint change when the price of peanut butter increases to $\$ 6$ ? How does this change your opportunity cost of jelly?
Answer: The change is illustrated in panel (b) of Exercise Graph 2.2. Since you can always still consume your endowment $E$, the new budget must contain $E$. But the opportunity costs have now changed, with the ratio of the two prices now equal to 1 . Thus, the new budget constraint has slope -1 and runs through $E$. The opportunity cost of jelly has now fallen from $3 / 2$ to 1 . This should make sense: Before, PB was cheaper than jelly and so, for every jar of jelly you had to give up more than a jar of peanut butter.

Now that they are the same price, you only have to give up one jar of PB to get 1 jar of jelly.

B: Consider the same economic circumstances described in $2.2 A$ and use $x_{1}$ to represent jars of peanut butter and $x_{2}$ to represent jars of jelly.
(a) Write down the equation representing the budget line and relate key com-ponents to your graph from 2.2A(a).
Answer: The budget line has to equate your wealth to the cost of your con-
sumption. Your wealth is equal to the value of your endowment, which is $p_{1} e_{1}+p_{2} e_{2}$ (where $e_{1}$ is your endowment of PB and $e_{2}$ is your endowment
of jelly). The cost of your consumption is just your spending on the two goods -
i.e. $p_{1} x_{1}+p_{2} x_{2}$. The resulting equation is

$$
\begin{equation*}
p_{1} e_{1}+p_{2} e_{2}=p_{1} x_{1}+p_{2} x_{2} . \tag{2.2.i}
\end{equation*}
$$

When the values given in the problem are plugged in, the left hand side becomes $4(6)+6(2)=36$ and the right hand side becomes $4 x_{1}+6 x_{2}$ - resulting in the equation $36=4 x_{1}+6 x_{2}$. Taking $x_{2}$ to one side, we then get

$$
\begin{gather*}
2 \\
x_{2}=6-\overline{3} x_{1}, \tag{2.2.ii}
\end{gather*}
$$

which is exactly what we graphed in panel (a) of Exercise Graph 2.2 - a line with vertical intercept of 6 and slope of $-2 / 3$.
(b) Change your equation for your budget line to reflect the change in eco-nomic circumstances described in $2.2 A(b)$ and show how this new equation relates to your graph in $2.2 A(b)$.
Answer: Now the left hand side of equation (2.2.i) is $6(6)+6(2)=48$ while the right hand side is $6 x_{1}+6 x_{2}$. The equation thus becomes $48=6 x_{1}+6 x_{2}$ or, when $x_{2}$ is taken to one side,

$$
\begin{equation*}
x_{2}=8-x_{1} . \tag{2.2.iii}
\end{equation*}
$$

This is an equation of a line with vertical intercept of 8 and slope of -1 - exactly what we graphed in panel (b) of Exercise Graph 2.2.

## Exercise 2.3

Consider a budget for good $x_{1}$ (on the horizontal axis) and $x_{2}$ (on the vertical axis) when your economic circumstances are characterized by prices $p_{1}$ and $p_{2}$ and an exogenous income level I.

A: Draw a budget line that represents these economic circumstances and care-fully label the intercepts and slope.

Answer: The sketch of this budget line is given in Exercise Graph 2.3.


Exercise Graph 2.3 : A budget constraint with exogenous income $I$
The vertical intercept is equal to how much of $x_{2}$ one could by with $I$ if that is all one bought — which is just $I / p_{2}$. The analogous is true for $x_{1}$ on the horizontal intercept. One way to verify the slope is to recognize it is the "rise" $\left(I / p_{2}\right)$ divided by the "run" ( $I$
$\left./ p_{1}\right)$ - which gives $p_{1} / p_{2}$ - and that it is negative since the budget constraint is downward sloping.
(a) Illustrate how this line can shift parallel to itself without a change in $I$.

Answer: In order for the line to shift in a parallel way, it must be that the slope $-p_{1} / p_{2}$ remains unchanged. Since we can't change $I$, the only values we can change are $p_{1}$ and $p_{2}$ - but since $p_{1} / p_{2}$ can't change, it means the only thing we can do is to multiply both prices by the same constant. So, for instance, if we multiply both prices by 2 , the ratio of the new prices is $2 p_{1} /\left(2 p_{2}\right)=p_{1} / p_{2}$ since the 2 's cancel. We therefore have
not changed the slope. But we have changed the vertical intercept from $I / p_{2}$ to $I$
$/\left(2 p_{2}\right)$. We have therefore shifted in the line without changing its slope.
This should make intuitive sense: If our money income does not change but all prices double, then I can by half as much of everything. This is equivalent to prices staying the same and my money income dropping by half.
(b) Illustrate how this line can rotate clockwise on its horizontal intercept with-out a change in $p_{2}$.
Answer: To keep the horizontal intercept constant, we need to keep $I / p_{1}$ constant. But to rotate the line clockwise, we need to increase the verti-cal intercept $I / p_{2}$. Since we can't change $p_{2}$ (which would be the easiest
way to do this), that leaves us only $I$ and $p_{1}$ to change. But since we can't change $I$ $/ p_{1}$, we can only change these by multiplying them by the same constant. For instance, if we multiply both by 2 , we don't change the hor-izontal intercept since $2 I /\left(2 p_{1}\right)=I / p_{1}$. But we do increase the vertical intercept from $I / p_{2}$ to $2 I / p_{2}$. So, multiplying both $I$ and $p_{1}$ by the same constant (greater than 1 ) will accomplish our goal.
This again should make intuitive sense: If you double my income and the price of good 1, I can still afford exactly as much of good 1 if that is all I buy with my income. ( Thus the unchanged horizontal intercept). But, if I only buy good 2, then a doubling of my income without a change in the price of good 2 lets me buy twice as much of good 2 . The scenario is exactly the same as if $p_{2}$ had fallen by half (and $I$ and $p_{1}$ had remained unchanged.)

B: Write the equation of a budget line that corresponds to your graph in 2.3A.
Answer: $p_{1} x_{1}+p_{2} x_{2}=I$, which can also be written as

$$
\begin{gather*}
x_{2}=\frac{I}{p_{2}}-\frac{p_{1}}{2} x_{1} \tag{2.3.i}
\end{gather*}
$$

(a) Use this equation to demonstrate how the change derived in $2.3 A(a)$ can happen.
 get

$$
\begin{gather*}
\frac{I}{\alpha p_{1}} \underline{(1 / \alpha) I} \underline{p}_{1} \\
x_{2}=\alpha p_{2}-\alpha p_{2} x_{1}=p_{2}-p_{2} x_{1} \tag{2.3.ii}
\end{gather*}
$$

Thus, multiplying both prices by $\alpha$ is equivalent to multiplying income by $1 / \alpha$ (and leaving prices unchanged).
(b) Use the same equation to illustrate how the change derived in $2.3 A(b)$ can happen.


$$
\begin{equation*}
x_{2}=\frac{\beta I}{p_{2}}-\frac{\beta p_{1}}{p_{2}} x_{1}=\frac{I}{(1 / \beta) p_{2}}-\frac{p}{(1 / \beta) p_{2}} x_{1} \tag{2.3.iii}
\end{equation*}
$$

Thus, this is equivalent to multiplying $p_{2}$ by $1 / \beta$. So long as $\beta>1$, it is therefore equivalent to reducing the price of good 2 (without changing the other price or income).

## Exercise 2.4

Suppose there are three goods in the world: $x_{1}, x_{2}$ and $x_{3}$.
A: On a 3-dimensional graph, illustrate your budget constraint when your eco-nomic circumstances are defined by $p_{1}=2, p_{2}=6, p_{3}=5$ and $I=120$. Carefully label intercepts.

Answer: Panel (a) of Exercise Graph 2.4 illustrates this 3-dimensional budget with each intercept given by $I$ divided by the price of the good on that axis.


Exercise Graph 2.4 : Budgets over 3 goods: Answers to $2.4 \mathrm{~A}, \mathrm{~A}(\mathrm{~b})$ and $\mathrm{A}(\mathrm{c})$
(a) What is your opportunity cost of $x_{1}$ in terms of $x_{2}$ ? What is your opportu-nity cost of $x_{2}$ in terms of $x_{3}$ ?
Answer: On any slice of the graph that keeps $x_{3}$ constant, the slope of the budget is $-p_{1} / p_{2}=-1 / 3$. Just as in the 2 -good case, this is then the op-portunity cost of $x_{1}$ in terms of $x_{2}-$ since $p_{1}$ is a third of $p_{2}$, one gives up $1 / 3$ of a unit of $x_{2}$ when one chooses to consume 1 unit of $x_{1}$. On any verti-cal slice that holds $x_{1}$ fixed, on the other hand, the slope is $-p_{3} / p_{2}=-5 / 6$. Thus, the opportunity cost of $x_{3}$ in terms of $x_{2}$ is $5 / 6$, and the opportunity cost of $x_{2}$ in terms of $x_{3}$ is the inverse i.e. $6 / 5$.
(b) Illustrate how your graph changes if I falls to $\$ 60$. Does your answer to (a) change?
Answer: Panel (b) of Exercise Graph 2.4 illustrates this change (with the dashed plane equal to the budget constraint graphed in panel (a).) The answer to part (a) does not change since no prices and thus no opportu-nity costs changed. The new plane is parallel to the original.
(c) Illustrate how your graph changes if instead $p_{1}$ rises to $\$ 4$. Does your an-swer to part (a) change?
Answer: Panel (c) of Exercise Graph 2.4 illustrates this change (with the dashed plane again illustrating the budget constraint from part (a).) Since
only $p_{1}$ changed, only the $x_{1}$ intercept changes. This changes the slope on any slice that holds $x_{3}$ fixed from $-1 / 3$ to $-2 / 3$ - thus doubling the opportunity cost of $x_{1}$ in terms of $x_{2}$. Since the slope of any slice holding $x_{1}$ fixed remains unchanged, the opportunity cost of $x_{2}$ in terms of $x_{3}$ remains unchanged. This makes sense since $p_{2}$ and $p_{3}$ did not change, leaving the tradeoff between $x_{2}$ and $x_{3}$ consumption unchanged.

B: Write down the equation that represents your picture in 2.4 . Then suppose that a new good $x_{4}$ is invented and priced at $\$ 1$. How does your equation change? Why is it difficult to represent this new set of economic circumstances graphi-cally?

Answer: The equation representing the graphs is $p_{1} x_{1}+p_{2} x_{2}+p_{3} x_{3}=I$ or, plugging in the initial prices and income relevant for panel (a), $2 x_{1}+6 x_{2}+5 x_{3}=$
120. With a new fourth good priced at 1 , this equation would become $2 x_{1}+6 x_{2}+5 x_{3}$ $+x_{4}=120$. It would be difficult to graph since we would need to add a fourth dimension to our graphs.

## Exercise 2.5

Everyday Application: Watching a Bad Movie: On one of my first dates with my wife, we went to see the movie "Spaceballs" and paid $\$ 5$ per ticket.

A:Halfway through the movie, my wife said: "What on earth were you thinking? This movie sucks! I don't know why I let you pick movies. Let's leave."
(a) In trying to decide whether to stay or leave, what is the opportunity cost of staying to watch the rest of the movie?

Answer: The opportunity cost of any activity is what we give up by un-dertaking that activity. The opportunity cost of staying in the movie is whatever we would choose to do with our time if we were not there. The price of the movie tickets that got us into the movie theater is NOT a part of this opportunity cost - because, whether we stay or leave, we do not get that money back.
(b) Suppose we had read a sign on the way into theater stating "Satisfaction Guaranteed! Don't like the movie half way through - see the manager and get your money back!'" How does this change your answer to part (a)?
Answer: Now, in addition to giving up whatever it is we would be doing if we weren't watching the movie, we are also giving up the price of the movie tickets. Put differently, by staying in the movie theater, we are giv-ing up the opportunity to get a refund - and so the cost of the tickets is a real opportunity cost of staying.

## Exercise 2.6

Everyday Application: Renting a Car versus Taking Taxis: Suppose my brother and I both go on a week-long vacation in Cayman and, when we arrive at the air-port on the island, we have to choose between either renting a car or taking a taxi to our hotel. Renting a car involves a fixed fee of $\$ 300$ for the week, with each mile driven afterwards just costing 20 cents - the price of gasoline per mile. Taking a taxi involves no fixed fees, but each mile driven on the island during the week now costs $\$ 1$ per mile.

A: Suppose both my brother and I have brought $\$ 2,000$ on our trip to spend on "miles driven on the island" and "other goods". On a graph with miles driven on the horizontal and other consumption on the vertical axis, illustrate my budget constraint assuming I chose to rent a car and my brother's budget constraint assuming he chose to take taxis.

Answer: The two budget lines are drawn in Exercise Graph 2.6. My brother could spend as much as $\$ 2,000$ on other goods if he stays at the airport and does not rent any taxis, but for every mile he takes a taxi, he gives up $\$ 1$ in other good consumption. The most he can drive on the island is 2,000 miles. As soon as I pay the $\$ 300$ rental fee, I can at most consume $\$ 1,700$ in other goods, but each mile costs me only 20 cents. Thus, I can drive as much as $1700 / 0.2=8,500$ miles.


Exercise Graph 2.6 : Graphs of equations in exercise 2.6
(a) What is the opportunity cost for each mile driven that I faced?

Answer: I am renting a car - which means I give up 20 cents in other consumption per mile driven. Thus, my opportunity cost is 20 cents. My opportunity cost does not include the rental fee since I paid that before even getting into the car.
(b) What is the opportunity cost for each mile driven that my brother faced?

Answer: My brother is taking taxis - so he has to give up $\$ 1$ in other consumption for every mile driven. His opportunity cost is therefore $\$ 1$ per mile.

B:Derive the mathematical equations for my budget constraint and my brother's budget constraint, and relate elements of these equations to your graphs in part A. Use $x_{1}$ to denote miles driven and $x_{2}$ to denote other consumption.

Answer: My budget constraint, once I pay the rental fee, is $0.2 x_{1}+x_{2}=1700$ while my brother's budget constraint is $x_{1}+x_{2}=2000$. These can be rewritten with $x_{2}$ on the left hand side as

$$
\begin{equation*}
x_{2}=1700-0.2 x_{1} \text { for me, and } \tag{2.6.i}
\end{equation*}
$$

$$
\begin{equation*}
x_{2}=2000-x_{1} \text { for my brother. } \tag{2.6.ii}
\end{equation*}
$$

The intercept terms ( 1700 for me and 2000 for my brother) as well as the slopes ( -0.2 for me and -1 for my brother) are as in Exercise Graph 2.6.
(a) Where in your budget equation for me can you locate the opportunity cost of a mile driven?

Answer: My opportunity cost of miles driven is simply the slope term in my budget equation - i.e. 0.2 . I give up $\$ 0.20$ in other consumption for every mile driven.
(b) Where in your budget equation for my brother can you locate the opportu-nity cost of a mile driven?
Answer: My brother's opportunity cost of miles driven is the slope term in his budget equation - i.e. 1 ; he gives up $\$ 1$ in other consumption for every mile driven.

## Exercise 2.7

Everyday Application: Dieting and Nutrition: On a recent doctor's visit, you have been told that you must watch your calorie intake and must make sure you get enough vitamin E in your diet.

A: You have decided that, to make life simple, you will from now on eat only steak and carrots. A nice steak has 250 calories and 10 units of vitamins, and a serving of carrots has 100 calories and 30 units of vitamins Your doctor's instruc-tions are that you must eat no more than 2000 calories and consume at least 150 units of vitamins per day.
(a) In a graph with "servings of carrots" on the horizontal and steak on the vertical axis, illustrate all combinations of carrots and steaks that make up a 2000 calorie a day diet.
Answer: This is illustrated as the "calorie constraint" in panel (a) of Ex-ercise Graph 2.7. You can get 2000 calories only from steak if you eat 8 steaks and only from carrots if you eat 20 servings of carrots. These form the intercepts of the calorie constraint.


Exercise Graph 2.7 : (a) Calories and Vitamins; (b) Budget Constraint
(b) On the same graph, illustrate all the combinations of carrots and steaks that provide exactly 150 units of vitamins.

Answer: This is also illustrated in panel (a) of Exercise Graph 2.7. You can get 150 units of vitamins from steak if you eat 15 steaks only or if you eat 5 servings of carrots only. This results in the intercepts for the "vitamin constraint".
(c) On this graph, shade in the bundles of carrots and steaks that satisfy both of your doctor's requirements.
Answer: Your doctor wants you to eat no more than 2000 calories - which means you need to stay underneath the calorie constraint. Your doctor also wants you to get at least 150 units of vitamin E - which means you must choose a bundle above the vitamin constraint. This leaves you with
the shaded area to choose from if you are going to satisfy both require-ments.
(d) Now suppose you can buy a serving of carrots for $\$ 2$ and a steak for $\$ 6$. You have $\$ 26$ per day in your food budget. In your graph, illustrate your budget constraint. If you love steak and don't mind eating or not eating carrots, what bundle will you choose (assuming you take your doctor's instructions seriously)?

Answer: With $\$ 26$ you can buy $13 / 3$ steaks if that is all you buy, or you can buy 13 servings of carrots if that is all you buy. This forms the two inter-cepts on your budget constraint which has a slope of $-p_{1} / p_{2}=-1 / 3$ and is depicted in panel (b) of the graph. If you really like steak and don't mind eating carrots one way or another, you would want to get as much steak as possible given the constraints your doctor gave you and given your budget constraint. This leads you to consume the bundle at the inter-
section of the vitamin and the budget constraint in panel (b) - indicated by ( $x_{1}$, $x_{2}$ ) in the graph. It seems from the two panels that this bundle also satisfies the calorie constraint and lies inside the shaded region.

B:Continue with the scenario as described in part $A$.
(a) Define the line you drew in $A(a)$ mathematically.

Answer: This is given by $100 x_{1}+250 x_{2}=2000$ which can be written as

$$
x_{2}=8-\frac{2}{-5} x_{1} .
$$

(b) Define the line you drew in $A(b)$ mathematically.

Answer: This is given by $30 x_{1}+10 x_{2}=150$ which can be written as

$$
\begin{equation*}
x_{2}=15-3 x_{1} . \tag{2.7.ii}
\end{equation*}
$$

(c) In formal set notation, write down the expression that is equivalent to the shaded area in $A(c)$.

Answer:

$$
\begin{equation*}
\text { (C) }_{\left(x_{1}, x_{2}\right)} \mathbf{R}_{+}^{2} \mid 100 x_{1}+250 x_{2} \leq 2000 \text { and } 30 x_{1}+10 x_{2} \geq 150 \tag{2.7.iii}
\end{equation*}
$$

(d) Derive the exact bundle you indicated on your graph in $A(d)$.

Answer: We would like to find the most amount of steak we can afford in the shaded region. Our budget constraint is $2 x_{1}+6 x_{2}=26$. Our graph sug-gests that this budget constraint intersects the vitamin constraint (from equation (2.7.ii)) within the shaded region (in which case that intersec-tion gives us the most steak we can afford in the shaded region). To find
this intersection, we can plug equation (2.7.ii) into the budget constraint $2 x_{1}+6 x_{2}$ $=26$ to get

$$
\begin{equation*}
2 x_{1}+6\left(15-3 x_{1}\right)=26, \tag{2.7.iv}
\end{equation*}
$$

and then solve for $x_{1}$ to get $x_{1}=4$. Plugging this back into either the bud-get constraint or the vitamin constraint, we can get $x_{2}=3$. We know this lies on the vitamin constraint as well as the budget constraint. To check to make sure it lies in the shaded region, we just have to make sure it also satisfies the doctor's orders that you consume fewer than 2000 calories. The bundle $\left(x_{1}, x_{2}\right)=(4,3)$ results in calories of $4(100)+3(250)=1150$, well within doctor's orders.

## Exercise 2.8

Everyday Application: Setting up a College Trust Fund: Suppose that you, after studying economics in college, quickly became rich - so rich that you have nothing better to do than worry about your 16-year old niece who can't seem to focus on her future. Your niece currently already has a trust fund that will pay her a nice yearly income of $\$ 50,000$ starting when she is 18, and she has no other means of support.

A: You are concerned that your niece will not see the wisdom of spending a good portion of her trust fund on a college education, and you would therefore like to use $\$ 100,000$ of your wealth to change her choice set in ways that will give her greater incentives to go to college.
(a) One option is for you to place $\$ 100,000$ in a second trust fund but to restrict your niece to be able to draw on this trust fund only for college expenses of up to $\$ 25,000$ per year for four years. On a graph with "yearly dollars spent on college education" on the horizontal axis and "yearly dollars spent on other consumption" on the vertical, illustrate how this affects her choice set.

Answer: Panel (a) of Exercise Graph 2.8 illustrates the change in the bud-get constraint for this type of trust fund. The original budget shifts out by $\$ 25,000$ (denoted $\$ 25 \mathrm{~K}$ ), except that the first $\$ 25,000$ can only be used for college. Thus, the maximum amount of other consumption remains $\$ 50,000$ because of the stipulation that she cannot use the trust fund for non-college expenses.


Exercise Graph 2.8 : (a) Restricted Trust Fund; (b) Unrestricted; (c) Matching Trust Fund
(b) A second option is for you to simply tell your niece that you will give her $\$ 25,000$ per year for 4 years and you will trust her to "do what's right". How does this impact her choice set?
Answer: This is depicted in panel (b) of Exercise Graph 2.8 - it is a pure income shift of $\$ 25,000$ since there are no restrictions on how the money can be used.
(c) Suppose you are wrong about your niece's short-sightedness and she was planning on spending more than $\$ 25,000$ per year from her other trust fund on college education. Do you think she will care whether you do as described in part (a) or as described in part $(b)$ ?

Answer: If she was planning to spend more than $\$ 25 \mathrm{~K}$ on college anyhow, then the additional bundles made possible by the trust fund in (b) are not valued by her. She would therefore not care whether you set up the trust fund as in (a) or (b).
(d) Suppose you were right about her - she never was going to spend very much on college. Will she care now?

Answer: Now she will care - because she would actually choose one of the bundles made available in (b) that is not available in (a) and would therefore prefer (b) over (a).
(e) A friend of yours gives you some advice: be careful - your niece will not value her education if she does not have to put up some of her own money for it. Sobered by this advice, you decide to set up a different trust fund that will release 50 cents to your niece (to be spent on whatever she wants) for every dollar that she spends on college expenses. How will this affect her choice set?

Answer: This is depicted in panel (c) of Exercise Graph 2.8. If your niece now spends $\$ 1$ on education, she gets 50 cents for anything she would like to spend it on so, in effect, the opportunity cost of getting $\$ 1$ of additional education is just 50 cents. This "matching" trust fund therefore reduces the opportunity cost of education whereas the previous ones did not.
(f) If your niece spends $\$ 25,000$ per year on college under the trust fund in part (e), can you identify a vertical distance that represents how much you paid to achieve this outcome?

Answer: If your niece spends $\$ 25,000$ on her education under the "match-ing" trust fund, she will get half of that amount from your trust fund - or $\$ 12,500$. This can be seen as the vertical distance between the before and after budget constraints (in panel (c) of the graph) at $\$ 25,000$ of education spending.

B: How would you write the budget equation for each of the three alternatives discussed above?

Answer: The initial budget is $x_{1}+x_{2}=50,000$. The first trust fund in (a) expands this to a budget of

$$
\begin{equation*}
x_{2}=50,000 \text { for } x_{1} \leq 25,000 \text { and } x_{1}+x_{2}=75,000 \text { for } x_{1}>25,000, \tag{2.8}
\end{equation*}
$$

while the second trust fund in (b) expands it to $x_{1}+x_{2}=75,000$. Finally, the last "matching" trust fund in (e) (depicted in panel (c)) is $0.5 x_{1}+x_{2}=50,000$.

## Exercise 2.9

Business Application: Pricing and Quantity Discounts: Businesses often give quantity discounts. Below, you will analyze how such discounts can impact choice sets.

A: I recently discovered that a local copy service charges our economics depart-ment $\$ 0.05$ per page (or $\$ 5$ per 100 pages) for the first 10,000 copies in any given month but then reduces the price per page to $\$ 0.035$ for each additional page up to 100,000 copies and to $\$ 0.02$ per each page beyond 100,000. Suppose our department has a monthly overall budget of $\$ 5,000$.
(a) Putting "pages copied in units of 100 " on the horizontal axis and "dol-lars spent on other goods" on the vertical, illustrate this budget constraint. Carefully label all intercepts and slopes.
Answer: Panel (a) of Exercise Graph 2.9 traces out this budget constraint and labels the relevant slopes and kink points.


Exercise Graph 2.9: (a) Constraint from 2.9A(a); (b) Constraint from 2.9A(b)
(b) Suppose the copy service changes its pricing policy to $\$ 0.05$ per page for monthly copying up to 20,000 and $\$ 0.025$ per page for all pages if copying exceeds 20,000 per month. (Hint: Your budget line will contain a jump.)

Answer: Panel (b) of Exercise Graph 2.9 depicts this budget. The first portion (beginning at the $x_{2}$ intercept) is relatively straightforward. The second part arises for the following reason: The problem says that, if you copy more than 2000 pages, all pages cost only $\$ 0.025$ per page - includ-ing the first 2000. Thus, when you copy 20,000 pages per month, you total bill is $\$ 1,000$. But when you copy 2001 pages, your total bill is $\$ 500.025$.
(c) What is the marginal (or "additional") cost of the first page copied after 20,000 in part (b)? What is the marginal cost of the first page copied after 20,001 in part (b)?


#### Abstract

Answer: The marginal cost of the first page after 20,000 is $-\$ 499.975$, and the marginal cost of the next page after that is 2.5 cents. To see the dif-ference between these, think of the marginal cost as the increase in the total photo-copy bill for each additional page. When going from 20,000 to 20,001 , the total bill falls by $\$ 499.975$. When going from 20,001 to 20,002 , the total bill rises by 2.5 cents.


B: Write down the mathematical expression for choice sets for each of the sce-narios in 2.9A(a) and 2.9A(b) (using $x_{1}$ to denote "pages copied in units of 100 " and $x_{2}$ to denote "dollars spent on other goods").

Answer: The choice set in (a) is

$$
\begin{array}{rll}
\left\{\left(x_{1}, x_{2}\right) \quad \mathbf{R}_{+}{ }^{2} \mid x_{2}\right. & =5000-5 x_{1} & \text { for } x_{1} \leq 100 \text { and } \\
x_{2} & =4850-3.5 x_{1} & \text { for } 100<x_{1} \leq 1000 \text { and } \\
x_{2} & =3350-2 x_{1} & \text { for } \left.x_{1}>1000\right\} \tag{2.9.i}
\end{array}
$$

The choice set in (b) is

$$
\begin{array}{rll}
\left\{\left(x_{1}, x_{2}\right)\right. & \mathbf{R}_{+}^{2} \mid x_{2}=5000-5 x_{1} & \text { for } x_{1} \leq 200 \text { and } \\
x_{2}=5000-2.5 x_{1} & \text { for } \left.x_{1}>200\right\} \tag{2.9.ii}
\end{array}
$$

## Exercise 2.10

Business Application: Supersizing: Suppose I run a fast-food restaurant and I know my customers come in on a limited budget. Almost everyone that comes in for lunch buys a softdrink. Now suppose it costs me virtually nothing to serve a medium versus a large soft-drink, but I do incur some extra costs when adding items (like a dessert or another side-dish) to someone's lunch tray.

A:Suppose for purposes of this exercise that cups come in all sizes, not just small, medium and large; and suppose the average customer has a lunch budget B. On a graph with "ounces of soft-drink" on the horizontal axis and "dollars spent on other lunch items" on the vertical, illustrate a customer's budget constraint assuming I charge the same price p per ounce of soft-drink no matter how big a cup the customer gets.

Answer: Panel (a) of Exercise Graph 2.10 illustrates the original budget, with the price per ounce denoted $p$. The horizontal intercept is the money budget $B$ divided by the price per ounce of soft drink; the vertical intercept is just $B$ (since the good on the vertical axis is denominated in dollars - with the price of " $\$$ 's of lunch items" therefore implicitly set to 1 .


Exercise Graph 2.10 : (a) Original Budget; (b) The Daryls' proposal; (c) Larry's proposal
(a) I have three business partners: Larry, his brother Daryl and his other brother Daryl. The Daryls propose that we lower the price of the initial ounces of soft-drink that a consumer buys and then, starting at 10 ounces, we in-crease the price. They have calculated that our average customer would be able to buy exactly the same number of ounces of soft-drink (if that is all he bought on his lunch budget) as under the current single price. Illustrate how this will change the average customer's budget constraint.

Answer: Panel (b) illustrates the Daryls' proposal. The budget is initially shallower (because of the initial lower price and then becomes steeper at 10 ounces because of the new higher price.) The intercepts are un-changed because nothing has been done to allow the average customer to buy more of non-drink items if that is all she buys, and because the
new prices have been constructed so as to allow customers to achieve the same total drink consumption in the event that they do not buy anything else.
(b) Larry thinks the Daryls are idiots and suggests instead that we raise the price for initial ounces of soft-drink and then, starting at 10 ounces, de-crease the price for any additional ounces. He, too, has calculated that, under his pricing policy, the average customer will be able to buy exactly the same ounces of soft-drinks (if that is all the customer buys on his lunch budget). Illustrate the effect on the average customer's budget constraint.
Answer: Larry's proposal is graphed in panel (c). The reasoning is similar to that in the previous part, except now the initial price is high and then becomes low after 10 ounces.
(c) If the average customer had a choice, which of the three pricing systems - the current single price, the Daryls' proposal or Larry's proposal - would he choose?

Answer: Customers would surely prefer the Daryls' proposal - since the choice set it forms contains all the other choice sets.
P.S: If you did not catch the reference to Larry, his brother Daryl and his other brother Daryl, I recommend you rent some old versions of the 1980's Bob Newhart Show.

B: Write down the mathematical expression for each of the three choice sets de-scribed above, letting ounces of soft-drinks be denoted by $x_{1}$ and dollars spend on other lunch items by $x_{2}$.

Answer: The original budget set in panel (a) of Exercise Graph 2.10 is simply $p x_{1}+x_{2}$ $=B$ giving a choice set of

$$
\begin{equation*}
{ }_{\left(x_{1}, x_{2}\right)} \mathbf{R}_{+}^{2} \mid x_{2}=B-p x_{1}^{\underline{\mathbf{a}}} \text {. } \tag{2.10.i}
\end{equation*}
$$

In the Daryls' proposal, we have an initial price $p<p$ for the first 10 ounces, and then a price $p>p$ thereafter. We can calculate the $x_{2}$ intercept of the steeper line following the kink point in panel (b) of the graph by simply multi-plying the $x_{1}$ intercept of $B / p$ by the slope $p$ of that line segment to get $B p / p$. The choice set from the Daryls' proposal could then be written as

$$
\begin{array}{rlr}
\left\{\left(x_{1}, x_{2}\right) \quad \mathbf{R}_{+}^{2} \mid x_{2}\right. & =B-p_{n \prime}^{\prime} x_{1} & \text { for } x_{1} \leq 10 \text { and } \\
x_{2} & =\frac{B p}{p}-p^{\prime \prime} x_{1} & \text { for } \left.x_{1}>10 \text { where } p^{\prime}<p<p^{\prime \prime}\right\}(2 . .10 . i i)
\end{array}
$$

We could even be more precise about the relationship of $p, p$ and $p$ The two lines intersect at $x_{1}=10$, and it must therefore be the case that $B-10 p=(B p / p)$
$-10 p^{\prime \prime}$. Solving this for $p$, we get that

$$
p^{\prime}=\underline{B(p-p ")}_{+p^{\prime \prime} .}
$$

Larry's proposal begins with a price $p ">p$ and then switches at 10 ounces to a price $p$ $<p$ (where these prices have no particular relation to the prices we just used for the Daryl's proposal). This results in the choice set

$$
\begin{aligned}
& \left\{\left(x_{1}, x_{2}\right) \quad \mathbf{R}_{+}^{2} \mid x_{2}=B-p^{\prime \prime} x_{1}, \quad \text { for } x_{1} \leq 10\right. \text { and } \\
& \left.x_{2}=p-p x_{1} \quad \text { for } x_{1}>10 \text { where } p<p<p \quad\right\}(2 . .10 . \mathrm{iv})
\end{aligned}
$$

We could again derive an analogous expression for $p$ in terms of $p$ and $p$.

## Exercise 2.11

Business Application: Frequent Flyer Perks: Airlines offer frequent flyers differ-ent kinds of perks that we will model here as reductions in average prices per mile flown.

A: Suppose that an airline charges 20 cents per mile flown. However, once a customer reaches 25,000 miles in a given year, the price drops to 10 cents per mile flown for each additional mile. The alternate way to travel is to drive by car which costs 16 cents per mile.
(a) Consider a consumer who has a travel budget of $\$ 10,000$ per year, a budget which can be spent on the cost of getting to places as well as "other con-sumption" while traveling. On a graph with "miles flown" on the horizon-tal axis and "other consumption" on the vertical, illustrate the budget con-straint for someone who only considers flying (and not driving) to travel destinations.

Answer: Panel (a) of Exercise Graph 2.11 illustrates this budget constraint.


Exercise Graph 2.11 : (a) Air travel; (b) Car travel; (c) Comparison
(b) On a similar graph with "miles driven" on the horizontal axis, illustrate the budget constraint for someone that considers only driving (and not flying) as a means of travel.

Answer: This is illustrated in panel (b) of the graph.
(c) By overlaying these two budget constraints (changing the good on the hor-izontal axis simply to "miles traveled"), can you explain how frequent flyer perks might persuade some to fly a lot more than they otherwise would?
Answer: Panel (c) of the graph overlays the two budget constraints. If it were not for frequent flyer miles, this consumer would never fly - be-cause driving would be cheaper. With the frequent flyer perks, driving is cheaper initially but becomes more expensive per additional miles trav-eled if a traveler flies more than 25,000 miles. This particular consumer would therefore either not fly at all (and just drive), or she would fly a lot because it can only make sense to fly if she reaches the portion of the
air-travel budget that crosses the car budget. (Once we learn more about how to model tastes, we will be able to say more about whether or not it makes sense for a traveler to fly under these circumstances.)

B: Determine where the air-travel budget from $A(a)$ intersects the car budget from $A(b)$.

Answer: The shallower portion of the air-travel budget (relevant for miles flown above $25,000)$ has equation $x_{2}=7500-0.1 x_{1}$, where $x_{2}$ stands for other con-sumption and $x_{1}$ for miles traveled. The car budget, on the other hand, has equation $x_{2}=10000-0.16 x_{1}$. To determine where they cross, we can set the two equations equal to one another and solve for $x_{1}$ - which gives $x_{1}=41,667$ miles traveled. Plugging this back into either equation gives $x_{2}=\$ 3,333$.

## Exercise 2.12

Business Application: Choice in Calling Plans: Phone companies used to sell minutes of phone calls at the same price no matter how many phone calls a cus-tomer made. (We will abstract away from the fact that they charged different prices at different times of the day and week.) More recently, phone companies, particularly cell phone companies, have become more creative in their pricing.

A: On a graph with "minutes of phone calls per month" on the horizontal axis and "dollars of other consumption" on the vertical, draw a budget constraint assuming the price per minute of phone calls is $p$ and assuming the consumer has a monthly income $I$.

Answer: Exercise Graph 2.12 gives this budget constraint as the straight line with vertical intercept $I$.


Exercise Graph 2.12 : Phone Plans
(a) Now suppose a new option is introduced: You can pay $\$ P_{x}$ to buy into a phone plan that offers you x minutes of free calls per month, with any calls
beyond $x$ costing $p$ per minute. Illustrate how this changes your budget constraint and assume that $P_{x}$ is sufficiently low such that the new budget
contains some bundles that were previously unavailable to our consumer. Answer:
The second budget constraint in the graph begins at $I-P_{x}$ - which is how much monthly income remains available for other con-sumption once the fixed fee for the first $x$ minutes is paid. The price per additional minute is the same as before so after $x$ calls have been made, the slope of the new budget is the same as the original.
(b) Suppose it actually costs phone companies close to p per minute to pro-vide a minute of phone service so that, in order to stay profitable, a phone company must on average get about per minute of phone call. If all con-
sumers were able to choose calling plans such that they always use exactly $x$ minutes per month, would it be possible for phone companies to set $P_{x}$ sufficiently low such that new bundles become available to consumers?

Answer: If the phone company needs to make an average of $p$ per minute of phone calls, and if all consumers plan ahead perfectly and choose call-ing plans under which they use all their free minutes, then the company would have to set $P_{x}=p$ $x$. But that would mean that the kink point on the new budget would occur exactly on the original budget - thus mak-ing no new bundles available for consumers.
(c) If some fraction of consumers in any given month buy into a calling plan
but make fewer than $x$ calls, how does this enable phone companies to set $P_{x}$ such that new bundles become available in consumer choice sets?

Answer: If some consumers do not in fact use all their "free minutes", then the phone company could set $P_{x}<p x$ and still collect an average of $p$ per minute of phone call. This would cause the kink point of the new budget to shift to the right of the original budget - making new bundles available for consumers. Consumers who plan ahead well are, in some sense, receiving a transfer from consumers who do not plan ahead well.

B: Suppose a phone company has 100,000 customers who currently buy phone minutes under the old system that charges $p$ per minute. Suppose it costs the company $c$ to provide one additional minute of phone service but the company also has fixed costs F C (that don't vary with how many minutes are sold) of an amount that is sufficiently high to result in zero profit. Suppose a second identi-
cal phone company has 100,000 customers that have bought into a calling plan that charges $P_{x}=k p x$ and gives customers $x$ free minutes before charging $p$ for minutes above $x$.
(a) If people on average use half their "free minutes" per month, what is $k$ (as a functions of F C , p, c and $x$ ) if the second company also makes zero profit? Answer: The profit of the second company is its revenue minus its costs.
Revenue is

$$
\begin{equation*}
100,000\left(P_{x}\right)=100,000(k p x) \tag{2.12.i}
\end{equation*}
$$

Each customer only uses $x / 2$ minutes, which means the cost of providing the phone minutes is $100,000(c x / 2)=50,000 c x$. The company also has to cover the fixed costs $F C$. So, if profit is zero for the second company (as it is for the first), then

$$
\begin{equation*}
100000(k p x)-50000(c x)-F C=0 . \tag{2.12.ii}
\end{equation*}
$$

Solving this for $k$, we get

$$
\begin{equation*}
k=\frac{F C}{100000 p x}+\frac{c}{2 p} . \tag{2.12.iii}
\end{equation*}
$$

(b) If there were no fixed costs (i.e. F C = 0) but everything else was still as stated above, what does $c$ have to be equal to in order for the first company to make zero profit? What is $k$ in that case?
Answer: $c=p$ and $k=1 / 2$. This should make intuitive sense: Under the simplified scenario, the fact that people on average use only half their
"free minutes" implies that the second company can set its fixed fee of $x$ minutes at half the price that the other company would charge for con-suming that many minutes.

## Exercise 2.13

Policy Application: Food Stamp Programs and other Types of Subsidies: The U.S. government has a food stamp program for families whose income falls below a certain poverty threshold. Food stamps have a dollar value that can be used at su-permarkets for food purchases as if the stamps were cash, but the food stamps cannot be used for anything other than food.

A:Suppose the program provides $\$ 500$ of food stamps per month to a particular family that has a fixed income of \$1,000 per month.
(a) With "dollars spent on food" on the horizontal axis and "dollars spent on nonfood items" on the vertical, illustrate this family's monthly budget con-straint. How does the opportunity cost of food change along the budget constraint you have drawn?

Answer: Panel (a) of Exercise Graph 2.13 illustrates the original budget - with intercept 1,000 on each axis. It then illustrates the new budget under the food stamp program. Since food stamps can only be spent on food, the "other goods" intercept does not change - owning some food stamps still only allows households to spend what they previously had on other goods. However, the family is now able to buy $\$ 1,000$ in other goods even as it buys food - because it can use the food stamps on the first $\$ 500$ worth of food and still have all its other income left for other consump-tion. Only after all the food stamps are spent - i.e. after the family has bought $\$ 500$ worth of food - does the family give up other consump-tion when consuming additional food. As a result, the opportunity cost of food is zero until the food stamps are gone, and it is 1 after that. That is, after the food stamps are gone, the family gives up $\$ 1$ in other consump-tion for every $\$ 1$ of food it purchases.


Exercise Graph 2.13 : (a) Food Stamps; (b) Cash; (c) Re-imburse half
(b) How would this family's budget constraint differ if the government replaced the food stamp program with a cash subsidy program that simply gave this
family $\$ 500$ in cash instead of $\$ 500$ in food stamps? Which would the fam-ily prefer, and what does your answer depend on?
Answer: In this case, the original budget would simply shift out by $\$ 500$ as depicted in panel (b). If the family consumes more than $\$ 500$ of food under the food stamp program, it would not seem like anything really changes under the cash subsidy. ( We can show this more formally once we introduce a model of tastes). If, on the other hand, the family con-sumes $\$ 500$ of food under the food stamps, it may well be that it would prefer to get cash instead so that it can consume more other goods in-stead.
(c) How would the budget constraint change if the government simply agreed to reimburse the family for half its food expenses?

Answer: In this case, the government essentially reduces the price of $\$ 1$ of food to 50 cents because whenever $\$ 1$ is spent on food, the government reimburses the family 50 cents. The resulting change in the family budget is then depicted in panel (c) of the graph.
(d) If the government spends the same amount for this family on the program described in (c) as it did on the food stamp program, how much food will the family consume? Illustrate the amount the government is spending as a vertical distance between the budget lines you have drawn.

Answer: If the government spent $\$ 500$ for this family under this program, then the family will be consuming $\$ 1,000$ of food and $\$ 500$ in other goods. You can illustrate the $\$ 500$ the government is spending as the distance between the two budget constraints at $\$ 1,000$ of food consumption. The reasoning for this is as follows: On the original budget line, you can see that consuming $\$ 1,000$ of food implies nothing is left over for "other con-sumption". When the family consumes $\$ 1,000$ of food under the new pro-gram, it is able to consume $\$ 500$ in other goods because of the program - so the government must have made that possible by giving $\$ 500$ to the family.

B:Write down the mathematical expression for the choice set you drew in 2.13A(a), letting
$x_{1}$ represent dollars spent on food and $x_{2}$ represent dollars spent on non-food consumption. How does this expression change in 2.13A(b) and 2.13A(c)?

Answer: The original budget constraint (prior to any program) is just $x_{2}=1000-x_{1}$, and the budget constraint with the $\$ 500$ cash payment in $\mathrm{A}(\mathrm{b})$ is $x_{2}=1500-x_{1}$. The choice set under food stamps (depicted in panel (a)) then is

$$
\left\{\left(x_{1}, x_{2}\right) \quad \mathbf{R}_{+}^{2} \left\lvert\, \begin{array}{cc}
x_{2}=1000 & \text { for } x_{1} \leq 500 \text { and } \\
& x_{2}=1500-x_{1}  \tag{2.13.i}\\
\text { for } \left.x_{1}>500\right\},
\end{array}\right.\right.
$$

while the choice set in panel (b) under the cash subsidy is

$$
\begin{align*}
& \text { (C) } \\
& \left(x_{1}, x_{2}\right) \mathbf{R}_{+}^{2 \mid x_{2}=1500-x_{1}}{ }^{\text {a }} \text {. } \tag{2.13.ii}
\end{align*}
$$

Finally, the choice set under the re-imbursement plan from $\mathrm{A}(\mathrm{c})$ is

$$
{ }_{\left(x_{1}, x_{2}\right)}^{1 / 2} \mathbf{R}_{+}^{2 \left\lvert\, x_{2}=1000-\frac{1}{2} x_{1}\right.}{ }^{3 / 4} .
$$

## Exercise 2.14

Policy Application: Public Housing and Housing Subsidies: For a long period, the U.S. government focused its attempts to meet housing needs among the poor through public housing programs. Eligible families could get on waiting lists to apply for an apartment in a public housing development and would be offered a particular apartment as they moved to the top of the waiting list.

A:Suppose a particular family has a monthly income of \$1,500 and is offered a 1,500 square foot public housing apartment for $\$ 375$ in monthly rent. Alterna-tively, the family could choose to rent housing in the private market for $\$ 0.50$ per square foot.
(a) Illustrate all the bundles in this family's choice set of "square feet of hous-ing" (on the horizontal axis) and "dollars of monthly other goods consump-tion" (on the vertical axis).

Answer: The full choice set would include all the bundles that are avail-able through the private market plus the bundle the government has made available. In panel (a) of Exercise Graph 2.14, the private market con-straint is depicted together with the single bundle that the government makes available through public housing. ( That bundle has $\$ 1,125$ in other monthly consumption because the government charges $\$ 375$ for the 1,500 square foot public housing apartment.)


Exercise Graph 2.14 : (a) Public Housing; (b) Rental Subsidy
(b) In recent years, the government has shifted away from an emphasis on public housing and toward providing poor families with a direct subsidy to allow them to rent more housing in the private market. Suppose, instead of offering the family in part (a) an apartment, the government offered to pay half of the family's rental bill. How would this change the family's budget constraint?

## Exercise 2.14

$\qquad$ Answer: The change in policy is depicted in panel (b) of the graph.
(c) Is it possible to tell which policy the family would prefer?

Answer: Since the new budget in panel (b) contains the public housing bundle from panel (a) but also contains additional bundles that were pre-viously not available, the housing subsidy must be at least as good as the public housing program from the perspective of the household.

B: Write down the mathematical expression for the choice sets you drew in 2.14A(a) and 2.14A(b), letting $x_{1}$ denote square feet of monthly housing consumption and $x_{2}$ denote dollars spent on non-housing consumption.
Answer: The public housing choice set (which includes the option of not par-ticipating in public housing and renting in the private market instead) is given by

$$
\begin{equation*}
{ }_{\left(x_{1}, x_{2}\right)}^{\text {(C) }}{ }_{+}^{2}\left(x_{1}, x_{2}\right)=(1500,1125) \text { or } x_{2} \leq 1500-0.5 x_{1} \underline{\mathbf{a}} . \tag{2.14.i}
\end{equation*}
$$

The rental subsidy in panel (b), on the other hand, creates the choice set

$$
\begin{equation*}
{ }_{\left(x_{1}, x_{2}\right)} \mathbf{R}_{+}^{2} \mid x_{2} \leq 1500-0.25 x_{1}{ }^{\underline{\mathbf{a}}} . \tag{2.14.ii}
\end{equation*}
$$

## Exercise 2.15

Policy Application: Taxing Goods versus Lump Sum Taxes: I have finally con-vinced my local congressman that my wife's taste for grits are nuts and that the world should be protected from too much grits consumption. As a result, my congressman has agreed to sponsor new legislation to tax grits consumption which will raise the price of grits from $\$ 2$ per box to $\$ 4$ per box. We carefully observe my wife's shopping behavior and notice with pleasure that she now purchases 10 boxes of grits per month rather than her previous 15 boxes.

A:Putting "boxes of grits per month" on the horizontal and "dollars of other consumption" on the vertical, illustrate my wife's budget line before and after the tax is imposed. ( You can simply denote income by I.)

Answer: The tax raises the price, thus resulting in a rotation of the budget line as illustrated in panel (a) of Exercise Graph 2.15. Since no indication of an income level was given in the problem, income is simply denoted $I$.


Exercise Graph 2.15 : (a) Tax on Grits; (b) Lump Sum Rebate
(a) How much tax revenue is the government collecting per month from my wife? Illustrate this as a vertical distance on your graph. (Hint: If you know how much she is consuming after the tax and how much in other consumption this leaves her with, and if you know how much in other con-sumption she would have had if she consumed that same quantity before the imposition of the tax, then the difference between these two "other con-sumption" quantities must be equal to how much she paid in tax.)

Answer: When she consumes 10 boxes of grits after the tax, she pays $\$ 40$ for grits. This leaves her with $(I-40)$ to spend on other goods. Had she bought 10 boxes of grits prior to the tax, she would have paid $\$ 20$, leaving her with $(I-20)$. The difference between $(I-40)$ and $(I-20)$ is $\$ 20$ - which is equal to the vertical distance in panel (a). You can verify that this is exactly how much she indeed must have paid - the tax is $\$ 2$ per

## Exercise 2.15

box and she bought 10 boxes, implying that she paid $\$ 2$ times 10 or $\$ 20$ in grits taxes.
(b) Given that I live in the South, the grits tax turned out to be unpopular in my congressional district and has led to the defeat of my congressman. His replacement won on a pro-grits platform and has vowed to repeal the grits tax. However, new budget rules require him to include a new way to raise the same tax revenue that was yielded by the grits tax. He proposes to sim-ply ask each grits consumer to pay exactly the amount he or she paid in grits taxes as a monthly lump sum payment. Ignoring for the moment the difficulty of gathering the necessary information for implementing this proposal, how would this change my wife's budget constraint?
Answer: In panel (b) of Exercise Graph 2.15, the previous budget under the grits tax is illustrated as a dashed line. The grits tax changed the op-portunity cost of grits — and thus the slope of the budget (as illustrated in panel (a)). The lump sum tax, on the other hand, does not alter oppor-tunity costs but simply reduces income by $\$ 20$, the amount of grits taxes my wife paid under the grits tax. This change is illustrated in panel (b).

B: State the equations for the budget constraints you derived in $A(a)$ and $A(b)$, letting grits be denoted by $x_{1}$ and other consumption by $x_{2}$.

Answer: The initial (before-tax) budget was $x_{2}=I-2 x_{1}$ which becomes $x_{2}=I-4 x_{1}$ after the imposition of the grits tax. The lump sum tax budget constraint, on the other hand, is $x_{2}=I-20-2 x_{1}$.

## Exercise 2.16

Policy Application: Public Schools and Private School Vouchers: Consider a sim-ple model of how economic circumstances are changed when the government enters the education market.

A:Suppose a household has an after-tax income of \$50,000 and consider its bud-get constraint with "dollars of education services" on the horizontal axis and "dollars of other consumption" on the vertical. Begin by drawing the household's budget line (given that you can infer a price for each of the goods on the axes from the way these goods are defined) assuming that the household can buy any level of school spending on the private market.

Answer: The budget line in this case is straightforward and illustrated in panel
(a) of Exercise Graph 2.16 as the constraint labeled "private school constraint".


Exercise Graph 2.16 : (a) Public Schools; (b) Private School Voucher
(a) Now suppose the government uses its existing tax revenues to fund a pub-lic school at \$7,500 per pupil; i.e. it funds a school that anyone can at-tend for free and that provides $\$ 7,500$ in education services. Illustrate how this changes the choice set.(Hint: One additional point will appear in the choice set.)

Answer: Since public education is free (and paid for from existing tax rev-enues - i.e. no new taxes are imposed), it now becomes possible to con-sume a public school that offers $\$ 7,500$ of educational services while still consuming $\$ 50,000$ in other consumption. This adds an additional bun-dle to the choice set - the bundle $(7,500,50,000)$ denoted "public school bundle" in panel (a) of the graph.
(b) Continue to assume that private school services of any quantity could be purchased but only if the child does not attend public schools. Can you think of how the availability of free public schools might cause some chil-dren to receive more educational services than before they would in the ab-sence of public schools? Can you think of how some children might receive fewer educational services once public schools are introduced?

Answer: If a household purchased less than $\$ 7,500$ in education services for a child prior to the introduction of the public school, it seems likely that the household would jump at the opportunity to increase both con-sumption of other goods and consumption of education services by switch-ing to the public education bundle. At the same time, if a household pur-chased more than $\$ 7,500$ in education services prior to the introduction of public schools, it is plausible that this household will also switch to the public school bundle - because, while it would mean less eduction ser-vice for the child, it would also mean a large increase in other consump-tion. ( We will be able to be more precise once we introduce a model of tastes.)
(c) Now suppose the government allows an option: either a parent can send her child to the public school or she can take a voucher to a private school and use it for partial payment of private school tuition. Assume that the voucher is worth $\$ 7,500$ per year; i.e. it can be used to pay for up to $\$ 7,500$ in private school tuition. How does this change the budget constraint? Do you still think it is possible that some children will receive less education than they would if the government did not get involved at all (i.e. no public schools and no vouchers)?

Answer: The voucher becomes equivalent to cash so long as at least $\$ 7,500$ is spent on education services. This results in the budget constraint de-picted in panel (b) of Exercise Graph 2.16. Since one cannot use the voucher to increase other consumption beyond $\$ 50,000$, the voucher does not make any private consumption above $\$ 50,000$ possible. However, it does make it possible to consume any level of education service between 0 and $\$ 7,500$ without incurring any opportunity cost in terms of other consumption. Only once the full voucher is used and $\$ 7,500$ in education services have been bought will the household be giving up a dollar in other consumption for every additional dollar in education services.

It is easy to see how this will lead some parents to choose more education for their children (just as it was true that the introduction of the public school bundle gets some parents to increase the education services con-sumed by their children.) But the reverse no longer appears likely - if someone choses more than $\$ 7,500$ in education services in the absence of public schools and vouchers, the effective increase in household income implied by the voucher/public school combination makes it unlikely that such a household will reduce the education services given to her child. (Again, we will be able to be more precise once we introduce tastes and we will see that it would take unrealistic tastes for this to happen.)

B:Letting dollars of education services be denoted by $x_{1}$ and dollars of other consumption by $x_{2}$, formally define the choice set with just the public school (and a private school market) as well as the choice set with private school vouchers defined above.

Answer: The first choice set (in panel (a) of the graph) is formally defined as (C)

$$
\begin{equation*}
\left(x_{1}, x_{2}\right) \mathbf{R}_{+}^{2 \mid x_{2} \leq 50000-x_{1} \text { or }\left(x_{1}, x_{2}\right)=(7500,50000)^{\mathfrak{a}}, ~} \tag{2.16.i}
\end{equation*}
$$

while the introduction of vouchers changes the choice set to

$$
\left\{\left(x_{1}, x_{2}\right) \quad \mathbf{R}_{+}^{2} \left\lvert\, \begin{array}{cl}
x_{2}=50000 & \text { for } x_{1} \leq 7500 \text { and } \\
& x_{2}=57500-x_{1} \tag{2.16.ii}
\end{array}\right. \text { for } x_{1}>7500\right\} .
$$

## Exercise 2.17

Policy Application: Tax Deductions and Tax Credits: In the U.S. income tax code, a number of expenditures are "deductible". For most tax payers, the largest tax deduction comes from the portion of the income tax code that permits taxpayers to deduct home mortgage interest (on both a primary and a vacation home). This means that taxpayers who use this deduction do not have to pay income tax on the portion of their income that is spent on paying interest on their home mortgage(s). For purposes of this exercise, assume that the entire yearly price of housing is interest expense.

A: True or False: For someone whose marginal tax rate is $33 \%$, this means that the government is subsidizing roughly one third of his interest/house payments.

Answer: Consider someone who pays $\$ 10,000$ per year in mortgage interest. When this person deducts $\$ 10,000$, it means that he does not have to pay the $33 \%$ income tax on that amount. In other words, by deducting $\$ 10,000$ in mort-gage interest, the person reduces his tax obligation by $\$ 3,333.33$. Thus, the gov-ernment is returning 33 cents for every dollar in interest payments made - ef-fectively causing the opportunity cost of paying $\$ 1$ in home mortgage interest to be equal to 66.67 cents. So the statement is true.
(a) Consider a household with an income of $\$ 200,000$ who faces a tax rate of $40 \%$, and suppose the price of a square foot of housing is $\$ 50$ per year. With square footage of housing on the horizontal axis and other consumption on the vertical, illustrate this household's budget constraint with and with-out tax deductibility. (Assume in this and the remaining parts of the ques-tion that the tax rate cited for a household applies to all of that household's income.)

Answer: As just demonstrated, the tax deductibility of home mortgage interest lowers the price of owner-occupied housing, and it does so in proportion to the size of the marginal income tax rate one faces.


Exercise Graph 2.17: Tax Deductions versus Tax Credits

Panel (a) of Exercise Graph 2.17 illustrates this graphically for the case described in this part. With a 40 percent tax rate, the household could consume as much as $0.6(200,000)=120,000$ in other goods if it consumed no housing. With a price of housing of $\$ 50$ per square foot, the price falls to $(1-0.4) 50=30$ under tax deductibility. Thus, the budget rotates out to the solid budget in panel (a) of the graph. Without deductibility, the consumer pays $\$ 50$ per square foot - which makes $120,000 / 50=2,400$ the biggest possible house she can afford. But with deductibility, the biggest house she can afford is $120,000 / 30=4,000$ square feet.
(b) Repeat this for a household with income of $\$ 50,000$ who faces a tax rate of $10 \%$.

Answer: This is illustrated in panel (b). The household could consume as much as $\$ 45,000$ in other consumption after paying taxes, and the de-ductibility of house payments reduces the price of housing from $\$ 50$ per square foot to $(1-0.1) 50=$ $\$ 45$ per square foot. This results in the in-dicated rotation of the budget from the lower to the higher solid line in the graph. The rotation is smaller in magnitude because the impact of deductibility on the after-tax price of housing is smaller. Without de-ductibility, the biggest affordable house is $45,000 / 50=900$ square feet, while with deductibility the biggest possible house is $45,000 / 45=1,000$ square feet.
(c) An alternative way for the government to encourage home ownership would be to offer a tax credit instead of a tax deduction. A tax credit would allow all taxpayers to subtract a fraction $k$ of their annual mortgage payments directly from the tax bill they would otherwise owe. (Note: Be careful - a tax credit is deducted from tax payments that are due, not from the taxable income.) For the households in (a) and (b), illustrate how this alters their budget if $k=0.25$.

Answer: This is illustrated in the two panels of Exercise Graph 2.17 - in panel (a) for the higher income household, and in panel (b) for the lower income household. By subsidizing housing through a credit rather than a deduction, the government has reduced the price of housing by the same amount $(k)$ for everyone. In the case of deductibility, the government had made the price subsidy dependent on one's tax rate - with those facing higher tax rates also getting a higher subsidy. The price of housing how falls from $\$ 50$ to $(1-0.25) 50=\$ 37.50$ - which makes the largest affordable house for the wealthier household $120,000 / 37.5=3,200$ square feet and, for the poorer household, $45,000 / 37.5=1,200$ square feet. Thus, the poorer household benefits more from the credit when $k=0.25$ while the richer household benefits more from the deduction.
(d) Assuming that a tax deductibility program costs the same in lost tax rev-enues as a tax credit program, who would favor which program?

Answer: People facing higher marginal tax rates would favor the deductibil-ity program while people facing lower marginal tax rates would favor the tax credit.

B: Let $x_{1}$ and $x_{2}$ represent square feet of housing and other consumption, and let the price of a square foot of housing be denoted $p$.
(a) Suppose a household faces a tax rate t for all income, and suppose the en-tire annual house payment a household makes is deductible. What is the household's budget constraint?
Answer: The budget constraint would be $x_{2}=(1-t) I-(1-t) p x_{1}$.
(b) Now write down the budget constraint under a tax credit as described above. Answer: The budget constraint would now be $x_{2}=(1-t) I-(1-k) p x_{1}$.

## Preparing a Syllabus for the Course in Three Quick Steps

This textbooks clearly has far too much material for a one-semester course in microeconomics and in fact was written as a relatively comprehensive two-semester book. Part A in each chapter is non-mathematical but rigorous, written with an eye toward making the math that is added in part $B$ make sense. One decision you have to make is how much use you will make of A-parts versus B-parts. In some universities, students might be taking a second intermediate microeconomics course following a non-mathematical course earlier - in which case a heavy emphasis on the B-parts is clearly warranted. In other universities, microeconomics is taught across multiple semesters, with each semester containing an equal emphasis on math and intuition. In such cases, you will probably use both A and B parts but will restrict yourself to only half the topics in the text. (Which half will probably depend on whether you go first or sccond.) Or you might be in a university where you are teaching a relatively non-mathematical intermediate microeconomics course and you'll rely most heavily on just the A-parts. (If you wish to use none of the mathematical B-parts, you may want to use the non-mathematical spin-off book entitled Microeconomics: An Intuitive Approach.)

I'll say little more about the balance between the intuitive and math sections you are clearly in the best position to make that judgment. Instead, what follows is an outline for a threc-step process for constructing the syllabus - where the overall aim for a one-semester (or one-quarter course) should be to plan to cover roughly half the material (or a bit less) in the textbook. The three steps consist of:

1. Include all the foundational material on consumer theory, producer theory and competitive equilibrium - and decide which other topics that relate to this foundational material you want to add.
2. Choose a path through the second half of the book depending on your focus and the types of tools beyond the foundational tools you want your students to know.
3. Decide how to conclude the course.


Graph 0.1: Building the Consumer Model Portion of the Syllabus

## Step 1: Building Foundational Material into the Beginning of the Syllabus

The text begins with the consumer model, then proceeds to the producer model before putting them together to discuss competitive equilibrium

Graph 0.1 begins with a guide for constructing the Consumer Model Portion of the Syllabus. The shaded boxes represent material that is foundational - with solid arrows indicating the manner in which the material builds. The non-shaded boxes are optional in the sense that later material rarely if ever depends on it (and when it does, it is contained in small sub-sections that can be skipped). Dashed arrows indicate at what point these optional materials can be covered. Of course you can choose any point after that in the syllabus to cover these optional materials — the dashed arrows simply indicate the earliest that the students are prepared to tackle them. While the first two sections of the chapter on Risk (top left of the Graph) might, for instance, reasonably be covered early in the course, the general equilibrium section is probably best saved for after Chapter 15 (as is the Edgeworth Box material).

My own preference is to develop the worker/saver model (on the right hand side of Graph 0.1 ) jointly with the standard consumer model (in the center of the Graph) because all the same tools are used and students can therefore get a fecling for how we really are doing the same thing in all these cases, but this is a matter of preference. I also know that some instructors like to cover elasticities earlier than where they appear in the text, and this is possible as indicated in Graph 0.1


Graph 0.2: Building the Producer Model Portion of the Syllabus
(although my own preference is to cover elasticities right before I start using the concept extensively in Chapter 18).

Graph 0.2 presents a similar flow chart for the producer theory portion of the course (with the arrows this time pointing up). While in principle it might be possible to cover later material without going into two-input production (Chapter 12) at all, I doubt many instructors who adopt this book will opt for this - and I have therefore indicated Chapter 12 as foundational even though one could envision glancing over some of that material and still making it through much of the rest of the book. The optional sections of Chapter 13 take some time to develop, and I suspect that most instructors will opt to skip them. However, each of these sections (13.2 and 13.3) comes with an intuitive introductory section that could easily be incorporated without going into the detail that follows.


Graph 0.3: Building the Final Foundational Pieces of the Syllabus

The foundational elements of consumer theory (Graph 0.1) and producer theory (Graph 0.2) then combine to build up to the treatment of competitive equilibrium as illustrated in Graph 0.3. Chapter 14 describes the competitive partial equilibrium and Chapter 15 illustrates its welfare properties. These two chapters are, as indicated by the shading, foundational for the rest of the text. But you may wish to elaborate on them further by investigating the general equilibrium material in the next two chapters. These are not, however, foundational to the rest of the text, and you could, in principle, also cover them in the consumer theory section (see Graph 0.1), although my recommendation would be to hold off until after the partial equilibrium and its welfare properties have been developed.

## Step 2: Choosing a Path Following the Foundational Material in the Middle of the Syllabus

If you are teaching both the A- and B-parts of each of the chapters, you will probably have covered a semester's worth of material by the time you make it through the consumer theory (Graph 0.1 ), producer theory (Graph 0.2) and Competitive Equilibrium (Graph 0.3). Your syllabus should therefore be pretty much done, with perhaps one or two chapters from the second half of the book added.

For those teaching primarily the A- or the B-parts of the foundational material, a choice now has to be made as to which path to choose through the rest of the book. Even if you cover only the shaded core material in Graph 0.9 of the Appendix (which summarizes some of the previous flow charts), you probably do not have enough time to cover Chapters 18 through 30 in their entirety. Several obvious options emerge from Graph 0.10 which is the second flow chart in the Appendix (and which illustrates the various paths outlined below):

1. A Traditional Theory Focus without Game Theory would take you from Chapters 18 through 23 - covering all the major violations of the first welfare theorem without any formal use of game theory. This is illustrated in Graph 0.4 which would follow in your syllabus immediately after the choices you made in Graph 0.3.


Graph 0.4: Building No-Game-Theory-Path into the Syllabus
2. A Game Theory Focus could skip all but the first section of Chapter 18 through Chapter 22, introduce some initial strategic thinking in the context of Monopolies in Chapter 23 before covering Game Theory in Chapter 24. Note that the game theory chapter covers Nash and subgame perfect equilibrium in part A and the Bayesian analogs - Bayesian Nash and perfect Bayesian Nash equilibrium - in part B. The remainder of the game theory-based chapters, however, draw primarily on part A of Chapter 24, with the only sequenced chapters (indicated by the solid arrows in Graph 0.5) involving Chapters 24 and 25.


Graph 0.5 : Building a Heavy Game Theory Emphasis into the Syllabus
3. A Business or Industrial Organization (IO) Focus would share a lot in common with the game theory path outlined in Graph 0.5 but with some slight modifications outlined in Graph 0.6.


Graph 0.6: Building a Business or IO Emphasis into the Syllabus
4. Finally, a Policy Focus can take a variety of forms, depending primarily on whether you decide to cover game theory or not. If you do not, then the Policy Focus looks a lot like the No-Game-Theory Focus in Graph 0.4; otherwise, you have the flexibility to build in some game theory features by covering part A of Chapter 24 and then either some additional material on market power (Chapters 25 and/or 26) or on public goods and the free rider problem (Chapter 27). Thesc options are illustrated in Graph 0.7.


Graph 0.7: Options for a Policy Emphasis in the Syllabus

## Step 3: Choosing a Conclusion for the Syllabus

The last part to finishing up your syllabus is to simply choose how to conclude your course (with the understanding that the last few planned parts of a course often tend to be short-changed as we rush to finish up a semester). The options, laid out in Graph 0.8, include a chapter on Politics which, in my experience, students enjoy a great deal. (The best students - or those in a very mathematical course - are sometimes quite taken by part B, a proof of Arrow's Impossibility Theorem.) Chapter 29 covers normative issues in the first section before providing an overview to behavioral economics. Both these chapters have a way of emphasizing that economics is really about more than what students might think, and so they tend to open up horizons. The concluding Chapter 30 is very brief and simply tries to get back to the big picture theme flowing throughout the book. (I have tried to write this chapter, as well as the rest of the book, in a very non-idcological way - my hope is that you will find it laying out a way of thinking that can fit with a variety of ideological predisposition.)


Graph 0.8: Options for Concluding the Syllabus

## Appendix: Overview in Two Pages



Graph 0.9: Tools Building up to First Welfare Theorem


Graph 0.10: Exploring what Lies Beneath the First Welfare Theorem

## Microeconomics:

## An Intuitive Approach, 2E

## Chapter 2 -

## A Consumer's Economic Circumstances

## Consumer Choice Sets and Budget Constraints

## People make the best choices they can

 given their circumstances
## "Constraints"

- Current Income
- Assets (from Savings)
- Skills
- Time
- Future Income (for Borrowing)
- (Psychological - Ch. 29)


## Consumer Choice Sets and

 Budget Constraints- Consumers are "small", have no power over prices "price-takers"
- We begin by assuming that decisions leading to currently available income are in the past

The choice that remains is how to spend this available income

Such income that the consumer takes "as given" is called "exogenous"
© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or schoolapproved learning management system for classroom use.

## Consumer Choice Sets... Shopping on a Fixed (Exogenous) Income

- Suppose I have \$200 to spend on pants and shirts. (I can spend less, but never more).
- The price of pants is $\$ 20$ and the price of shirts is $\$ 10$.
- Given those restrictions, I can buy any "bundle" of pants and shirts that I want.
- The set of all "bundles" of shirts and pants that I could buy is then called my "Choice Set"


# Consumer Choice Sets Budget Constraint and Choice Set Shopping on a Fixed (Exogenous) Income 

Bundles of pants and shirts can then be represented as points in 2 dimensions with the number of pants read on the horizontal axis and the number of shirts on the vertical.

## Consumer Choice Sets Shopping on a Fixed (Exogenous) Income


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or

## Comisumereftdicaicetsets...Shopping on a Fixed (Exogenous) Income


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-

## Shopping on a Fixed (Exogenous) Income



## Comsumméniaic eefets-.. - 

Number


The slope of the budget line is -2 in our case. This is because I have to give up 2 shirts for every 1 pair of pants - because pants are twice as expensive as shirts.

More generally, this slope is equal to minus the price of the good on the horizontal divided by the price of the good on the vertical axis. It represents the opportunity cost of the good on the horizontal in terms of the good on the vertical.

The budget line together with the shaded area beneath it is known as the consumer's choice set. Bundles within this set (and below the line) (such as $E$ ) are affordable and leave the consumer with some money.

Number
Go to Math
© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or schoolapproved learning management system for classroom use.

© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-
approved learning management system for classroom use.

## Consumer Choice Sets.:. $=$ An Increase of Decrease in Eixed Incomes




[^0] for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-

## Consumer Choice Sets:a $=$ An Increase of Decrease in Eixed Incomes



Go to Math

## Consumer Choice Sets...A Change in Price



# Consumer Choice Sets...A Change in Price 


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-
approved learning management system for classroom use.

## Consumer Choice Sets...A Change in Price


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-
approved learning management system for classroom use.

## Consumer Choice Sets...A Change in Price


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.


## Consumer Cholce Sets... $=$ Kinky 見udgets


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-
approved learning management system for classroom use.

© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.

## 

## Kinky Budgets



© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-


[^1]
## Consumer Choice Sets... Kinky Budgets



Discuss
Convexity
© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.


Suppose now that, in addition to shirts and pants, we have a third good we can choose: Socks.

We begin with our previous space of bundles consisting of two goods (shirts and pants.)

## Modeling More General ChoicesChoice Sets with Three Goods



The introduction of socks then adds a third dimension - because bundles of goods now consist of three numbers: one for pants, one

With our income of $\$ 200$ a $\$ 20$ price for pants, and a \$10 price for shirts, we can buy at most 10 pants (point A) and at most 20 shirts (point $B$ ).

And if we suppose that the price of socks is $\$ 5$, we can buy at most 40 socks (if we buy nothing else). That gives us point $C$ on the socks axis.


## Modeling More General ChoicesChoice Sets with Three Goods



We similarly get the 2dimensional budget constraint assuming there are no pants when we connect $B$ and $C$.

This gives all the bundles of shirts and socks that exhaust our \$200 exogenous income.


And, when we connect $A$ and $C$, we get the 2 dimensional budget constraint assuming there are no shirts and all we are choosing is bundles of pants and socks.


When we then fill in the plane that connects the three 2-dimensional budget lines we have drawn, we get the 3dimensional budget constraints over pants, shirts and socks.

The bundles that lie on or below this plane then constitute the choice set for this consumer.

[^2] for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-


One bundle that lies on the budget constraint, for instance, is bundle $D$. This bundle contains 5 pants, 5 shirts and 10 socks.

The 5 pants cost $\$ 100$ (at $\$ 20$ each), the 5 shirts cost \$50 (at \$10 each), and the 10 socks cost $\$ 50$ (at \$5 each). Thus, bundle D costs $\$ 200$.

## Modeling More General ChoicesModeling CompositeCompositeGoods Goods

- But if we have more than 3 goods, it becomes impossible to graph the budget constraint.
- We thus often use the trick of aggregating all goods except for one into a "composite good".
- A composite good is an index of "dollars worth of all other goods", with the price of a composite good therefore equal to 1.
- When a composite good is put on the vertical axis, the slope of the budget is then simply (minus) the price of the good on the horizontal.

Consumer Choice Sets... -


## Consumer Choice Sets <br> Incomes Arising from Endowments



## Consumer Choice Sets... ... Incomes Arising from Endowments

## Incomes Arising from Endowments


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-

## Consumer Choice Sets...Incomes Arising from Endowments



## Budget Math

Bundles of pants and shirts can be represented as

$$
\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2}
$$

where $x_{1}$ represents the number of pants and $x_{2}$ represents the number of shirts.

The symbol $\in$ stands for "is an element of" ...
... and the symbol $\mathbb{R}_{+}^{2}$ stands for the positive quadrant of 2-dimensional space

## Budget Math



## Budget Math


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-

## Andgetedalstin Exogenous Income



© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or schoolapproved learning management system for classroom use.

## KidlekiceudgatsPrice



## Back to Graphs

© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part,
except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or
school-approved learning management system for classroom use.

© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.


## Non-Convex and Convex Sets



## Dlonirceoserexvaitd Tbnaex


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or schoolapproved learning management system for classroom use.

The budget line equation $p_{1} x_{1}+p_{2} x_{2}=I$ extends straightforwardly to 3 goods, with expenditure on the third good $\left(p_{3} x_{3}\right)$ simply added to the right hand side to give us

$$
p_{1} x_{1}+p_{2} x_{2}+p_{3} x_{3}=I
$$

with the corresponding choice set defined as

$$
C\left(p_{1}, p_{2}, p_{3}, I\right)=\left\{\left(x_{1}, x_{2}, x_{3}\right) \in \mathbb{R}_{+}^{3} \mid p_{1} x_{1}+p_{2} x_{2}+p_{3} x_{3} \leq I\right\}
$$

And if furthermore extends to the $n$-good case, with a budget line of

$$
p_{1} x_{1}+p_{2} x_{2}+\ldots+p_{n} x_{n}=I
$$

and corresponding choice set

$$
C\left(p_{1}, p_{2}, \ldots, p_{n}, I\right)=\left\{\left(x_{1}, x_{2}, \ldots, x_{n}\right) \in \mathbb{R}_{+}^{n} \mid p_{1} x_{1}+p_{2} x_{2}+\ldots+p_{n} x_{n} \leq I\right\}
$$

## Elooiceosifexvaith Cbnevergsetds

© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.

## Composite Goods

When we are primarily interested in one of $n$ goods that a person consumes, we often model that good as $x_{1}$ and aggregate the remaining ( $n-1$ ) goods into a composite good $\left(x_{2}\right)$ defined as "dollars worth of other consumption".

Since a "dollar's worth of other consumption" costs by definition \$1, we can then simply set the price of the composite good to $p_{2}=1$ and write the budget equation as

$$
p_{1} x_{1}+x_{2}=I
$$

Solving this for $x_{2}$, we get the budget line

$$
x_{2}=I-p_{1} x_{1}
$$

with intercept $I$ and slope $-p_{1}$.
Back to Graphs

## Endowments


© 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-approved learning management system for classroom use.

## $2 B$

## Consumer Choice Sets \& Budget Equations

- For ease of understanding, refer to the A section of the text for each topic
- 2B. 1 Shopping on a Fixed Income
- Choice set: pants \& shirts at Walmart
- 2B.1.1 Defining Choice Sets \& Budget Lines Mathematically
- If pants are denoted by variable $x_{1}$, and shorts by $x_{2}$, we can define the choice set formally as:

$$
\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid 20 x_{1}+10 x_{2} \leq 200\right\} .
$$

## 2B. 1 Shopping on a Fixed Income

## 2B.1.1 Defining Choice Sets... Mathematically

- We can define the budget line as the set of bundles that lie on the boundary of the choice set:

$$
\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid 20 x_{1}+10 x_{2}=200\right\} .
$$

- If the price of pants is $p_{1}$, the price of shirts $p_{2}$, and income as I, we define a consumer's choice set $C$ as:

$$
C\left(p_{1}, p_{2}, I\right)=\left\{\left(x_{1}, x_{2}\right) \in \mathbf{R}_{+}^{2} \mid p_{1} x_{1}+p_{2} x_{2} \leq I\right\} .
$$

- We can define budget line $B$ as:

$$
B\left(p_{1}, p_{2}, I\right)=\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid p_{1} x_{1}+p_{2} x_{2}=I\right\},
$$

- Subtract $p_{1} x_{1}$ from both sides and divide both by $p_{2}$ :

$$
x_{2}=\frac{I}{p_{2}}-\frac{p_{1}}{p_{2}} x_{1}
$$

## 2B. 1 Shopping on a Fixed Income

## 2B.1.2 An Increase (or Decrease) in Fixed Income

- When fixed income changes, only the first term $m_{2}$ in equation 2.5 changes; the second term remains the same
- The choice set has become larger, but the tradeoff between goods remains the same


## 2B.1.3 A Change in Price

- A 50\% coupon effectively lowers the price of pants from \$20 to \$10
- In equation 2.5, $p_{1}$ does not appear in the intercept term, but does appear in the slope term
- The $x_{2}$-axis intercept remains unchanged $\left(I / p_{2}\right)$, but the slope becomes shallower as $p_{1} / p_{2}$ becomes smaller


## 2B. 3 Kinky Budgets Choice sets witngitre Than Two Goods

## 2B. 2 Kinky Budgets

- Kinked budget lines are more difficult to describe mathematically
- Consider the $50 \%$ off coupon for the first 6 pairs of pants
- We could define the choice set as:

$$
\begin{aligned}
C\left(p_{1}, p_{2}, I\right)=\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid 0.5 p_{1} x_{1}+p_{2} x_{2}\right. & \leq I \text { for } x_{1} \leq 6 \text { and } \\
p_{1} x_{1}+p_{2} x_{2} & \left.\leq I+3 p_{1} \text { for } x_{1}>6\right\} .
\end{aligned}
$$

- Graph 2.4a:

$$
\begin{aligned}
B\left(p_{1}, p_{2}, l\right)=\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid 0.5 p_{1} x_{1}+p_{2} x_{2}\right. & =I \text { for } x_{1} \leq 6 \text { and } \\
p_{1} x_{1}+p_{2} x_{2} & \left.=I+3 p_{1} \text { for } x_{1}>6\right\} .
\end{aligned}
$$

## 3B.3 Kinky Bydgets <br> Choice Sets withenore Than Two Goods

## 2B. 3 Choice Sets with More Than Two Goods

- We can mathematically formulate the choice sets, or treat the goods as a composite good


## 2B.3.1 Choice Sets with 3 or More Goods

- The choice set is $C\left(p_{1}, p_{2}, p_{3}, l\right)=\left\{\left(x_{1}, x_{2}, x_{3}\right) \in \mathbb{R}_{+}^{3} \mid p_{1} x_{1}+p_{2} x_{2}+p_{3} x_{3} \leq I\right\}$, with the corresponding budget constraint defined by:

$$
B\left(p_{1}, p_{2}, p_{3}, I\right)=\left\{\left(x_{1}, x_{2}, x_{3}\right) \in \mathbb{R}_{+}^{3} \mid p_{1} x_{1}+p_{2} x_{2}+p_{3} x_{3}=I\right\} .
$$

- For the general case of $n$ different goods with $n$ different prices, we would extend 2.8 and 2.9 to

$$
C\left(p_{1}, p_{2}, \ldots, p_{n}, I\right)=\left\{\left(x_{1}, x_{2}, \ldots, x_{n}\right) \in \mathbb{R}_{+}^{n} \mid p_{1} x_{1}+p_{2} x_{2}+\ldots+p_{\pi} x_{n} \leq I\right\},
$$

and

$$
B\left(p_{1}, p_{2}, \ldots, p_{n}, I\right)=\left\{\left(x_{1}, x_{2}, \ldots, x_{n}\right) \in \mathbb{R}_{+}^{n} \mid p_{1} x_{1}+p_{2} x_{2}+\ldots+p_{\pi} x_{n}=l\right\} .
$$

## 2 B. 4

## Choice Sets That Arise from Endowments

- Sometimes, money that can be devoted to consumption is not exogenous, but arises endogenously from the decisions a consumer makes and the prices she faces in the market
- In Section 2A.4, I returned to Walmart with 10 shirts and 5 pants to get a store credit at the current price
- My income can be expressed as $I=5 p_{1}+10 p_{2}$.
- My choice set is then composed of all combinations of pants and shirts such that my total spending is no more than this income level $C\left(p_{1}, p_{2}\right)=\left\{\left(x_{1}, x_{2}\right) \in \mathbb{R}_{+}^{2} \mid p_{1} x_{1}+p_{2} x_{2} \leq 5 p_{1}+10 p_{2}\right\}$.
- When the inequality in (2.15) is replaced with an equality to get the equation for the budget line, we get

$$
p_{1} x_{1}+p_{2} x_{2}=5 p_{1}+10 p_{2} .
$$

## 2 B .4

## Choice Sets That Arise from Endowments

- Subtracting $p_{1} x_{1}$ from both sides and dividing both by $p_{2}$, this turns into $x_{2}=5 \frac{p_{1}}{n_{2}}+10-\frac{p_{1}}{n_{2}} x_{1}$.
- Graph 2.6, we plotted this budget set for the case where Walmart was charging $\$ 10$ for both shirts and pants. When these prices are plugged into equation (2.17), we get

$$
x_{2}=15-x_{1},
$$

- We can denote someone's endowment as the number of goods of each kind a consumer has as he enters Walmart
- If my endowment of good 1 is e1, and my endowment of good 2 is e2, we can define my choice set as a function of my endowment and the prices of the two goods

$$
C\left(p_{1}, p_{2}, e_{1}, e_{2}\right)=\left\{\left(x_{1}, x_{2}\right) \mid p_{1} x_{1}+p_{2} x_{2} \leq p_{1} e_{1}+p_{2} e_{2}\right\},
$$


[^0]:    © 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except

[^1]:    © 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except for use as permitted in a license distributed with a certain product or service or otherwise on a password-protected website or school-

[^2]:    © 2017 Cengage Learning ${ }^{\circledR}$ May not be scanned, copied or duplicated, or posted to a publicly accessible website, in whole or in part, except

