

**Solution Manual for Separation Process Engineering Includes Mass
Transfer Analysis 4th Edition Wankat 0133443655 9780133443653**

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Solution Manual:

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New Problems and new solutions are listed as new immediately after the solution number. These new problems are: 2A8, 2A10 parts c-e, 2A11, 2A12, 2A13, 2A14, 2C4, 2D1-part g, 2D3, 2D6, 2D7, 2D11, 2D13, 2D14, 2D20, 2D22, 2D23, 2D31, 2D32, 2E3, 2F4, 2G2, 2G3, 2H1, 2H3, 2H4, 2H5 and 2H6.

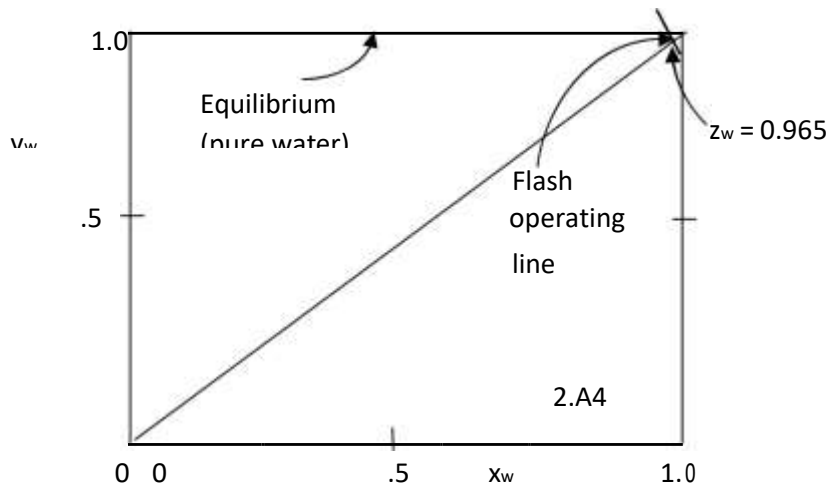
2.A1. Feed to flash drum is a liquid at high pressure. At this pressure its enthalpy can be calculated as a liquid. eg. $h_{T_F, P_{high}} = c_{p, LIQ} (T_F - T_{ref})$. When pressure is dropped the mixture is above

its bubble point and is a two-phase mixture (It “flashes”). In the flash mixture enthalpy is unchanged but temperature changes. Feed location cannot be found from T_F and z on the graph because equilibrium data is at a lower pressure on the graph used for this calculation.

2.A2. Yes.

2.A3. The liquid is superheated when the pressure drops, and the energy comes from the amount of superheat.

2.A4.



2.A6. In a flash drum separating a multicomponent mixture, raising the pressure will:

- i. Decrease the drum diameter and decrease the relative volatilities. *Answer is i.*

2.A8. *New Problem in 4th ed.*

- a. At 100°C and a pressure of 200 kPa what is the K value of n-hexane? 0.29
- b. As the pressure increases, the K value
 - a. increases, b. decreases, c. stays constant
- c. Within a homologous series such as light hydrocarbons as the molecular weight increases, the K value (at constant pressure and temperature)
 - a. increases, b. decreases, c. stays constant
- d. At what pressure does pure propane boil at a temperature of -30°C? 160 kPa

- 2.A9. a. The answer is 3.5 to 3.6
 b. The answer is 36°C
 c. This part is new in 4th ed. 102°C

2.A10. Parts c, d, and e are new in 4th ed. a. 0.22; b. No; c. From y-x plot for Methanol $x = 0.65$, $y_M = 0.85$; thus, $y_w = 0.15$. d. $K_M = 0.579/0.2 = 2.895$, $K_w = (1 - 0.579)/(1 - 0.2) = 0.52625$. e. $\alpha_{M-w} = K_M/K_w = 2.895/0.52625 = 5.501$.

2.A11. New problem in 4th edition. Because of the presence of air this is not a binary system. Also, it is not at equilibrium.

2.A12. New problem in 4th edition. The entire system design includes extensive variables and intensive variables necessary to solve mass and energy balances. Gibbs phase rule refers only to the intensive variables needed to set equilibrium conditions.

2A13. New problem in 4th edition. Although V is an extensive variable, V/F is an intensive variable and thus satisfies Gibbs phase rule.

2A14. New problem in 4th edition. $1.0 \text{ kg/cm}^2 = 0.980665 \text{ bar} = 0.96784 \text{ atm}$.

Source: <http://www.unit-conversion.info/pressure.html>

2.B1. Must be sure you don't violate Gibbs phase rule for intensive variables in equilibrium.

Examples:

$F, Z, T_{\text{drum}}, P_{\text{drum}}$	F, T_F, z, p	F, h_F, z, p
F, Z, y, P_{drum}	F, T_F, z, y	F, h_F, z, y
F, Z, x, p_{drum}	F, T_F, z, x	etc.
F, Z, y, p_{drum}	$F, T_F, z, T_{\text{drum}}, p_{\text{drum}}$	
F, Z, x, T_{drum}	F, T_F, y, p	
Drum dimensions, $z, F_{\text{drum}}, p_{\text{drum}}$	$F, T_F, y, T_{\text{drum}}$	
Drum dimensions, z, y, p_{drum}	F, T_F, x, p	
etc.	$F, T_F, x, T_{\text{drum}}$	
	F, T_F, y, x	

2.B2. This is essentially the same problem (disguised) as problem 2-D1c and e but with an existing (larger) drum and a higher flow rate.

With $y = 0.58$, $x = 0.20$, and $V/F = 0.25$ which corresponds to 2-D1c.

If $F = 1000 \frac{\text{lb mole}}{\text{hr}}$, $D = .98$ and $L = 2.95$ ft from Problem 2-D1e.

Since $D \propto \sqrt{V}$ and for constant V/F , $V \propto F$, we have $D \propto \sqrt{F}$.

With $F = 25,000$:

$$\sqrt{F_{\text{new}}/F_{\text{old}}} = 5, D_{\text{new}} = 5 D_{\text{old}} = 4.90, \text{ and } L_{\text{new}} = 3 D_{\text{new}} = 14.7.$$

Existing drum is too small.

Feed rate drum can handle:

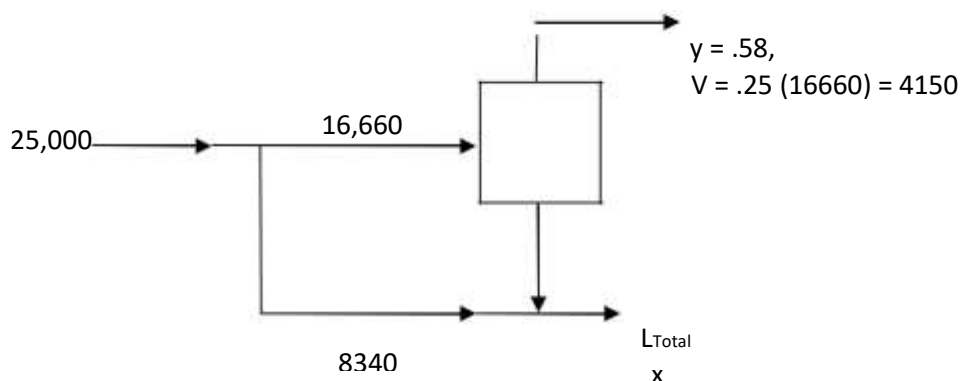
$$F \propto D^2$$

$$\frac{F_{\text{existing}}}{1000} = \frac{D_{\text{exist}}^2}{.98^2} \quad \text{gives}$$

$$F_{\text{existing}} = 16,660 \text{ lbmol/h}$$

Alternatives

- Do drums in parallel. Add a second drum which can handle remaining 8340 lbmol/h.
- Bypass with liquid mixing



Since x is not specified, use bypass. This produces less vapor.

- Look at Eq. (2-62), which becomes

$$D = \sqrt{\frac{V MW_v}{3K_{\text{drum}} 3600 L_v v}}$$

Bypass reduces V

- K_{drum} is already 0.35. Perhaps small improvements can be made with a better demister → Talk to the manufacturers.
- ρ_v can be increased by increasing pressure. Thus operate at higher pressure. Note this will change the equilibrium data and raise temperature. Thus a complete new calculation needs to be done.
- Try bypass with vapor mixing.
- Other alternatives are possible.

2.C2.

$$\frac{V}{F} = \frac{z_A}{K_B - 1} + \frac{z_B}{K_A - 1}$$

$$X = \frac{F z_i}{L}$$

2.C5. a. Start with

$$L = V K_i \quad \text{and let } V = F L$$

$$x_i = \frac{F z_i}{L F L K_i} \quad \text{or } x_i = \frac{z_i}{L K_i}$$

$$\text{Then } y_i = K_i x_i \frac{\frac{K_i z_i}{L - 1} - \frac{L}{F}}{\frac{K_i z_i}{L - 1} - \frac{L}{F}}$$

$$\text{From } y_i x_i = z_i \text{ we obtain } \frac{\frac{K_i z_i}{L - 1} - \frac{L}{F}}{\frac{K_i z_i}{L - 1} - \frac{L}{F}} z_i = z_i$$

2.C4. *New Problem.* Prove that the intersection of the operating and $y = x$ lines for binary flash distillation occurs at the mole fraction of the feed.

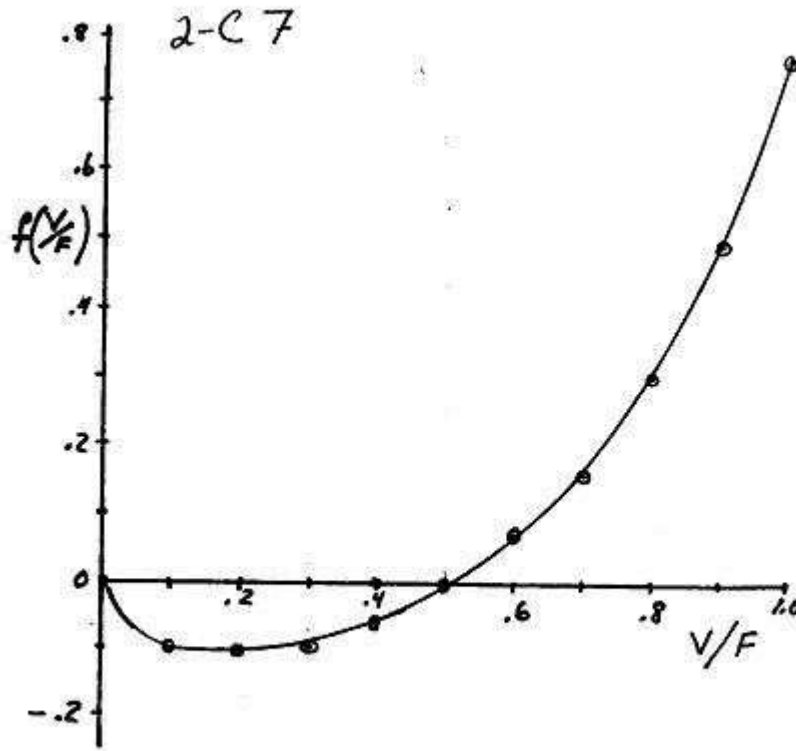
SOLUTION: $y = \frac{L}{V} y + \frac{F}{V} z$, rearrange: $y(1 - \frac{L}{V}) = \frac{F}{V} z$, or $y = \frac{V - L}{V} \frac{F}{F} z$ since $V + L = F$, the result is $y = z$ and

therefore $x = y = z$ (2-18)

The intersection is at the feed composition.

2.C7. $\frac{z_i}{K_i} \frac{V - L}{F} = z_i$ From data in Example 2-2 obtain:

V/F	0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
f	0	-.09	-.1	-.09	-.06	-.007	.07	.16	.3	.49	.77



2.C8. Derivation of Eqs. (2-62) and (2-63). Overall and component mass balances are,

$F = V$, $L_1 = L_2$ and $Fz_i = L_1 x_{i,L1} = L_2 x_{i,L2} = Vy_i$. Substituting in Eqs. (2-60b) and 2-60c)

$$Fz_i = L_1 K_{i,L1} x_{i,L1} = L_2 K_{i,L2} x_{i,L2} = VK_{i,L2} x_{i,L2}$$

Solving,

$$x_{i,L2} = \frac{Fz_i}{L_2 K_{i,L2} + VK_{i,L2}} = \frac{Fz_i}{L_1 K_{i,L1} + FV L_1 + VK_{i,L2}}$$

Dividing numerator and denominator by F and collecting terms.

$$x_{i,L2} = \frac{z_i}{1 + \frac{L_1}{F} K_{i,L1} + K_{i,L2} + \frac{V}{F} K_{i,L2}}$$

Since $x_{i,L2} = \frac{K_{i,L2} z_i}{L_1 K_{i,L1} + FV L_1 + VK_{i,L2}}$,

Stoichiometric equations, $x_{i,L2} = 1$, $y_i = 1$, thus, $y_i x_{i,L2} = 0$

which becomes (2-62)

$$0 = 1 + \frac{L_1}{F} K_{i,L1} + K_{i,L2} + \frac{V}{F} K_{i,L2}$$

Since $x_{i,L1} = \frac{K_{i,L1} z_i}{L_1 K_{i,L1} + FV L_1 + VK_{i,L2}}$, we have $x_{i,L1} = \frac{K_{i,L1} z_i}{L_1 K_{i,L1} + FV L_1 + VK_{i,L2}}$

$$1 + \frac{L_1}{F} K_{i,L1} + K_{i,L2} + \frac{V}{F} K_{i,L2}$$

In addition, $x_{i,L1} x_{i,L2} = 0$ (2-63)

$$0 = 1 + \frac{L_1}{F} K_{i,L1} + K_{i,L2} + \frac{V}{F} K_{i,L2}$$

2.D1. a. $V = 0.4 \times 100 = 40$ and $L = F + V = 60$ kmol/h

Slope op. line $L/V = 3/2$, $y = x + z = 0.6$

See graph. $y = 0.77$ and $x = 0.48$

b. $V = 0.4$, $1500 = 600$ and $L = 900$. Rest same as part a.

c. Plot $x = 0.2$ on equil. Diagram and $y = x + z = 0.3$. y_{int} except $z = F/V = 1.2$, $V/F = z/1.2 = 0.25$. From equil $y = 0.58$.

d. Plot $x = 0.45$ on equilibrium curve.

$$\text{Slope} = \frac{L}{V} = \frac{F \cdot V}{V} = \frac{1 \cdot V \cdot F}{V \cdot F} = \frac{.8}{.2} = 4$$

Plot operating line, $y = x = z$ at $z = 0.51$. From mass balance $F = 37.5 \text{ kmol/h}$.
 e. Find Liquid Density.

$$\overline{MW}_L = x_m \overline{MW}_m + x_w \overline{MW}_w = .2(32.04) + .8(18.01) = 20.82$$

$$\text{Then, } \overline{V}_L = x_m \frac{\overline{MW}_m}{\rho_m} + x_w \frac{\overline{MW}_w}{\rho_w} = .2 \frac{32.04}{.7914} + .8 \frac{18.01}{1.00} = 22.51 \text{ ml/mol}$$

$$\rho_L = \frac{\overline{MW}_L}{\overline{V}_L} = \frac{20.82}{22.51} = 0.925 \text{ g/ml}$$

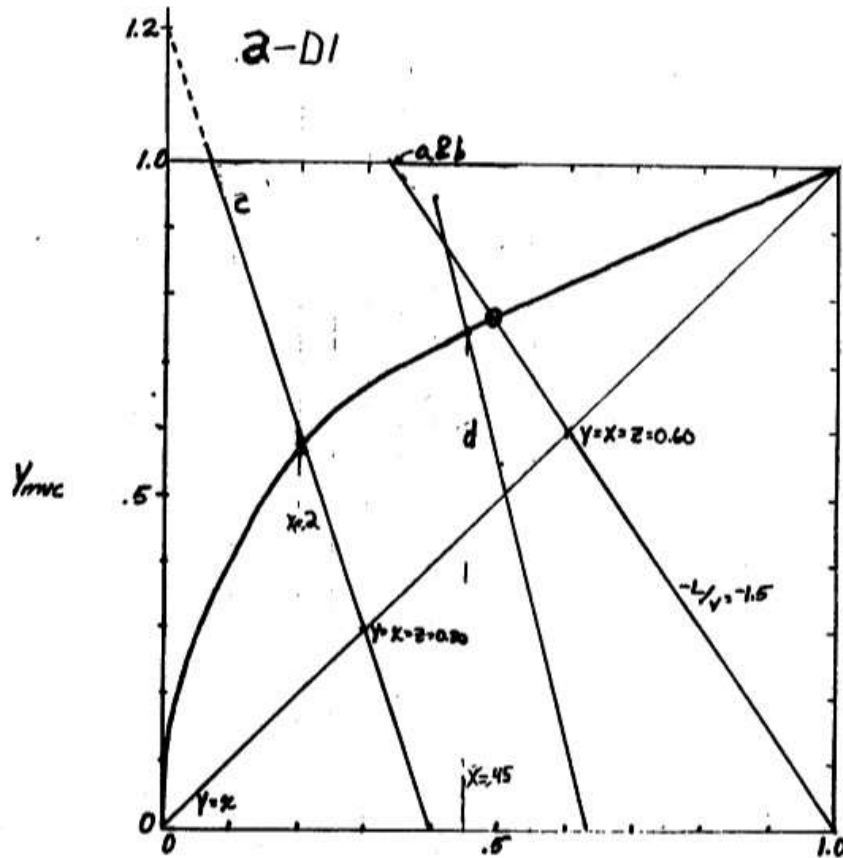
Vapor Density: $\rho_v = p(\overline{MW})_v / RT$ (Need temperature of the drum)

$$\overline{MW}_v = y_m \overline{MW}_m + y_w \overline{MW}_w = .58(32.04) + .42(18.01) = 26.15 \text{ g/mol}$$

Find Temperature of the Drum T : From Table 3-3 find T when

$$y = .58, x = .20, T = 81.7 \text{ C} = 354.7 \text{ K}$$

$$\rho_v = \frac{1 \text{ atm} \cdot 26.15 \text{ g/mol}}{82.0575 \frac{\text{ml atm}}{\text{mol K}} \cdot 354.7 \text{ K}} = 0.0091 \text{ g/ml}$$



Find Permissible velocity:

$$u_{perm} = \frac{K}{\sqrt{V}} \sqrt{\frac{W_v}{V} \exp \left[\frac{A}{B} \left(\frac{C}{n_{F_{IV}}} \right)^2 + \frac{D}{n_{F_{IV}}} + \frac{E}{n_{F_{IV}}} \right]} \quad 2-60$$

$$V = \frac{V}{F} = \frac{0.25 \cdot 1000 \cdot 250 \text{ lbmol/h}}{W_v} = \frac{V \cdot \overline{MW}_v}{250 \cdot 26.15 \text{ lbmol}} = 6537.5 \text{ lb/h}$$

$$L = F \cdot V = 1000 \cdot 250 = 750 \text{ lbmol/h, and } W_L = L \cdot \overline{MW}_L = 750 \cdot 20.82 = 15,615 \text{ lb/h,}$$

$$F_{lv} \frac{W}{W_V} \sqrt{\frac{L}{L}} \frac{15615}{6537.5} \frac{8.89 \cdot 10^4}{.925} = 0.0744, \text{ and } n F_{lv} = 2.598$$

Then $K_{drum} = .442$, and $u_{perm} = .442 \sqrt{\frac{.925 \cdot 8.98 \cdot 10^4}{8.98 \cdot 10^4}} = 14.19 \text{ ft/s}$

$$A_{cs} = \frac{V \cdot MW_v}{250 \cdot 26.15 \cdot 454 \text{ g/lb}} = 2.28 \text{ ft}^2$$

$$u_{perm} = 3600 \cdot v = 14.19 \cdot 3600 \cdot 8.98 \cdot 10^4 \text{ g/ml} = 28316.85 \text{ ml/ft}^3$$

D $4 \sqrt{A_{cs}} = 1.705 \text{ ft}$. Use 2 ft diameter. L ranges from 3 D = 6 ft to 5 D = 10 ft. Note that this design is conservative if a demister is used.

f. Plot T vs x from Table 3-3. When T = 77 C, x = 0.34, y = 0.69. This problem is now very similar to 3-D1c. Can calculate V/F from mass balance, $Fz = Lx = Vy$. This is

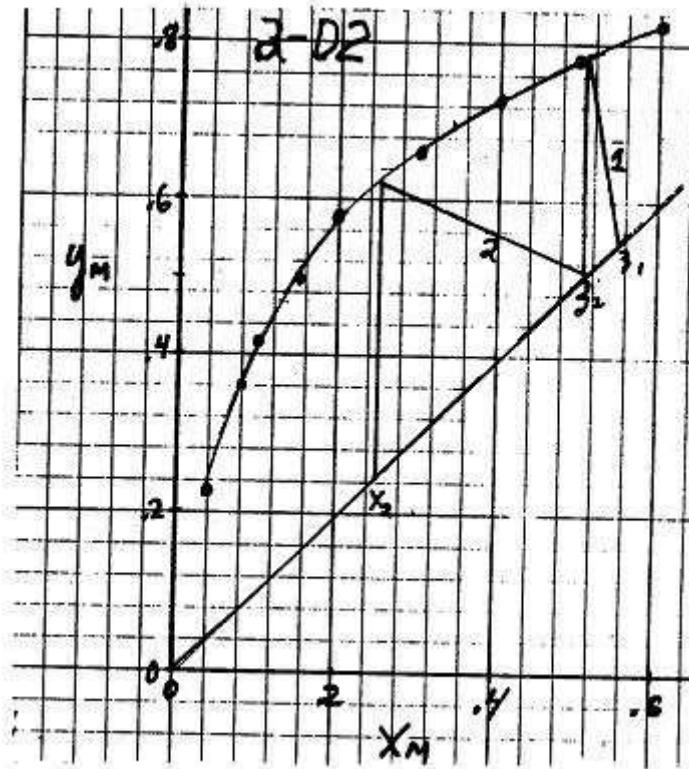
$$Fz = F V x = Vy \text{ or } \frac{V}{F} = \frac{z y}{y x} = \frac{0.4 \cdot 0.34}{0.69 \cdot 0.34} = 0.17$$

g. Part g is a new problem. V = 16.18 mol/h, L = 33.82, y = 0.892, x = 0.756.

2-D2. Work backwards. Starting with x_2 , find $y_2 = 0.62$ from equilibrium. From equilibrium point

plot op. line of slope $\frac{L}{V} = 2.1$ $\frac{V}{F} = 0.17$ $\frac{V}{F} = \frac{z_1 - x_1}{y_1 - x_1} = 3.7$ Find $z_2 = 0.51$ x_1 (see

Figure). From equilibrium, $y = 0.78$. For stage 1, $\frac{V}{F} = \frac{z_1 - x_1}{y_1 - x_1} = \frac{0.55 - 0.51}{0.78 - 0.51} = 0.148$.



2.D3. *New Problem in 4th edition.. Part a.*

x ethane	T °C	y ethane
0	63.19	0
.025	56.18	0.1610
.05	49.57	0.2970
.10	37.57	0.5060
.15	27.17	0.6503
.20	18.26	0.7492
.25	10.64	0.8175
.30	4.11	0.8652
1.0	-37.47	1.0

b. See Figure. a. If 1 bubble of vapor product ($V/F = 0$) vapor product, vapor $y_E = 0.7492$ (highest) liquid $x_E = z_E = 0.20$ (highest) and $T = 18.26$ °C. If 1 drop of liquid product ($V/F = 1$) $y_E = z_E = 0.20$ (lowest), $x_E = 0.035$, T (by linear interpolation) $\sim 56.18 + [(49.57 - 56.18)/(0.297 - 0.161)][0.2 - 0.16] = 54.2$ °C (highest).

c. See figure. Slope = $-L/V = -(1 - V/F)/(V/F) = -0.6/0.4 = -1.5$. $x_E = 0.12$, $y_E = 0.57$, $T = 33.4$ °C. **d.** From equilibrium data $y_E = 0.7492$. For an $F = 1$, $L = 1 - V$, Ethane balance: $0.2L = 1(0.3) - 0.7492V$. Solve 2 equations: $V/F = 0.1821$. Can also find V/F from slope of operating line.

e. If do linear interpolation on equilibrium data, $x = 0.05 + (45 - 49.57)(0.1 - 0.05)/(37.57 - 49.57) = 0.069$. From equilibrium plot $y = 0.375$.

Mass balance for basis $F = 1$, $L = 1 - V$ and $0.069L = 0.18 - 0.375V$. Solve simultaneously, $V/F = 0.363$.

2.D4. *New problem in 3rd edition.* Highest temperature is dew point $V/F = 0$

$$\text{Set } z_i = y_i \cdot \frac{K_i}{K_{ref}^{New}} \quad \text{Want } x_i = y_i \cdot \frac{K_i}{K_{ref}^{Old}} \quad \text{K}_i = 1.0$$

If pick C4 as reference: First guess $\text{butane} = 1.0$, $T = 41$ °C : $K_{C3} = 3.1, K_{C6} = 0.125$

$$\frac{y_i}{K_i} = \frac{0.2}{3.1} - \frac{0.35}{1.0} - \frac{0.45}{0.125} = 4.0145 \quad T \text{ too low}$$

Guess for reference: $K_{C4} = 4.014$, $T = 118$ °C : $K_{C3} = 8.8, K_{C6} = 0.9$

$$\frac{y_i}{K_i} = \frac{0.2}{8.8} - \frac{0.35}{4.0145} - \frac{0.45}{0.9} = 0.6099$$

$$K_{C4,NEW} = 4.0145 \cdot 0.6099 = 2.45, T = 85 : K_{C2} = 6.0, K_{C6} = 0.44$$

$$\frac{y_i}{K_i} = \frac{.2 \cdot .35 \cdot .45}{2.45 \cdot .44} = 1.20 K_i$$

$$K_{C4,NEW} = 2.45 \cdot 1.2 = 2.94, T = 96^\circ C : K_{C3} = 6.9, K_{C6} = 0.56$$

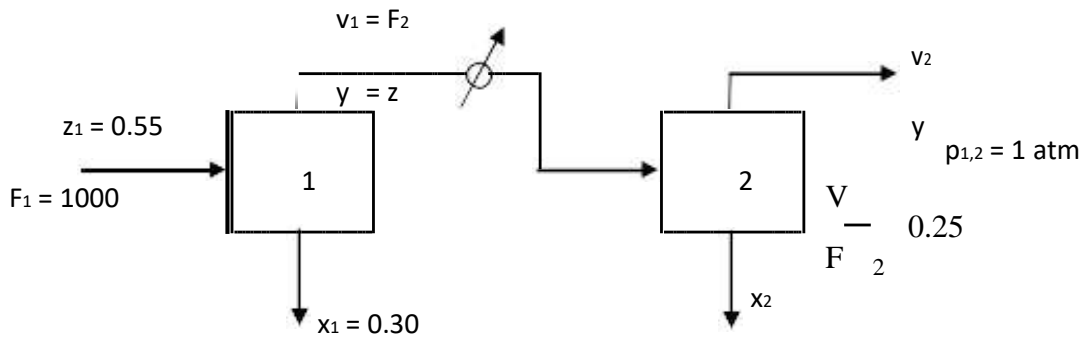
$$\frac{y_i}{K_i} = \frac{.2 \cdot .35 \cdot .45}{2.94 \cdot .56} = 0.804 \text{ Gives } 84^\circ C K_i$$

Use $90.5^\circ \rightarrow$ Avg last two T $K_{C4} = 2.7, K_{C3} = 6.5, K_{C6} = 0.49$

$$y_i/K_i = \frac{.2 \cdot .35 \cdot .45}{6.5 \cdot 2.7 \cdot .49} = 1.079, T \sim 87-88^\circ C$$

Note: hexane probably better choice as reference.

2.D5. a)



b) $y_{iV} = \frac{L}{V} x_i + \frac{F}{V} z$ Plot 1 Op line.

$$y_1 = 0.66 = z_2$$

$y = x = z = 0.55$ to $x_1 = 0.3$ on eq. curve (see graph)

$$\text{Slope} = \frac{L}{V} = \frac{0.55 - 0.80}{.55 - 0} = \frac{.25}{.55} = 0.454545 \frac{L}{V} \quad F = 1000$$

$$V_1 = 687.5 \text{ kmol/h} = F_2$$

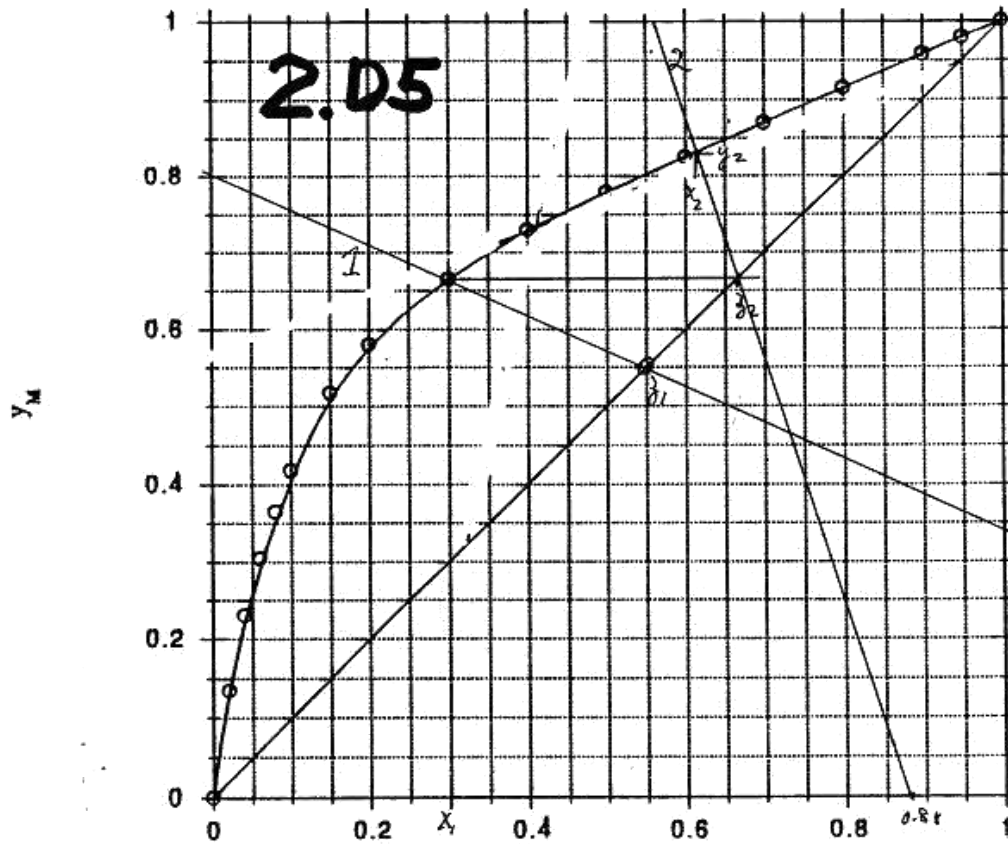
$$\frac{V}{F} = \frac{687.5}{1000} = 0.6875$$

c) Stage 2 $\frac{V}{F} = 0.25, \frac{L}{V} = \frac{0.75F}{0.25F}$ Plot op line

At $x = 0, y = z = \frac{F}{L} z = \frac{0.66}{0.25} = 2.64$. At $y = 0, x_2 = \frac{F}{L} z = \frac{0.66}{0.75} = 0.88$

From graph $y = 0.82, x = 0.63$ $V = \frac{F}{0.25} = \frac{1000}{0.25} = 4000$ $F_2 = 171.875 \text{ kmol/h}$

F_2



2.D6. *New problem in 4th ed. a.)* The answer is $VP = 19.30$ mm Hg

$$\log_{10} VP \quad 6.8379 \quad \frac{1310.62}{100} \quad 1.2856$$

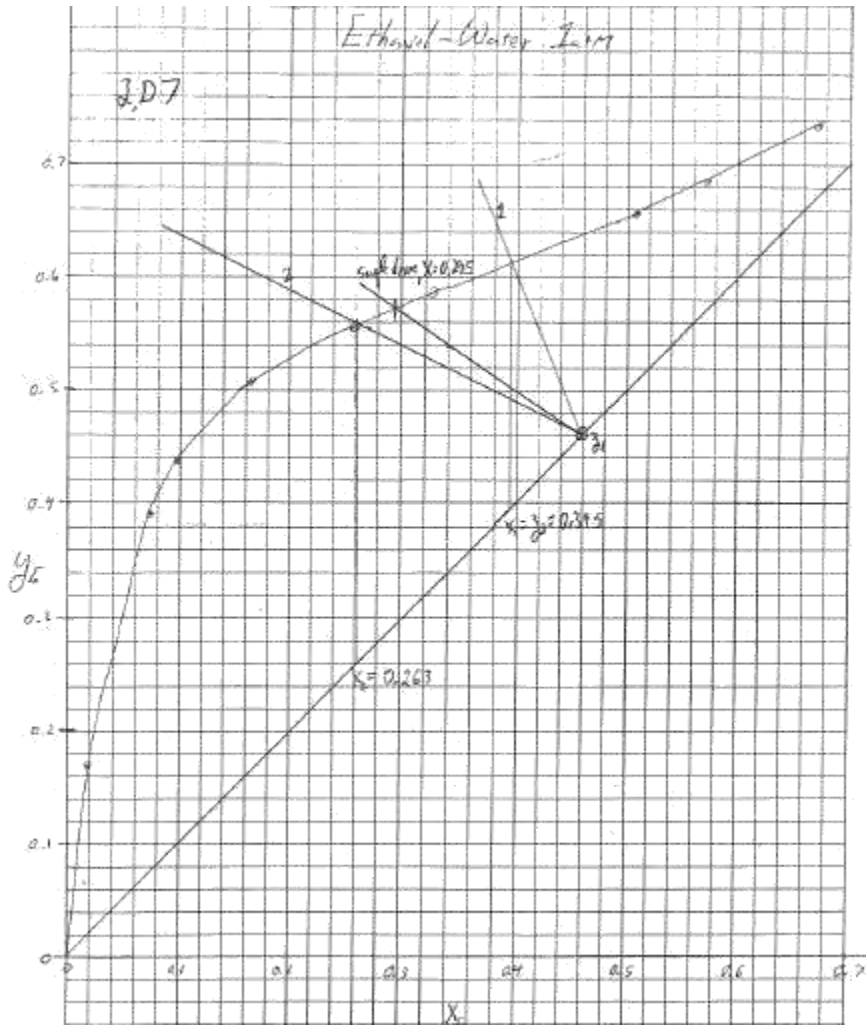
$$\frac{0.01693}{P} \quad \frac{VP}{P} \quad \frac{19.30}{P}$$

b.) The answer is $K =$
 2.D7. *New problem 4th ed.* $K_{tot} = 1.5760$

Part a. Drum 1: $V_1/F_1 = 0.3$, Slope op line = $-L/V = -7/3 = -7/3$, $y=x=z_1=0.46$. $L_1 = F_2 = 70$. From graph $x_1 = z_2 = 0.395$

Drum 2: $V_1/F_1 = 30/70$, Slope op line = $-L/V = -7/3$, $y=x=z_2=0.395$. $L_1 = F_2 - V_2 = 40$.
 From graph $x_2 = 0.263$

Part b. Single drum: $V/F = 0.6$, Slope op line = $-L/V = -40/60 = -2/3$, From graph $x = 0.295$.
 More separation with 2 drums.



2.D8. Use Rachford-Rice eqn:
$$\frac{V}{F} \sum \frac{K_i - 1}{K_i} z_i = 0$$
. Note that 2 atm = 203 kPa.

Find K_i from DePriester Chart: $K_1 = 7.3, K_2 = 4.1, K_3 = 0.115$
 Converge on $V/F = 0.076, V = 152 \text{ kmol/h}, L = 1848 \text{ kmol/h}$.

From $x_i = \frac{z_i}{1 + \frac{V}{F} K_i}$ we obtain $x_1 = 0.0077, x_2 = 0.0809, x_3 = 0.9113$

2.D9. From $y_i = K_i x_i$, we obtain $y_1 = 0.5621, y_2 = 0.3649, y_3 = 0.1048$
 Need h_F to plot on diagram. Since pressure is high, feed remains a liquid

$$h_F = \bar{C}_P T_F - T_{ref}, T_{ref} = 0 \text{ from chart}$$

$$C_{P_L} = C_{P_{EtOH}} x_{EtOH} + C_{P_w} x_w$$

Where x_{EtOH} and x_w are mole fractions. Convert weight to mole fractions.
 Basis: 100 kg mixture: 30 kg EtOH $\frac{30}{46.07} = 0.651 \text{ kmol}$

70 kg water 70/18.016 3.885 Total = 4.536 kmol

Avg. MW $\frac{100}{4.536} = 22.046$ Mole fracs: $x_E = \frac{0.6512}{4.536} = 0.1435$, $x_W = 0.8565$.

Use $C_{P_{L_{EtOH}}}$ at 100 C as an average C_P value.

$\bar{C}_P = 37.96 \cdot 0.1435 + 18.0 \cdot 0.8565 = 20.86 \frac{\text{kcal}}{\text{kmol C}}$

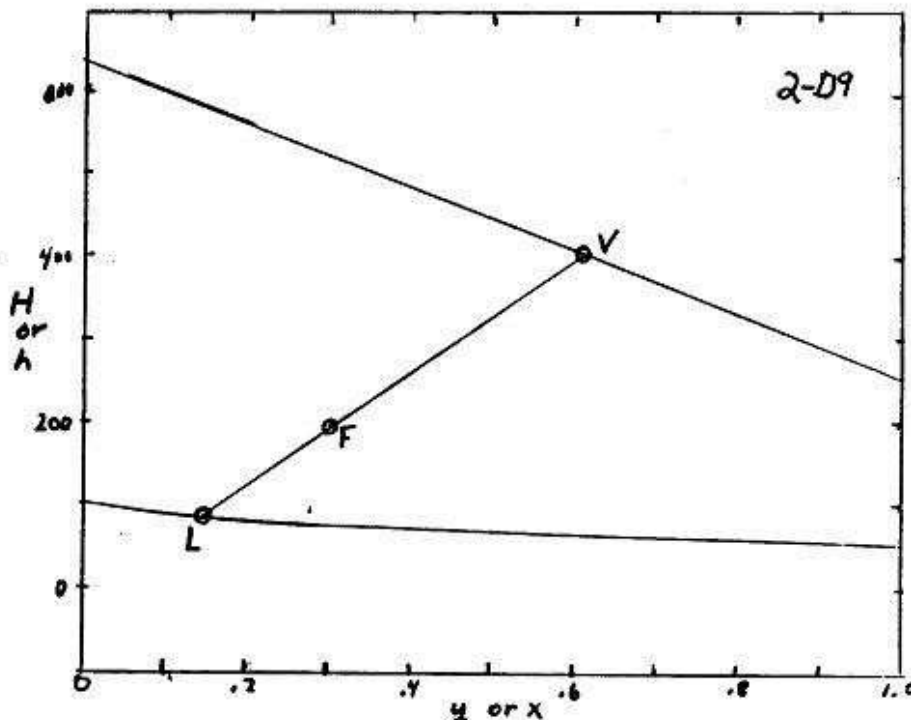
Per kg this is $\frac{\bar{C}_P}{MW_{avg}} = \frac{20.86}{22.046} = 0.946 \frac{\text{kcal}}{\text{kg C}}$

$h_F = 0.946 \cdot 2000 = 189.2 \text{ kcal/kg}$

which can now be plotted on the enthalpy composition diagram.

Obtain $T_{\text{drum}} = 88.2 \text{ C}$, $x_E = 0.146$, and $y_E = 0.617$.

For $F = 1000$ find L and V from $F = L + V$ and $Fz = Lx + Vy$ which gives $V = 326.9$, and $L = 673.1$



Note: If use wt. fracs. $\bar{C}_P = 23.99$ & $\bar{C}_P = 1.088$ and $h_F = 217.6$. All wrong.

2.D.10 Solution 400 kPa, 70°C

$z_{C4} = 35$ Mole % n-butane $x_{C6} = 0.7$

From DePriester chart

$K_{C3} = 5$, $K_{C4} = 1.9$, $K_{C6} = 0.3$

Know $y_i = K_i x_i$, $x_i = \frac{z_i}{\sum y_i}, x_i y_i = 1 z_i$

-

1 K_i 1 F

$$\text{R.R.} \quad \frac{K_i - 1 z_i}{\frac{1}{z_{C6}} K_i - 1} \frac{V}{F} z_{C6} = 0 \quad z_{C3} = 1 - z_{C6} - z_{C4} = 0.65 - z_{C6}$$

$$\text{C6: } 0.7 \quad \frac{V}{F} z_{C6} = 0.71 - 0.7 \frac{V}{F} z_{C6} = 0.7 - 0.49 \frac{V}{F} z_{C6}$$

$$1 - K_{C6} = 1 - F = 1 - 0.7 F$$

$$\text{RR Eq:} \quad \frac{4.65 z_{C6}}{1 - 4 \frac{V}{F}} - \frac{0.935}{1 - 0.9 \frac{V}{F}} - \frac{0.7 z_{C6}}{10.7 \frac{V}{F}} = 0$$

2 equations & 2 unknowns. Substitute in for z_{C6} . Do in Spreadsheet. Use Goal – Seek to find V/F . $V/F = 0.594$ when R.R. equation 0.000881.

$$z_{C6} = 0.7 - 0.49 \frac{V}{F} = 0.7 - (0.49)(0.594) = 0.40894$$

2.D11. *New Problem 4th ed.* Obtain $K_{\text{ethylene}} = 2.2$, $K_{\text{propylene}} = 0.56$ from De Priester chart.

$K_E = y_E/x_E$ and $K_P = y_P/x_P$ Since $y_p = 1 - y_E$ and $x_p = 1 - x_E$, $K_p = (1 - y_E)/(1 - x_E)$.
 Thus, 2 eqs and 2 unknowns. Solve for y_E and x_E .
 $x_E = (1 - K_p) / (K_E - K_p)$ and $y_E = K_E x_E = K_E (1 - K_p) / (K_E - K_p)$
 $x_E = (1 - 0.56) / (2.2 - 0.56) = 0.268$ and $y_E = K_E x_E = (2.2)(0.268) = 0.590$
 Check: $x_p = 1 - x_E = 1 - 0.268 = 0.732$ and $y_p = 1 - y_E = 1 - 0.590 = 0.410$
 $K_p = y_p/x_p = 0.410/0.732 = 0.56$ OK

2.D12. For problem 2.D1c, plot $x = 0.2$ on equilibrium diagram with feed composition of 0.3. The resulting operating line has a y intercept $z/V/F = 1.2$. Thus $V/F = 0.25$ (see figure in Solution to 2.D1) Vapor mole fraction is $y = 0.58$.

Find Liquid Density.

$$\bar{M}_L = x_m \bar{M}_m + x_w \bar{M}_w = 0.2(32.04) + 0.8(18.01) = 20.82$$

$$\text{Then, } \bar{V}_L = x_m \frac{\bar{M}_m}{\rho_m} + x_w \frac{\bar{M}_w}{\rho_w} = 0.2 \frac{32.04}{0.7914} + 0.8 \frac{18.01}{1.00} = 22.51 \text{ ml/mol}$$

$$\rho_L = \frac{\bar{M}_L}{\bar{V}_L} = \frac{20.82}{22.51} = 0.925 \text{ g/ml}$$

Find Vapor Density. $\rho_v = \frac{p \bar{M}_v}{RT}$ (Need temperature of the drum)

$$\bar{M}_v = y_m \bar{M}_m + y_w \bar{M}_w = 0.58(32.04) + 0.42(18.01) = 26.15 \text{ g/mol}$$

Find Temperature of the Drum T:

From Table 2-7 find T corresponding to $y = 0.58$, $x = 0.2$, $T = 81.7^\circ\text{C} = 354.7\text{K}$

$$\rho_v = \frac{1 \text{ atm} \cdot 26.15 \text{ g/mol}}{82.0575 \frac{\text{ml atm}}{\text{mol K}} \cdot 354.7 \text{ K}} = 8.98 \cdot 10^{-4} \text{ g/ml}$$

Find Permissible velocity: $u_{\text{perm}} = K_{\text{drum}} L v v$

$$K_{\text{drum, horizontal}} = \frac{1.25}{nF_{IV}^4} = 1.25 \quad K_{\text{drum, vertical}} = \exp(A + B nF_{IV} + C nF_{IV}^2 + D nF_{IV}^3 + E)$$

Since $V = V/F = 0.25 \cdot 1000 = 250$ lbmol/h,
 $W_V = V \cdot MW_V = 250 \cdot 26.15$ lb/lbmol = 6537.5 lb/h

$L = F - V = 1000 - 250 = 750$ lbmol/h, and $W_L = L \cdot MW_L = 750 \cdot 20.82 = 15,615$ lb/h,

$$F_{IV} = \frac{W_V}{W_V + W_L} = \frac{6537.5}{6537.5 + 15615} = 0.0744, \text{ and } nF_{IV} = 2.598$$

$$K_{\text{drum, vertical}} = 0.442, \text{ and } K_{\text{drum, horiz}} = \frac{0.5525}{0.925} = 0.598$$

$$u_{\text{perm}} = \frac{0.5525}{\sqrt{\frac{0.925 \cdot 8.98 \cdot 10^4}{8.98 \cdot 10^4}}} = 17.74 \text{ ft/s}$$

$$A_{CS} = \frac{V \cdot MW_V}{u_{\text{perm}} \cdot 3600} = \frac{250 \cdot 26.15}{17.74 \cdot 3600} = 454 \text{ g/lbm}$$

$$A_{CS} = 1.824 \text{ ft}^2, \quad A_T = A_{CS} / 0.2 = 9.12 \text{ ft}^2$$

With $L/D = 4$, $D = \sqrt{4A_T} = 3.41$ ft and $L = 13.6$ ft

2.D13. *New Problem 4th ed.* $x_{\text{butane}} = 1 - x_E = 0.912$, $y_{\text{butane}} = 1 - y_E = 0.454$. $K_E = y_E/x_E = 0.546/0.088 = 6.20$, $K_{\text{butane}} = y_B/x_B = 0.454/0.912 = 0.498$.

Plot K_E and K_{butane} on DePriester chart. Draw straight line between them. Intersections with T and P axis give $T_{\text{drum}} = 15^\circ\text{C}$, and $p_{\text{drum}} = 385$ kPa from Figure 2-12.

Use mass balances to find V/F : $F = L + V$ and $Fz_E = Lx_E + Vy_E$. Substitute $L = F - V$ into ethane balance and divide both sides by F . Obtain: $z = (1 - V/F)x + y(V/F)$.

Solve for $V/F = (z-x)/(y-x) = (0.36 - 0.088)/(0.546 - 0.088) = 0.594$.

Spreadsheet used as a check (using $T=15$ and $p = 385$) gave $V/F = 0.593$.

2.D14. *New Problem 4th ed.* DePriester chart, Fig. 2-12: $K_{C1} = 50$, $K_{C4} = 1.1$, and $K_{C5} = 0.37$; $z_1 = 0.12$, $z_4 = 0.48$, $z_5 = 0.40$

Rachford-Rice equation:
$$\frac{K_{C2} - 1}{1 - K_{C1}} \frac{z_{C1}}{F} + \frac{K_{C4} - 1}{1 - K_{C4}} \frac{z_{C4}}{F} + \frac{K_{C5} - 1}{1 - K_{C5}} \frac{z_{C5}}{F} = 0$$

$$5.88 \frac{0.12}{F} - 0.048 \frac{0.48}{F} - 0.252 \frac{0.40}{F} = 0$$

Equation becomes: $1 - 49(V/F) + 0.1(V/F) - 0.63(V/F) = 0$

Trials: $V/F = 0.4$, Eq. = -0.005345; $V/F = 0.39$, Eq. = 0.004506; $V/F = 0.394$, Eq. = 0.000546, which is close enough with DePriester chart.

Liquid mole fractions:

$$x_{C1} = \frac{z_{C1}}{1 - K_{C1} + (V/F)} = \frac{0.12}{1 - 50 + 0.394} = 0.00591; \quad x_{C4} = 0.4618, \quad x_{C5} = 0.5321, \text{ and } \sum x_i = 0.9998$$

$$x_{C1} = \frac{z_{C1}}{1 - K_{C1} + (V/F)} = \frac{0.12}{1 - 50 + 0.394} = 0.00591;$$

Vapor mole fractions: $y_i = K_i x_i$: $y_{C1} = 50(0.00591) = 0.2955$, $y_{C4} = 0.5080$, $y_{C5} = 0.1969$, $\sum y_i = 1.0004$.

2.D15. This is an unusual way of stating problem. However, if we count specified variables we see that problem is not over or under specified. Usually V/F would be the variable, but here it isn't. We can still write R-R eqn. Will have three variables: z_{C2} , z_{iC4} , z_{nC4} . Need two other eqns: z_{iC4}/z_{nC4} constant, and $z_{C2} + z_{iC4} + z_{nC4} = 1.0$. Thus, solve three equations and three unknowns simultaneously.

Do It. Rachford-Rice equation is,

$$\frac{K_{C2} - 1}{1 - K_{C2}} \frac{z_{C2}}{F} - \frac{K_{iC4} - 1}{1 - K_{iC4}} \frac{z_{iC4}}{F} + \frac{K_{nC4} - 1}{1 - K_{nC4}} \frac{z_{nC4}}{F} = 0$$

Can solve for $z_{C2} = 1 - z_{iC4}$ and $z_{iC4} = (.8) z_{nC4}$. Thus $z_{C2} = 1 - 1.8 z_{nC4}$. Substitute for z_{iC4} and z_{C2} into R-R eqn.

$$\frac{K_{C2} - 1}{1 - K_{C2}} \frac{1 - 1.8 z_{nC4}}{F} - \frac{.8 K_{iC4} - 1}{1 - K_{iC4}} \frac{z_{nC4}}{F} + \frac{K_{nC4} - 1}{1 - K_{nC4}} \frac{z_{nC4}}{F} = 0$$

Thus,

$$z_{nC4} = \frac{\frac{K_{C2} - 1}{1 - K_{C2}} \frac{1}{F}}{1.8 \frac{K_{C2} - 1}{1 - K_{C2}} \frac{1}{F} - \frac{.8 K_{iC4} - 1}{1 - K_{iC4}} \frac{1}{F} + \frac{K_{nC4} - 1}{1 - K_{nC4}} \frac{1}{F}}$$

Can now find K values and plug away. $K_{C2} = 2.92$, $K_{iC4} = .375$, $K_{nC4} = .26$. Solution is $z_{nC4} = 0.2957$, $z_{iC4} = .8 (.2957) = 0.2366$, and $z_{C2} = 0.4677$

2.D16. $z_{C1} = 0.5$, $z_{C4} = 0.1$, $z_{C5} = 0.15$, $z_{C6} = 0.25$, $K_{C1} = 50$, $K_{C4} = .6$, $K_{C5} = .17$, $K_{C6} = 0.05$
1st guess. Can assume all C₁ in vapor, ~ 1/3 C₄ in vapor, C₅ & C₆ in bottom

$V/F = 1.5$.1 / 3 = .53 This first guess is not critical.

$$\text{R.R. eq. } f = \frac{V}{F} \frac{K_i - 1}{1 - K_i} \frac{z_i}{V/F} = 0$$

$$\frac{49.5}{1 - 49.53} - \frac{.4 \cdot .1}{1 - .4 \cdot .53} - \frac{.83 \cdot .15}{1 - .83 \cdot .53} + \frac{.95 \cdot .25}{1 - .95 \cdot .53} = 0.157$$

Eq. 3.33

$$\frac{V}{F_2} = \frac{V}{F_1} \frac{f V F_1}{z_i K_i - 1} \frac{1}{V^2}$$

$$1 - K_i = \frac{1}{F}$$

where $V/F_1 = 0.53$ and $f V/F_1 = 0.157 \cdot V/F_1$

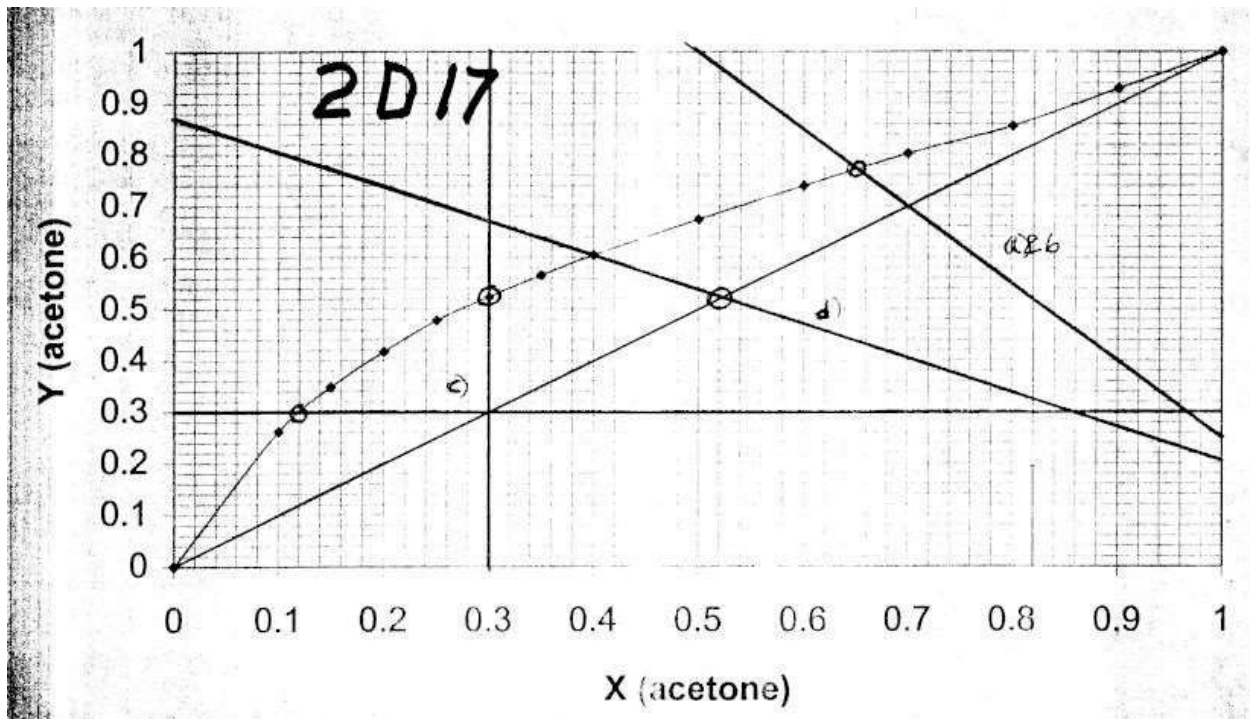
calculate $F_2 = .53 \cdot 0.157 / 2.92 = 0.584$

$V = .584 \cdot 150 = 87.6$ kmol/h and $L = 150 - 87.6 = 62.4$

$$x_{C1} = \frac{z_{C1}}{1 + K_{C1} \frac{V}{F}} = \frac{.5}{1 + 49.584 \cdot 0.016883} = 0.844$$

Similar for other components.

- 2-D17.
- $V = 0.4F = 400$, $L = 600$ Slope $L/F = 1.5$
Intercepts $y = x = z = 0.70$. Plot line and find $x_A = 0.65$, $y_A = 0.77$ (see graph)
 - $V = 2000$, $L = 3000$. Rest identical to part a.
 - Lowest x_A is horizontal op line ($L = 0$). $x_A = 0.12$
Highest y_A is vertical op line ($V = 0$). $y_A = 0.52$. See graph



- d. $V = 600$, $L = 400$, $-L/V = -0.667$.
Find $x_A = 0.40$ on equilibrium curve. Plot op line & find intersection point with $y = x$ line. $z_A = 0.52$

2.D18. From $x_i = \frac{z_i}{1 + K_i \frac{V}{F}}$, we obtain $\frac{z_h}{x_h} = \frac{V}{K_h + 1}$

Guess T_{drum} , calculate K_h , K_b and K_p , and then determine V/F .

Check: $\frac{K_1 + 1}{1 + K_1 \frac{V}{F}} z_i = 0?$

Initial guess: T_{drum} must be less than temperature to boil pure hexane

$K_h = 1.0$, $T = 94\text{ C}$. Try 85 C as first guess (this is not very critical and the calculation will tell us if there is a mistake). $K_h = 0.8$, $K_b = 4.8$, $K_p = 11.7$.

$$\frac{V}{F} = \frac{0.6}{0.85 \cdot 1} = 1.471. \text{ Not possible. Must have } K_h = 0.85^{\frac{0.6}{0.706}}$$

Try $T = 73\text{ C}$ where $K_h = 0.6$. Then $K_b = 3.8$, $K_p = 9.9$.

$$\frac{V}{F} = \frac{0.6}{0.85 \cdot 1} = 0.735$$

Check:

$$\frac{K_i \cdot 1 \cdot z_i}{1 \cdot K_i \cdot 1 \cdot V/F} = \frac{8.9 \cdot .1}{1 \cdot 8.9 \cdot .735} + \frac{2.8 \cdot .3}{1 \cdot 2.8 \cdot .735} + \frac{.4 \cdot .6}{1 \cdot .4 \cdot .735} = 0.05276$$

Converge on $T \sim 65.6\text{ C}$ and $V/F \sim 0.57$.

2.D19. 90% recovery n-hexane means $0.9 F z_{C6} = L x_{C6}$ Substitute

in $L = F V$ to obtain $z_{C6} = 0.9 \frac{1}{V/F} x_{C6}$

$$C_8 \text{ balance: } z_{C6} F = L x_{C6} = V y_{C6} = F V x_{C6} = K_{C6} V x_{C6}$$

$$\text{or } z_{C6} = \frac{1}{V/F} x_{C6} = K_{C6} \frac{V}{F} x_{C6}$$

equations and two unknowns. Remove x_{C6} and solve

$$z_{C6} = \frac{.93 C_6}{1} = \frac{.9 z_{C6} K_{C6} V}{F}$$

Solve for V/F . $\frac{V}{F} = \frac{.1}{.9 K_{C6}}$. Trial and error scheme.

Pick T , Calc K_{C6} , Calc V/F , and Check if $V/F = 0$?

$$\text{If not } K_{ref} = \frac{K_{old}}{1 + df T}$$

Try $T = 70\text{ C}$. $K_{C4} = 3.1$, $K_{C5} = .93$, $K_{C6} = .37$ K_{ref}

$$\frac{V}{F} = \frac{.9 \cdot .37 \cdot .1}{.1} = 0.231.$$

Rachford Rice equation

$$\frac{2.1 \cdot .4}{1} + \frac{.08 \cdot .25}{1} + \frac{.63 \cdot .35}{1} = 0.28719$$

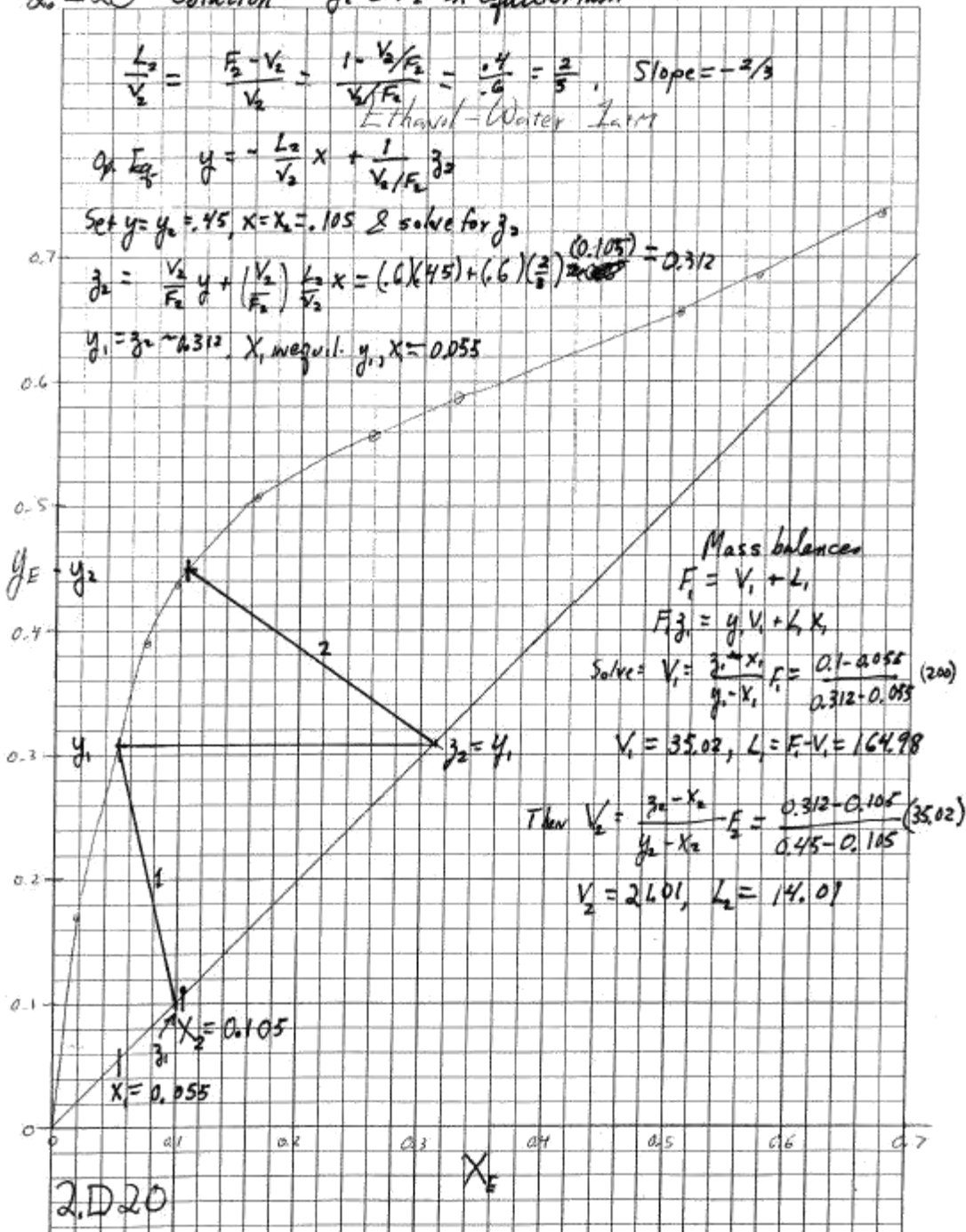
$$f = \frac{1 \cdot 2.1 \cdot .231}{K \cdot T} + \frac{1 \cdot .08 \cdot .231}{.37} + \frac{1 \cdot .63 \cdot .231}{.37} = 0.28719$$

$$K_{ref} = \frac{K_{new}}{1 + df T} \quad 1 \cdot 0.28719 = 0.28745 \text{ use } .28$$

Converge on $T_{\text{New}} \sim 57$ C. Then $K_{C4} = 2.50$, $K_{C8} = .67$, and $V/F = 0.293$.

2.D20. *New Problem 4th ed.*

2.D20 Solution: y_2 & x_2 in equilibrium



2.D21. a.) $K_{C2} \ 4.8 \ K_{C5} \ 0.153$
 $\underline{V} \ \underline{z_A} \ \underline{z_B} \ \underline{V} \ \underline{0.55} \ \underline{0.45}$

Soln to Binary R.R. eq. $F \ K_B \ 1 \ K_A \ 1 \ , F \ .153 \ 1 \ 4.8 \ 1 \ 0.5309$

$x_{C2} \ \frac{0.55}{V} \ \frac{0.55}{1 \ 3.8 \ .5309} \ 0.1823, \ y_{C2} \ 0.8749, \ x_{C5} \ 0.8177, \ y_{C5} \ 0.1251$

1 K_{C2} 1 F

Need to convert F to kmol. Avg MW 0.55 30.07 0.45 72.15 49.17

$$F = 100,000 \frac{\text{kg}}{\text{hr}} \left| \frac{\text{kmol}}{49.17 \text{ kg}} \right| = 2033.7 \text{ kmol/h}, \quad V = V_F/F = 1079.7, \quad L = F/V = 954.0 \text{ kmol/h}$$

b.)
$$u = \frac{K}{\text{Perm drum}} \sqrt{\frac{L_v}{v}}$$

To find
$$\overline{MW}_L = 0.1823 \cdot 30.07 + 0.8177 \cdot 72.15 = 64.48$$

$$\overline{MW}_v = 0.8749 \cdot 30.07 + 0.1251 \cdot 72.15 = 35.33$$

For liquid assume ideal mixture:

$$\overline{V}_L = \overline{V}_1 x_1 + \overline{V}_2 x_2 + \overline{V}_5 x_5 = \overline{MW}_L \cdot \overline{c}_2 + \overline{MW}_L \cdot \overline{c}_5$$

$$\overline{V}_L = 0.1823 \cdot 30.07 + 0.8177 \cdot 72.15 = 103.797 \text{ ml/mol}$$

$$\rho_L = \frac{\overline{MW}_L}{\overline{V}_L} = \frac{64.48}{103.797} = 0.621 \text{ g/ml}$$

For vapor: ideal gas:
$$v = \frac{\overline{MW}_v}{RT} = \frac{35.33}{82.0575 \text{ mol K} \cdot 303.16 \text{ K}} = 0.009814 \text{ g/ml}$$

K_{drum} : Use Eq. (2-60) with $F_{IV} = \frac{W_L}{W_v} \sqrt{\frac{v}{L}}$

$$W_L = 997.7 \frac{\text{kg}}{\text{h}} \left| \frac{64.48 \text{ kg}}{\text{kmol}} \right| = 6,433.7 \text{ kg/h}, \quad W_v = 881.5 \left| \frac{35.33}{\text{kmol}} \right| = 31,143.4 \text{ kg/h}$$

$$F_{IV} = \frac{6433.7 \cdot 0.009814}{31,143.3 \cdot 0.621} = 0.2597$$

$$K_{\text{drum exp}} = 1.877478 \cdot 0.81458 \cdot n^{0.2597} = 0.18707 \cdot n^{0.2597^2}$$

$$0.0145229 \cdot n^{0.2597^3} = 0.0010149 \cdot n^{0.2597^4} = 0.3372$$

$$u_{\text{Perm}} = 0.3372 \sqrt{\frac{0.621 \cdot 0.009814 \frac{\text{ft}}{\text{s}}}{0.009814 \frac{\text{kmol}}{\text{kg}}}} \left| \frac{1.0 \text{ m}}{3.2808 \text{ ft}} \right| = 0.8111 \text{ m/s}$$

$$A = \frac{V \overline{MW}_v}{u_{\text{Perm}}} = \frac{1079.7 \cdot 35.33}{0.8111} = 47,100 \frac{\text{m}^3}{\text{s}} = 1.392 \text{ m}^2$$

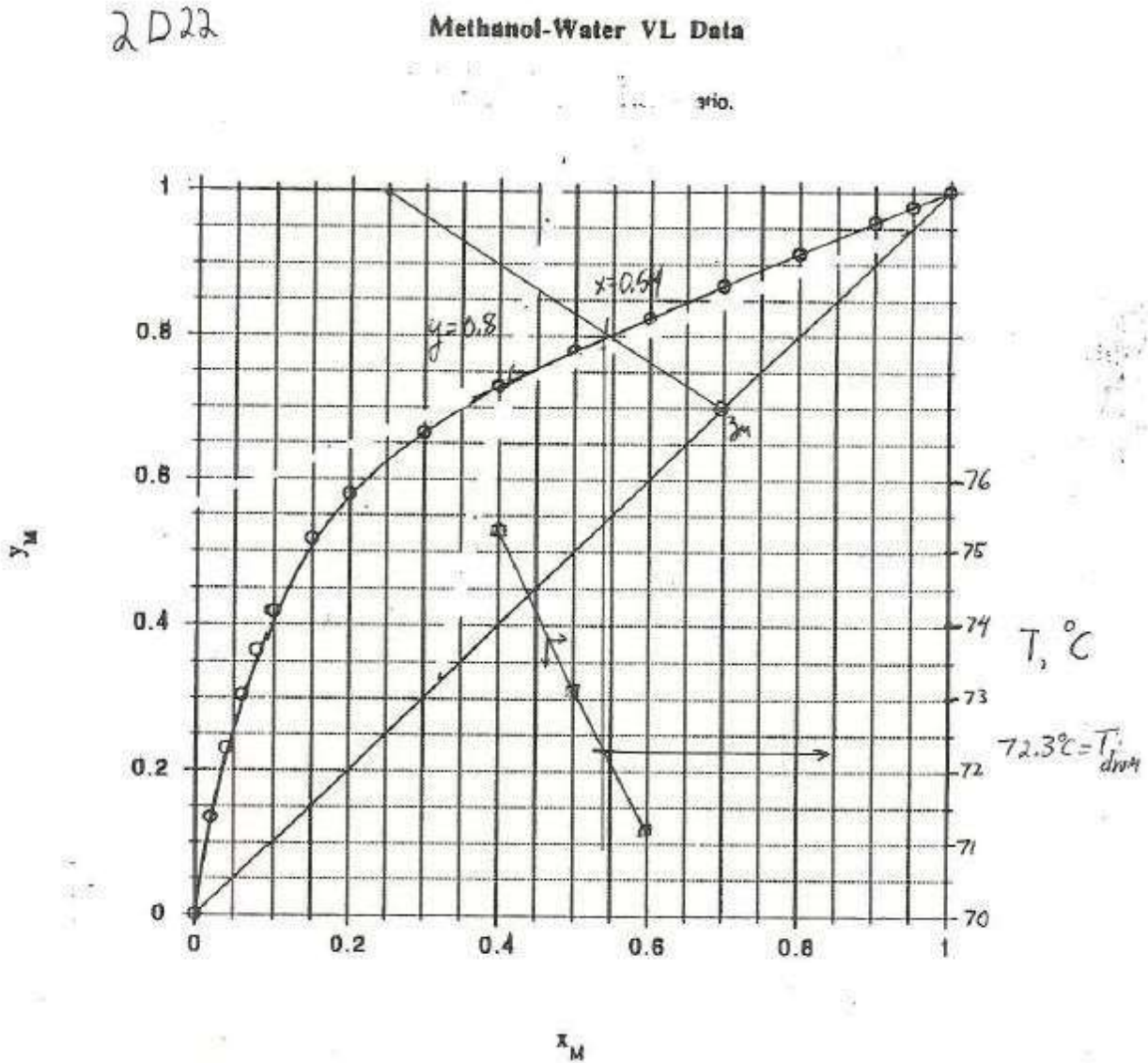
$$C = \frac{0.009814 \text{ g}}{\text{cm}^3} \cdot \frac{1000 \text{ g}}{\text{kg}} = 0.009814 \text{ kg/m}^3$$

$$D = \sqrt{4AC} = 1.33 \text{ m} \text{ . Arbitrarily } L/D = 4, \quad L = 5.32 \text{ m}$$

a. $V = F - L = 50 - 20 = 20 \text{ kmol/h}$. $V/F = 3/5$, Slope operating line = $-L/V = -20/30 = -2/3$, $z_M = 0.7$

From graph, $y = 0.8$, $x = 0.54$.

b. From graph of T vs. x_M , $T_{\text{drum}} = 72.3^\circ\text{C}$. (see graph).



2.D23. New Problem 4th ed.

Part a. $F_{\text{new}} = (1500 \text{ kmol/h})(1.0 \text{ lbmol}/(0.45359 \text{ kmol})) = 3307 \text{ lb mol/h}$. V , W_v , L , and W_L are the values in Example 2-4 divided by 0.45359. The conversion factor divides out in F_{IV} term. Thus, F_{IV} , K_{drum} , and u_{perm} are the same as in Example 2-4. The Area increases because V

increases: $\text{Area} = \text{Area}_{\text{Example 2-4}}/0.45359 = 16.047/0.45359 = 35.38 \text{ ft}^2$.

$$\text{Diameter} = \sqrt{4 \text{ Area} / \pi} = 6.71 \text{ feet}$$

Probably round this off to 7.0 feet and use a drum height of 28 feet.

b. $F_{\text{parallel}} = 3307 - 1500 = 1807 \text{ lbmol/h}$.

F_{IV} , K_{drum} , and u_{perm} are the same as in Example 2-4. $V_{\text{parallel}} = (V/F) F_{\text{parallel}} = 0.51 (1807) = 921.6 \text{ kmol/h}$.

$$A_c = 16.047 \frac{V_{parallel}}{V_{Example_2_4}} = 16.047 (921.6 / 765) = 19.33 \text{ ft}^2$$

Then, Diameter = $\sqrt{4 \text{ Area} / \pi} = 4.96 \text{ feet}$, Use a 5.0 feet diameter and a length of 20 feet.

2.D24. $p = 300 \text{ kPa}$ At any T. $K_{C3} = y_{C3} / x_{C3}$, K's are known. $K_{C6} = y_{C6} / x_{C6} = 1 - y_{C3} / 1 - x_{C3}$

Substitute 1st equation into 2nd $K_{C6} = 1 - K_{C3} x_{C3} / 1 - x_{C3}$

Solve for x_{C3} , $1 - x_{C3} K_{C6} = 1 - K_{C3} x_{C3}$, $x_{C3} K_{C3} - K_{C6} = 1 - K_{C6}$

$$x_{C3} = \frac{1 - K_{C6}}{K_{C3} - K_{C6}} \quad \& \quad y_{C3} = \frac{K_{C3} (1 - K_{C6})}{K_{C3} - K_{C6}}$$

At 300 kPa pure propane $K_{C3} = 1.0$ boils at -14°C (Fig. 2-10)

At 300 kPa pure n-hexane $K_{C6} = 1.0$ boils at 110°C

Check: at -14°C $x_{C3} = \frac{1 - K_{C6}}{K_{C3} - K_{C6}} = 1$, $y_{C3} = \frac{K_{C3} (1 - K_{C6})}{K_{C3} - K_{C6}} = 1.0$

$$x_{C3} = \frac{1 - K_{C6}}{K_{C3} - K_{C6}} = \frac{1 - 1.0}{1.0 - 1.0} = \frac{0}{0}$$

at 110°C $x_{C3} = 0$, $y_{C3} = 0$

Pick intermediate temperatures, find K_{C3} & K_{C6} , calculate x_{C3} & y_{C3} .

T	K_{C3}	K_{C6}	x_{C3}	y_{C3}
0°C	1.0	0.0	$\frac{1 - 0.0}{1.0 - 0.0} = 1.0$	1.0
10°C	1.45	0.0	0.684	0.684
20°C	1.45	0.0	0.684	0.684
30°C	1.45	0.0	0.684	0.684
40°C	1.45	0.0	0.684	0.684
50°C	1.45	0.0	0.684	0.684
60°C	1.45	0.0	0.684	0.684
70°C	6.4	0.38	0.103	0.659

See Graph

b. $x_{C3} = 0.3$, $V/F = 0.4$, $L/V = 0.6$ $0.4 / 1.5$
Operating line intersects $y = x + 0.3$, Slope 1.5

$$y = \frac{L}{V} x + \frac{F}{V} z \quad \text{at } x = 0, \quad y = \frac{F}{V} z = \frac{0.3}{0.4} = 0.75$$

Find $y_{C3} = 0.63$ and $x_{C3} = 0.062$

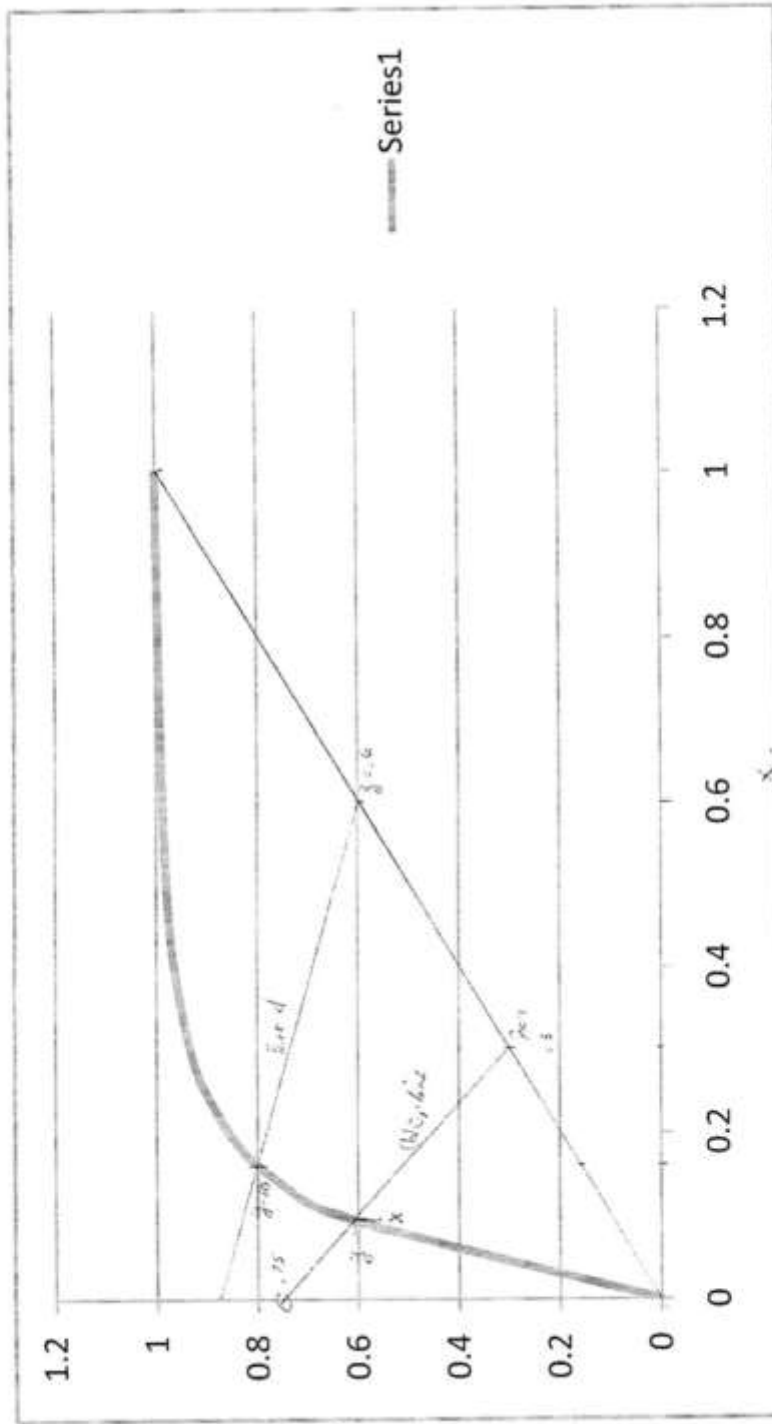
Check with operating line: $0.63 = 1.5(0.062) + 0.75 = 0.657$ OK within accuracy of the graph.

c. Drum T: $K_{C3} = y_{C3} / x_{C3} = 0.63 / 0.062 = 10.2$, DePriester Chart T = 109°C
 $\frac{L}{V} = \frac{y}{x} = \frac{0.8}{0.16} = 5.0$ d. $y = 0.8$, $x \sim 0.16$ Slope

$$V/F = f = 1/1.45 = 0.69$$

$$0.45 \quad \frac{1}{f} .45$$

306 HW 1, 2008
 Prob 1



2.D25. 20% Methane and 80% n-butane. $T_{\text{drum}} = 50^\circ\text{C}$, $\frac{V}{F} = 0.40$, Find p_{drum}

$$0 = f - \frac{V}{F} \left[\frac{K_A z_A}{1 + K_A} - \frac{K_B z_B}{1 + K_B} \right]$$

Pick $p_{\text{drum}} = 1500 \text{ kPa}$: $K_{C4} = 13$, $K_{nC4} = 0.4$
 (Any pressure with $K_{C1} = 1$ and $K_{C4} = 1.0$ is OK)

Trial 1 $f = \frac{12.2}{1 + 12.4} - \frac{0.8}{1 + 0.4} = 0.2178$ Need lower p_{drum}

$$K_{C4} = \frac{K_{C4} P_{\text{old}}}{1 + K_{C4} P_{\text{old}}} = \frac{0.4}{1 + 0.2138 \cdot 0.511} \text{ with } d = 1.0$$

P1160 $K_{C1} = 16.5$, $f = \frac{15.5 \cdot 0.2}{1 + 15.5 \cdot 0.4} - \frac{0.489 \cdot 0.8}{1 + 0.489 \cdot 0.4} = 0.4305 - 0.4863 = 0.055769$

$$K_{C4} P_{\text{new}} = \frac{0.511}{0.055769} = 0.541, P_{\text{new}} = 1100, K_{C1} = 17.4$$

$$f_3 = \frac{16.4 \cdot 0.2}{1 + 16.4 \cdot 0.4} - \frac{0.459 \cdot 0.8}{1 + 0.459 \cdot 0.4} = 0.0159, \text{ OK. Drum pressure} = 1100 \text{ kPa}$$

b.) $x_i = \frac{z_i}{1 + K_i} = \frac{0.2}{1 + 16.4 \cdot 0.4} = 0.02645$
 $y_{C1} = K_{C1} x_{C1} = 17.4 \cdot 0.02645 = 0.4603$

2.D26. a) Can solve for L and V from M.B. $100 = F = V + L$
 $45 = Fz = 0.8V = 0.2162L$
 $L = 59.95$ and $V = 40.05$

Find: y
 $K_{C3} = \frac{0.8}{x} = 3.700$, $K_{C5} = \frac{0.2}{0.2162} = 0.7838$

These K values are at same T, P. Find these 2 K values on DePriester chart.

Draw straight line between them. Extend to T_{drum} , p_{drum} . Find 10°C , 160 kPa.

2.D27. a.) $\log_{10} \frac{VP}{T} = 6.853 - \frac{1064.8}{233.01} = 2.2832$, $VP = 191.97 \text{ mmHg}$

b.) $VP = 3760 - 2280 \text{ mmHg}$, $\log_{10} \frac{VP}{T} = 6.853 - \frac{1064.8}{T} = 2.2832$
 Solve for $T = 71.65^\circ\text{C}$

c.) $P_{\text{tot}} = 191.97 \text{ mm Hg}$ [at boiling for pure component $P_{\text{tot}} = VP$]

d.) C5: $\log_{10} VP = 6.853 - \frac{1064.8}{30 \cdot 233.01} = 2.8045$, $VP = 637.51 \text{ mm Hg}$

$$K_{C5} = VP_{C5} / P_{\text{tot}} = 637.51 / 500 = 1.2750$$

$$C6: \log_{10} \frac{VP_{C6}}{c6} = 6.876 - \frac{1171.17}{30} \frac{2.2725}{224.41}, \quad VP_{C6} = 187.29 \text{ mm Hg}$$

$$K_{C6} = 187.29/500 = 0.3746$$

e.) $K_A = y_A/x_A \quad K_B = y_B/x_B \quad (1 - y_A)/(1 - x_A)$

If K_A & K_B are known, two eqns. with 2 unknowns K_A & y_A Solve.

$$x_{C5} = \frac{1}{K_{C5}} \frac{K_{C6}}{K_{C6}} = \frac{10.3746}{1.2750 \cdot 0.3746} = 0.6946$$

$$y_{C5} = K_{C5} x_{C5} = 1.2750 \cdot 0.6946 = 0.8856$$

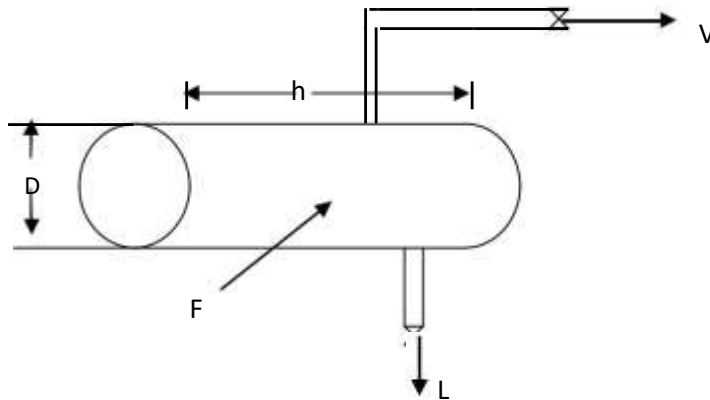
f.) Overall, M.B., $F = L + V$ or $1 = L + V$

$$C5: Fx_F = Lx + Vy = 0.75 = 0.6946L + 0.8856V$$

Solve for L & V: $L = 0.7099$ & $V = 0.2901$ mol

g.) Same as part f, except units are mol/min.

2.D28.



From example 2-4, $x_H = 0.19$, $T_{\text{drum}} = 378K$, $V/F = 0.51$, $y_H = 0.6$, $z_H = 0.40$

$MW_v = 97.39$ lbm/lbmole (Example 2-4)

$$v = 3.14 \cdot 10^3 \text{ g mol} \left| \frac{1}{454 \text{ g/lbm}} \right| \frac{28316.85 \text{ cm}^3}{\text{ft}^3} \cdot 0.198 \frac{\text{lbm}}{\text{ft}^3}$$

Example 2.4

$$u_{\text{perm drum}} = \frac{K_{\text{horiz}}}{\sqrt{L_v}}, \quad K_{\text{horiz}} = 1.25, \quad K_{\text{vertical}}$$

From Example 2-4, $K_{\text{vertical}} = 0.4433$, $K_{\text{horiz}} = 1.25$, $0.4433 = 0.5541$

$$u_{\text{perm}} = \frac{0.6960 \cdot 0.00314 \cdot 1.2}{0.5541 \cdot 0.00314} \cdot 8.231 \text{ ft s} \quad [\text{densities from Example 2-4}]$$

$$V = \frac{F}{F} = \frac{0.51 \cdot 3000 \frac{\text{lbmol}}{\text{h}}}{1530 \frac{\text{lbmol}}{\text{h}}} = 1$$

$$A_{\text{vap}} = \frac{1530 \frac{\text{lbmol}}{\text{h}} \cdot 97.39 \frac{\text{lbm}}{\text{lbmole}}}{8.231 \frac{\text{s}}{\text{h}} \cdot 3600 \frac{\text{s}}{\text{h}} \cdot 0.1958 \frac{\text{ft}}{\text{ft}}} = 25.68 \text{ ft}^2$$

$$A_{\text{total}} = A_{\text{vap}} / 0.2 = 128.4 \text{ ft}^2, D_{\text{min}} = \sqrt{4A_{\text{total}} / \pi} = 12.8 \text{ ft}$$

$$V_{\text{liq}} = \frac{160,068 \cdot 55 \cdot 85}{8603.8 \text{ ft}^3, h_{\text{liq}} = 83.51 \text{ ft and } h/D = 6.5.$$

$$V_{\text{liq}} = 43.41 \cdot 60 \text{ min/h} \cdot D^2$$

2.D29. The stream tables in Aspen Plus include a line stating the fraction vapor in a given stream. Change the feed pressure until the feed stream is all liquid (fraction vapor = 0). For the Peng-Robinson correlation the appropriate pressure is 74 atm.

The feed *mole* fractions are: methane = 0.4569, propane = 0.3087, n-butane = 0.1441, i-butane = 0.0661, and n-pentane = 0.0242.

b. At 74 atm, the Aspen Plus results are; L = 10169.84 kg/h = 201.636 kmol/h, V = 4830.16 kg/h = 228.098 kmol/h, and T_{drum} = -40.22 °C.

The vapor mole fractions are: methane = 0.8296, propane = 0.1458, n-butane = 0.0143, i-butane = 0.0097, and n-pentane = 0.0006.

The liquid mole fractions are: methane = 0.0353, propane = 0.4930, n-butane = 0.2910, i-butane = 0.1298, and n-pentane = 0.0509.

c. Aspen Plus gives the liquid density = 0.60786 g/cc, liquid avg MW = 50.4367, vapor density = 0.004578 g/cc = 4.578 kg/m³, and vapor avg MW = 21.17579 g/mol = kg/kmol.

The value of u_{perm} (in ft/s) can be determined by combining Eqs. (2-64), (2-65) and (2-69)

$$F_{lv} = (W_L/W_V)[\rho_V/\rho_L]^{0.5} = (10169.84/4830.16)[0.004578/0.60786]^{0.5} = 0.18272$$

Resulting K_{vertical} = 0.378887, K_{horizontal} = 0.473608, and u_{perm} = 5.436779 ft/s = 1.657 m/s

$$A_{\text{vap}} = \frac{4830.16 \frac{\text{kg}}{\text{h}}}{1.657 \frac{\text{m}}{\text{s}} \cdot 3600 \frac{\text{s}}{\text{h}} \cdot 4.578 \frac{\text{kg}}{\text{m}^3}} = 0.177 \text{ m}^2$$

$$A_{\text{total}} = A_{\text{vap}} / 0.2 = 0.884 \text{ m}^2, D_{\text{min}} = \sqrt{4A_{\text{total}} / \pi} = 1.06 \text{ m}$$

$$h/D = 6 \Rightarrow h = 6D^2, \text{ thus } V_{\text{liq}} = 54.23 \text{ m}^3$$

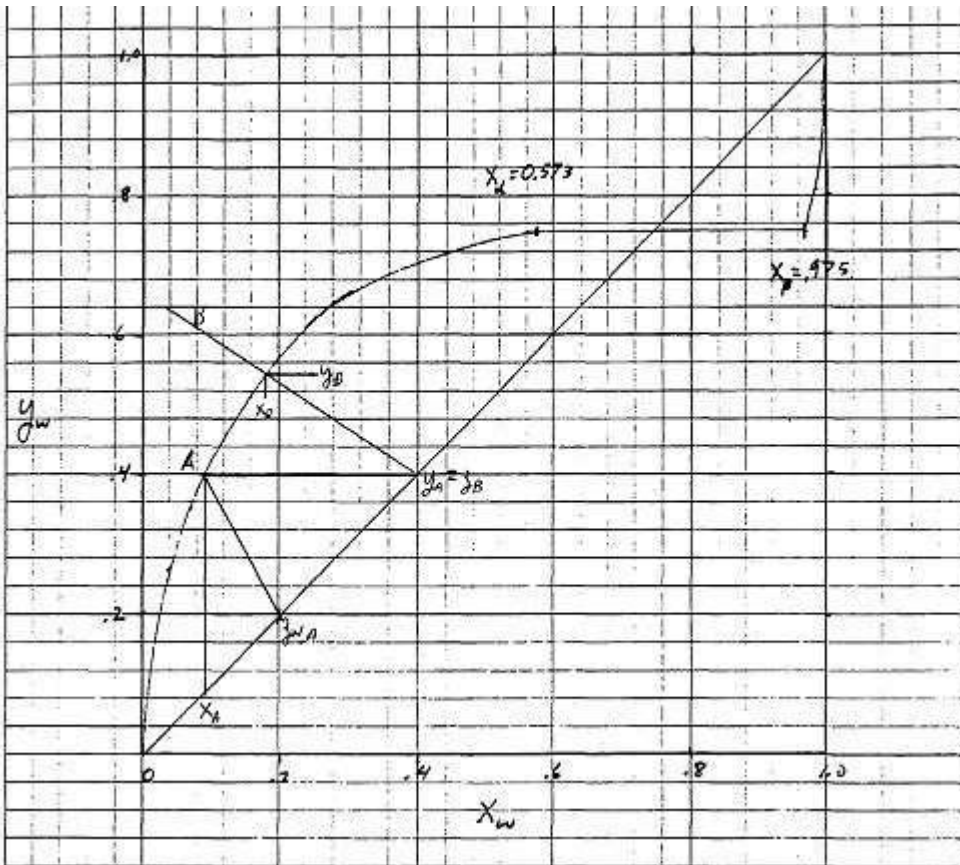
$$V_{\text{liq}} = (\text{Vol rate})(\text{hold time} + \text{surge time}) = \left(\frac{10169.84 \text{ kg/h}}{607.86 \text{ kg/m}^3} \right) (9/60 \text{ st})$$

$$\text{st} = 607.86 V_{\text{liq}} / 10169.84 \cdot 9/60 = 0.103 \text{ hours} = 6.18 \text{ min}$$

2.D30.. a. From the equilibrium data if $y_A = .40$ mole fraction water, then $x_A = 0.09$ mole fraction water. Can find L_A and V_A by solving the two mass balances for stage A simultaneously.
 $L_A + V_A = F_A = 100$ and $L_A (.09) + V_A (.40) = (100) (.20)$. The results are $V_A = 35.48$ and $L_A = 64.52$.

b. In chamber B, since 40 % of the vapor is condensed, $(V/F)_B = 0.6$. The operating line for this flash chamber is, $y = -(L/V)x + F_B/V z_B$ where $z_B = y_A = 0.4$ and $L/V + .4F_B/.6F_B = 2/3$. This operating line goes through the point $y = x = z_B = 0.4$ with a slope of $-2/3$. This is shown on the graph. Obtain $x_B = 0.18$ & $y_B = 0.54$. $L_B = (\text{fraction condensed})(\text{feed to B}) = 0.4(35.48) = 14.19 \text{ kmol/h}$ and $V_B = F_B - L_B = 21.29$.

c. From the equilibrium if $x_B = 0.20$, $y_B = 0.57$. Then solving the mass balances in the same way as for part a with $F_B = 35.48$ and $z_B = 0.4$, $L_B = 16.30$ and $V_B = 19.18$. Because $x_B = z_A$, recycling L_B does not change $y_B = 0.57$ or $x_A = 0.09$, but it changes the flow rates $V_{B,\text{new}}$ and $L_{A,\text{new}}$. With recycle these can be found from the overall mass balances: $F = V_{B,\text{new}} + L_{A,\text{new}}$ and $Fz_A = V_{B,\text{new}}y_B + L_{A,\text{new}}x_A$. Then $V_{B,\text{new}} = 22.92$ and $L_{A,\text{new}} = 77.08$.



Graph for problem 2.D30.

2.D31. New problem in 4th US edition. Was 2.D13 in 3rd International Edition.

a) Since K's are for mole fractions, need to convert feed to mole fractions.

Basis: 100 kg feed

50 kg n C ₄	$\frac{1 \text{ kmol}}{58.12 \text{ kg}}$	0.8603 kmol	z	0.555
50 kg n C ₅	$\frac{1 \text{ kmol}}{72.5 \text{ kg}}$	0.6897 kmol n C ₅	z	0.445
Total 1.5499 kmol			s	

DePriester Chart $K_{C4} = 2.05$, $K_{C5} = 0.58$, Result similar if use Raoult's law .

$$\frac{V}{F} = \frac{0.555}{1} \quad \frac{0.445}{1.3214} \quad \frac{0.42}{1.42} \quad \frac{0.445}{0.8976}$$

$$F = \frac{0.58}{1} \quad 1.05$$

Check $f = \frac{1.05 \cdot 0.555}{1 \cdot 0.05 \cdot 0.8976} - \frac{0.42 \cdot 0.445}{1.42 \cdot 0.8976} = 0.3000 - 0.29999 = 0 \text{ OK}$

Eq. 3.23 $x_{C4} = \frac{0.555}{1 \cdot K_{C4} + V/F} = \frac{0.555}{1 \cdot 2.05 + 11.056 \cdot 0.8976} = 0.2857$,

$$x_{C5} = 0.7143 \quad y_{C4} = K_{C4} x_{C4} = 0.5857, \quad y_{C5} = 0.4143$$

b) From problem 2.D.g., $K_{C4} = 1.019$ and $K_{C5} = 0.253$.

Solving RR equation,

$$\frac{V}{F} = \frac{z_A}{K_B + 1} - \frac{z_B}{K_A + 1} = \frac{0.555}{0.253 + 1} - \frac{0.445}{1.019 + 1} = 0.2328 - 0.219 = 0.0138$$

NOT possible. Won't flash at 0°C.

2.D32. New problem in 4th US edition. Was 2.D28 in 3rd International Edition.

$V/F_A = 2/3$, $L/V = 1/2$, Slope 1/2 Through $y = x$, $z_A = 0.6$ See figure

a. L

$\frac{1}{3} F = 33.33$, $x_{M,A} = 0.375$ (from Figure) $V = \frac{2}{3} F = 66.67$, $y_{M,A} = 0.72$ (from Figure)

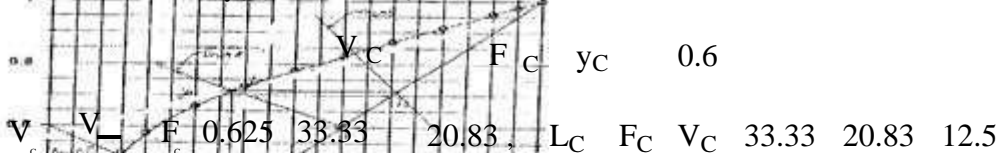
$$\frac{V}{F_B} = 0.4 = \frac{L}{V_B} \frac{1 - f}{f} = \frac{0.6}{0.4} = 1.5$$

Through $y = x$, $z_B = y_A = 0.72$

$$V_B = 0.4 F_B = 0.4 V_A = 0.4 \cdot 66.67 = 26.67, \quad L_B = 0.6 F_B = 0.6 \cdot 66.67 = 40.00$$

b. $z_C = x_A = 0.375$, $x_C = 0.15$, $F_C = L_A = 33.33$, From equilibrium $y_C = 0.51$

At $x = 0$, $y_C = 0.60$, $F_C = \frac{V}{z_C} = \frac{0.375}{0.625} = 0.625$



2.E1. From Aspen Plus run with 1000 kmol/h at 1 bar, $L = V = 500$ kmol/h, $W_L = 9212.78$ kg/h, $W_V = 13010.57$ kg/h, liquid density = 916.14 kg/m³, liquid avg MW = 18.43, vapor density = 0.85 kg/m³, and

vapor avg MW = 26.02, $T_{\text{drum}} = 94.1$ °C, and $Q = 6240.85$ kW.

The diameter of the vertical drum in meters (with u_{perm} in ft/s) is

$$D = \left\{ \frac{4(MW_V) V}{3600 \pi \rho_V u_{\text{perm}} (1 \text{ m}/3.281 \text{ ft})} \right\}^{0.5} = \left\{ \frac{4(26.02)(500)}{3600(3.14159)(0.85)(1/3.281)u_{\text{perm}}} \right\}^{0.5}$$

$$F_{lv} = (W_L/W_V)[\rho_V/\rho_L]^{0.5} = (9212.78/13010.57)[0.85/916.14]^{0.5} = 0.02157$$

Resulting $K_{\text{vertical}} = 0.404299$, and $u_{\text{perm}} = 13.2699$ ft/s, and $D = 1.16$ m. Appropriate standard size would be used. Mole fractions isopropanol: liquid = 0.00975, vapor = 0.1903

b. Ran with feed at 9 bar and p_{drum} at 8.9 bar with $V/F = 0.5$. Obtain $W_L = 9155.07$ kg/h, $W_V = 13068.27$, density liquid = 836.89, density vapor = 6.37 kg/m³

$$D = \left\{ \frac{4(MW_V) V}{3600 \pi \rho_V u_{\text{perm}} (1 \text{ m}/3.281 \text{ ft})} \right\}^{0.5} = \left\{ \frac{4(26.14)(500)}{3600(3.14159)(6.37)(1/3.281)u_{\text{perm}}} \right\}^{0.5}$$

$$F_{lv} = (W_L/W_V)[\rho_V/\rho_L]^{0.5} = (9155.07/13068.27)[6.37/836.89]^{0.5} = 0.06112$$

Resulting $K_{\text{vertical}} = .446199$, $u_{\text{perm}} = 5.094885$ ft/s, and $D = 0.684$ m. Thus, the method is feasible.

c. Finding a pressure to match the diameter of the existing drum is trial and error. If we do a linear interpolation between the two simulations to find a pressure that will give us $D = 1.0$ m (if linear), we find $p = 3.66$. Running this simulation we obtain, $W_L = 9173.91$ kg/h, $W_V = 13049.43$, density liquid = 874.58, density vapor = 2.83 kg/m³, $MW_V = 26.10$

$$D = \left\{ \frac{4(MW_V) V}{3600 \pi \rho_V u_{\text{perm}} (1 \text{ m}/3.281 \text{ ft})} \right\}^{0.5} = \left\{ \frac{4(26.10)(500)}{3600(3.14159)(2.83)(1/3.281)u_{\text{perm}}} \right\}^{0.5}$$

$$F_{lv} = (W_L/W_V)[\rho_V/\rho_L]^{0.5} = (9173.91/13049.43)[2.83/874.58]^{0.5} = 0.0400$$

Resulting $K_{\text{vertical}} = .441162$, $u_{\text{perm}} = 7.742851$ ft/s, and $D = 0.831$ m.

Plotting the curve of D versus p_{drum} and setting $D = 1.0$, we interpolate $p_{\text{drum}} = 2.1$ bar. At $p_{\text{drum}} = 2.1$ bar simulation gives, $W_L = 9188.82$ kg/h, $W_V = 13034.53$, density liquid = 893.99, density vapor = 1.69 kg/m³, $MW_V = 26.07$.

$$D = \left\{ \frac{4(MW_V) V}{3600 \pi \rho_V u_{\text{perm}} (1 \text{ m}/3.281 \text{ ft})} \right\}^{0.5} = \left\{ \frac{4(26.07)(500)}{3600(3.14159)(1.69)(1/3.281)u_{\text{perm}}} \right\}^{0.5}$$

$$F_{lv} = (W_L/W_V)[\rho_V/\rho_L]^{0.5} = (9188.82/13034.53)[1.69/893.99]^{0.5} = 0.0307$$

Resulting $K_{\text{vertical}} = .42933$, $u_{\text{perm}} = 9.865175$ ft/s, and $D = 0.953$ m.

This is reasonably close and will work OK. $T_{\text{drum}} = 115.42\text{ }^{\circ}\text{C}$, $Q = 6630.39\text{ kW}$,
Mole fractions isopropanol: liquid = 0.00861, vapor = 0.1914

In this case there is an advantage operating at a somewhat elevated pressure.

2.E2. This problem was 2.D13 in the 2nd edition of *SPE*.

a. Will show graphical solution as a binary flash distillation. Can also use R-R equation. To generate equil. data can use

$$x_{C6} + x_{C8} = 1.0, \text{ and } y_{C6} = K_{C6} x_{C6}, \quad y_{C8} = K_{C8} x_{C8} = 1.0$$

Substitute for x_{C6}

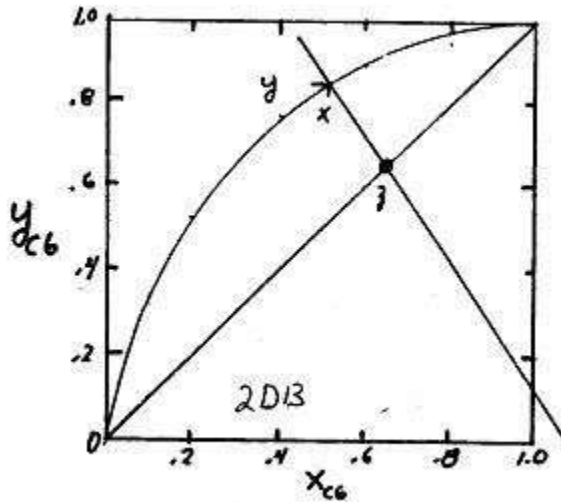
$$x_{C6} = \frac{1 - K_{C8} x_{C8}}{K_{C6} - K_{C8}}$$

Pick T, find K_{C6} and K_{C8} (e.g. from DePriester charts), solve for x_{C6} . Then $y_{C6} = K_{C6} x_{C6}$

T°C	K_{C6}	K_{C8}	x_{C6}	$y_{C6} = K_{C6} x_{C6}$
125	4	1.0	0	0
120	3.7		.0357	.321
110	3.0		.1379	.141
100	2.37		.2595	.615
90	1.8		.4406	.793
80	1.4		.650	.909
66.5	1.0	.17	1.0	1.0

Op Line Slope $\frac{L}{V} = \frac{1 - V/F}{V/F} = \frac{.6}{.4} = 1.5$, Intersection $y = x = z = 0.65$.

See Figure. $y_{C6} = 0.85$ and $x_{C6} = 0.52$. Thus $K_{C6} = .85/.52 = 1.63$.
This corresponds to $T = 86^\circ\text{C} = 359\text{K}$



b. Follows Example 2-4.

$$\begin{array}{r} \overline{MW}_L \\ \frac{x_{C6}}{V} \end{array} = \frac{x_{C6} \overline{MW}_{C6} + x_{C8} \overline{MW}_{C8}}{x_{C6} \overline{MW}_{C6} + x_{C8} \overline{MW}_{C8}} = \frac{.52 \cdot 86.17 + .48 \cdot 114.22}{.52 \cdot 86.17 + .48 \cdot 114.22} = \frac{145.98}{145.98} \text{ ml/mol}$$

$$\overline{MW}_L = \frac{99.63}{.682 \text{ g/ml}} = 146.2 \text{ g/mol}$$

$$\frac{28316 \text{ ml/ft}^3}{42.57} = \frac{\text{lbm}}{3}$$

V_L 145.98 454 g/lbm ft

$$\begin{aligned}
 & \overline{MW}_v = y_{C6} MW_{C6} + y_{C8} MW_{C8} = .85(86.17) + .15(114.22) = 90.38 \\
 & p \frac{\overline{MW}_v}{RT} = \frac{1.0 \text{ atm}}{82.0575 \frac{\text{ml atm}}{\text{mol K}} \cdot 359 \text{ K}} = 0.00307 \text{ g/ml} = 0.19135 \text{ lbm}^3/\text{ft}
 \end{aligned}$$

Now we can determine flow rates

$$\begin{aligned}
 V &= \frac{F}{F} = \frac{10,000 \text{ lbmol/h}}{4000} = 2.5 \\
 W_v &= V \overline{MW}_v = 2.5 \cdot 90.38 = 225.95 \text{ lb/h}
 \end{aligned}$$

$$L = F - V = 6000 \text{ lbmol/h}, W_L = L \overline{MW}_L = 6000 \cdot 99.63 = 597,780 \text{ lb/h}$$

$$F_{iv} = \frac{W_L}{W_v} \sqrt{\frac{v}{L}} = \frac{597,780}{361,520} \sqrt{\frac{0.19135}{42.57}} = 0.111, nF_{iv} = 2.1995$$

$$\begin{aligned}
 K_{\text{drum}} \exp &= 1.87748 \cdot 0.81458 \cdot 2.1995 = 3.417 \\
 &= 0.01452 \cdot 2.1995^3 + 0.00101 \cdot 2.1995^4 = 0.423
 \end{aligned}$$

$$u_{\text{Perm}} = \frac{K_{\text{drum}}}{K} = \frac{0.423}{42.57} = 0.00993 \text{ ft/s}$$

$$\begin{aligned}
 A_{Cs} &= \frac{V \overline{MW}_v}{u_{\text{Perm}}} = \frac{4000 \cdot 90.38}{6.3 \cdot 3600 \cdot 0.19135} = 83.33 \text{ ft}^2
 \end{aligned}$$

$$D = \sqrt{4A_{Cs}/\pi} = \sqrt{4 \cdot 83.33 / \pi} = 10.3 \text{ ft. Use } 10.5 \text{ ft.}$$

L ranges from $3 \times 10.5 = 31.5 \text{ ft}$ to $5 \times 10.5 = 52.5 \text{ ft}$.

Note: This u_{Perm} is at 85% of flood. If we want to operate at lower % flood (say 75%)

$$u_{\text{Perm } 75\%} = 0.75/0.85 u_{\text{Perm } 85\%} = 0.75/0.85 \cdot 6.3 = 5.56 \text{ ft/s}$$

75% of flood, $A_{Cs} = 94.44$ which is $D = 10.96$ or 11.0 ft .

2.E3. *New problem 4th edition.* The difficulty of this problem is it is stated in weight units, but the VLE data is in molar units. The easiest solution path is to work in weight units, which requires converting some of the equilibrium data to weight units and replotting – good practice. The difficulty with trying to work in molar units is the ratio $L/V = 0.35/0.65 = 0.5385$ in weight units becomes in molar units,

$$\frac{L}{V} = \frac{L}{V} \frac{(MW)_{\text{vapor}}}{(MW)_{\text{liquid}}}, \text{ but } x \text{ and } y \text{ are not known the molecular weights are unknown.}$$

$$\frac{L}{V} = \frac{L}{V} \frac{(MW)_{\text{vapor}}}{(MW)_{\text{liquid}}}$$

In weight units, $V = F(V/F) = 2000 \text{ kg/h} (0.35) = 700 \text{ kg/h}$. $L = F - V = 1300 \text{ kg/h}$.

In weight units the equilibrium data (Table 2-7) can be converted as follows:

Basis: 1 mol, $x = 0.4$ and $y = 0.729$, $T = 75.3 \text{ C}$

Liquid: $0.4 \text{ mol methanol} \times 32.04 \text{ g/mol} = 12.816 \text{ g}$

$0.6 \text{ mol water} \times 18.016 \text{ g/mol} = 10.8096 \text{ g}$

Total = $23.6256 \text{ g} \rightarrow x = 0.5425 \text{ wt frac methanol}$

$$\begin{aligned} \text{Vapor: } 0.729 \text{ mol methanol} &= 23.357 \text{ g} \\ 0.271 \text{ mol water} &= \underline{4.881 \text{ g}} \\ &28.238 \text{ g} \rightarrow y = 0.8271 \text{ wt frac methanol.} \end{aligned}$$

Similar calculations for: 0.3 mole frac liquid give $x_{wt} = 0.433$ and $y_{wt} = 0.7793$, $T = 78.0$ C

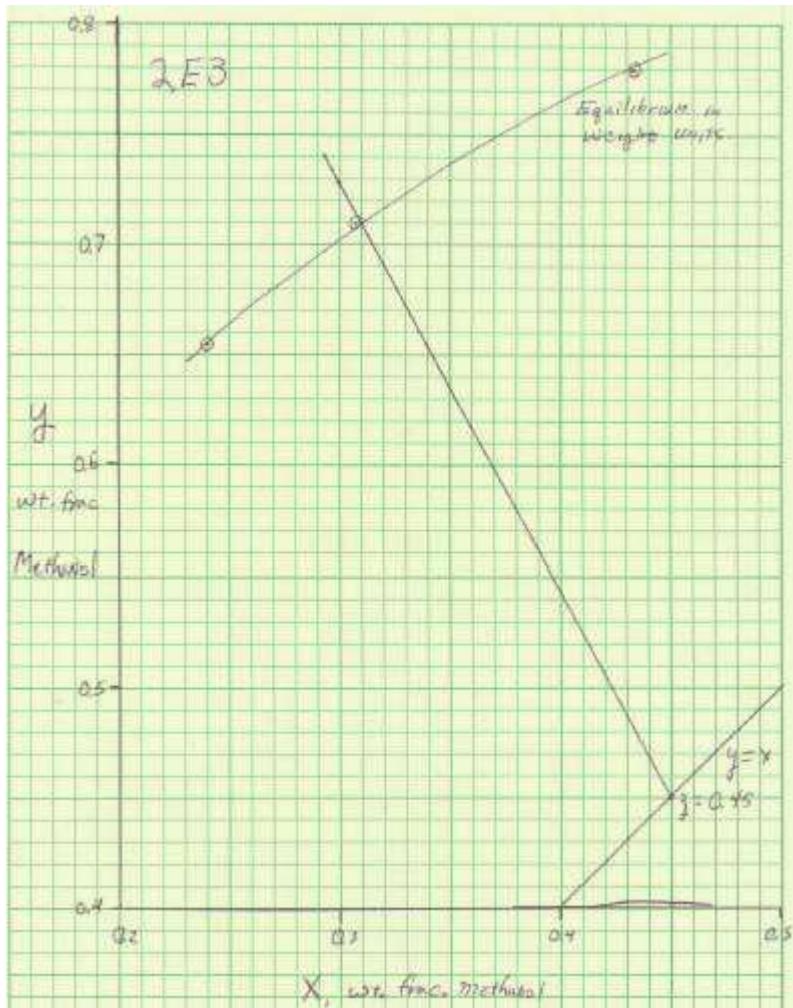
0.2 mole frac liquid give $x_{wt} = 0.3078$ and $y_{wt} = 0.7099$, $T = 81.7$ C

0.15 mole frac liquid give $x_{wt} = 0.2389$ and $y_{wt} = 0.6557$, $T = 84.4$ C.

Plot this data on y_{wt} vs x_{wt} diagram. Operating line is $y = -(L/V)x + (F/V)z$ in weight units.

Slope = - 1.857, $y = x = z = 0.45$, and y intercept = $z/(V/F) = 1.286$ all in weight units.

Result is $x_{M,wt} = 0.309$, $y_{M,wt} = 0.709$ (see graph). Note that plotting only the part of the graph needed to solve the problem, the scale could be increased resulting in better accuracy. By linear interpolation $T_{drum} = 81.66$ C.



2.F1

x_B	0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1
y_B	0	.22	.38	.52	.62	.71	.79	.85	.91	.96	1

Benzene-toluene equilibrium is plotted in Figure 13-8 of *Perry's Chemical Engineers Handbook*, 6th ed.

2.F2. See Graph. Data is from *Perry's Chemical Engineers Handbook*, 6th ed., p. 13-12.

Stage 1) $z_{F_1} = .4$ $f = 1/3$ Slope $\frac{2.3}{1.3} = 2$,
Intercept $\frac{.4}{1/3} = 1.2$ $y_1 = .872$ $x_1 = .164$ z_2

Stage 2) $z_{F_2} = .164$ $f = 2/3$ Slope $\frac{1.3}{2/3} = 1.95$
Intercept $\frac{.164}{2/3} = .246$ $x_2 = .01$ $y_2 = .240$ z_3

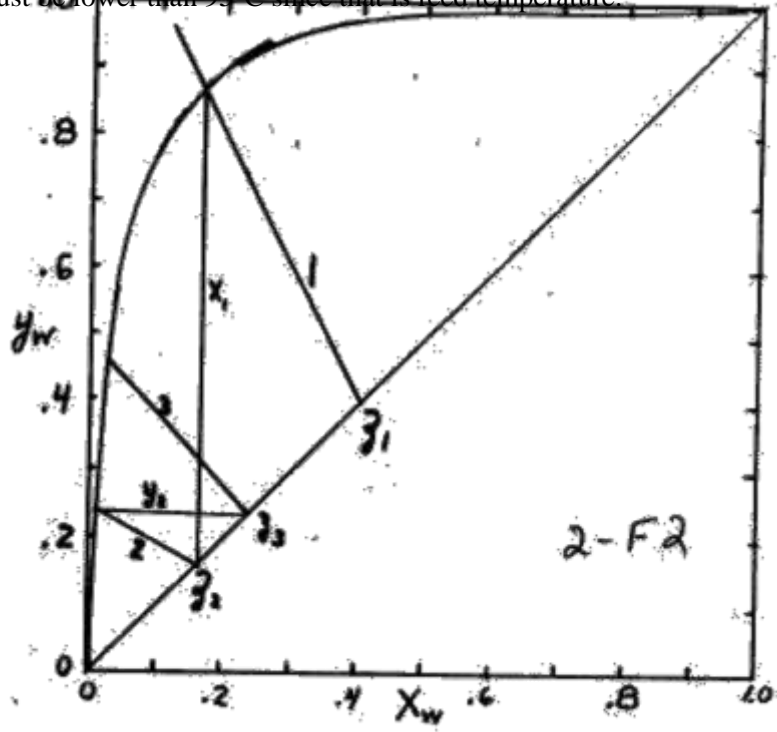
Stage 3) $z_{F_3} = .240$ $f = 1/2$ Slope 1
Intercept $\frac{.240}{1/2} = .480$ $x_3 = .022$ $y_3 = .461$

2.F3. *Bubble Pt.* At $P = 250$ kPa. Want $K_1 z_1 = 1$. Solution uses DePriester chart for K values.

Guess $T = 18$ C, $K_1 = 1$, $K_2 = .043$, $K_3 = .00095$, $z_1 = .52$
Converge to $T = 0$ C

Dew Pt. Calc. Want $\frac{z_1}{K_1} = 1.0$
Try $T = 0$ C, $K_1 = 1.93$, $K_2 = 0.11$, $K_3 = 0.0033$, $z_1 = 120.26$

Converge to $T = 124^\circ\text{C}$. This is a wide boiling feed.
 T_{drum} must be lower than 95°C since that is feed temperature.



First Trial: Guess $T_{d,1} = 70\text{ C} : K_1 = 7.8, K_2 = 1.07, K_3 = .083$

Guess $V/F = 0.5$. Rachford Rice Eq.

$$f = \frac{V/F}{V/F + 1} = \frac{0.5}{0.5 + 1} = 0.333$$

$$V/F = 0.6 \text{ gives } f = 0.36$$

By linear interpolation: $V/F = 0.56, f = 0.56 \cdot 0.0016$ which is close enough for first trial.

$$V = V/F \cdot F = 0.56 \cdot 44 = 24.64$$

$$x_i = \frac{z_i}{1 + K_i(V/F)} \text{ and } y_i = K_i x_i$$

$$x_1 = 0.1075, x_2 = 0.088, x_3 = 0.806, x_4 = 1.001$$

Data: Pick $T_{ref} = 25\text{ C}$. (Perry's 6th ed; p. 3-127), and (Perry's 6th ed; p. 3-138)

$$\begin{aligned} 1 & 81.76 \text{ cal/g} & 44 & 3597.44 \text{ kcal/kmol} \\ 2 & 87.54 \text{ cal/g} & 72 & 6302.88 \text{ kcal/kmol} \\ 3 & 86.80 \text{ cal/g} & 114 & 9895.2 \text{ kcal/kmol} \end{aligned}$$

at $T = 0\text{ C}, C_{pL1} = 0.576 \text{ cal / (g C)}, 44 = 25.34 \text{ kcal/(kmol C)}$.

For $T = 20 \text{ to } 123\text{ C}, C_{pL3} = 65.89 \text{ kcal/(kmol C)}$

at $T = 75\text{ C}, C_{pL2} = 39.66 \text{ kcal/(kmol C)}$. (Himmelblau/Appendix E-7)

$$C_{pv} = a + bT + cT^2$$

propane	$a = 16.26$	$b = 5.398 \times 10^{-2}$	$c = -3.134 \times 10^{-5}$
n-pentane	$a = 27.45$	$b = 8.148 \times 10^{-2}$	$c = -4.538 \times 10^{-5}$
**n-octane	$a = 8.163$	$b = 140.217 \times 10^{-3}$	$c = -44.127 \times 10^{-6}$

** Smith & Van Ness p. 106

$$\text{Energy Balance: } E(T_d) = V H_v + L h_L - F h_F = 0$$

$$F h_F = 100 \cdot 0.577 \cdot 25.34 + 0.091 \cdot 39.66 \cdot 392 + 65.89 \cdot 95.25 = 297,773 \text{ kcal/h}$$

$$L h_L = 44 \cdot 0.1075 \cdot 25.34 + 0.088 \cdot 39.66 \cdot 72 + 0.806 \cdot 65.89 \cdot 114 = 117,450$$

$$V H_v = 56 \cdot 0.839 \cdot 3597.4 + 16.26 \cdot 5.398 \cdot 10^2 \cdot 45 = 45,067$$

$$0.67 \cdot 9895.3 + 8.163 \cdot 140.217 \cdot 10^3 = 45240,423$$

$E(T_{drum}) = 60,101$ Thus, T_{drum} is too high.

Converge on $T_{drum} = 57.2\text{ C} : K_1 = 6.4, K_2 = .8, K_3 = .054$

For $V/F = 0.513, f = 0.513 \cdot 0.0027 = 0.0013851$. $V = 51.3, L = 48.7$

x_1 .137, x_2 .101, x_3 .762, x_1 1.0000
 y_1 .878, y_2 .081, y_3 .041, y_1 1.0000

$$Fh_F = 297,773; Lh_L = 90,459; Vh_V = 209,999; E T_{\text{drum}} = 2685$$

Thus T_{drum} must be very close to 57.3°C .

$$x_1 = .136, x_2 = .101, x_3 = .762, y_1 = .328, y_2 = .081, y_3 = .041$$

$$V = 51.3 \text{ kmol/h}, L = 48.7 \text{ kmol/h}$$

Note: With different data T_{drum} may vary significantly.

2.F4. *New Problem 4th edition.* This is a mass and energy balance problem disguised as a flash distillation problem. Data is readily available in steam tables. At 5000 kPa and 500K the feed is a liquid, $h_F = 17.604 \text{ kJ/mol}$. For an adiabatic flash, $h_F = [Vh_V + Lh_L]/F$
 Vapor and liquid are in equilibrium. Saturated steam at 100 kPa is at $T = 372.76\text{K}$, $h_L = 7.5214 \text{ kJ/mol}$, $h_V = 48.19 \text{ kJ/mol}$

Mass balance: $F = V + L$ where F in $\text{kmol/min} = (1500 \text{ kg/min})(1 \text{ kmol}/18.016 \text{ kg}) = 83.259 \text{ kmol/min}$
 EB: $Fh_F = Vh_V + Lh_L \rightarrow$
 $(83.259 \text{ kmol/min})(17.604 \text{ kJ/mol})(1000 \text{ mol/kmol}) = (48.19)(1000)V + (7.5214)(1000)L$.
 Solve equations simultaneously. $L = 62.617 \text{ kmol/min} = 1128.12 \text{ kg/min}$ and $V = 20.642 \text{ kmol/min} = 371.88 \text{ kg/min}$

2.G1. Used Peng-Robinson for hydrocarbons.

$$\text{Find } T_{\text{drum}} = 33.13 \text{ C}, L = 34.82 \text{ and } V = 65.18 \text{ kmol/h}$$

In order ethylene, ethane, propane, propylene, n-butane, x_i (y_i) are:
 0.0122 0.0748, 0.0866 0.3005, 0.3318 0.3781, 0.0306 0.0404, 0.5388 0.2062.

2.G2. *New problem in 4th edition.* Part a. $p = 31.26 \text{ kPa}$ with $(V/F)_{\text{feed}} = 0.0009903$.

Part b. Use $p_{\text{feed}} = 31.76 \text{ kPa}$, $(V/F)_{\text{feed}} = 0.0$

Part c. Drum $p = 3.9 \text{ bar}$, $T_{\text{drum}} = 19.339$, $V/F = 0.18605$,

Liquid mole fractions: $C_1 = 0.14663$, $C_2 = 0.027869$ ($\sum = 0.05253$ is in spec), $C_5 = 0.6171$, $C_6 = 0.3404$.

Vapor mole fractions: $C_1 = 0.68836$, $C_2 = 0.20057$, $C_5 = 0.9523$, and $C_6 = 0.01584$.

2.G3. *New problem 4th edition.* K values in Aspen Plus are higher by 17.6% (methane), 7.04% (n-butane) and 0.07% n-pentane. Since the K values are higher V/F is higher by 10.2%.

Results:

	x	y	K
Methane	0.004599	0.27039	58.79
n-butane	0.44567	0.52474	1.1774
n-pentane	0.54973	0.20488	0.37269

$$(V/F)_{\text{drum}} = 0.43419; (V/F)_{\text{feed}} = 0.3654; Q = -3183.4 \text{ cal/s}$$

2.G4.

COMP	x(I)	y(I)
METHANE	0.12053E-01	0.84824
BUTANE	0.12978	0.78744E-01
PENTANE	0.29304	0.47918E-01
HEXANE	0.56513	0.25101E-01
V/F = 0.58354		

2.G5. *N.* Used NRTL. $T = 368.07$, $Q = 14889 \text{ kW}$, 1^{st} liquid/total liquid = 0.4221,

Comp	Liquid 1, x_1	Liquid 2, x_2	Vapor, y
------	-----------------	-----------------	------------

Furfural	0.630	0.0226	0.0815
Water	0.346	0.965	0.820
Ethanol	0.0241	0.0125	0.0989

2.G6. Used Peng Robinson. Feed pressure = 10.6216 atm, Feed temperature = 81.14°C, V/F = 0.40001, Q_{drum} = 0. There are very small differences in feed temperature with different versions of AspenPlus.

COMP	x(I)	y(I)
METHANE	0.000273	0.04959
BUTANE	0.18015	0.47976
PENTANE	0.51681	0.39979
HEXANE	0.30276	0.07086
V/F = 0.40001		

2.H1. New Problem 4th ed A. 563.4 R, b.V/F = .4066. c. 18.264 psia

2.H3. New Problem. 4th ed. Answer V/F = 0.564; x_E = 0.00853, x_{hex} = 0.421, x_{hept} = .570; y_E = .421,

y_{Hex} = 0.378, y_{Hept} = .201.

2H4. New Problem, 4th ed. Answer: p_{drum} = 120.01, kPa = 17.40 psia

x_B = 0.1561, x_{pen} = 0.4255, x_{hept} = 0.4184, y_B = 0.5130, y_{Pen} = 0.4326, y_{hept} = 0.0544

2H5. New problem 4th ed.

- SOLUTION. P = 198.52 kPa.
- V/F = 0.24836, ethane x = 0.00337, y = 0.0824; Propane x = 0.05069, y = 0.3539; Butane x = 0.1945, y = 0.3536; Pentane x = 0.3295, y = 0.1584; Hexane x = 0.3198, y = 0.0469; Heptane x = 0.1022, y = 0.00464
- T = 34.48°C
- T = -1.586°C and V/F = 0.0567

2H6. New problem in 4th ed.

	A	B	C	D	E	F	G	H	I	J
1										
2	Example 2-2 on spreadsheet									
3	K1	7 K2	2.4 K3	0.8 K4	0.3					
4	z1	0.3 z2	0.1 z3	0.15 z4	0.45					
5	Guess V/F	0.500823								
6	x1	0.074908 x2	0.058784 x3	0.166697 x4	0.692922					
7	y1	0.524353 y2	0.141081 y3	0.12 y4	0.207877	sum ↓				
8	y _k -x _i	0.449445	0.082297	-0.0467	-0.48505	-2.1E-07				
9						chk			-0.00021	
10		Goal seek 9I to zero by changing B5								