# Solution Manual for Statistics Informed Decisions Using Data 5th Edition Sullivan III 9780134133539 

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## Chapter 2 <br> Organizing and Summarizing Data

## Section 2.1

1. Raw data are the data as originally collected, before they have been organized or coded.
2. Number (or count); proportion (or percent)
3. The relative frequencies should add to 1 , although rounding may cause the answers to vary slightly.
4. A bar graph is used to illustrate qualitative data. It is a chart in which rectangles are used to illustrate the frequency or relative frequency with which a category appears. A Pareto chart is a bar chart with bars drawn in order of decreasing frequency or relative frequency.
5. (a) The largest segment in the pie chart is for "Washing your hands" so the most commonly used approach to beat the flu bug is washing your hands. $61 \%$ of respondents selected this as their primary method for beating the flu.
(b) The smallest segment in the pie chart is for "Drinking Orange Juice" so the least used method is drinking orange juice. $2 \%$ of respondents selected this as their primary method for beating the flu.
(c) $25 \%$ of respondents felt that flu shots were the best way to beat the flu.
6. (a) $\frac{128,000}{1,350,000} \approx 0.0948$; approximately $9.48 \%$ of cosmetic surgeries in 2009 were for tummy tucks.
(b) $\frac{138,000}{} \approx 0.102$; approximately 10.2\% 1,350,000
of cosmetic surgeries in 2009 were for nose reshaping.
(c) The graph accounts for $312,000+$ 284,000
$+150,000+138,000+128,000=$ $1,012,000$ surgeries. Thus, $1,350,000-$ $1,012,000=338,000$ surgeries are not accounted for in the graph.
7. (a) The highest bar corresponds to the position OF (outfield), so OF is the position with the most MVPs.
(b) The bar for first base (1B) reaches the line for 15 . Thus, there were 15 MVPs who played first base.
(c) The bar for outfield (OF) is 30 on the vertical axis. The bar for first base (1B) reaches 15 . Since $30-15=15$, there were 15 more MVPs who played outfield than first base.
(d) Each of the three outfield positions should be reported as MVPs, rather than treating the three positions as one position.
8. (a) $29,936,000$ whites were living in poverty.
(b) $12745 /(29936+11041+12745+1974)=$ $0.229=22.9 \%$
In 2013, about $22.9 \%$ of the impoverished in the United States were Hispanic.
(c) This graph should use relative frequencies, rather than frequencies. The graph does not account for the different population size of each ethnic group. Without knowing the population sizes, we cannot determine whether a group is disproportionally impoverished.
9. (a) $69 \%$ of the respondents believe divorce is morally acceptable.
(b) $23 \%$ believe divorce is morally wrong. So, 240 million * $0.23=55.2$ million adult Americans believe divorce is morally wrong.
(c) This statement is inferential, since it is a generalization based on the observed data.
10. (a) $5 \%$ of identity theft was loan fraud.
(b) $26 \%$ of the identity fraud cases in a recent year involved credit card fraud. So, 10 million $* 0.26=2.6$ million cases of credit card fraud occurred in a recent year.
11. (a) The proportion of 18-34 year old respondents who are more likely to buy when made in America is 0.42 . For 34-44 year olds, the proportion is 0.61 .
(b) The 55+ age group has the greatest proportion of respondents who are more likely to buy when made in America.
(c) The 18-34 age group has a majority of respondents who are less likely to buy when made in America.
(d) As age increases, so does the likelihood that a respondent will be more likely to buy a product that is made in America.
12. (a) The proportion of males who would like to be richer is 0.46 . The proportion of females who would like to be richer is 0.41 .
(b) The attribute that females desire more than males is to be thinner.
(c) The attribute that males prefer over females two-to-one is to be younger.
(d) Equal proportions of males and females desire to be smarter.
13. (a) Total students surveyed $=125+324+$ $552+1257+2518=4776$ Relative frequency of "Never"
$=125 / 4776 \approx 0.0262$, and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| Never | 0.0262 |
| Rarely | 0.0678 |
| Sometimes | 0.1156 |
| Most of the time | 0.2632 |
| Always | 0.5272 |

(b) $52.72 \%$
(c) $0.0262+0.0678=0.0940$ or $9.40 \%$


(f) "How Often Do You Wear Your Seat Belt?"

(g) The statement is inferential since it is inferring something about the entire population based on the results of a sample survey.
14. (a) Total students surveyed $=249+118+$ $249+345+716+3093=4770$
Relative frequency of "I do not drive" $=\frac{249}{4770} \approx 0.0522$, and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| I do not drive | 0.0522 |
| Never | 0.0247 |
| Rarely | 0.0522 |
| Sometimes | 0.0723 |
| Most of the time | 0.1501 |
| Always | 0.6484 |

(b) $64.84 \%$
(c) $0.0247+0.0522=0.0769$ or $7.7 \%$
(d)

(e)

(f)
"How Often Do You Wear a Seat Belt When Driving a Car?"

(g) Total students $=118+249+345+716+$ $3093=4521$
Relative frequency of "Never"
$=\frac{118}{4521} \approx 0.0261$, and so on.

| Response | Relative Frequency |
| :---: | :---: |
| Never | 0.0261 |
| Rarely | 0.0551 |
| Sometimes | 0.0763 |
| Most of the time | 0.1584 |
| Always | 0.6841 |

The relative frequencies of all categories are very similar except that students are more likely to wear their seatbelt 'Always' when driving.
(h) The statement is descriptive because it is describing the particular sample.
15. (a) Total adults surveyed $=377+192+132$ $+81+243=1025$
Relative frequency of "More than 1 hour a day" $=377 / 1025 \approx 0.3678$, and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| More than 1 hr a day | 0.3678 |
| Up to 1 hr a day | 0.1873 |
| A few times a week | 0.1288 |
| A few times a month or less | 0.0790 |
| Never | 0.2371 |

(b) 0.2371 (about 24\%)
(c)

(d)

(e)

(f) The statement provides an estimate, but no level of confidence is given.
16. (a) Total adults surveyed $=103+204+130$
$+79+5=521$
Relative frequency of "Several times a week" $=\frac{103}{521} \approx 0.197$, and so on.

Relative

| Response | Relative <br> Frequency |
| :--- | :---: |
| Several times a week | 0.197 |
| Once or twice a week | 0.392 |
| A few times a month | 0.250 |
| Vary rarely | 0.152 |
| Never | 0.010 |

(b) The proportion surveyed who dine out once or twice a week is $204 /(103+204+130+79+5)=0.392$

How Often Do You Dine Out?

(c)

How Often Do You Dine Out?

17. (a) Total adults $=1936$

Relative frequency for "none" is:
$173 / 1936=0.09$, and so on.

| Number of Texts | Rel. Freq. (Adults) |
| :--- | :---: |
| None | 0.089 |
| 1 to 10 | 0.505 |
| 11 to 20 | 0.129 |
| 21 to 50 | 0.129 |
| 51 to 100 | 0.069 |
| $101+$ | 0.079 |

(b) Total teens $=627$

Relative frequency for "none" is: $13 / 627=0.021$, and so on.

Number of Texts
Rel. Freq. (Teens)

| None | 0.021 |
| :--- | :--- |
| 1 to 10 | 0.220 |
| 11 to 20 | 0.110 |
| 21 to 50 | 0.180 |
| 51 to 100 | 0.180 |
| $101+$ | 0.289 |

Number of Texts Each Day

(d) Answers will vary. Adults are much more likely to send fewer texts per day, while teens are much more likely to do more texting.
18. (a), (b)

Total males $=99.4$ million
Relative frequency for "Not HS graduate" is $12.3 / 99.4=0.124$, and so on.

Total females $=107.6$ million Relative frequency for "Not HS graduate" is $12.2 / 107.6=0.113$, and so on.

| Educational Attainment | Males | Females |
| :--- | :---: | :---: |
| Not a HS graduate | 0.124 | 0.113 |
| High school graduate | 0.302 | 0.295 |
| Some college, no degree | 0.166 | 0.170 |
| Associate's degree | 0.089 | 0.108 |
| Bachelor's degree | 0.200 | 0.202 |
| Advanced degree | 0.120 | 0.112 |

(c)

Educational Attainment, 2009

(d) Answers will vary. It appears that females are slightly more likely to start, but not finish college. Males appear to be slightly more likely to attain an advanced degree.
19. (a) Total males $=99$; Relative frequency for "Professional Athlete" is $40 / 99=0.404$, and so on.

Total number of females $=100$; Relative frequency for "Professional Athlete" is $18 / 100=0.18$, and so on.

| Dream Job | Men | Women |
| :--- | :---: | :---: |
| Professional Athlete | 0.404 | 0.180 |
| Actor/Actress | 0.263 | 0.370 |
| President of the | 0.131 | 0.130 |
| United States |  |  |
| Rock Star | 0.131 | 0.130 |
| Not Sure | 0.071 | 0.190 |

(b)

Dream Job

(c) Answers will vary. Males are much more likely to want to be a professional athlete. Women are more likely to aspire to a career in acting than men. Men's desire to
careers in acting due to the perceived glamour of famous female actresses.
20. (a) Relative frequency for "White" luxury cars $=\frac{25}{100}=0.25$, and so on.

Relative frequency for "White" sport cars $=\frac{10}{100}=0.10$, and so on.

Relative Frequencies

| Color | Luxury Cars | Sport Cars |
| :---: | :---: | :---: |
| White | 0.25 | 0.10 |
| Black | 0.22 | 0.15 |
| Silver | 0.16 | 0.18 |
| Gray | 0.12 | 0.15 |
| Blue | 0.07 | 0.13 |
| Red | 0.07 | 0.15 |
| Gold | 0.06 | 0.05 |
| Green | 0.03 | 0.02 |
| Brown | 0.02 | 0.07 |

(b)

Car Color

become athlete $\S$ भfflay be influenced by the prominence of male sporting figures in popular culture. Women may aspire to
(c) Answers will vary. White is the most popular color for luxury cars, while silver is the most popular for sports cars. People who drive luxury cars may enjoy the clean look of a white vehicle. People who drive sports cars may prefer the flashier look of silver.
21. (a), (b)

Total number of Trading Days $=30$; relative frequency for Down is $15 / 30=$ 0.5 , and so on.

| Winner | Freq. | Rel. Freq. |
| :--- | :---: | :---: |
| Down | 15 | 0.500 |
| No Change | 2 | 0.067 |
| Up | 13 | 0.433 |

(c)

Daily Price Change of Walt Disney Stock

(d)

Daily Price Change of Walt Disney Stock

(e)

22. (a), (b) Total number of responses $=25$; relative frequency for "edit details" is $7 / 25=0.28$.

| Response | Freq. | Rel. Freq. |
| :--- | :---: | :---: |
| Edit details | 7 | 0.28 |
| Say nothing | 4 | 0.16 |
| Tell all | 14 | 0.56 |

(c)

Bachelor Party Details to Fiancé

(d)

Bachelor Party Details to Fiancé

(e)

Bachelor Party Details to Financé

23. (a), (b)

Total number of responses $=40$; relative frequency for "Sunday" is $3 / 40=0.075$.

Response Freq. Rel. Freq.

| Sunday | 3 | 0.075 |
| :--- | :---: | :---: |
| Monday | 2 | 0.050 |
| Tuesday | 5 | 0.125 |
| Wednesday | 6 | 0.150 |
| Thursday | 2 | 0.050 |
| Friday | 14 | 0.350 |
| Saturday | 8 | 0.200 |

(c) Answers will vary. If you own a restaurant, you will probably want to advertize on the days when people will be most likely to order takeout: Friday. You might consider avoiding placing an ad on Monday and Thursday, since the readers are least likely to choose to order takeout on these days.
(d)

(e)

Favorite Day to Eat Out

24. (a), (b)

Total number of patients $=50$
Relative frequency for "Type A"
$=\frac{18}{50}=0.36$, and so on.

| Blood Type | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| A | 18 | 0.36 |
| AB | 4 | 0.08 |
| B | 6 | 0.12 |
| O | 22 | 0.44 |

(c) Type O is the most common.
(d) Type AB is the least common.
(e) We estimate that $44 \%$ of the population has type O blood. This is considered inferential statistics because a conclusion about the population is being drawn based on sample data.
(f) Answers will vary; in 2008 the Red Cross reported that $45 \%$ of the population had type O blood (either + or - ). Results will differ because of sampling variability.

(g)
(h)

(f)


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Blood Types

25. (a)

| State | AR | CA | CT | GA | HI | IL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 1 | 1 | 1 | 1 | 1 | 1 |


| State | IA | KY | MA | MO | NE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 1 | 1 | 4 | 1 | 1 |


| State | NH | NJ | NY | NC | OH |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 1 | 2 | 4 | 2 | 7 |


| State | PA | SC | TX | VT | VA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 1 | 1 | 2 | 2 | 8 |

The U.S. Presidents' Birthplaces

(b) More presidents were born in Virginia than in any other state.
(c) Answers will vary. The data do not take the year of statehood into account. For example, Virginia has been a state for roughly 62 years more than California. The population of the United States was more concentrated in the east in the early years, so it was more likely that the president would be from that part of the country.
26. (a) It would make sense to draw a pie chart for land area since the 7 continents contain all the land area on Earth.
Total land area is $11,608,000+5,100,000$
$+\ldots+9,449,000+6,879,000=$
$57,217,000$ square miles.
The relative frequency (percentage) for
Africa is $\frac{11,608,000}{57,217,000}=0.2029$.

| Continent | Land Area <br> $\left(\mathrm{mi}^{2}\right)$ | Rel. Freq. |
| :---: | :---: | :---: |
| Africa | $11,608,000$ | 0.2029 |
| Antarctica | $5,100,000$ | 0.0891 |
| Asia | $17,212,000$ | 0.3008 |
| Australia | $3,132,000$ | 0.0547 |
| Europe | $3,837,000$ | 0.0671 |
| North America | $9,449,000$ | 0.1651 |
| South America | $6,879,000$ | 0.1202 |


(b) It would not make sense to draw a pie chart for the highest elevation because there is no whole to which to compare the parts.
27. Answers will vary.
28. Answers will vary.
29. (a) The researcher wants to determine if online homework improves student learning over traditional pencil-and-paper homework.
(b) This study is an experiment because the researcher is actively imposing treatments (the homework style) on subjects.
(c) Answers will vary. Some examples are same teacher, same semester, and same course.
(d) Assigning different homework methods to entire classes could confound the results because there may be differences between the classes. The instructor may give more instruction to one class than the other. The instructor is not blinded, so he or she may treat one group differently from the other.
(e) Number of students: quantitative, discrete Average age: quantitative, continuous Average exam score: quantitative, continuous
Type of homework: qualitative
College experience: qualitative
(f) Letter grade is a qualitative variable at the ordinal level of measurement. Answers will vary. It is possible that ordering the data from A to F is better because it might give more "weight" to the higher grade and the researcher wants to show that a higher percent of students passed using the online homework.
(g) The graph being displayed is a side-byside relative frequency bar graph.
(h) Yes; the "whole" is the set of students who received a grade for the course for each homework method.
(i) The table shows that the two groups with no prior college experience had roughly
the same average exam grade. From the bar graph, we see that the students using online homework had a lower percent for As, but had a higher percent who passed
with a C or better.
30. Relative frequencies should be used when the size of two samples or populations differ.
31. Answers will vary. If the goal is to illustrate the levels of importance, then arranging the bars in a bar chart in decreasing order makes sense. Sometimes it is useful to arrange the categorical data in a bar chart in alphabetical
helpful for comparing parts of a whole. A pie chart cannot be drawn if the data do not include all possible values of the qualitative variable.
33. No, the percentages do not sum to $100 \%$.

## Section 2.2

1. classes
2. lower; upper
3. class width
4. Skewed left means that the left tail is longer than the right tail.
5. True
6. False
7. False. The distribution shape shown is skewed right.
8. False. The distribution shape is bell-shaped.
9. (a) The value with the highest frequency is 8 .
(b) The value with the lowest frequency is 2 .
(c) The value of 7 was observed 15 times.
(d) The value of 5 was observed 11 times and the value of 4 was observed 7 times. Therefore, the value of 5 was observed 4 more times than the value of 4 (e.g. $11-7=4$ ).
(e) $\frac{15}{100}=0.15$ or $15 \%$ of the time a 7 was observed.
order. A pie chart does not readily allow for arranging the data in order.
10. A bar chart is preferred when trying to compare two specific values. Pie charts are
(f) The distribution is approximately bellshaped.
11. (a) The most frequent number of cars sold in a week was 4 cars.
(b) There were 9 weeks in which 2 cars sold.
(c) Total frequency $=4+2+9+8+12+8+$ $5+2+1+1=52$ (as required)
Percentage of time two cars are sold
$=\begin{gathered}9 \\ 52\end{gathered} \cdot 100=17.3 \%$
(d) Slightly skewed to the right
12. (a) Total frequency $=2+3+13+42+58+$ $40+31+8+2+1=200$
(b) 10 (e.g. $70-60=10$ )
(c)

| IQ Score (class) | Frequency |
| :---: | :---: |
| $60-69$ | 2 |
| $70-79$ | 3 |
| $80-89$ | 13 |
| $90-99$ | 42 |
| $100-109$ | 58 |
| $110-119$ | 40 |
| $120-129$ | 31 |
| $130-139$ | 8 |
| $140-149$ | 2 |
| $150-159$ | 1 |

(d) The class " $100-109$ " has the highest frequency.
(e) The class " $150-159$ " has the lowest frequency.
(f) $\frac{8+2+1}{200}=0.055=5.5 \%$
(g) No, there were no IQs above 159.
12. (a) The class width is 200 (e.g. $200-0=$ 200).
(b) 0-199, 200-399, 400-599, 600-799, 800-999, 1000-1199, 1200-1399
(c) The highest frequency is in class 0-199.
(d) The distribution is skewed right.
(e) Answers will vary. The statement is incorrect because they are comparing counts from populations of different size. To make a fair comparison, the reporter should use rates of fatalities such as the number of fatalities per 1000 residents.
13. (a) Likely skewed right. Most household incomes will be to the left (perhaps in the
$\$ 50,000$ to $\$ 150,000$ range), with fewer higher incomes to the right (in the millions).
(c) Likely skewed right. Most households will have, say, 1 to 4 occupants, with fewer households having a higher number of occupants.
(d) Likely skewed left. Most Alzheimer's patients will fall in older-aged categories, with fewer patients being younger.
14. (a) Likely skewed right. More individuals would consume fewer alcoholic drinks per week, while less individuals would consume more alcoholic drinks per week.
(b) Likely uniform. There will be approximately an equal number of students in each age category.
(c) Likely skewed left. Most hearing-aid patients will fall in older-aged categories, with fewer patients being younger.
(d) Likely bell-shaped. Most heights will occur, say, in the 66- to 70 -inch range, with heights tapering off equally in both directions.
15. (a) Total number of households $=$
$16+18+12+3+1=50$
Relative frequency of 0 children $=16 / 50$ $=0.32$, and so on.

| Number of Children <br> Under Five | Relative <br> Frequency |
| :---: | :---: |
| 0 | 0.32 |
| 1 | 0.36 |
| 2 | 0.24 |
| 3 | 0.06 |
| 4 | 0.02 |

(b) $\frac{12}{50}=0.24$ or $24 \%$ of households have two children under the age of 5 .
(c) $\frac{18+12}{50}=\frac{30}{50}=0.6$ or $60 \%$ of households
(b) Likely bell-shaped. Most scores will occur near the middle range, with scores
tapering off equally in both directions.
have one or two children under the age of 5 .
16. (a) Total number of free throws $=$ $16+11+9+7+2+3+0+1+0+1=50$. Relative frequency of 1 throw until a miss $=16 / 50=0.32$, and so on.

| Number of Free <br> Throws Until a Miss | Relative <br> Frequency |
| :---: | :---: |
| 1 | 0.32 |
| 2 | 0.22 |
| 3 | 0.18 |
| 4 | 0.14 |
| 5 | 0.04 |
| 6 | 0.06 |
| 7 | 0.00 |
| 8 | 0.02 |
| 9 | 0.00 |
| 10 | 0.02 |

(b) $\frac{7}{50}=0.14 ; 14 \%$ of the time she first missed on the fourth try.
(c) $\frac{1}{50}=0.02 ; 2 \%$ of the time she first missed on the tenth try.
(d) "At least 5" means that the basketball player misses on the $6^{\text {th }}$ shot or $7^{\text {th }}$ shot or
$8^{\text {th }}$, etc. $\frac{3+0+1+0+1}{50}=\frac{5}{50}=0.10$ or $10 \%$ of the time.
17. From the legend, $1 \mid 0$ represents 10 , so the original data set is $10,11,14,21,24,24,27$, $29,33,35,35,35,37,37,38,40,40,41,42$, $46,46,48,49,49,53,53,55,58,61,62$.
18. From the legend, $24 \mid 0$ represents 240 , so the original data set is $240,244,247,252,252$, 253, 259, 259, 263, 264, 265, 268, 268, 269, 270, 271, 271, 273, 276, 276, 282, 283, 288.
19. From the legend, $1 \mid 2$ represents 1.2 , so the original data set is $1.2,1.4,1.6,2.1,2.4,2.7$, $2.7,2.9,3.3,3.3,3.3,3.5,3.7,3.7,3.8,4.0$, 4.1, 4.1, 4.3, 4.6, 4.6, 4.8, 4.8, 4.9, 5.3, 5.4, 5.5, 5.8, 6.2, 6.4.
20. From the legend, $12 \mid 3$ represents 12.3 , so the original data set is $12.3,12.7,12.9,12.9,13.0$, $13.4,13.5,13.7,13.8,13.9,13.9,14.2,14.4$,
21. (a) There are six classes.
(b) Lower class limits: $10,14,18,22,26,30$ Upper class limits: $13.9,17.9,21.9,25.9$, 29.9, 33.9
(c) The class width can be found by subtracting consecutive lower class limits. For example, $14-10=4$. Therefore, the class width is 4 (players).
22. (a) There are eight classes.
(b) Lower class limits: $0,1.0,2.0,3.0,4.0$, 5.0, 6.0, 7.0

Upper class limits: $0.9,1.9,2.9,3.9,4.9$, 5.9, 6.9, 7.9
(c) The class width can be found by subtracting consecutive lower class limits. For example, $2.0-1.0=1.0$. Therefore, the class width is 1.0 .
23. (a) Total frequency $=$
$4+7+17+91+282+206=607$
Relative frequency for $10-13.9$ is $4 / 607=0.0066$, and so on.

| Speed (Km/hr) | Relative <br> Frequency |
| :---: | :---: |
| $10-13.9$ | 0.0066 |
| $14-17.9$ | 0.0115 |
| $18-21.9$ | 0.0280 |
| $22-25.9$ | 0.1499 |
| $26-29.9$ | 0.4646 |
| $30-33.9$ | 0.3394 |

$14.4,14.7,14.7,14.8,14.9,15.1,15.2,15.2$, 15.5, 15.6, 16.0, 16.3.
(b)



The percentage of players who had a top speed between 30 and $33.9 \mathrm{~km} / \mathrm{h}$ is $33.94 \%$. The percent of players who had a top speed less than $13.9 \mathrm{~km} / \mathrm{h}$ is $0.66 \%$.
24. (a) Total frequency $=$
$3371+3400+1237+286+1045+121$ $+7+2=9469$
Relative frequency for $0-0.9$ is $3371 / 9469=0.3561$, and so on.

| Magnitude | Relative <br> Frequency |
| :---: | :---: |
| $0-0.9$ | 0.3560 |
| $1.0-1.9$ | 0.3591 |
| $2.0-2.9$ | 0.1306 |
| $3.0-3.9$ | 0.0302 |
| $4.0-4.9$ | 0.1104 |
| $5.0-5.9$ | 0.0128 |
| $6.0-6.9$ | 0.0007 |
| $7.0-7.9$ | 0.0002 |

(b)

Magnitude of Earthquakes Worldwide: October 2014

(c)


The percentage of earthquakes that registered between 4.0 and $4.9 \mathrm{~km} / \mathrm{h}$ is $11.04 \%$. The percent of earthquakes that registered 4.9 or less is $98.63 \%$.
25. (a) The data are discrete. The possible values for the number of color televisions in a household are countable.
(b), (c)

The relative frequency for 0 color televisions is $1 / 40=0.025$, and so on.

| Number of <br> Color TVs | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| 0 | 1 | 0.025 |
| 1 | 14 | 0.350 |
| 2 | 14 | 0.350 |
| 3 | 8 | 0.200 |
| 4 | 2 | 0.050 |
| 5 | 1 | 0.025 |

(d) The relative frequency is 0.2 , so $20 \%$ of the households surveyed had 3 color televisions.
(e) $0.05+0.025=0.075$
$7.5 \%$ of the households in the survey had 4 or more color televisions.
(f)


(h) The distribution is skewed right.
26. (a) The data are discrete. The possible values for the number of customers waiting for a table are countable.
(b), (c)

Relative frequency of 3 customers waiting $=2 / 40=0.05$, and so on.

| Number of <br> Customers | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| 3 | 2 | 0.050 |
| 4 | 3 | 0.075 |
| 5 | 3 | 0.075 |
| 6 | 5 | 0.125 |
| 7 | 4 | 0.100 |
| 8 | 8 | 0.200 |
| 9 | 4 | 0.100 |
| 10 | 4 | 0.100 |
| 11 | 4 | 0.100 |
| 12 | 0 | 0.000 |
| 13 | 2 | 0.050 |
| 14 | 1 | 0.025 |

(d) $10.0+10.0+0.0+5.0+2.5=27.5 \%$ of the Saturdays had 10 or more customers waiting for a table at 6 p.m.
(e) $5.0+7.5+7.5=20.0 \%$ of the Saturdays had 5 or fewer customers waiting for a table at 6 p.m.
(f)
Customers Waiting for a Table

Customers Waiting for a Table
(g)

(h) The distribution is more or less symmetric.
27. (a), (b) Relative frequency of a Gini Index of $20-24.9=5 / 136=0.037$, and so on.

| Gini Index | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $20-24.9$ | 5 | 0.037 |
| $25-29.9$ | 16 | 0.118 |
| $30-34.9$ | 28 | 0.206 |
| $35-39.9$ | 27 | 0.199 |
| $40-44.9$ | 20 | 0.147 |
| $45-49.9$ | 17 | 0.125 |
| $50-54.9$ | 13 | 0.096 |
| $55-59.9$ | 5 | 0.037 |
| $60-64.9$ | 5 | 0.037 |


(c)
(d)

(e) The shape of the distribution is skewed right.
(f) Relative frequency of a Gini Index of $20-29.9=21 / 136=0.154$, and so on.

| Gini Index | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $20-29.9$ | 21 | 0.154 |
| $30-39.9$ | 55 | 0.404 |
| $40-49.9$ | 37 | 0.272 |
| $50-59.9$ | 18 | 0.132 |
| $60-69.9$ | 5 | 0.037 |



The shape of the distribution is skewed right.
(g) Answers will vary. The graph with a class width of 5 provides more detail, so it seems to be a superior graph.
28. (a), (b)

Relative frequency for the median income $35,000-39,999$ is
$2 / 51=0.0392$, and so on.

| Income | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $35,000-39,999$ | 2 | 0.0392 |
| $40,000-44,999$ | 10 | 0.1961 |
| $45,000-49,999$ | 5 | 0.0980 |
| $50,000-54,999$ | 15 | 0.2941 |
| $55,000-59,999$ | 6 | 0.1176 |
| $60,000-64,999$ | 9 | 0.1765 |
| $65,000-69,999$ | 3 | 0.0588 |
| $70,000-74,999$ | 1 | 0.0196 |


(c)

(e) The shape of the distribution is approximately symmetric.
(f) Relative frequency for the median income 35,000-44,999 is $12 / 51=0.2353$, and so on.

| Income | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $35,000-44,999$ | 12 | 0.2353 |
| $45,000-54,999$ | 20 | 0.3922 |
| $55,000-64,999$ | 15 | 0.2941 |
| $65,000-74,999$ | 4 | 0.0784 |



Distribution appears to be approximately symmetric, however, one could argue it is slightly skewed to the right (since the tail on the right is longer than the tail on the left).
(g) Answers will vary, but the graph with a class width of $\$ 5000$ seems to show more details about the data so it seems better.
29. (a), (b)

Total number of data points $=51$
Relative frequency of $0-0.499$ is $7 / 51=0.1373$, and so on.

| Cigarette <br> Tax | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $0.00-0.499$ | 7 | 0.1373 |
| $0.50-0.999$ | 13 | 0.2549 |
| $1.00-1.499$ | 7 | 0.1373 |
| $1.50-1.999$ | 8 | 0.1569 |
| $2.00-2.499$ | 5 | 0.0980 |
| $2.50-2.999$ | 5 | 0.0980 |
| $3.00-3.499$ | 3 | 0.0588 |
| $3.50-3.999$ | 2 | 0.0392 |
| $4.00-4.499$ | 1 | 0.0196 |

(c)

(d)

(e) The distribution appears to be right skewed.
(f) Relative frequency of 0-0.999 is: $20 / 51=0.3922$, and so on.

| Cigarette Tax | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $0.00-0.999$ | 20 | 0.3922 |
| $1.00-1.999$ | 15 | 0.2941 |
| $2.00-2.999$ | 10 | 0.1961 |
| $3.00-3.999$ | 5 | 0.0980 |
| $4.00-4.999$ | 1 | 0.0196 |



The distribution is right skewed.
(g) Answers will vary. The first distribution gives a more detailed pattern and does a nice job summarizing the data.
30. (a), (b)

Relative frequency for $0.00-0.39=7 / 28$ $=0.2500$, and so on.

| Dividend | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $0.00-0.39$ | 7 | 0.2500 |
| $0.40-0.79$ | 4 | 0.1429 |
| $0.80-1.19$ | 5 | 0.1786 |
| $1.20-1.59$ | 2 | 0.0714 |
| $1.60-1.99$ | 3 | 0.1071 |
| $2.00-2.39$ | 4 | 0.1429 |
| $2.40-2.79$ | 2 | 0.0714 |
| $2.80-3.19$ | 1 | 0.0357 |

Dividend Yield

(d)

Dividend Yield

(e) The distribution is skewed right.
(f) Relative frequency for $0.00-0.79=11 / 28$ $=0.3929$, and so on.

| Dividend | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $0.00-0.79$ | 11 | 0.3929 |
| $0.80-1.59$ | 7 | 0.2500 |
| $1.60-2.39$ | 7 | 0.2500 |
| $2.40-3.19$ | 3 | 0.1071 |

Dividend Yield


Dividend Yield


The distribution is skewed right.
(g) Answers will vary. Both distributions indicate the data are skewed right. The first graph is preferred because it gives more detailed information. The second graph is a little too compressed to get a complete view of what is happening with the data.
31. Answers will vary. One possibility follows.
(a) Choose a lower class limit of first class of 0 with a class width of 200 .
(b), (c)

Relative frequency for $0-199$ is $4 / 51=0.0784$, and so on.

| Violent <br> Crime Rate | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $0-199.9$ | 4 | 0.0784 |
| $200-399.9$ | 26 | 0.5098 |
| $400-599.9$ | 17 | 0.3333 |
| $600-799.9$ | 3 | 0.0588 |
| $800-999.9$ | 0 | 0.0000 |
| $1000-1199.9$ | 0 | 0.0000 |
| $1200-1399.9$ | 1 | 0.0196 |

Violent Crime Rate in 2013

(e)

Violent Crime Rate in 2013

32. Answers will vary. One possibility follows.
(a) We can determine a class width by subtracting the smallest value from the largest, dividing by the desired number of classes, then rounding up. For example, $\frac{23.59-6.37}{6}=2.87 \rightarrow 3$
Our first lower class limit should be a nice number below the smallest data value. In this case, 6 is a good first lower limit since it is the nearest whole number below the smallest data value. Thus, we will have a class width of 3 , and the first class will have a lower limit of 6 .
(b), (c)

Relative frequency for $6-8.99=15 / 35$ $=0.4286$, and so on.

| Volume | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $6-8.99$ | 15 | 0.4286 |
| $9-11.99$ | 9 | 0.2571 |
| $12-14.99$ | 4 | 0.1143 |
| $15-17.99$ | 4 | 0.1143 |
| $18-20.99$ | 2 | 0.0571 |
| $21-23.99$ | 1 | 0.0286 |

Daily Volume of Altria Stock

(e)

Daily Volume of Altria Stock

(f) The distribution is skewed right.
33. (a) President Ages at Inauguration

| 4 | 23 |
| :--- | :--- |
| 4 | 6677899 |


| 4 | 6677899 |
| :--- | :--- |
| 5 | 0011112244444 |

5555566677778
60111244
61589
Legend: 412 represents 42 years
(b) The distribution appears to be roughly symmetric and bell-shaped.
34. (a) Divorce Rates in 2011

| 2 | 4 |
| :--- | :--- |
| 2 | 677899999 |
| 3 | 12223344 |
| 3 | 56677888999 |
| 4 | 00123344 |
| 4 | 5889 |
| 5 | 223 |
| 5 | 6 |

Legend: 24 represents 2.4 per 1000 population
(b) The distribution appears to be roughly symmetric and bell-shaped. One could argue that the distribution is slightly skewed right.

## Fat in McDonald's Breakfast

0|39
11266
21224577
30012267
$4{ }^{4} 6$
51159
35. (a) Legend: 511 represents 51 grams of fat.
(b) The distribution appears to be roughly symmetric and bell-shaped.

## Gasoline Mileages

| 2 | 233 |
| :--- | :--- |
| 2 | 55567889999 |
| 3 | $000 \times 0111111111222223333333333334444444444444$ |
| 3 | 55555555566666666666778 |
| 4 | 0223 |

36. (a) Legend: 212 represents 22 mites per gallon.
(b) The distribution appears to be symmetric and bell-shaped.
37. (a) Five Year Rate of Return Rounded to the

| neerest tenth:2 | 12.4 | 13.6 | 13.0 |  |
| :---: | :---: | :---: | :---: | :---: |
| 10.5 | 10.3 | 13.1 | 15.7 | 14.9 |
| 14.1 | 12.8 | 13.3 | 9.9 | 15.6 |
| 12.3 | 13.9 | 13.4 | 19.4 | 13.4 |
| 12.2 | 14.8 | 11.9 | 10.1 | 13.6 |
| 14.6 | 14.8 | 13.5 | 13.9 | 13.2 |
| 14.0 | 15.2 | 8.3 | 9.0 | 8.7 |
| 14.9 | 16.0 | 13.7 | 13.9 | 12.8 |

(b) Five Year Rate of Return


Legend: $8 \mid 3$ represents $8.3 \%$
(c) The distribution is bell-shaped.
38. (a) Home appreciation values rounded to the nearest whole number:

| 69 | 149 | 94 | 118 | 87 |
| :---: | :---: | :---: | :---: | :---: |
| 113 | 130 | 65 | 113 | 109 |
| 350 | 122 | 104 | 94 | 101 |
| 185 | 150 | 225 | 117 | 107 |
| 136 | 135 | 113 | 87 | 113 |
| 115 | 197 | 71 | 96 | 91 |
| 85 | 105 | 210 | 109 | 125 |
| 220 | 136 | 127 | 110 | 87 |
| 75 | 105 | 104 | 97 | 133 |
| 207 | 93 | 80 | 145 | 67 |
| 80 |  |  |  |  |

Home Appreciation

```
579
15
005777
134467
14455799
03333578
257
03566
59
```

0

| 5 |
| :--- |
| 7 |
| 7 |
| 0 |
| 05 |

05
0

Legend: 6|5 represents 65
(b) The shape of the distribution is skewed to the right.
(c) Answers will vary. However, a histogram is probably a better choice because of the wide range of possible values.
39. (a) Violent crime rates rounded to the nearest tens:

| 450 | 1240 | 350 | 260 | 410 | 560 | 320 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 600 | 490 | 220 | 450 | 350 | 320 | 280 |
| 430 | 380 | 500 | 270 | 240 | 640 | 200 |
| 470 | 240 | 120 | 260 | 300 | 410 |  |
| 420 | 210 | 480 | 610 | 470 | 210 |  |
| 310 | 410 | 410 | 190 | 250 | 140 |  |
| 280 | 350 | 450 | 290 | 350 | 190 |  |
| 550 | 260 | 230 | 560 | 250 | 300 |  |

(b) Violent Crime Rates by State, 2013

| 1 | 2499 |
| :--- | :--- |
| 2 | 0112344556667889 |
| 3 | 0012255558 |
| 4 | 1111235557789 |
| 5 | 0566 |
| 6 | 014 |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 1 |  |
| 2 | 4 |

Legend: $1 \mid 2$ represents 120 violent crimes per 100,000 population
(c) Violent Crime Rates by State, 2013

(d) Answers will vary. The first display is decent. It clearly shows that the distribution is skewed right and has an outlier. The second display is not as good as the first. Splitting the stems did not reveal any additional information and has made the display more cluttered and cumbersome.
40. (a) Ages of Academy Award Winners

Best Actor Best Actress


Legend: 6|7|4 represents 76 years old for Best Actor and 74 years old for Best Actress.
(b) Answers will vary. It appears that Academy Award winners for best actor tend to be older on the whole than winners for best actress.
41. (a)

Home Run Distances
McGwire Bonds


Legend: 013417 represents 340 feet for McGwire and 347 feet for Bonds
(b) Answers will vary. For both players, the distances of home runs mainly fall from 360 to 450 feet. McGwire has quite a few extremely long distances.
42. Answers will vary.
43. Answers will vary. It is disconcerting that some schools have a negative ROI.

44.



There are several similarities in the distribution of the ideal number of children, as reported by males and females. However, females seem more likely to deem larger families as ideal.
A histogram would better serve us in comparing the preferences between males and females.
45.

Televisions in Houschold

46.

47. Because the data are quantitative, either a stem-and-leaf plot or a histogram would be appropriate. There were 20 people who spent less than 30 seconds, 7 people spent at least 30 seconds but less than 60 seconds, etc. One possible histogram is:


The data appear to be skewed right with a gap and one potential outlier. It seems as if the majority of surfers spent less than one minute viewing the page, while a few surfers spent several minutes viewing the page.
48. Age: histogram, stem-and-leaf plot, or dot plot; Income: histogram or stem-and-leaf plot; Marital status: bar graph or pie chart; Number of vehicles: histogram, stem-and-leaf plot, or dot plot
49. Classes should not overlap to avoid any confusion as to which class an observation belongs to.
50. Histograms are useful for large data sets or data sets with a large amount of spread. Stem-and-leaf plots are nice because the raw data can easily be retrieved. A disadvantage of stem-and-leaf plots is that sometimes the data must be rounded, truncated, or adjusted in some way that requires extra work. Furthermore, if these steps are taken, the original data is lost and a primary advantage of stem-and-leaf plots is lost.
51. There is no such thing as the correct choice for a class width, however some choices are better than others. For example, if the class width is too small, the histogram will show many gaps between the bars. If the class width is too large, the histogram may not provide enough detail.
53. Answers will vary. The exercise illustrates the fact that there is no such thing as the "correct" histogram. However, some histograms are better than others and class width can affect the shape of a graph.
54. Answers will vary. Sample histograms are given below.

Skewed Right



Bell-Shaped

52. Relative frequencies should be used when comparing two data sets with different sample sizes.

A histogram is skewed left if it has a long tail on the left side. A histogram is skewed right if it has a long tail on the right side. A histogram is symmetric if the left and right sides of the graph are roughly mirror images of each other.

## Section 2.3

1. An ogive is a line graph of cumulative frequencies or cumulative relative frequencies against upper class limits.
2. Time series are data measuring the value of a variable at different points in time.
3. True
4. False; when plotting a frequency polygon, we plot the frequency (or number) for each class above the class midpoint and connect the points with straight line segments.
5. (a) 0.5 ; The class width is the difference between successive class midpoints. (e.g. $1.25-0.75=0.5$ ).

There are 6 classes represented in the graph. The 8 plotted points are for the 6 class midpoints plus two additional points to connect the graph to the horizontal axis on the ends.
(b) The midpoint of the first class is 1.25 . The lower limit of the first class is 1.00 and the upper limit is 1.49.
(c) The midpoint of the last class is 3.75 . The lower limit of the last class is 3.50 and the upper limit is 3.99 .
(d) The lower and upper limits of the class with 25 students are 2.50 and 2.99, respectively.
(e) The lower and upper limits of the class with the fewest students are 1.00 and 1.49 , respectively.
6. (a) 4 ; The class width is the difference between successive class upper limits (e.g. $2-(-2)=4$ ).

There are 6 classes represented in the graph. The 8 plotted points are for the 6 class midpoints plus two additional points to connect the graph to the horizontal axis on the ends.
(b) The midpoint of the first class is 2 . The lower limit of the first class is 0 and the upper limit is 3.9 .
(c) The midpoint of the last class is 22 . The lower limit of the last class is 20 and the upper limit is 23.9 .
(d) The most popular number of hours spent exercising each week is 0 to 3.9 hours, which is the group with the highest frequency.
(e) The least popular number of hours spent exercising each week is 16 to 19.9 hours, which is the group with the lowest frequency.
(f) The lower and upper limits of the class with 55 students are 4 and 7.9 , respectively.
7. (a) 5; The class width is the difference between successive class midpoints. (e.g. $24.9-19.9=5$ ).
(b) From the graph, it appears that approximately $10 \%$ of all four-year universities have a graduation rate below $34.9 \%$.
(c) From the graph, it appears that approximately $60 \%$ of all four-year universities have a graduation rate below 59.9\%.
(d) From the graph, it appears that approximately $5 \%$ of all four-year universities have a graduation rate above $90 \%$.
8. (a) 2 ; The class width is the difference between successive class upper limits (e.g. 3.9-1.9).
(b) From the graph, it appears that approximately $92 \%$ of all tornadoes had a length less than 9.9 miles.
(c) From the graph, it appears that approximately $80 \%$ of all tornadoes had a length less than 5.9 miles.
(d) From the graph, it appears that more than $50 \%$ of all tornadoes exceed a length of 2 miles.
9. (a) From the graph, it appears the unemployment rate in 2011 was about $9 \%$.
(b) The highest unemployment rate was about $9.8 \%$. This occurred in 2010.
(c) The highest inflation rate was about $4.3 \%$. This occurred in 2008.
(d) The unemployment rate and inflation rate were closest in 2001. The unemployment rate and inflation rate were furthest in 2009.
(e) The misery index for 1999 was approximately $4.2+1.8=6$. The misery index for 2014 was approximately $6.5+$ $1.5=8$. According to the misery index, the year 2014 was more "miserable" than the year 1999.
(f) Since 2010, the misery index has been declining due to the decreases in unemployment each year.
10. (a) To the nearest year, the average age of a man who first married in 1980 was 25.
(b) To the nearest year, the average age of a woman who first married in 1960 was 21.
(c) The largest difference in the average age of men and women at which they first married occurred in 1950. The approximate age difference was $24-20.5=3.5$ years.
(d) The least amount of difference in the average age of men and women at which they first married occurred in 2000. The approximate age difference was $26.5-25.2=1.3$ years.
11. (a), (b)

| Speed <br> $(\mathrm{km} / \mathrm{h})$ | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | :---: | :---: |
| $10-13.9$ | 4 | 0.0066 |
| $14-17.9$ | 11 | 0.0181 |
| $18-21.9$ | 28 | 0.0461 |
| $22-25.9$ | 119 | 0.1960 |
| $26-29.9$ | 401 | 0.6606 |
| $30-33.9$ | 607 | 1.0000 |

(c)

(d)

Top Speed at the 2014 World Cup

12. (a), (b)

Total number of earthquakes is:
9469
Second class cumulative frequency is $3371+3400=6671$, and so on.
Second class cumulative relative frequency $=6771 / 9469=0.7151$, and so on.

| Earthquake <br> Magnitude | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | :---: | :---: |
| $0.0-0.9$ | 3371 | 0.3560 |
| $1.0-1.9$ | 6771 | 0.7151 |
| $2.0-2.9$ | 8008 | 0.8457 |
| $3.0-3.9$ | 8294 | 0.8759 |
| $4.0-4.9$ | 9339 | 0.9863 |
| $5.0-5.9$ | 9460 | 0.9990 |
| $6.0-6.9$ | 9467 | 0.9998 |
| $7.0-7.9$ | 9469 | 1.0000 |

(c)

(d)

13. (a), (b) Cumulative frequency of a Gini Index of $25-29.9=5+16=21$, and so on. The relative cumulative frequency of 25-29.9 is $21 / 136=-.1544$, and so on.

| Gini <br> Index | Cumulative <br> Frequency | Rel. <br> Cum. <br> Freq. |
| :---: | :---: | :---: |
| $20-24.9$ | 5 | 0.0368 |
| $25-29.9$ | 21 | 0.1544 |
| $30-34.9$ | 49 | 0.3603 |
| $35-39.9$ | 76 | 0.5588 |
| $40-44.9$ | 96 | 0.7059 |
| $45-49.9$ | 113 | 0.8309 |
| $50-54.9$ | 126 | 0.9265 |
| $55-59.9$ | 131 | 0.9632 |
| $60-64.9$ | 136 | 1.0000 |

(c)

(d)

14. (a), (b)

Second class cumulative frequency is $2+10=12$, and so on.
Second class cumulative relative frequency $=12 / 51=0.2353$, and so on.

| Income | Cum. <br> Freq. | Rel. <br> Cum. <br> Freq. |
| :---: | :---: | :---: |
| $35,000-39,999$ | 2 | 0.0392 |
| $40,000-44,999$ | 12 | 0.2353 |
| $45,000-49,999$ | 17 | 0.3333 |
| $50,000-54,999$ | 32 | 0.6275 |
| $55,000-59,999$ | 38 | 0.7451 |
| $60,000-64,999$ | 47 | 0.9216 |
| $65,000-69,999$ | 50 | 0.9804 |
| $70,000-74,999$ | 51 | 1.0000 |

(c)

(d)

15. (a)

BP Stock Closing Price: 2010

(b) The value of the BP stock at the end of May 2010 was 35.72 and was only 24.02 at the end of June 2010. The percentage change in the BP stock price from May to June 2010 was
$(24.02-35.72) / 35.72=-0.328$, which is a decrease of $32.8 \%$.
16. (a)

(b) The closing price of Twitter stock in November 2013 was 41.57 and was 63.65 in December 2013. The percentage change from November to December 2013 was $(63.65-41.57) / 41.57=0.531$, which is an increase of $53.1 \%$.

The closing price of Twitter stock in November 2013 was 41.57 and was 41.47 in October 2014. The percentage change from November 2013 to October 2014 was (41.47-41.57)/41.57 $=-0.002$, which is a decrease of $0.2 \%$. The closing price of Twitter stock increased $53.1 \%$ between November and December 2013, so an investor would have been wise to sell in December 2013.
17. (a)


Answers will vary. The time-series plot shows that debt as a percent of gross domestic product remained relatively stable around $60 \%$ from 1996 to 2007 and then began to increase steadily from 2008 to 2014.
18.


Answers will vary. The time-series plot shows that the percentage of high school graduates enrolling in college seems to have increased over the given time period amid a variety of fluctuations with a slight downturn in 2012.
19. (a)

| Return <br> (Percent) | Consumer <br> Defense | Industrial |
| :---: | :---: | :---: |
| -20 to -10.01 | 0.0435 | 0.0000 |
| -10 to -0.01 | 0.0217 | 0.0235 |
| 0 to 9.99 | 0.0543 | 0.1882 |
| 10 to 19.99 | 0.5217 | 0.2471 |
| 20 to 29.99 | 0.2391 | 0.3059 |
| 30 to 39.99 | 0.0543 | 0.1647 |
| 40 to 49.99 | 0.0326 | 0.0235 |
| 50 to 59.99 | 0.0109 | 0.0235 |
| 60 to 69.99 | 0.0000 | 0.0000 |
| 70 to 79.99 | 0.0217 | 0.0118 |
| 80 to 89.99 | 0.0000 | 0.0118 |

(b)


(c)

Three-Year Rate of Return

(d)

Three-Year Rate of Return

(e) Answers will vary. However, industrial stocks had a higher proportion of highreturn stocks and had fewer stocks with negative returns.
20. Answers will vary. Reports should address the fact that the number of people going to the beach and participating in underwater activities (e.g. scuba diving, snorkeling) has also increased, so an increase in shark attacks is not unexpected. A better comparison would be the rate of attacks per 100,000 beach visitors. The number of fatalities could decrease due to better safety equipment (e.g. bite resistant suits) and better medical care.
22. Answers will vary. The cumulative relative frequency is the proportion of observations less than or equal to the current class. All the observations are less than or equal to the highest class, so the cumulative relative frequency of the last class must be 1 , or $100 \%$.
23. Time-series plots are drawn with quantitative variables. They are drawn to see trends in the data.
21. Answers will vary.

## Section 2.4

1. The lengths of the bars are not proportional. For example, the bar representing the cost of Clinton's inauguration should be slightly more than 9 times as long as the one for Carter's cost, and twice as long as the bar representing Reagan's cost.
2. (a) Answers will vary. The lengths of the bars are not proportional. For example, the bar for soda is $1 / 3$ the size of the bar for a cheeseburger, but the number of steps for a cheeseburger is just over twice that for the soda. In addition, it is unclear where the graph begins: at the base of each figure or the bottom of the platform.
(b) Answers will vary. The pictures could be replaced by simple bars (of the same width) that are proportional in area.
3. (a) The vertical axis starts at $\$ 21,500$ instead of $\$ 0$. This tends to indicate that the median earnings for females changed at a faster rate than actually occurred.
(b) This graph indicates that the median earnings for females has decreased slightly over the given time period.

4. (a) The vertical axis starts at 4 instead of 0 .

This may lead the reader to conclude, for example, the percentage of employed people aged 55-64 who are members of a union is more than double the percentage of those aged 25-34 years.
Union Membership

5. The bar for $12 \mathrm{p}-6 \mathrm{p}$ covers twice as many hours as the other bars. By combining two 3hour periods, this bar looks larger compared to the others, making afternoon hours look more dangerous. If this bar were split into two periods, the graph may give a different impression. For example, the graph may show that daylight hours are safer.
6. The article is basing its conclusion on a comparison of categories that do not cover the same number of years. A better comparison is the incidence rate (number of accidents per 100,000 licensed drivers). [Note: only about $14 \%$ of licensed drivers in 2005 were aged 24 years or younger.]
7. Answers will vary. This graph is misleading because it does not take into account the size of the population of each state. For example, Vermont is going to pay less in total taxes than California simply because its population is so much lower. There are many variables that should be considered on per capita basis. For example, this graph would be less misleading if it was drawn to represent taxes paid per capita (per person).
8. (a) The oil reserves in 2014 were 691.0 million barrels, whereas the oil reserves in 1977 were 7.5 million barrels. The oil reserves in 2014 were 92 times as large as in 1977 (e.g. 691/7.5=92.1). Thus, the graphic for 2014 should be roughly 92 times larger than the graphic for 1977.
(b) Assuming no change in U.S. oil production, the U.S. strategic oil reserves would last approximately 90 days (e.g. 691/7.7 = 89.74 days).
9. (a) The graphic is misleading because the bars are not proportional. The bar for housing should be a little more than twice the
(b) The graphic could be improved by adjusting the bars so that their lengths are proportional.
10. The graph does not support the safety manager's claim. The vertical scale starts at
0.17 instead of 0 , so the difference between the bars is distorted. While there was a decrease, it appears that the decrease is roughly $10 \%$ of the
1992
rate.
11. (a) Answers will vary. Here is a timeseries plot that a politician might use to support the position that health care is increasing.

(b) Answers will vary. Here is a time-series plot that the health care industry might use to refute the opinion of the politician.

Health Care as a Percent of GDP

(c) Answers will vary. Changing the scale on the graph will affect the message. The message is also affected by using the variable "Health Care per Capita" rather than "Health Care as a Percent of GDP."
12. (a) A graph that is not misleading will use a vertical scale starting at $\$ 0$ and bars of equal width. One example:

Unleaded Gasoline Cost

(b) A graph that is misleading might use bars of unequal width or will use a vertical scale that does not start at $\$ 0$. One example, as follows, is misleading because it starts at $\$ 1.25$ instead of 0 without indicating a gap. This might cause the reader to conclude that cost of unleaded gasoline has risen more sharply than actually occurred.

13. (a) A graph that is not misleading will use a vertical scale starting at $0 \%$ and bars of equal width. One example:

(b)


This graphic is misleading because the vertical scale starts at $10 \%$ instead of $0 \%$ without indicating a gap. This might cause the reader to think that the proportion of overweight adults in the United States is increasing more quickly than they really are.
14. (a) A bar graph
(b) A reader cannot tell whether the graph ends at the top of the nipple on the baby bottle, or at the end of the milk.
(c) Answers will vary. Here is an example of a graph that is not misleading.

Ideal Number of Children

15. Answers will vary. Three-dimensional graphs are deceptive because the pieces are not proportional. For example, the area for P (pitcher) looks substantially larger than the area for 3B (third base), even though both are the same percentage. Graphs should not be drawn using three dimensions. Instead, use two dimensions.
16. Answers will vary. This is a histogram so the bars should touch. In addition, there are no labels and no title.

## Chapter 2 Review Exercises

1. (a) There are $614+154+1448=2216$ participants.
(b) The relative frequency of the respondents indicating that it makes no difference is

$$
\frac{1448}{2216} \approx 0.653
$$

(c) A Pareto chart is a bar chart where the bars are in descending order. Convincing Voice in
Purchasing a Car

(d) Answers will vary.
2. (a) Total homicides $=8438+1486+685+$ $1621=12230$
Relative frequency for firearms is $8438 / 12230=0.6899$, and so on.

| Type of Weapon | Relative Frequency |
| :--- | :--- |
| Firearms | 0.6899 |
| Knives or cutting <br> instruments | 0.1215 |
| Personal weapons | 0.0560 |
| Other weapon | 0.1325 |

(b) The relative frequency is 0.6899 , so $68.99 \%$ of the homicides were committed using a firearm.
(c)

(d)

(e) Weapons Used in Homicides

3. (a), (b), and (c)

Total births (in thousands) $=3+275+$ $902+1128+1044+487+110+7+1=$ 3957
Relative frequency for 10-14 year old mothers $=3 / 3957 \approx 0.0008$, and so on. Cumulative frequency for 15-19 year old mothers $=3+275=278$, and so on. Cumulative relative frequency for 15-19
(d) The distribution is roughly symmetric and bell-shaped.


(f)

year old mothers $=278 / 3957 \approx 0.0703$, and so on.

| Age of <br> Mother | Rel. <br> Freq. | Cumul. <br> Freq. | Cumul. <br> Rel. Freq. |
| :---: | :---: | :---: | :---: |
| $10-14$ | 0.0008 | 3 | 0.0008 |
| $15-19$ | 0.0695 | 278 | 0.0703 |
| $20-24$ | 0.2280 | 1180 | 0.2982 |
| $25-29$ | 0.2851 | 2308 | 0.5833 |
| $30-34$ | 0.2638 | 3352 | 0.8471 |
| $35-39$ | 0.1231 | 3839 | 0.9702 |
| $40-44$ | 0.0278 | 3949 | 0.9980 |
| $45-49$ | 0.0018 | 3956 | 0.9997 |
| $50-54$ | 0.0003 | 3957 | 1.0000 |

(g)

(h)

(i)

(j) From the relative frequency table, the relative frequency of $20-24$ is 0.2280 , so the percentage is $22.80 \%$.
(k) $\frac{1044+487+110+7+1}{3957}=\frac{1649}{3957} \approx 0.4167$
$41.67 \%$ of live births were to mothers aged 30 years or older.
4. (a), (b)

| Affiliation | Frequency | Relative <br> Frequency <br> Democrat |
| :---: | :---: | :---: |
| 46 | 0.46 |  |
| Independent | 16 | 0.16 |
| Republican | 38 | 0.38 |

Political Affiliation

(c)

(e) Democrat appears to be the most common affiliation in Naperville.
5. (a), (b), (c), and (d)

| Family <br> Size | Freq. | Rel. <br> Freq. | Cumul. <br> Freq. | Cumul. <br> Rel. <br> Freq. |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| 0 | 7 | 0.1167 | 7 | 0.1167 |
| 1 | 7 | 0.1167 | 14 | 0.2333 |
| 2 | 18 | 0.3000 | 32 | 0.5333 |
| 3 | 20 | 0.3333 | 52 | 0.8667 |
| 4 | 7 | 0.1167 | 59 | 0.9833 |
| 5 | 1 | 0.0167 | 60 | 1.0000 |

(e) The distribution is more or less symmetric.

Number of Children for Couples Married 7 Years


Number of Children for Couples Married 7 Years

(g) From the relative frequency table, the relative frequency of two children is 0.3000 , so $30 \%$ of the couples have two children.
(h) From the frequency table, the relative frequency of at least two children (i.e. two or more) is
$0.3000+0.3333+0.1167+0.0167=0.7667$ or $76.67 \%$. So, $76.67 \%$ of the couples have at least two children.
(i)

6. (a), (b)

| Homeownership <br> Rate | Frequency | Relative <br> Frequency |
| :--- | :--- | :--- |
| $45-49.9$ | 1 | 0.0196 |
| $50-54.9$ | 3 | 0.0588 |
| $55-59.9$ | 1 | 0.0196 |
| $60-64.9$ | 12 | 0.2353 |
| $65-69.9$ | 17 | 0.3333 |
| $70-74.9$ | 15 | 0.2941 |
| $75-75.9$ | 2 | 0.0392 |


(e) The distribution is skewed left.
(f)

| Homeownership <br> Rate | Frequency | Relative <br> Frequency |
| :--- | :--- | :--- |
| $40-49.9$ | 1 | 0.0196 |
| $50-59.9$ | 4 | 0.0784 |
| $60-69.9$ | 29 | 0.5686 |
| $70-79.9$ | 17 | 0.3333 |




The distribution is skewed left.
Answers will vary. Both class widths give a good overall picture of the distribution. The first class width provides a little more detail to the graph, but not necessarily enough to be worth the trouble. An intermediate value, say a width of 8 , might be a reasonable compromise.
7. (a), (b), (c), and (d)

Answers will vary. Using 2.2000 as the lower class limit of the first class and 0.0200 as the class width, we obtain the following.

| Class | Freq. | Rel. <br> Freq. | Cumul. <br> Freq. | Cumul. <br> Rel.Freq. |
| :---: | :---: | :---: | :---: | :---: |
| $2.2000-2.2199$ | 2 | 0.0588 | 2 | 0.0588 |
| $2.2200-2.2399$ | 3 | 0.0882 | 5 | 0.1471 |
| $2.2400-2.2599$ | 5 | 0.1471 | 10 | 0.2941 |
| $2.2600-2.2799$ | 6 | 0.1765 | 16 | 0.4706 |
| $2.2800-2.2999$ | 4 | 0.1176 | 20 | 0.5882 |
| $2.3000-2.3199$ | 7 | 0.2059 | 27 | 0.7941 |
| $2.3200-2.3399$ | 5 | 0.1471 | 32 | 0.9412 |
| $2.3400-2.3599$ | 1 | 0.0294 | 33 | 0.9706 |
| $2.3600-2.3799$ | 1 | 0.0294 | 34 | 1 |

(e)


The distribution is roughly symmetric.

8. Hours Spent Online
$\left.{ }_{13}^{12}\right|_{467}$

| 13 | 467 |
| :--- | :--- |
| 14 | 06578 |
| 15 | 1236 |


| 15 | 1236 |
| :--- | :--- | :--- |
| 16 | 456 |

17 113499
18. O6 $8 \mathrm{k9} 9$
$19 / 2$
$\begin{array}{lll}201 & 108 \\ 21 & 119\end{array}$
$\begin{array}{ll}21 & 119 \\ 22 & 29 \\ 24 & 18\end{array}$

| 23 | 48 |
| :--- | :--- |
| 24 | 4 |
| 25 | 7 |

26
Lefent-13.14- merage 13 A hours per mokk.
The distribution is slightly skewed right.
9. (a) Grade inflation seems to be happening in colleges. GPAs have increased every time period for all schools.
(b) Answers may vary. GPAs increased about $5.6 \%$ for public schools. GPAs increased about $6.8 \%$ for private schools. Private schools have higher grade inflation because the GPAs are higher and they are increasing faster.
(c) The graph is misleading because it starts at 2.6 on the vertical axis.
10. (a) Answers will vary. The adjusted gross income share of the top $1 \%$ of earners shows steady increases overall, with a few minor exceptions. The adjusted gross income share of the bottom $50 \%$ of earners shows steady decreases overall, with a few minor exceptions.

Percentage of Adjusted Gross Incomes (AGI) Earned

(b) Answers will vary. The income tax share of the top $1 \%$ of earners shows steady increases overall, with few exceptions, including a notable decrease from 2007 to 2008. The income tax share of the bottom $50 \%$ of earners shows steady decreases over time.

11. (a) Graphs will vary. One way to mislead would be to start the vertical scale at a value other than 0 . For example, starting the vertical scale at $\$ 30,000$ might make the reader believe that college graduates earn more than three times what a high school graduate earns (on average).
(b) A graph that does not mislead would use equal widths for the bars and would start the vertical scale at $\$ 0$. Here is an example of a graph that is not misleading:

2013 Average Earnings

12. (a) Flats are preferred the most ( $40 \%$ ) and extra-high heels are preferred the least (1\%).
(b) The graph is misleading because the bar heights and areas for each category are not proportional.

## Chapter 2 Test

1. (a) A 5 Star rating was the most popular rating with 1675 votes.
(b) $35+67+246+724+1675=2747$ postings were posted on Yelp for Hot Doug's restaurant.
(c) $1675-724=951$

There were 951 more 5 Star ratings than 4 Star ratings.
(d) There were 16755 Star ratings out of a total of 2747 ratings. $\frac{1675}{2747} \approx 0.6098$
Approximately $61 \%$ of all ratings were 5 Star ratings.
(e) No, it is not appropriate to describe the shape of the distribution as skewed right. The data represented by the graph are qualitative, so the bars in the graph could be placed in any order.
2. (a) There were 1005 responses. The relative frequency who indicated they preferred new tolls was $\frac{412}{1005}=0.4100$, and so on.

| Response | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| New Tolls | 412 | 0.4100 |
| Inc. Gas Tax | 181 | 0.1801 |
| No New Roads | 412 | 0.4100 |

(b) The relative frequency is 0.1801 , so the percentage of respondents who would like to see an increase in gas taxes is $18.01 \%$.


How Would You Prefer to Pay
for New Road Construction? for New Road Construction?

3. (a), (b)

| Education | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| No high school <br> diploma | 9 | 0.18 |
| High school | 16 | 0.32 |
| graduate |  |  |
| Some college | 9 | 0.18 |
| Associate's degree | 4 | 0.08 |
| Bachelor's degree | 8 | 0.16 |
| Advanced degree | 4 | 0.08 |

(c)

Educational Attainment of Commuters

(d) Educational Attainment of Commuters

(e) The largest bar (and largest pie segment) corresponds to "High School Graduate," so high school graduate is the most common educational level of a commuter.
4. (a), (b), (c), and (d)

| No. of <br> Cars | Freq. | Rel. <br> Freq. | Cumul. <br> Freq. | Cumul. <br> Rel. Freq. |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 5 | 0.10 | 5 | 0.10 |
| 2 | 7 | 0.14 | 12 | 0.24 |
| 3 | 12 | 0.24 | 24 | 0.48 |
| 4 | 6 | 0.12 | 30 | 0.60 |
| 5 | 8 | 0.16 | 38 | 0.76 |
| 6 | 5 | 0.10 | 43 | 0.86 |
| 7 | 2 | 0.04 | 45 | 0.90 |
| 8 | 4 | 0.08 | 49 | 0.98 |
| 9 | 1 | 0.02 | 50 | 1 |

(e)


The distribution is skewed right.
(f)

Number of Cars Arriving at McDonald's

(g) The relative frequency of exactly 3 cars is 0.24 . So, for $24 \%$ of the weeks, exactly three cars arrived between 11:50 am and 12:00 noon.
(h) The relative frequency of 3 or more cars

$$
\begin{aligned}
= & 0.24+0.12+0.16+0.10 \\
& +0.04+0.08+0.02=0.76
\end{aligned}
$$

So, for $76 \%$ of the weeks, three or more cars arrived between 11:50 am and 12:00 noon.
(i)

5. Answers may vary. One possibility follows:
(a), (b)

Using a lower class limit of the first class of 20 and a class width of 10 :
Total number of data points $=40$
Relative frequency of $20-29=1 / 40$ $=0.025$, and so on.

| HDL <br> Cholesterol | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $20-29$ | 1 | 0.025 |
| $30-39$ | 6 | 0.150 |
| $40-49$ | 10 | 0.250 |
| $50-59$ | 14 | 0.350 |
| $60-69$ | 6 | 0.150 |
| $70-79$ | 3 | 0.075 |

Serum HDL of 20-29 Year Olds

(d)

(e) The distribution appears to be roughly bell-shaped.
6.

(a), (b)Closing Price \begin{tabular}{c|c|c|}
\hline Cumul. <br>
Freq.

 

Cumul. <br>
Rel. Freq.

$|$

(b0,000-99,999 \& 4 \& 0.08 <br>
$100,000-149,999$ \& 17 \& 0.34 <br>
$150,000-199,999$ \& 36 \& 0.72 <br>
$200,000-249,999$ \& 43 \& 0.86 <br>
$250,000-299,999$ \& 46 \& 0.92 <br>
$300,000-349,999$ \& 48 \& 0.96 <br>
$350,000-399,999$ \& 49 \& 0.98 <br>
$400,000-449,999$ \& 49 \& 0.98 <br>
$450,000-499,999$ \& 50 \& 1 <br>
\hline
\end{tabular}

(c) The cumulative relative frequency for the class $\$ 150,000-\$ 199,000$ is 0.72 .
Therefore, $72 \%$ of the homes sold for less than $\$ 200,000$.

Closing Price of Homes Sold


The distribution is skewed right.
(e)

(f)

7. The stem-and-leaf diagram below shows an approximately uniform distribution.

Time Spent on Homework

| 4 | 0567 |
| ---: | :--- | :--- |
| 5 | 26 |
| 6 | 13 |
| 7 | 01338 |
| 8 | 59 |
| 9 | 1369 |
| 10 | 3899 |
| 11 | 0018 |
| 12 | 556 |
| Legend: 410 represents 40 minutes. |  |

8. The curves in the figure below appear to follow the same trend. Birth rate increases as per capita income increases.

9. Answers may vary. It is difficult to interpret this graph because it is not clear whether the scale is represented by the height of the steps, the width of the steps, or by the graphics above the steps. The graphics are misleading because they must be increased in size both vertically and horizontally to avoid distorting the image. Thus, the resulting areas are not proportionally correct. The graph could be redrawn using bars whose widths are the same and whose heights are proportional based on the given percentages. The use of graphics should be avoided, or a standard size graphic representing a fixed value could be used and repeated as necessary to illustrate the given percentages.

## Case Study: The Day the Sky Roared

1. 




During the April 3-4, 1974 outbreak, about 44\% of the tornadoes exceeded F-3 on the Fujita Wind Damage Scale. This was much greater than the $1 \%$ that typically occurs.
2. The histogram will vary depending on the class width.

3. Histograms may vary depending on class widths. For comparison purposes, the same class width was used for each histogram.


The distributions all appear to be skewed right, though the distribution for F-5 tornadoes is difficult to see due to the low sample size. There is an obvious shift in the distributions. As the strength of the tornado increases, the duration of the tornado increases.
4. There were 305 deaths during the outbreak. Of these, 259 were due to the more severe tornadoes.
$\frac{259}{305} \approx 0.8492$
Roughly $85 \%$ of the deaths during the outbreak were due to the more severe tornadoes. This may be a little high, but it is consistent since it is greater than $70 \%$.

5. The provided data is not sufficient to determine whether or not tornadoes are more likely to strike rural areas. Some research at Texas A\&M University indicates that tornadoes are more likely to occur in urban or suburban areas, possibly due to greater temperature differences. The data does indicate that the number of deaths decreases as the population of the community increases. The higher the population density, the greater the chance that a tornado is detected and reported early, thereby providing more time for residents to take shelter.

6. Answers will vary. The outbreak of April 3-4, 1974 seemed to be more severe in intensity than usual with $20 \%$ of the tornadoes being classified as F-4 or F-5. While the shape of the duration distribution was roughly the same for each intensity level, the duration of a tornado increased with its intensity. The number of deaths decreased as the community size increased.

# Chapter 2 <br> Organizing and Summarizing Data 

## Overview

Remember, this course is divided into four parts that correspond to the four parts of our definition of Statistics. Chapters 2 through 4 represent the organizing and summarizing portion of the definitiondescriptive statistics.

Chapter 2 discusses describing data through tables and graphs. We summarize raw qualitative data in Section 2.1 and raw quantitative data in Sections 2.2 and 2.3. Section 2.4 provides the opportunity to present misleading graphs.

## What to Emphasize

The material in this chapter is elementary. Many of your students have likely seen much of this content in prior classes. Therefore, do not get bogged down in the details of construction of the graphs. Instead, focus on proper graphics construction and how to display qualitative and quantitative data in a fashion that clearly tells the story of the data.

- Summarizing Qualitative Data - We begin with a discussion of summarizing qualitative data in tables. This should not be a challenge for the students, so don't spend a lot of class time on this material. Ideally, you will use software such as StatCrunch to build frequency and relative frequency tables. The same goes for the construction of bar graphs and pie charts. Do not emphasize by-hand construction-nobody would ever be expected to construct one of these graphs by hand. Instead, emphasize when each type of graph should be constructed. Bar graphs are typically used when we wish to compare one value of a variable to another, while pie charts are useful when comparing a part to the whole. For example, what proportion of taxes collected by the federal government are from personal income taxes? This is easier to see from a pie chart than a bar graph. Bar graphs can be used to display ordinal data (Poor, Fair, Good, Excellent). Can the same information be displayed effectively in a pie chart?

Also, emphasize side-by-side bar graphs and the fact that they should be constructed using relative frequencies (since it is not "fair" to compare frequencies when the sample/population sizes differ). Plus, a version of side-by-side bar graphs will be used in Chapters 4 and 12 when we study conditional distributions.

- Summarizing Quantitative Data - We decided to segment summarizing quantitative data into two sections-the popular displays (Section 2.2) and other graphs (Section 2.3). Section 2.3 is optional and can be skipped without loss of continuity. When considering which topics you might skip, ask yourself if the topic will be needed or revisited later in the course. For example, graphs such as frequency polygons are not utilized later in the course, so you might consider skipping this topic. That said, some graphs allow for interesting results, such as time series plots. So, judgment should be used when deciding what to skip.

In Section 2.2, do not get bogged down on by-hand creation of frequency or relative frequency distributions or the construction of histograms. Allow technology to do the work so that you may focus on the fact that there are many acceptable class widths that provide a nice summary of the data. However, be sure to emphasize that some class widths are really poor. In fact, spend time making sure students understand the results from the "Exploring Histograms with StatCrunch" activity in the Student Activity Notebook. In addition, spend time on distribution shape. Require students to justify their conclusions regarding shape, rather than simply claiming a distribution is skewed right.

Section 2.3 is entirely optional and may be skipped without loss of continuity. That said, you may consider at least requiring that students review time series graphs since they are popular in the media, and time series data is discussed at various points in the course (especially when we present correlation versus causation).

- Graphical Misrepresentations of Data - While this is an optional section, it does have merit. The media is full of examples where graphs mislead or misrepresent data. Be sure to alert students to be on the lookout for poor graphics and require students to clearly label each graph they create.


## Ideas for Traditional/Online/Blended/Flipped

Again, real data should be utilized to illustrate concepts.
Whether you are in a traditional or online setting, require students to justify results. For example, create four histograms of the same set of data and ask students (either through discussion groups or small in-class groups) to rank the graphs from best to worst. Change things up by not including titles or labels. Ask students how a graphic might be improved. Activities such as these not only require students to know how the graphics are constructed, but also get them thinking about appropriate techniques. Another idea is to give various data sets to students and ask them to summarize the information. Don't tell them what type of graphic to create-let them decide. Mix the data up between qualitative and quantitative. For example, include a small data set with discrete data (collect data from your class on number of siblings, which is likely best summarized using a dot plot) along with larger data sets that might be better summarized using histograms (use data from the 2014 World Cup at http://www.statcrunch.com/app/index.php?dataid=1130049). If a student or group chooses a histogram, ask for justification of the choice. In a classroom, perhaps the students could be required to present the graphic to the class and explain what message the graphic conveys.

A great applet that may be used to emphasize that there is no such thing as the "correct" class width when constructing a histogram is the Histogram with Sliders applet in StatCrunch. Use a data set to build the applet and allow students to experiment with various starting points and class widths.

Look through the Student Activity Workbook for in-class activities.

## Classroom Examples

## Section 2.1

1. The 2010 Census results include a summary of the racial composition of the population. The races reported by the populations of the United States and the State of California are summarized below. The data are given in millions. (Source: census.gov)

| Race | U.S. | California |
| :--- | :---: | :---: |
| White | 223.6 | 21.5 |
| Black or African American | 38.9 | 2.3 |
| American Indian and Alaska Native | 2.9 | 0.4 |
| Asian | 14.7 | 4.9 |
| Native Hawaiian and Other Pacific Islander | 0.5 | 0.1 |
| Some Other Race | 19.1 | 6.3 |
| Two or More Races | 9 | 1.8 |

a. Construct a relative frequency distribution for races in the U.S.

| Relative Frequency |  |
| :--- | :--- |
| Race | (U.S.) |
| White | 0.7241 |
| Black or African American | 0.1261 |
| American Indian and Alaska Native | 0.0095 |
| Asian | 0.0475 |
| Native Hawaiian and Other Pacific Islander | 0.0017 |
| Some Other Race | 0.0619 |
| Two or More Races | 0.0292 |

b. What percentage of U.S. residents claims two or more races? 2.92\%
c. What percentage of U.S. residents is not Asian? 95.25\%
d. Construct a frequency bar graph for races in the U.S.

e. Construct a relative frequency bar graph for races in the U.S.

Races in the United States

f. Construct a pie chart for races in the U.S.

2. Use the data in Problem 1 to answer this question.
a. Construct a relative frequency distribution for the races in California.

| Relative Frequency |  |
| :--- | :--- |
| Race | (California) |
| White | 0.5759 |
| Black or African American | 0.0617 |
| American Indian and Alaska Native | 0.0097 |
| Asian | 0.1305 |
| Native Hawaiian and Other Pacific Islander | 0.0039 |
| Some Other Race | 0.1696 |
| Two or More Races | 0.0487 |

b. What percentage of California residents claims two or more races? 4.87\%
c. What percentage of U.S. residents is not Asian? 86.95\%
d. Construct a frequency bar graph for California.

Races in California


Race
e. Construct a relative frequency bar graph for California.

Races in California


## f. Construct a pie chart for California.


3. Draw a side-by-side relative frequency bar graph of the populations of the United States and California. What do you notice?

4. The table shows the gold medal winners in hockey in the Winter Olympics since 1920.

| Year | Winner |  | Year | Winner |  | Year |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Winner |  |  |  |  |  |  |
| 1920 | Canada |  | 1960 | U.S.A. |  | 1992 |
| 1924 | Canada |  | 1964 | Soviet Union | 1994 | Czech Republic |
| 1928 | Canada | 1968 | Soviet Union | 1998 | Sweden |  |
| 1932 | Canada | 1972 | Soviet Union | 2002 | Canada |  |
| 1936 | Great Britain | 1976 | Soviet Union | 2006 | Sweden |  |
| 1948 | Canada | 1980 | U.S.A. | 2010 | Canada |  |
| 1952 | Canada | 1984 | Soviet Union | 2014 | Canada |  |
| 1956 | Soviet Union | 1988 | Soviet Union |  |  |  |

a. Construct a frequency distribution.
b. Construct a relative frequency distribution.

| Winner $\boldsymbol{*}$ | Frequency $\boldsymbol{*}$ | Relative Frequency $\boldsymbol{*}$ |
| :--- | ---: | ---: |
| Canada | 9 | 0.39130435 |
| Czech Republic | 1 | 0.043478261 |
| Great Britain | 1 | 0.043478261 |
| Soviet Union | 7 | 0.30434783 |
| Sweden | 2 | 0.086956522 |
| U.S.A. | 2 | 0.086956522 |
| Unified Team | 1 | 0.043478261 |

c. Construct a frequency bar graph.

Gold Medal Winners in Hockey

d. Construct a relative frequency bar graph.

e. Construct a pie chart.

5. In-Class Activity (Requires one bag of multicolored candy, such as M\&M's or Skittles for each student.) Ask the students bring one bag of candy, such as M\&M's or Skittles to class. Have them create a frequency distribution of the counts of each color of candy in their bag. Have the students create a bar graph, relative frequency bar graph, and a pie chart illustrating the number of each type they observed.

## Section 2.2

1. The following data represent the number of live births in the United States in 2012 for women 15 to 49 years of age.

| Age | Live Births |
| :--- | ---: |
| $15-19$ | 10,908 |
| $20-24$ | 916,811 |
| $25-29$ | $1,123,900$ |
| $30-34$ | $1,013,416$ |
| $35-39$ | 472,318 |
| $40-44$ | 109,579 |
| $45-49$ | 7157 |
| $50-54$ | 600 |

Source: National Vital Statistics Report
a. Determine the number of classes. 8
b. Determine the class limits. $15-19 ; 20-24 ; 25-29 ; 30-34 ; 35-39 ; 40-44 ; 45-49 ; 50-54$
c. Determine the class width. 5
d. Construct a relative frequency distribution.

| Age | Live Births |
| :--- | ---: |
| $15-19$ | 0.0030 |
| $20-24$ | 0.2509 |
| $25-29$ | 0.3075 |
| $30-34$ | 0.2773 |
| $35-39$ | 0.1292 |
| $40-44$ | 0.0300 |
| $45-49$ | 0.0020 |
| $50-54$ | 0.0002 |

e. Construct a frequency histogram.

Number of Live Births by Age of Mother

f. Construct a relative frequency histogram.

Number of Live Births by Age of Mother

g. What percent of live births were to mothers 50-54 years of age? $0.02 \%$
2. The following data represent the graduation rate for a random sample of 60 colleges and universities in the United States. Data from www.payscale.com.

| 86 | 59 | 65 | 55 | 59 | 40 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 90 | 48 | 37 | 65 | 67 | 67 |
| 39 | 53 | 82 | 57 | 71 | 46 |
| 83 | 77 | 40 | 52 | 92 | 38 |
| 56 | 57 | 36 | 61 | 34 | 54 |
| 69 | 35 | 73 | 29 | 92 | 39 |
| 24 | 48 | 41 | 46 | 79 | 41 |
| 44 | 43 | 28 | 61 | 49 | 65 |
| 48 | 42 | 72 | 35 | 58 | 39 |
| 80 | 75 | 44 | 52 | 52 | 47 |

With a first class having lower class limit of 20 and a class width of 10 :
a. Construct a frequency distribution.

| Graduation Rate | Frequency |
| :---: | :---: |
| $20-29$ | 3 |
| $30-39$ | 9 |
| $40-49$ | 15 |
| $50-59$ | 12 |
| $60-69$ | 8 |
| $70-79$ | 6 |
| $80-89$ | 4 |
| $90-99$ | 3 |

b. Construct a relative frequency distribution.

| Graduation Rate | Relative Frequency |
| :---: | :---: |
| $20-29$ | 0.05 |
| $30-39$ | 0.15 |
| $40-49$ | 0.25 |
| $50-59$ | 0.2 |
| $60-69$ | 0.1333 |
| $70-79$ | 0.1 |
| $80-89$ | 0.0667 |
| $90-99$ | 0.05 |

c. Construct a frequency histogram of the data.

Graduation Rate of U.S. Colleges/Universities Frequency

d. Construct a relative frequency histogram of the data.

Graduation Rate of U.S. Colleges/Universities Relative Frequency

e. Describe the shape of the distribution. The distribution is skewed right.
2. Draw a stem-and-leaf plot of the data from Problem 1.

```
2 : 489
3 : 455678999
4 : 001123446678889
5 : 222345677899
6 : 11555779
7 : 123579
8 : 0236
9 : 022
```


## Legend $2 \mid 4$ represents 24

3. Go to http://en.wikipedia.org/wiki/United_States_congressional_apportionment. The site includes data on the number of representatives in the House of Representatives for each census year. Create a frequency and relative frequency histogram of the data for the latest census. Draw a dot plot of the data. Note: The data can be easily extracted using StatCrunch This! in StatCrunch.
4. Ask the students to compute their heights (in inches). Randomly select some students to report their heights. Create a histogram of the students' heights. It is a good idea to make a histogram for men and a histogram for women. Ask the students to identify the shape of the distribution.

## Section 2.3

1. A simple random sample of 4,000 women who gave birth was collected. The following table summarizes the mother's ages at the time they gave birth. (Based on data at: www.infoplease.com/ipa/A0005074.html)

| Age of Mother | $10-14$ | $15-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ | $40-44$ | $45-49$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 9 | 401 | 1006 | 1094 | 919 | 467 | 101 | 6 |

a. Create a cumulative frequency table summarizing the data. See below
b. Create a relative frequency table of the data. See below
c. Create a cumulative relative frequency table for the data. Note: Answers may vary slightly due to rounding.

| Age of <br> Mother | Frequency | Cumulative <br> Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | :---: | :---: | :---: | :---: |
| $10-14$ | 6 | 6 | 0.0015 | 0.0015 |
| $15-19$ | 401 | 407 | 0.1003 | 0.1018 |
| $20-24$ | 1006 | 1413 | 0.2515 | 0.3533 |
| $25-29$ | 1094 | 2507 | 0.2735 | 0.6268 |
| $30-34$ | 919 | 3426 | 0.2298 | 0.8565 |
| $35-39$ | 467 | 3893 | 0.1168 | 0.9733 |
| $40-44$ | 101 | 3994 | 0.0253 | 0.9985 |
| $45-54$ | 6 | 4000 | 0.0015 | 1.0000 |

d. Construct a frequency polygon of the data.

e. Construct a relative frequency ogive of the data.

Age of Mothers At The Time of Birth

2. The following data represent the per capita income in the United States from 2000-2012 in constant 2011 dollars (that is, adjusted for inflation). Draw a time series graph of the data.

| Year | Per Capita Income <br> (2011 Dollars) |
| :---: | :---: |
| 2000 | 29,795 |
| 2001 | 29,636 |
| 2002 | 29,092 |
| 2003 | 29,058 |
| 2004 | 29,000 |
| 2005 | 29,446 |
| 2006 | 30,010 |
| 2007 | 29,682 |
| 2008 | 28,755 |
| 2009 | 28,400 |
| 2010 | 27,968 |
| 2011 | 28,130 |
| 2012 | 28,281 |

Source: United States Census Bureau


## Section 2.4

1.The data in the table below represent the historical life expectancies (in years) of residents of the United States. (Source: National Center for Health Statistics, National Vital Statistics Reports, www.cdc.gov/nchs and http://www.cdc.gov/nchs/data/hus/hus10.pdf\#022)

| Year, $\boldsymbol{x}$ | Life Expectancy, $\boldsymbol{y}$ |
| :---: | :---: |
| 1950 | 68.2 |
| 1960 | 69.7 |
| 1970 | 70.8 |
| 1980 | 73.7 |
| 1990 | 75.4 |
| 2000 | 77.0 |
| 2010 | 77.7 |

a. Construct a misleading time-series plot that indicates that the life expectancy has risen sharply over time.

b. Construct a time-series plot that is not misleading.

2. The National Survey of Student Engagement is a survey that (among other things) asks first year students at liberal arts colleges how much time they spend preparing for class each week. The results are summarized below. (Source: NSSE)

| Hours | 0 | $1-5$ | $6-10$ | $11-15$ | $16-20$ | $21-25$ | $26-30$ | $31-35$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Percentage of <br> $1^{\text { }}$ year students | $0 \%$ | $13 \%$ | $25 \%$ | $23 \%$ | $18 \%$ | $10 \%$ | $6 \%$ | $5 \%$ |

a. Construct a pie chart that exaggerates the percentage of students who spend between 6 and 10 hours preparing for class each week.

Number of Hours Per Week Students Spend Studying

b. Construct a pie chart that is not misleading.

Number of Hours Per Week Students Spend Studying


| Hours |
| :---: |
|  |
| $1-5$ |
| 6-10 |
| 11-1 |
| 16-20 |
| 21-2 |
| 26-3 |
| 31 |

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Note: If you use Excel to create 3-D pie charts, you can rotate the graph so students may visualize the distortion created by the three-dimensional art.

