# Test Bank for Statistics 12th Edition McClave Sincich 0321755936 9780321755933

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# Ch. 2 Methods for Describing Sets of Data

# 2.1 Describing Qualitative Data

#### 1 Identify Classes/Compute Class Frequencies/Relative Frequencies/Percentages

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

	Solve	the	prob	lem.
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- 1) In an eye color study, 25 out of 50 people in the sample had brown eyes. In this situation, what does the number .50 represent?
  - A) a class relative frequency

B) a class

C) a class frequency

D) a class percentage

2) What class percentage corresponds to a class relative frequency of .37?

A) 37%

B) .37%

C) .63%

D) 63%

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

3) A sample of 100 e-mail users were asked whether their primary e-mail account was a free account, an institutional (school or work) account, or an account that they pay for personally. Identify the classes for the resulting data.

## 2 Construct Frequency/Relative Frequency Table

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

4) What number is missing from the table?

Grades		Relative
on Test	Frequency	Frequency
A	6	.24
В	7	
C	9	.36
D	2	.08
F	1	.04

A) .28

B) .07

C) .72

D) .70

5) What number is missing from the table?

Year in College	Emaguange	Relative Frequency
Conege	Frequency	rrequericy
Freshman	600	.30
Sophomore	560	.28
Junior		.22
Senior	400	.20

A) 440

B) 220

C) 480

D) 520

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

6) Complete the frequency table for the data shown below.

green	blue	brown	orange	blue
brown	orange	blue	red	green
blue	brown	green	red	brown
blue	brown	blue	blue	red

Color	Frequency
Green	
Blue	
Brown	
Orange	

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Answer the question True or False.

7) A frequency table displays the proportion of observations falling into each class.

A) True

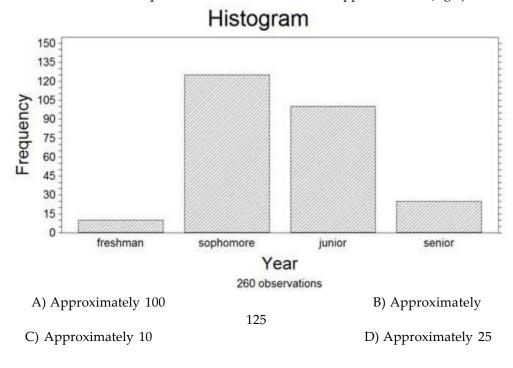
B) False

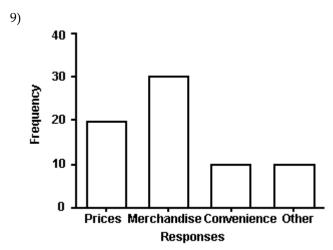
## 3 Construct, Interpret Bar Graph

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

8) 260 randomly sampled college students were asked, among other things, to state their year in school (freshman, sophomore, junior, or senior). The responses are shown in the bar graph below. How many of the students who responded would be classified as upperclassmen (e.g., juniors or seniors)?





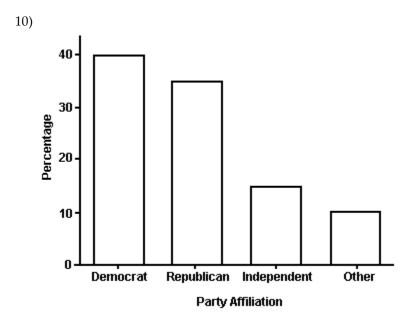
The manager of a store conducted a customer survey to determine why customers shopped at the store. The results are shown in the figure. What proportion of customers responded that merchandise was the reason they shopped at the store?

A)  $\frac{3}{7}$ 

B) 30

C)  $\frac{1}{2}$ 

D)  $\frac{2}{7}$ 



The bar graph shows the political affiliation of 1000 registered U.S. voters. What percentage of the voters belonged to one of the traditional two parties (Democratic or Republican)?

A) 75%

B) 40%

C) 35%

D) 25%

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

11) The data below show the types of medals won by athletes representing the United States in the Winter

Olympics.

gold	gold	silver	gold	bronze	silver	silver
bronze	gold	silver	silver	bronze	silver	gold
gold	silver	silver	bronze	bronze	gold	silver
gold	gold	bronze	bronze			

- a. Construct a frequency table for the data.
- b. Construct a relative frequency table for the

data. c. Construct a frequency bar graph for the data.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

- 12) The bars in a bar graph can be arranged by height in ascending order from left to right.

  A) True

  B) False
- 13) Either vertical or horizontal bars can be used when constructing a bar graph.

  A) True

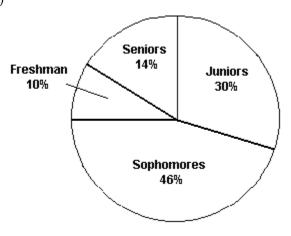
  B) False

## 4 Construct, Interpret Pie Chart

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

14)



The pie chart shows the classifications of students in a statistics class.

What percentage of the class consists of freshman, sophomores, and juniors?

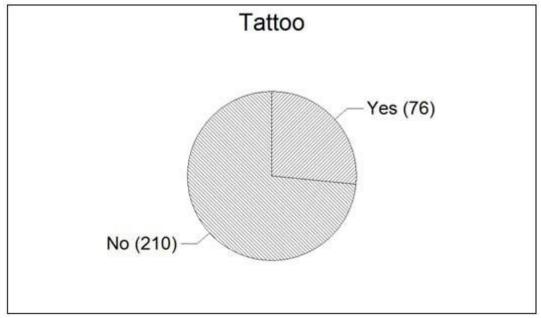
A) 86%

B) 14%

C) 44%

D) 54%

15) One of the questions posed to a sample of 286 incoming freshmen at a large public university was, "Do you have any tattoos?" Their responses are shown below in the pie chart. Please note that the values shown represent the number of responses in each category.



Based on the responses shown in the pie chart, what percentage of the freshmen responded with "Yes?" A) 76 B) 76% C) 26.6% D) 73.4%

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

16) The table shows the number of each type of book found at an online auction site during a recent search.

Type of Book	Number
Children's	51,033
Fiction	141,114
Nonfiction	253,074
Educational	67,252

- a. Construct a relative frequency table for the book data.
- b. Construct a pie chart for the book data.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

17) If 25% of your statistics class is sophomores, then in a pie chart representing classifications of the students in

your statistics class the slice assigned to sophomores is 90°.

A) True

B) False

18) The slices of a pie chart must be arranged from largest to smallest in a clockwise direction.

A) True

B) False

#### 5 Construct, Interpret Pareto Diagram

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

## Solve the problem.

19) What characteristic of a Pareto diagram distinguishes it from other bar graphs?

20) The table shows the number of each type of car sold in June.

Car	Number
compact	7,204
sedan	9,089
small SUV	20,418
large SUV	13,691
minivan	15,837
truck	15,350
Total	81,589

- a. Construct a relative frequency table for the car sales.
- b. Construct a Pareto diagram for the car sales using the class percentages as the heights of the bars.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

21) Class relative frequencies must be used, rather than class frequencies or class percentages, when constructing a

Pareto diagram.

A) True

B) False

22) A Pareto diagram is a pie chart where the slices are arranged from largest to smallest in a counterclockwise direction.

A) True

B) False

#### 6 Construct, Interpret Side-by-Side Bar Chart

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

## Solve the problem.

23) An annual survey sent to retail store managers contained the question "Did your store suffer any losses due to

employee theft?" The responses are summarized in the table for two years. Compare the responses for the two

years using side-by-side bar charts. What inferences can be made from the charts?

Employee	Percentage	Percentage
Theft	in year 1	in year 2
Yes	34	23
No	51	68
Don't know	15	9
Totals	100	100

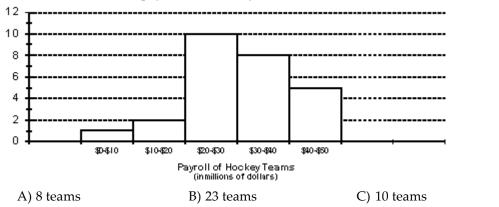
# 2.2 Graphical Methods for Describing Quantitative Data

## 1 Construct, Interpret Histogram

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

1) The payroll amounts for all teams in an international hockey league are shown below using a graphical technique from chapter 2 of the text. How many of the hockey team payrolls exceeded \$20 million (Note: Assume that no payroll was exactly \$20 million)?



SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

2) The data show the total number of medals (gold, silver, and bronze) won by each country winning at least one gold medal in the Winter Olympics.

D) 18 teams

a. Complete the class frequency table for the data.

Total Medals	Frequency
1-5	
6-10	
11-15	
16-20	
21-25	
26-30	

b. Using the classes from the frequency table, construct a histogram for the data.

3) The total points scored by a basketball team for each game during its last season have been summarized in the table below.

Score	Frequency
41-60	3
61-80	8
81-100	12
101-120	7

a. Explain why you cannot use the information in the table to construct a stem-and-leaf display for the data. b. Construct a histogram for the scores.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Answer the question True or False.

- 4) All class intervals in a histogram have the same width.
  - A) True

B) False

5) A histogram can be constructed using either class frequencies or class relative frequencies as the heights of the bars.

A) True

B) False

6) The bars in a histogram should be arranged by height in descending order from left to right.

A) True

B) False

#### 2 Construct, Interpret Stem-and-Leaf Display

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

7) A survey was conducted to determine how people feel about the quality of programming available on television. Respondents were asked to rate the overall quality from 0 (no quality at all) to 100 (extremely good

quality). The stem-and-leaf display of the data is shown below.

Stem	L	eat	f					
3	3	6						
4	0	3	4	7	8	9	9	9
5	0	3 1 2	1	2	3	4	5	
6	1	2	5	6	6			
7	5	8						
8								
9	3							

What percentage of the respondents rated overall television quality as very good (regarded as ratings of 80 and

above)?

A) 4%

B) 1%

C) 12%

D) 3%

8) 252 randomly sampled college students were asked, among other things, to estimate their college grade point average (GPA). The responses are shown in the stem-and-leaf plot shown below. Notice that a GPA of 3.65 would be indicated with a stem of 36 and a leaf of 5 in the plot. How many of the students who responded had GPA's that exceeded 3.55?

#### Stem and Leaf Plot of GPA

Leaf	f Digit U	nit = 0.01	Minimum 1.99	900	
19 9	epres	ents 1.99	Median 3.1050	0	
	_		Maximu	um 4.0000	
	Stem	Leaves			
1	19	9			
5	20	0668			
6	21	0			
11	22	05567			
15	23	0113			
20	24	00005			
33	25	0000000000067			
46	26	0000005577789			
61	27	000000134455578			
79	28	00000000144667799			
88	29	002356777			
116	30	000000000000000000001134	44559		
(19)	31	0000000000112235666			
117	32	000000000000000345568			
95	33	000000000025557			
80	34	000000000000000033344456	6667788		
49	35	000003355566677899			
31	36	000005			
25	37	022235588899			
13	38	00002579			
5	39	7			
4	40	0000			
252	cases in	cluded			
A) 31		B) 49	C	C) 39	D) 19

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

9) The scores for a statistics test are as follows:

```
87 76 91 77 94 96 88 85 66 89
79 96 54 98 83 88 82 56 18 69
```

Create a stem-and-leaf display for the data.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

10) For large data sets, a stem-and-leaf display is a better choice than a histogram.

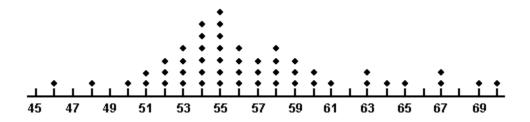
A) True B) False

## 3 Construct, Interpret Dot-Plot

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

11) A dot plot of the speeds of a sample of 50 cars passing a policeman with a radar gun is shown below.



What proportion of the motorists were driving above the posted speed limit of 60 miles per hour?

A) 0.18

B) 0.22

C) 0.04

D) 2

12) Which of the graphical techniques below can be used to summarize qualitative data?

A) bar graph

B) dot plot

C) stem-and-leaf plot

D) box plot

13) Parking at a university has become a problem. University administrators are interested in determining the average time it takes a student to find a parking spot. An administrator inconspicuously followed 300 students and recorded how long it took each of them to find a parking spot. Which of the following types of graphs should not be used to display information concerning the students parking times?

A) pie chart

B) stem-and-leaf display

C) histogram

D) box plot

14) Fill in the blank. One advantage of the \_\_\_\_\_\_ is that the actual data values are retained in the graphical summarization of the data.

- A) stem-and-leaf plot
- B) histogram

C) pie chart

#### Summation Notation

#### 1 Use Summation Notation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

# Solve the problem.

1) A data set contains the observations 2, 6, 4, 7, 3. Find  $\sum x$ .

D) 5

2) A data set contains the observations 8, 1, 6, 7, 2. Find

- - A) 576

- B) 154

D) 24

3) A data set contains the observations 5, 3, 6, 1, 4. Find  $\sum x^2$ .

A) 87

B) 361

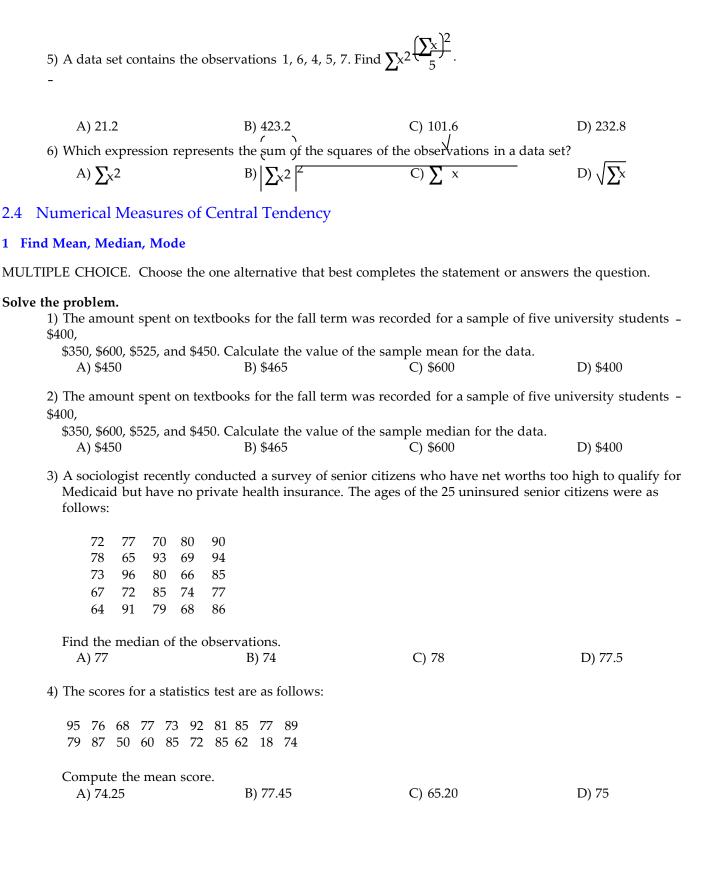
D) 19

4) A data set contains the observations 8, 3, 2, 6, 7. Find (x - 5).

A) 1

B) 51

D) 21



5) A shoe retailer keeps track of all types of information about sales of newly released shoe styles. One newly released style was marketed to tall people. Listed below are the shoe sizes of 12 randomly selected customers who purchased the new style. Find the mode of the shoe sizes.

$$9\frac{1}{2}$$
 11 12  $11\frac{1}{2}$ 
 $8\frac{1}{2}$   $10\frac{1}{2}$  8 11

10 11  $9\frac{1}{2}$  10

A) 11 B)  $10\frac{1}{4}$  C)  $10\frac{1}{2}$  D)  $9\frac{1}{2}$ 

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

6) Each year advertisers spend billions of dollars purchasing commercial time on network television. In the first 6 months of one year, advertisers spent \$1.1 billion. Who were the largest spenders? In a recent article, the top 10 leading spenders and how much each spent (in million of dollars) were listed:

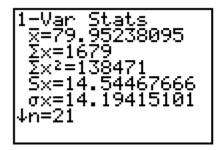
Company A	\$70.4	Company F	\$24.6
Company B	61.7	Company G	24.3
Company C	57.2	Company H	23.1
Company D	54.5	Company I	21.8
Company E	31.4	Company J	19.9

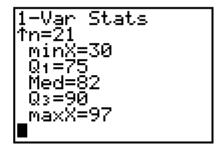
Calculate the mean and median for the data.

7) The data show the total number of medals (gold, silver, and bronze) won by each country winning at least one gold medal in the Winter Olympics. Find the mean, median, and mode of the numbers of medals won by these countries.

```
1 2 3 3 4 9 9 11 11
11 14 14 19 22 23 24 25 29
```

- 8) Calculate the mean of a sample for which  $\sum x = 196$  and n = 8.
- 9) The calculator screens summarize a data set.





- a. How many data items are in the set?
- b. What is the sum of the data?
- c. Identify the mean, median, and mode, if possible.

#### 2 Interpret Measures of Central Tendency

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Solve the problem.

- 10) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The statistician reported that the mean serve speed of a particular player was 95 miles per hour. Suppose that the statistician indicated that the serve speed distribution was skewed to the left. Which of the following values is most likely the value of the median serve speed?
  - A) 102 mph
- B) 88 mph
- C) 81 mph
- D) 95 mph
- 11) The amount spent on textbooks for the fall term was recorded for a sample of five hundred university students.

The mean expenditure was calculated to be \$500 and the median expenditure was calculated to be \$425. Which

of the following interpretations of the mean is correct?

- A) The average of the textbook costs sampled was \$500
- B) The most frequently occurring textbook cost in the sample was \$500
- C) 50% of the students sampled had textbook costs equal to \$500
- D) 50% of the students sampled had textbook costs that were less than \$500
- 12) The amount spent on textbooks for the fall term was recorded for a sample of five hundred university students.

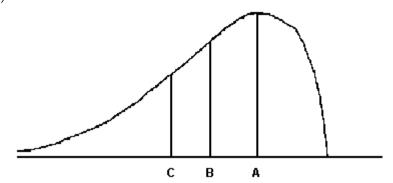
The mean expenditure was calculated to be \$500 and the median expenditure was calculated to be \$425. Which of the following interpretations of the median is correct?

- A) The average of the textbook costs sampled was \$425
- B) The most frequently occurring textbook cost in the sample was \$425
- C) 50% of the students sampled had textbook costs equal to \$425
- D) 50% of the students sampled had textbook costs that were less than \$425
- 13) During one recent year, U.S. consumers redeemed 6.79 billion manufacturers' coupons and saved themselves
  - \$2.56 billion. Calculate and interpret the mean savings per coupon.
    - A) The average savings was \$0.38 per coupon.
    - B) The average savings was 265.2 cents per coupon.
    - C) Half of all coupons were worth more than 265.2 cents in savings. D) Half of all coupons were worth more than \$0.38 in savings.
- 14) The output below displays the mean and median for the state high school dropout rates in year 1 and in year 5.

	Year 1	Year 5
N	51	51
MEAN	28.26	26.26
MEDIAN	27.41	25.28

Interpret the year 5 median dropout rate of 25.28.

- A) Half of the 51 states had a dropout rate below 25.28%.
- B) Most of the 51 states had a dropout rate close to 25.28%.
- C) The most frequently observed dropout rate of the 51 states was
- 25.28%. D) Half of the 51 states had a dropout rate of 25.28%.



for the distribution	drawn here	identify the mean.	median	and mode

A) A = mode, B = median, C = mean

B) A = median, B = mode, C = mean

C) A = mode, B = mean, C = median

D) A = mean, B = mode, C = median

16) In a distribution that is skewed to the right, what is the relationship of the mean, median, and mode?

A) mean > median > mode

B) median > mean > mode

C) mode > median > mode

D) mode > mean > median

17) Many firms use on-the-job training to teach their employees computer programming. Suppose you work in the personnel department of a firm that just finished training a group of its employees to program, and you have been requested to review the performance of one of the trainees on the final test that was given to all trainees. The mean of the test scores is 74. Additional information indicated that the median of the test scores was 84. What type of distribution most likely describes the shape of the test scores?

A) skewed to the left

B) symmetric

C) skewed to the right given

D) unable to determine with the information

18) A shoe company reports the mode for the shoe sizes of men's shoes is 12. Interpret this result.

- A) The most frequently occurring shoe size for men is size 12
- B) Most men have shoe sizes between 11 and 13.
- C) Half of the shoes sold to men are larger than a size 12
- D) Half of all men's shoe sizes are size 12

19) Which of the following is *not* a measure of central tendency?

A) range

- B) median
- C) mode

D) mean

20) The distribution of salaries of professional basketball players is skewed to the right. Which measure of central tendency would be the best measure to determine the location of the center of the distribution?

- A) median
- B) mode

C) mean

D) range

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

21) Parking at a university has become a problem. University administrators are interested in determining the average time it takes a student to find a parking spot. An administrator inconspicuously followed 280 students and recorded how long it took each of them to find a parking spot. The times had a distribution that was skewed to the left. Based on this information, discuss the relationship between the mean and the median for the

280 times collected.

22) The output below displays the mean and median for the state high school dropout rates in year 1 and in year 5.

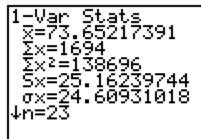
	Year 1	Year 5
N	51	51
MEAN	28.55	26.19
MEDIAN	27.85	25.82

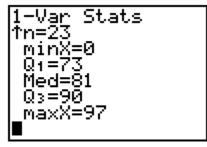
Use the information to determine the shape of the distributions of the high school dropout rates in year 1 and year 5.

23) The total points scored by a basketball team for each game during its last season have been summarized in the table below. Identify the modal class of the distribution of scores.

Score	Frequency
41-60	3
61-80	8
81-100	12
101-120	7

24) The calculator screens summarize a data set.





- a. Identify the mean and the median.
- b. Based only on the mean and the median, do you expect that the data set is skewed to the right, symmetric, or skewed to the left? Explain.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Answer the question True or False.

25) The mean and the median are useful measures of central tendency for both qualitative and quantitative data.

A) True B) False

26) In a symmetric and mound shaped distribution, we expect the values of the mean, median, and mode to differ greatly from one another.

A) True B) False

27) In symmetric distributions, the mean and the median will be approximately equal.

A) True B) False

28) In skewed distributions, the mean is the best measure of the center of the distribution since it is least affected by extreme observations.

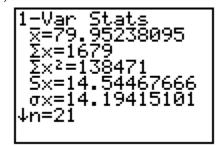
A) True B) False

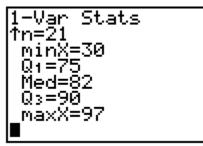
29) In practice, the population mean  $\mu$  is used to estimate the sample mean

A) True B) False

		general, .) True	the sa	imple	mean :	is a be	etter e	stimat	or of the po	pulation mean B) False	for larger sam	ple sizes.
2.5	Numer	rical M	easu	res of	f Vari	abilit	y					
1 Ca	lculate l	Range,	Varia	nce, S	tandar	rd Dev	viatio	n				
MUL	TIPLE C	HOICE.	. Cho	ose th	e one a	alterna	ative	that be	st complete	s the statement	or answers th	ne question.
Solve	first 6 mor	h year a	one ye	ear, ad	vertise	ers spe	ent \$1	.1 billi	on. Who we	ere the largest s	penders? In a	television. In the
	top	10 leadi	ing sp	ender	s and l	how n	nuch	each s <sub>l</sub>	ent (in mil	lion of dollars)	were listed:	
	(	Compan Compan Compan Compan	ny B ny C ny D	\$71.4 60.1 56.5 55 28.6	Co Co	ompan ompan ompan ompan ompan	y G y H y I	\$27.1 25.1 23.1 22.9 20.6				
		culate th		nple v	arianc		750 <b>2</b>	4.4		C) 2070 112		D) 1054.970
	А	.) 372.30	)/			Б) 3	759.2	44		C) 2070.113		D) 1854.860
	2) Calo	culate tl	he ran	ige of t	the fol	lowing	g data	a set:				
		, 9, 2, 8, .) 8	, 10, 6	, 6, 9		B) 1	0			C) 2	]	D) 12
		top spe							obiles are li	isted below. Ca	lculate the star	ndard deviation
	180,	100, 19	95, 130	), 155								
		38.177				B) 2	43.34	65		C) 174.0675		D) 137.11
	\$400, \$350	0, \$600,	\$525 <i>,</i>			alculat	te the			ole range for the	e data.	ersity students -
	A	.) \$99.37	/			В) \$	98.75			C) \$450		D) \$250
	\$400,		-							ded for a sample ble standard dev		ersity students -
		.) \$99.37					98.75		т по	C) \$450		D) \$250
SHOI	RT ANSV	VER. V	Vrite t	he wo	rd or p	phrase	that	best co	ompletes ea	ch statement or	answers the o	question.
		ages of se ages.	five r	randor	nly ch	osen p	profes	ssors a	re 69, 52, 55	i, 62, and 49. Ca	lculate the sar	mple variance of
	one		edal i	n the V	Winter	Olyn	npics.	Find t	he range, sa		•	try winning at least tandard deviation
	1	2	3	3	4	9	9	11	11			
	11	14	14	19	22	23	24	25	29			

8) The calculator screens summarize a data set.





a. Identify the smallest measurement in the data set. b. Identify the largest measurement in the data set.

c. Calculate the range of the data set.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

9) Calculate the variance of a sample for which n = 5,  $\sum x^2 = 1320$ ,  $\sum x = 80$ .

A) 10.00

B) 8.00

D) 3.16

10) Calculate the standard deviation of a sample for which n = 6,  $\sum_{x=0}^{\infty} x^2 = 830$ ,  $\sum_{x=0}^{\infty} x = 60$ .

B) 46.00

D) 164.00

11) Compute  $s^2$  and s for the data set: -2, -1, -3, -2, 1, -4

- A) 2.97; 1.72
- B) 1.8; 1.34
- C) 23.03; 4.8

D) 2.16; 1.47

12) Compute  $s^2$  and s for the data set;  $\frac{1}{5} \frac{3}{5} \frac{1}{5} \frac{1}{5} \frac{1}{5} \frac{1}{10}$ .

- A) 0.031; 0.176
- B) 0.013; 0.115
- C) 0.432; 0.658
- D) 3.1; 1.761

## 2 Interpret Measures of Variability

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

13) The range of scores on a statistics test was 42. The lowest score was 57. What was the highest score?

A) 99

B) 78

C) 70.5

D) cannot be determined

14) The temperature fluctuated between a low of 73°F and a high of 89°F. Which of the following could be calculated using just this information?

A) range

B) variance

C) standard deviation

D) median

15) Which of the following is a measure of the variability of a distribution?

A) range

- B) skewness
- C) median
- D) sample size

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

16) Various state and national automobile associations regularly survey gasoline stations to determine the current retail price of gasoline. Suppose one such national association contacts 200 stations in the United States to determine the price of regular unleaded gasoline at each station. In the context of this problem, define the

following descriptive measures:  $\mu$ ,  $\sigma$ , x, s.

17) Given the sample variance of a distribution, explain how to find the standard deviation.

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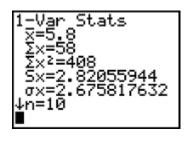
- 18) Which is expressed in the same units as the original data, the variance or the standard deviation?
- 19) Which measures variability about the mean, the range or the standard deviation?
- 20) For a given data set, which is typically greater, the range or the standard deviation?

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

21) The total points scored by a basketball team for each game during its last season have been summarized in the table below. Which statement following the table must be true?

Score	Frequency
41-60	3
61-80	8
81-100	12
101-120	7

- A) The range is at least 41 but at most 79.
- B) The range is 79.
- C) The range is at least 41 but at most 120.
- D) The range is at least 81 but at most 100.
- 22) Which number on the screen below is the sample standard deviation of the data?



A) 2.82

B) 408

C) 5.8

D) 2.67

#### Answer the question True or False.

- 23) The range is an insensitive measure of data variation for large data sets because two data sets can have the same range but be vastly different with respect to data variation.
  - A) True

- B) False
- 24) For any quantitative data set,  $\sum (x x) = 0$ .
  - A) True

- B) False
- 25) The sample variance and standard deviation can be calculated using only the sum of the data,  $\sum x$ , and the sample size, n.
  - A) True

- B) False
- 26) The sample variance is always greater than the sample standard deviation.
  - A) True

- B) False
- 27) A larger standard deviation means greater variability in the data.
  - A) True

B) False

# 2.6 Interpreting the Standard Deviation

## 1 Construct, Interpret Intervals About the Mean

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

- 1) The mean  $\bar{x}$  of a data set is 36.71, and the sample standard deviation s is 3.22. Find the interval representing measurements within one standard deviation of the mean.
  - A) (33.49, 39.93)
- B) (30.27, 43.15)
- C) (27.05, 46.37)
- D) (35.71, 37.71)

2) The following is a list of 25 measurements:

```
18
       14
          17
               19
                   16
                      14
                           18
                               15 17 11
13
   14
       11
           16
               18
                   15
                       13
                           17
                               15 14 19
12 16
       17
```

How many of the measurements fall within one standard deviation of the mean?

A) 16

B) 18

C) 13

- D) 25
- 3) A standardized test has a mean score of 500 points with a standard deviation of 100 points. Five students' scores are shown below.

Adam: 575 Beth: 690 Carlos: 750 Doug: 280 Ella: 440

Which of the students have scores within two standard deviations of the mean?

A) Adam, Beth, Ella

B) Adam, Beth

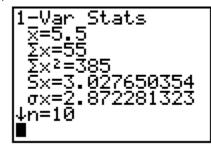
C) Adam, Beth, Carlos, Ella

D) Carlos,

Doug

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

- 4) The mean  $\bar{x}$  of a data set is 18, and the sample standard deviation s is 2. Explain what the interval (12, 24) represents.
- 5) The calculator screens summarize a data set.



- a. Identify the mean and the sample standard deviation. Round to one place after the decimal, where necessary.
- b. Find the interval that corresponds to measurements within two standard deviations of the mean.

#### 2 Use Empirical Rule

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Solve the problem.

6) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the

tournament. The statistician reported that the mean serve speed was 100 miles per hour (mph) and the standard deviation of the serve speeds was 15 mph. Assume that the statistician also gave us the information that the distribution of serve speeds was mound-shaped and symmetric. What percentage of the player's serves were between 115 mph and 145 mph?

A) approximately 16%
B) at most 13.5% C) at most 2.5%
D) at most 34%

7) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The statistician reported that the mean serve speed of a particular player was 98 miles per hour (mph) and the standard deviation of the serve speeds was 9 mph. Assume that the statistician also gave us the information that the distribution of the serve speeds was mound -shaped and symmetric. What proportion of the player's serves was between 107 mph and 116 mph?

A) 0.1350 B) 0.270 C) 0.95 D) 116

8) The amount of time workers spend commuting to their jobs each day in a large metropolitan city has a mean of

70 minutes and a standard deviation of 20 minutes. Assuming the distribution of commuting times is known to

be moundshaped and symmetric, what percentage of these commuting times are between 50 and 110 minutes?

A) approximately 68%

B) approximately 95%

C) approximately 97.5%

D) approximately 81.5%

9) The amount of television viewed by today's youth is of primary concern to Parents Against Watching Television (PAWT). 300 parents of elementary school-aged children were asked to estimate the number of hours per week that their child watches television. The mean and the standard deviation for their responses were 18 and 5, respectively. PAWT constructed a stem-and-leaf display for the data that showed that the distribution of times was a symmetric, mound-shaped distribution. Give an interval where you believe approximately 95% of the television viewing times fell in the distribution.

A) between 8 and 28 hours per week

B) less than 13 and more than 23 hours per

week

C) between 3 and 33 hours per week

D) less than 28

10) A sociologist recently conducted a survey of citizens over 60 years of age who have net worths too high to qualify for Medicaid but have no private health insurance. The ages of the 25 uninsured senior citizens were as follows:

68 73 66 76 86 74 61 89 65 90 69 92 76 62 81 63 68 81 70 73 60 87 75 64 82

Suppose the mean and standard deviation are 74.04 and 9.75, respectively. If we assume that the distribution of ages is mound-shaped and symmetric, what percentage of the respondents will be between 64.29 and 93.54 years old?

A) approximately 81.5%

B) approximately 68%

C) approximately 95%

D) approximately 84%

11) A small computing center has found that the number of jobs submitted per day to its computers has a distribution that is approximately mound-shaped and symmetric, with a mean of 88 jobs and a standard deviation of 7. Where do we expect approximately 95% of the distribution to fall?

A) between 74 and 102 jobs per day C) between 67 and 109 jobs per day

B) between 81 and 95 jobs per day D) between 102 and 109 jobs per day

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12) A study was designed to investigate the effects of two variables ■ (1) a student's level of mathematical anxiety and (2) teaching method ■ on a student's achievement in a mathematics course. Students who had a low level of mathematical anxiety were taught using the traditional expository method. These students obtained a mean

score of 260 with a standard deviation of 30 on a standardized test. Assuming a mound-shaped and symmetric distribution, what percentage of scores exceeded 200?

A) approximately 97.5%

B) approximately

95% C) approximately 100%

D)

approximately 84%

13) A study was designed to investigate the effects of two variables ■ (1) a student's level of mathematical anxiety and (2) teaching method ■ on a student's achievement in a mathematics course. Students who had a low level of mathematical anxiety were taught using the traditional expository method. These students obtained a mean

score of 350 with a standard deviation of 40 on a standardized test. Assuming a mound-shaped and symmetric distribution, in what range would approximately 99.7% of the students score?

A) between 230 and 470

B) below 470

C) above 470

D) below 230 and above 470

14) A recent survey was conducted to compare the cost of solar energy to the cost of gas or electric energy. Results of the survey revealed that the distribution of the amount of the monthly utility bill of a 3 - bedroom house using gas or electric energy had a mean of \$135 and a standard deviation of \$11. If the distribution can be considered mound-shaped and symmetric, what percentage of homes will have a monthly utility bill of more than \$124?

A) approximately 84% C) approximately 16%

B) approximately 95%

D) approximately 34%

15) Many firms use on-the-job training to teach their employees computer programming. Suppose you work in the personnel department of a firm that just finished training a group of its employees to program, and you have been requested to review the performance of one of the trainees on the final test that was given to all trainees. The mean and standard deviation of the test scores are 79 and 2, respectively, and the distribution of scores is mound-shaped and symmetric. What percentage of test-takers scored better than a trainee who scored 73?

A) approximately 100%

B) approximately 84%

C) approximately 95%

D) approximately 97.5%

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

- 16) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The statistician reported that the mean serve speed of a particular player was 104 miles per hour (mph) and the standard deviation of the serve speeds was 11 mph. Assume that the statistician also gave us the information that the distribution of serve speeds was mound-shaped and symmetric. Find the percentage of serves that were hit faster than 82 mph.
- 17) A small computing center has found that the number of jobs submitted per day to its computers has a distribution that is approximately mound-shaped and symmetric, with a mean of 86 jobs and a standard deviation of 5. On what percentage of days do the number of jobs submitted exceed 91?
- 18) By law, a box of cereal labeled as containing 36 ounces must contain at least 36 ounces of cereal. The machine filling the boxes produces a distribution of fill weights that is mound-shaped and symmetric, with a mean equal to the setting on the machine and with a standard deviation equal to 0.04 ounce. To ensure that most of the boxes contain at least 36 ounces, the machine is set so that the mean fill per box is 36.12 ounces. What percentage of the boxes do, in fact, contain at least 36 ounces?

- 19) Many firms use on-the-job training to teach their employees computer programming. Suppose you work in the personnel department of a firm that just finished training a group of its employees to program, and you have been requested to review the performance of one of the trainees on the final test that was given to all trainees. The mean and standard deviation of the test scores are 83 and 3, respectively, and the distribution of scores is mound-shaped and symmetric. If a firm wanted to give the best 2.5% of the trainees a big promotion, what test score would be used to identify the trainees in question?
- 20) The following data represent the scores of 50 students on a statistics exam. The mean score is 80.02, and the standard deviation is 11.9.

39	51	59	63	66	68	68	69	70	71
71	71	73	74	76	76	76	77	78	79
79	79	79	80	80	82	83	83	83	85
85	86	86	88	88	88	88	89	89	89
90	90	91	91	92	95	96	97	97	98

What percentage of the scores lies within one standard deviation of the mean? two standard deviations of the

mean? three standard deviations of the mean? Based on these percentages, do you believe that the distribution

of scores is mound-shaped and symmetric? Explain.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

21) The distribution of scores on a test is mound-shaped and symmetric with a mean score of 78. If 68% of the scores fall between 72 and 84, which of the following is most likely to be the standard deviation of the distribution?

۸ ۱	_
$\boldsymbol{A}$	n

B) 2

C) 3

D) 12

#### 3 Use Chebyshev's Rule

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Solve the problem.

22) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the

tournament. The statistician reported that the mean serve speed was 100 miles per hour (mph) and the standard deviation of the serve speeds was 15 mph. If nothing is known about the shape of the distribution, what percentage of the player's serve speeds are less than 70 mph?

A) approximately

2.5% B) at most 12.5%

C) at most

11% D) at

most 25%

- E) approximately 5%
- 23) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The statistician reported that the mean serve speed of a particular player was 104 miles per hour (mph) and the standard deviation of the serve speeds was 11 mph. If nothing is known about the shape of the distribution, give an interval that will contain the speeds of at least three-fourths of the player's serves.

A) 82 mph to 126 mph

B) 93 mph to 115 mph

C) 71 mph to 137 mph

D) 126 mph to 148 mph

24) The amount of time workers spend commuting to their jobs each day in a large metropolitan city has a mean of

70 minutes and a standard deviation of 20 minutes. Assuming nothing is known about the shape of the distribution of commuting times, what percentage of these commuting times are between 30 and 110 minutes?

A) at least 0%

B) at least 75%

C) at least 89%

D) at least 95%

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machine filling the boxes produces a distribut machine and with a standard deviation equal	8 ounces must contain at least 18 ounces of cereal. The ion of fill weights with a mean equal to the setting on the to 0.03 ounce. To ensure that most of the boxes contain at mean fill per box is 18.09 ounces. Assuming nothing is
	hat can be said about the proportion of cereal boxes that
contain less than 18 ounces.	
A) The proportion is at most 11%. C) The proportion is at most 5.5%.	B) The proportion is at least 89%. D) The proportion is less than 2.5%.
anxiety and (2) teaching method ■ on a stude had a low level of mathematical anxiety were students obtained a mean score of 370 with a no information concerning the shape of the dibetween 330 and 410?	ts of two variables <b>1</b> (1) a student's level of mathematical nt's achievement in a mathematics course. Students who taught using the traditional expository method. These standard deviation of 20 on a standardized test. Assuming stribution is known, what percentage of the students scored
A) at least 75%	B) approximately
95% C) at least 89% approximately 68%	D)
anxiety and (2) teaching method ■ on a stude had a low level of mathematical anxiety were	ts of two variables <b>1</b> (1) a student's level of mathematical nt's achievement in a mathematics course. Students who taught using the traditional expository method. These standard deviation of 50 on a standardized test. Assuming a ntage of the students scored over 620?  B) approximately 2.5% D) at most 5.5%
Results of the survey revealed that the distributed bedroom house using gas or electric energy has been supported by the survey revealed that the distributed by the survey revealed by the	ne cost of solar energy to the cost of gas or electric energy.  ution of the amount of the monthly utility bill of a 3 -  ad a mean of \$104 and a standard deviation of \$10. If  ibution, what percentage of homes will have a monthly  C) at most 11.1%  D) at least 88.9%
work in the personnel department of a firm the program, and you have been requested to revethat was given to all trainees. The mean and s	their employees computer programming. Suppose you nat just finished training a group of its employees to iew the performance of one of the trainees on the final test tandard deviation of the test scores are 74 and 2, but the distribution, what percentage of test-takers scored  B) at least 89% D) approximately 99.85%
30) If nothing is known about the shape of a distribution within 2 standard deviations of the mean?	ibution, what percentage of the observations fall
A) at least 75%	B) at most 25%
C) approximately 95%	D) approximately 5%
31) Fill in the blankgives us a method set, regardless of the shape of the distribution	d of interpreting the standard deviation of any data
A) Chebyshev's Rule	B) The Empirical Rule
C) both A and B	D) neither A nor B
32) Fill in the blank is a method of int	
have a mound-shaped, symmetric distributio	
<ul><li>A) The Empirical Rule</li><li>C) both A and B</li></ul>	B) Chebyshev's Rule D) neither A nor B
	D) INTURE A HOLD

33)			st likely to be the percentage of	f data within three
	standard deviations of A) 95%	B) 65%	C) 70%	D) 85%
Answer t	the question True or Fa	alse.		
34)	Both Chebyshev's rule deviations from the m		guarantee that no data item wil	ll be more than four standard
	A) True		B) False	
35)	) Chebyshev's rule appl	lies to qualitative data s	ets, while the empirical rule apposets.	plies to quantitative data
	A) True		B) False	
36)	) Chebyshev's rule appl A) True	ies to large data sets, wl	nile the empirical rule applies t B) False	o small data sets.
37)			est have a mean of 83 points with ored at least 70 on the test.  B) False	th a standard deviation of 4
2.7 Nu	ımerical Measures o	of Relative Standing		
1 Comp	ute, Interpret z-Score			
MULTIPI	LE CHOICE. Choose th	ne one alternative that b	est completes the statement or	answers the question.
	program, and you have that was given to all tr respectively, and the d	re been requested to revi rainees. The mean and st	at just finished training a group iew the performance of one of t tandard deviation of the test so mound-shaped and symmetric. trainee's $z$ -score. C) $z = -24$	The trainees on the final test ores are 72 and 3,
2)	The amount spent on	textbooks for the fall ter	m was recorded for a sample of	f five hundred university
st	calculated		600 and the standard deviation ent reported that their textbook	-
	the z-score for this stu A) +2	ident's textbook expend B) -2	iture. C) +3	D) -3
	Results of the survey rebedroom house using solar homes reported at A) Homes using sol B) The utility bills for and electricity.  C) Homes using sol electricity. D) Homes electricity.	revealed that the distribution gas or electric energy has monthly utility bills of \$\frac{1}{2}\$ ar power may have low or homes using solar power may actually has using solar power alw	e cost of solar energy to the cost of the amount of the moned a mean of \$112 and a standa 559, \$63, and \$64. Which of the er utility bills than homes using wer are about the same as those have higher utility bills than howays have lower utility bills that extrising each hour has a mean of	thly utility bill of a 3 - rd deviation of \$15. Three following statements is true? g only gas and electricity. e for homes using only gas and mes using only gas and n homes using only gas and

B) z = 2.96D) z = 0.33C) z = -21.6Copyright © 2013 Pearson Education, Inc.

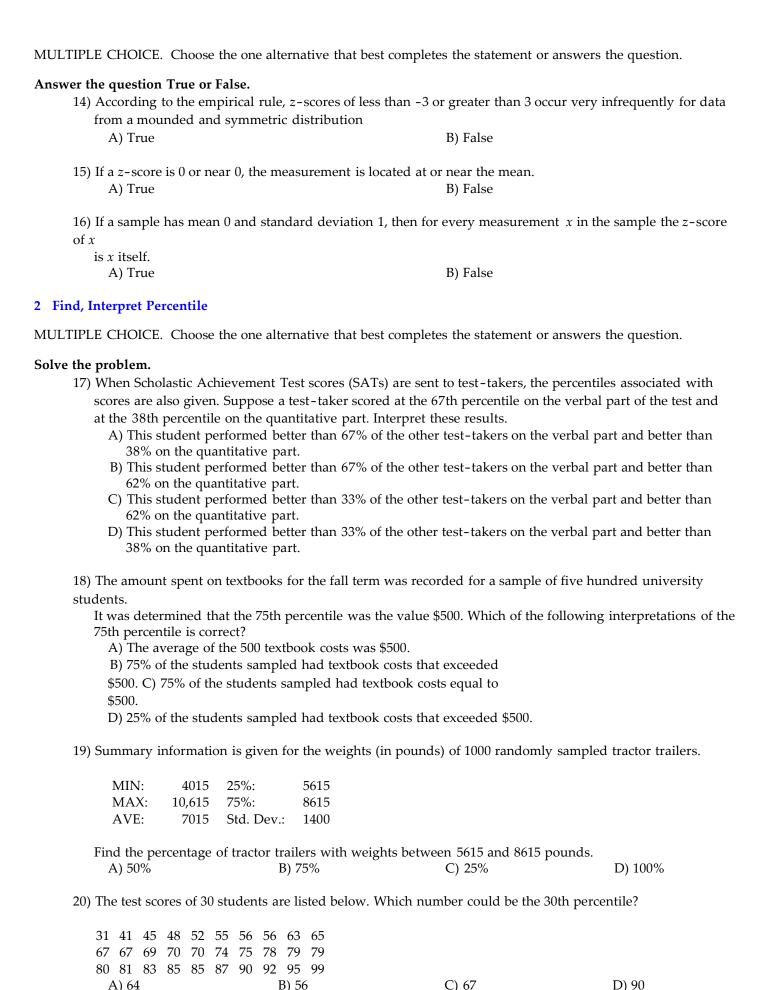
of advertising time is 8 minutes. Calculate the *z*-score for this amount of advertising time.

A) z = -2.96

	5) On a given day, the price of a gallon of milk had a mean price of \$2.30 with a standard deviation of \$0.0 A	5.
	particular food store sold milk for \$2.25/gallon. Interpret the z-score for this gas station.	
	A) The milk price of this food store falls 1 standard deviation below the milk gas price of all food store B) The milk price of this food store falls 1 standard deviation above the mean milk price of all food stores.	es.
	C) The milk price of this food store falls 5 standard deviations below the mean milk price of all food stores. D) The milk price of this food store falls 5 standard deviations above the mean milk price of all food stores.	l
	6) Which of the following is a measure of relative standing? A) z-score B) mean C) variance D) pie chart	
SHOR	T ANSWER. Write the word or phrase that best completes each statement or answers the question.	
	7) A study was designed to investigate the effects of two variables $\blacksquare$ (1) a student's level of mathematical anxiety and (2) teaching method $\blacksquare$ on a student's achievement in a mathematics course. Students who had a low level of mathematical anxiety were taught using the traditional expository method. These students obtained a mean score of 380 and a standard deviation of 50 on a standardized test. Find and interpret the $z$ -score of a student who scored 450 on the standardized test.	
	8) A recent survey was conducted to compare the cost of solar energy to the cost of gas or electric energy. Results of the survey revealed that the distribution of the amount of the monthly utility bill of a 3-bedroom house using gas or electric energy had a mean of \$142.00 and a standard deviation of \$15.00. Assuming the distribution is mound-shaped and symmetric, would you expect to see a 3-bedroom housing gas or electric energy with a monthly utility bill of \$239.50? Explain.	ıse
MULT	TIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.	
	9) Find the <i>z</i> -score for the value 100, when the mean is 69 and the standard deviation is 5. A) $z = 6.20$ B) $z = 6.00$ C) $z = -1.38$ D) $z = 1.38$	
SHOR	T ANSWER. Write the word or phrase that best completes each statement or answers the question.	
	10) Test scores for a history class had a mean of 79 with a standard deviation of 4.5. Test scores for a physical class had a mean of 69 with a standard deviation of 3.7. One student earned a 86 on the history test and 85 on the physics test. Calculate the <i>z</i> -score for each test. On which test did the student perform better?	
	11) The following data represent the scores of 50 students on a statistics exam. The mean score is 80.02, and the standard deviation is 11.9.	
	39 51 59 63 66 68 68 69 70 71 71 71 73 74 76 76 76 77 78 79 79 79 79 80 80 82 83 83 83 85 85 86 86 88 88 88 88 89 89 89 90 90 91 91 92 95 96 97 97 98	
	Find the <i>z</i> -scores for the highest and lowest exam scores.	
	12) The <i>z</i> -score for a value <i>x</i> is -2.5. State whether the value of <i>x</i> lies above or below the mean and by how many standard deviations.	
	13) Suppose that 50 and 75 are two elements of a population data set and their $z$ -scores are -3 and 2,	

respectively.

Find the mean and standard deviation.



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SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

- 21) A retail store's customer satisfaction rating is at the 88<sup>th</sup> percentile. What percentage of retail stores has higher customer satisfaction ratings than this store?
- 22) In a summary of recent real estate sales, the median home price is given as \$325,000. What percentile corresponds to a home price of \$325,000?

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

- 23) The mean of a data set is at the 50<sup>th</sup> percentile.
  - A) True

B) False

- 24) Percentile rankings are of practical value only with large data sets.
  - A) True

3) Fals

25) The process for finding a percentile is similar to the process for finding the median.

A) Tru

B) False

## 2.8 Methods for Detecting Outliers: Box Plots and z-Scores

#### 1 Determine if Datum is an Outlier

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

1) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the

tournament. The statistician reported that the mean serve speed of a particular player was 103 miles per hour

(mph) and the standard deviation of the serve speeds was 12 mph. Using the z-score approach for detecting outliers, which of the following serve speeds would represent outliers in the distribution of the player's serve speeds?

Speeds: 61 mph, 115 mph, and 127 mph

A) 61 is the only outlier. not. C) 61, 115, and 127 are all outliers. outlier. B) 61 and 115 are both outliers, but 127 is D) None of the three speeds is an

2) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The statistician reported that the mean serve speed of a particular player was 100 miles per hour (mph) and the standard deviation of the serve speeds was 15 mph. Using the z -score approach for detecting outliers, which of the following serve speeds would represent outliers in the distribution of the player's serve speeds?

Speeds: 50 mph, 80 mph, and 105 mph A) 50 is the only outlier.

not. C) 50, 80, and 105 are all outliers.

outliers.

- B) 50 and 80 are both outliers, 105 is
  - D) None of the three speeds are
- 3) The speeds of the fastballs thrown by major league baseball pitchers were measured by radar gun. The mean speed was 87 miles per hour. The standard deviation of the speeds was 3 mph. Which of the following speeds would be classified as an outlier?
  - A) 97 mph
- B) 81 mph
- C) 92 mph
- D) 84 mph

- 4) Which of the following statements concerning the box plot and *z*-score methods for detecting outliers is false?
  - A) The *z*-score method is less affected by an extreme observation in the data set. B) The box plot method uses the quartiles as a basis for detecting outliers.
  - C) The *z*-score method uses the mean and standard deviation as a basis for detecting outliers. D) The box plot method is less affected by an extreme observation in the data set.
- 5) Which of the following statements could be an explanation for the presence of an outlier in the data?
  - A) The measurement may be correct and from the same population as the rest but represents a rare event.

Generally, we accept this explanation only after carefully ruling out all others.

- B) The measurement is incorrect. It may have been observed, recorded, or entered into the computer incorrectly.
- C) The measurement belongs to a population different from that from which the rest of the sample was drawn.
- D) All of the above are explanations for outliers.

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

- 6) A radio station claims that the amount of advertising each hour has an a mean of 15 minutes and a standard deviation of 1.2 minutes. You listen to the radio station for 1 hour and observe that the amount of advertising time is 12.96 minutes. Based on your observation, what would you infer about the radio station's claim?
- 7) The following data represent the scores of 50 students on a statistics exam. The mean score is 80.02, and the standard deviation is 11.9.

39	51	59	63	66	68	68	69	70	71
71	71	73	74	76	76	76	77	78	79
79	79	79	80	80	82	83	83	83	85
85	86	86	88	88	88	88	89	89	89
90	90	91	91	92	95	96	97	97	98

Use the *z*-score method to identify potential outliers among the scores.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Answer the question True or False.

A) True

8) The <i>z</i> -score uses the quartiles to identify outliers in a data set.				
A) True	B) False			
9) An outlier is defined as any A) True	observation that falls within the outer fences of a box plot.  B) False			
10) Box plots are used to detect outliers in quantitative data	outliers in qualitative data sets, while $z$ -scores are used to detect sets.			
A) True	B) False			

11) An outlier in a data set may have a simple explanation such as a scale was not working properly or the researcher inverted the digits of a number when recording a measurement.

12	) An outlier may be caused by accidentally including the height of a six-year-old boy in a set of
	data representing the heights of 12-year-old boys.

A) True B) False

B) False

13) The outer fences of a box plot are three standard deviations from the mean.

A) True

B) False

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#### 2 Calculate Quartiles and IQR

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

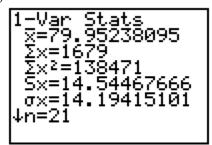
#### Solve the problem.

- 14) At the U.S. Open Tennis Championship a statistician keeps track of every serve that a player hits during the tournament. The lower quartile of a particular player's serve speeds was reported to be 94 mph. Which of the following interpretations of this information is correct?
  - A) 75% of the player's serves were hit at speeds greater than 94
  - mph. B) 25% of the player's serves were hit at 94 mph.
  - C) 75% of the player's serves were hit at speeds less than 94
  - mph. D) 94 serves traveled faster than the lower quartile.
- 15) A sociologist recently conducted a survey of citizens over 60 years of age who have net worths too high to qualify for Medicaid but have no private health insurance. The ages of the 25 uninsured senior citizens were as follows:

```
68 73 66 76 86 74 61 89 65 69 92 76
62 81 63 68 81 70 73 60 87 64 82
75
Find the upper quartile of the data.
A) 81.5
B) 65.5
C) 73
D) 92
```

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

- 16) The amount of television viewed by today's youth is of primary concern to Parents Against Watching Television (PAWT). Three hundred parents of elementary school-aged children were asked to estimate the number of hours per week that their child watches television. The upper quartile for the distribution was given as 15 hours. Interpret this value.
- 17) For a given data set, the lower quartile is 45, the median is 50, and the upper quartile is 57. The minimum value in the data set is 32, and the maximum is 81.
  - a. Find the interquartile range. b. Find the inner fences.
  - c. Find the outer fences.
  - d. Is either of the minimum or maximum values considered an outlier? Explain.
- 18) The calculator screens summarize a data set.



```
1-Var Stats
↑n=21
minX=30
Q1=75
Med=82
Q3=90
maxX=97
```

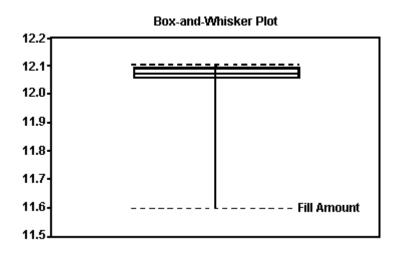
- a. Identify the lower and upper quartiles of the data set. b. Find the interquartile range.
- c. Is there reason to suspect that the data may contain an outlier? Explain.

#### 3 Construct, Interpret Boxplot

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

#### Solve the problem.

19) The box plot shown below displays the amount of soda that was poured by a filling machine into 12 - ounce soda cans at a local bottling company.



Based on the box plot, what shape do you believe the distribution of the data to have?

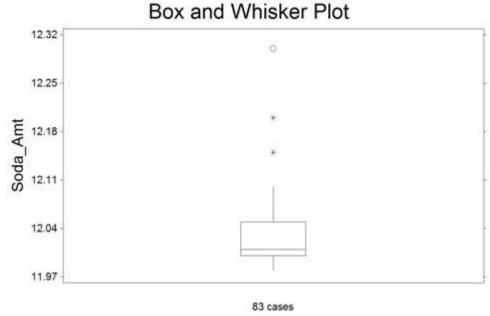
A) skewed to the left

B) approximately symmetric

C) skewed to the right

- D) skewed to the center
- 20) The box plot shown below was constructed for the amount of soda that was poured by a filling machine into

12-ounce soda cans at a local soda bottling company.



We see that one soda can received 12.15 ounces of soda on the plot above. Based on the box plot presented, how would you classify this observation?

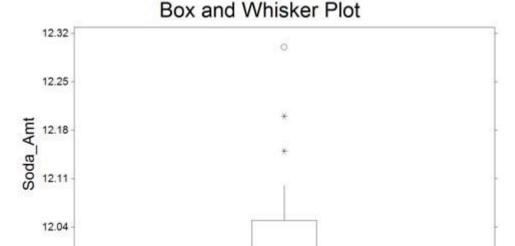
A) expected observation

B) suspect outlier

C) highly suspect outlier

D) it has a lot of soda

- 21) The box plot shown below was constructed for the amount of soda that was poured by a filling machine into
  - 12-ounce soda cans at a local soda bottling company.



83 cases

We see that one soda can received 12.30 ounces of soda on the plot above. Based on the box plot presented, how would you classify this observation?

A) expected observation

11.97

B) suspect outlier

C) highly suspect outlier

D) it has a lot of soda

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

22) The following data represent the scores of 50 students on a statistics exam.

39	51	59	63	66	68	68	69	70	71
71	71	73	74	76	76	76	77	78	79
79	79	79	80	80	82	83	83	83	85
85	86	86	88	88	88	88	89	89	89
90	90	91	91	92	95	96	97	97	98

- a. Find the lower quartile, the upper quartile, and the median of the scores.
- b. Find the interquartile range of the data and use it to identify potential outliers.
- c. In a box plot for the data, which scores, if any, would be outside the outer fences? Which scores, if any, would be outside the inner fences but inside the outer fences?
- 23) Use a graphing calculator or software to construct a box plot for the following data set.

# 2.9 Graphing Bivariate Relationships (Optional)

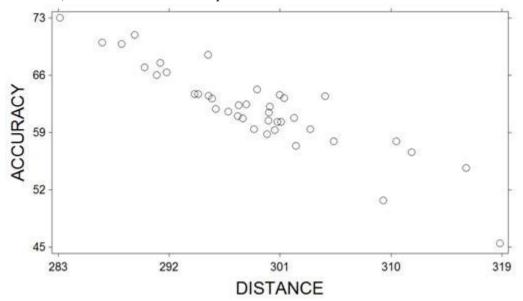
## 1 Construct, Interpret Scatterplot

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Solve the problem.

1) A sample of professional golfers was taken and their driving distance (measured as the average distance as

their drive off the tee) and driving accuracy (measured as the percentage of fairways that their drives landed in) were recorded. A scatterplot of the variables is shown below.



What relationship do these two variables exhibit?

- A) They exhibit no relationship
- C) They exhibit a negative linear relationship
- B) They exhibit a positive linear relationship
- D) They exhibit a curvillinear relationship

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

2) The data below represent the numbers of absences and the final grades of 15 randomly selected students from a statistics class. Construct a scattergram for the data. Do you detect a trend?

Student	Number of Absences	Final Grade as
1	5	79
2	6	78
3	2	86
4	12	56
5	9	75
6	5	90
7	8	78
8	15	48
9	0	92
10	1	78
11	9	81
12	3	86
13	10	75
14	3	89
15	11	65

3) The scores of nine members of a women's golf team in two rounds of tournament play are listed below.

Player									
Round 1 Round 2	85	90	87	78	92	85	79	93	86
Round 2	90	87	85	84	86	78	77	91	82

Construct a scattergram for the data.

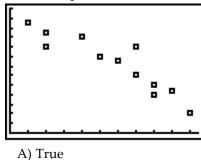
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

## Answer the question True or False.

- 4) Scatterplots are useful for both qualitative and quantitative data.
  - A) True

B) False

5) The scatterplot below shows a negative relationship between two variables.



B) False

# 2.10 Distorting the Truth with Descriptive Statistics

## 1 Understand Misleading Statistics

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

## Solve the problem.

- 1) Explain how stretching the vertical axis of a histogram can be misleading.
- 2) Explain how using a scale break on the vertical axis of a histogram can be misleading.
- 3) Explain how it can be misleading to draw the bars in a histogram so that the width of each bar is proportional to its height rather than have all bars the same width.
- 4) Explain how it can be misleading to report only the mean of a distribution without any measure of the variability.

# Ch. 2 Methods for Describing Sets of Data **Answer Key**

# 2.1 Describing Qualitative Data

- 1 Identify Classes/Compute Class Frequencies/Relative Frequencies/Percentages
  - 1) A
  - 2) A
  - 3) free account, institutional account, account paid for personally
- 2 Construct Frequency/Relative Frequency Table
  - 4) A
  - 5) A
  - 6)

Color	Frequency
Green	3
Blue	7
Brown	5
Orange	2
Red	3

7) B

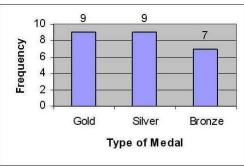
- 3 Construct, Interpret Bar Graph
  - 8) B
  - 9) A
  - 10) A
  - 11) a.

Medal	Frequency			
Gold	9			
Silver	9			
Bronze	7			

b.

Medal	Relative
	Frequency
Gold	.36
Silver	.36
Bronze	.28

c.

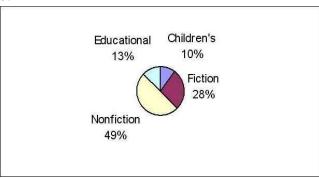


- 12) A
- 13) A
- 4 Construct, Interpret Pie Chart
  - 14) A
  - 15) C

# 16) a.

Type of Book	Relative		
	Frequency		
Children's	.10		
Fiction	.28		
Nonfiction	.49		
Educational	.13		

b.



- 17) A
- 18) B

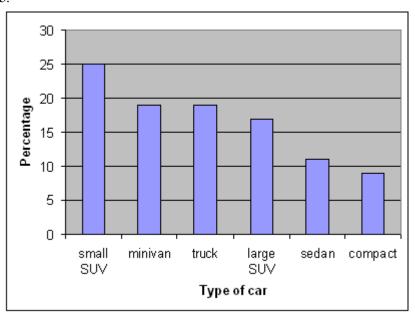
# 5 Construct, Interpret Pareto Diagram

19) In a Pareto diagram, the bars are arranged by height in a descending order from left to right.

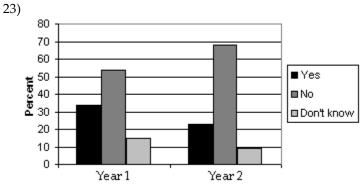
20) a.

Car	Relative
	Frequency
compact	0.09
sedan	0.11
small SUV	0.25
large SUV	0.17
minivan	0.19
truck	0.19

b.



- 21) B 22) B
- 6 Construct, Interpret Side-by-Side Bar Chart



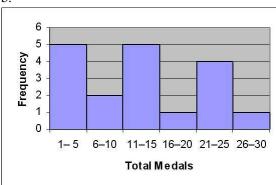
Losses due to employee theft have decreased from year 1 to year 2.

- 2.2 Graphical Methods for Describing Quantitative Data
- 1 Construct, Interpret Histogram
  - 1) B

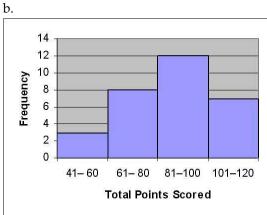
2) a.

Total Medals	Frequency	
1-5	5	
6-10	2	
11-15	5	
16-20	1	
21-25	4	
26-30	1	

b.



3) a. The exact scores would be needed to construct a stem-and-leaf display but the exact scores are not available in the table given.



- 4) A
- 5) A
- 6) B

2 Construct, Interpret Stem-and-Leaf Display

- 7) A
- 8) C
- 9)

Stem	
1	8
2	
2 3	
4	
5	4 6 6 9 6 7 9
6	6 9
7	6 7 9
8	2357889 14668
9	1 4 6 6 8

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- 10) B
- 3 Construct, Interpret Dot-Plot
  - 11) A
  - 12) A
  - 13) A
  - 14) A
- 2.3 Summation Notation
- 1 Use Summation Notation
  - 1) A
  - 2) A
  - 3) A
  - 4) A
  - 5) A
  - 6) A
- 2.4 Numerical Measures of Central Tendency
- 1 Find Mean, Median, Mode
  - 1) B
  - 2) A
  - 3) A
  - 4) A
  - 5) A
  - 6) The mean of the data is  $x = \frac{\sum x}{n}$

$$70.4 + 61.7 + 57.2 + 54.5 + 31.4 + 24.6 + 24.3 + 23.1 + 21.8 + 19.9$$

$$=\frac{388.9}{10}$$

 $= 38.89 \Rightarrow $38.89 \text{ million}$ 

The median is the average of the middle two observations.

$$M = \frac{31.4 + 24.6}{2} = 28.00 \Rightarrow $28.00 \text{ million}$$

7) The mean is the sum of the numbers divided by 18:

$$=\frac{234}{18}$$
 = 13 medals.

The median is the mean of the two middle numbers:  $\frac{11 + 11}{2} = 11$  medals.

The mode is the most frequent number of medals: 11 medals.

8) The mean is divided by

n:

$$\frac{\sum x}{n} = \frac{196}{8} = 24.5.$$

9) a. 
$$n = 21$$

b. 
$$\sum x = 1679$$

- c. mean:  $x \approx 79.95$ ; median: Med=82; mode: not possible
- 2 Interpret Measures of Central Tendency
  - 10) A
  - 11) A

- 12) D
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A
- 21) Since the distribution is skewed to the left, we know that the median time will exceed the mean time.
- 22) In both year 1 and year 5, the mean dropout rates exceed the median dropout rates. This indicates that both the year 1 and year 5 high school dropout rates have distributions that are skewed to the right.
- 23) The modal class is the class with the greatest frequency: 81-100 points.
- 24) a. mean:  $x \approx 73.65$ ; median: Med=81
  - b. We expect the data to be skewed to the left because the mean is less than the median.
- 25) B
- 26) B
- 27) A
- 28) B
- 29) B
- 30) A
- 2.5 Numerical Measures of Variability
- 1 Calculate Range, Variance, Standard Deviation
  - 1) A
  - 2) A
  - 3) A
  - 4) D
  - 5) A

6) 
$$s^2 = \frac{\sum (x - \overline{x})^2}{n - 1}$$

$$\overline{x} = \frac{\sum x}{n} = \frac{69 + 52 + 55 + 62 + 49}{5} = 57.4$$

$$s^2 = \frac{(69-57.4)^2 + (52-57.4)^2 + (55-57.4)^2 + (62-57.4)^2 + (49-57.4)^2}{5-1}$$

$$= 65.30$$

7) The range is 29 - 1 = 28 medals.

The variance is 
$$s^2 = \frac{\left(\sum x\right)^2}{n-1} = \frac{(234)^2}{4372 - 18} = \frac{1330}{17} \approx 78.24$$

The standard deviation is 
$$s = \sqrt{s} \ 2 = \sqrt{\frac{1330}{17}} \approx 8.85$$

- 8) a. minX=30
  - b.

maxX=97

c. 
$$97 - 30 = 67$$

- 9) A
- 10) A
- 11) A
- 12) A

2	Interpret Measures of Variability		
	13) A		
	14) A 15) A		
	16) $\mu$ is the mean price of the regular unleaded gasoline prices of all retail gas stations in the United States.		
	$\sigma$ is the standard deviation of the regular unleaded gasoline prices of all retail gas stations in the United States.		
	$\bar{x}$ is the mean price of the regular unleaded gasoline prices collected from the 200 stations sampled.		
<i>s</i> is the standard deviation of the regular unleaded gasoline prices collected from the 200 stations sampled 17) Take the square root of the sample variance to find the sample standard deviation. 18) standard deviation			
	19) standard deviation		
	20) range		
	21) A		
	22) A		
	23) A		
	24) A 25) B		
	26) B		
	27) A		
2.	6 Interpreting the Standard Deviation		
	Construct, Interpret Intervals About the Mean		
	1) A		
	2) A		
	3) A		
	4) measurements within three standard deviations of the mean		
	5) a. mean: $x = 5.5$ ; sample standard deviation: $S_{\chi} \approx$		
	3.0 b. $(5.5 - 2 \times 3.0, 5.5 + 2 \times 3.0) = (5, 11.5)$		
2	Use Empirical Rule		
	6) A		
	7) A		
	8) D 9) A		
	10) A		
	14) A		

- 11) A 12) A
- 13) A
- 14) A
- 15) A
- 16) We use the Empirical Rule to determine the percentage of serves with speeds faster than 82 mph. We do this by first

finding the percentage of serves with speeds between 82 and 104 mph. The Empirical Rule states that approximately

34.0% (68%/2) fall between 82 and 104 mph. Because the distribution is symmetric about the mean speed of 104 mph,

we know 50% of the serve speeds were faster than 104 mph. We add these findings together to determine that 34.0% + 50% = 84.0% of the serves were hit faster than 82 mph.

- 17) The value 91 falls one standard deviation above the mean in the distribution. Using the Empirical Rule, 68% of the days will have between 81 and 91 jobs submitted. Of the remaining 32% of the days, half, or 32%/2 = 16%, of the days will have more than 91 jobs submitted.
- 18) The value of 36 ounces falls three standard deviations below the mean. The Empirical Rule states that approximately all of the boxes will contain cereal amounts between 36.00 ounces and 36.24 ounces. Therefore, approximately 100% of the boxes contain at least 36 ounces.

- 19) The Empirical Rule states that 95% of the data will fall between 77 and 89. Because the distribution is symmetric, half of the remaining 5%, or 2.5%, will have test scores above 89. Thus, 89 is the cutoff point that will identify the trainees who will receive the promotion.
- 20) 74% of the scores lie within one standard deviation of the mean, 96% within two standard deviations, and 98% within

three standard deviations. These percentages are close to those given in the Empirical Rule, so the distribution is roughly mound-shaped and symmetric, though obviously skewed slightly to the left.

21) A

## 3 Use Chebyshev's Rule

- 22) D
- 23) A
- 24) B
- 25) A
- 26) A
- 27) A
- 28) A
- 29) A
- 30) A
- 31) A
- 32) A
- 33) A
- 34) B
- 35) B
- 36) B
- 37) A

## 2.7 Numerical Measures of Relative Standing

## 1 Compute, Interpret z-Score

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A

7) The *z*-score is 
$$z = \frac{x - \mu}{\sigma}$$
.

For a score of 45, 
$$z = \frac{450 - 380}{50} = 1.40$$
.

This student's score falls 1.40 standard deviations above the mean score of 380.

8) The z-score for the value \$239.50 is:

$$z = \frac{x - \overline{x}}{s} = \frac{239.5 - 142}{15} = 6.5$$

An observation that falls 6.5 standard deviations above the mean is very unlikely. We would not expect to see a

monthly utility bill of \$239.50 for this home.

- 9) A
- 10) history z-score = 1.56; physics z-score = 4.32; The student performed better on the physics test.
- 11) highest: z = 1.51; lowest: z = -3.45
- 12) The value of x lies 2.5 standard deviations below the mean.
- 13) mean: 65; standard deviation: 5
- 14) A
- 15) A
- 16) A

2	Find,	Interpret	Percenti	le
---	-------	-----------	----------	----

- 17) A
- 18) D
- 19) A
- 20) A
- 21) 12%
- 22) 50<sup>th</sup> percentile
- 23) B
- 24) A
- 25) A

# 2.8 Methods for Detecting Outliers: Box Plots and z-Scores

#### 1 Determine if Datum is an Outlier

- 1) A
- 2) A
- 3) A
- 4) A
- 5) D
- 6) The z-score for the value 12.96 is -1.7

Since the *z*-score would not indicate that 12.96 minutes represents an outlier, there is no evidence that the station's claim is incorrect.

- 7) The *z*-score of 39 is -3.46. Since this *z*-score is less than -3, the score of 39 is an outlier. All other scores have *z*-scores between -3 and 3, so there are no other outliers.
- 8) B
- 9) B
- 10) B
- 11) A
- 12) A
- 13) B

## 2 Calculate Quartiles and IQR

- 14) A
- 15) A
- 16) 75% of the TV viewing times are less than 15 hours per week. 25% of the times exceed 15 hours per week.
- 17) a. The interquartile range is 57 45 = 12.
  - b. The inner fences are 45 1.5(12) = 27 and 57 + 1.5(12) = 75.
  - c. The outer fences are 45 3(12) = 9 and 57 + 3(12) = 93.
  - d. The maximum of 81 is a potential outlier since it lies outside the inner fences. The minimum is within the inner

fence and is not considered to be an outlier.

18) a. lower quartile: Q1=75; upper quartile:

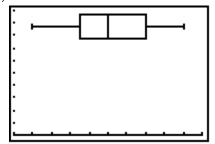
Q3=90 b. interquartile range: 90 - 75 = 15

c. Yes; the smallest measurement, 30, is three times the interquartile range less than the lower quartile, so it is a suspected outlier.

#### 3 Construct, Interpret Boxplot

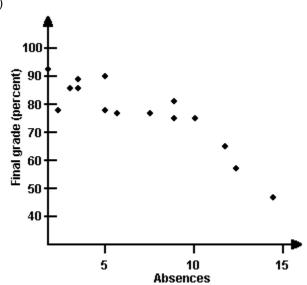
- 19) A
- 20) B
- 21) C
- 22) a. The lower quartile is 73, the upper quartile is 89, and the median is 81.
  - b. The interquartile range is 89 73 = 16. The score of 39 is a potential outlier since it is less than 73 1.5(16) = 49. c. No scores fall outside the outer fences, 25 and 137. Only the score of 39 lies between the inner and outer fences.

23) The horizontal axis extends from 10 to 20, with each tick mark representing one unit.

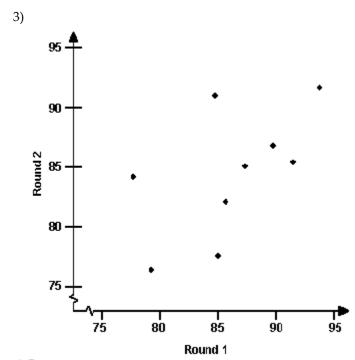


- 2.9 Graphing Bivariate Relationships (Optional)
- 1 Construct, Interpret Scatterplot
  - 1) C

2)



There appears to be a trend in the data. As the number of absences increases, the final grade decreases.



4) B

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5) A

# 2.10 Distorting the Truth with Descriptive Statistics

## 1 Understand Misleading Statistics

- 1) Stretching the vertical axis may overemphasize the differences in the heights of the bars making the taller bars look
  - much taller than the shorter bars.
- 2) Using a scale break on the vertical axis may make the shorter bars look disproportionately shorter than the taller bars.
- 3) The reader may think that the area of the bar represents the quantity rather than the height of the bar, giving a disproportionate emphasis on the taller bars.
- 4) When comparing means from two different distributions, the difference between them may be insignificant if the variability in one or both of the distributions is large.