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Two forces are applied as shown to a hook. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.



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Two forces are applied as shown to a bracket support. Determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.





Two structural members *B* and *C* are bolted to bracket *A*. Knowing that both members are in tension and that P = 10 kN and Q = 15 kN, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.





Two structural members B and C are bolted to bracket A. Knowing that both members are in tension and that P = 6 kips and Q = 4 kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.





The 300-lb force is to be resolved into components along lines a-a' and b-b'. (*a*) Determine the angle α by trigonometry knowing that the component along line a-a' is to be 240 lb. (*b*) What is the corresponding value of the component along b-b'?

SOLUTION

301			A
(<i>a</i>)	Using the triangle ru	le and law of sines:	F. + F=30016
		$\frac{\sin\beta}{240 \text{ lb}} = \frac{\sin 60^{\circ}}{300 \text{ lb}}$	10° ~
		$\sin\beta = 0.69282$	E 1-24016
		$\beta = 43.854^{\circ}$	1aa - 21010
		$\alpha + \beta + 60^{\circ} = 180^{\circ}$	
		$\alpha = 180^{\circ} - 60^{\circ} - 43.854^{\circ}$	
		= 76.146°	$\alpha = 76.1^{\circ} \blacktriangleleft$
(<i>b</i>)	Law of sines:	$\frac{F_{bb'}}{\sin 76.146^{\circ}} = \frac{300 \text{ lb}}{\sin 60^{\circ}}$	$F_{bb'} = 336 \text{ lb} \blacktriangleleft$



The 300-lb force is to be resolved into components along lines a-a' and b-b'. (*a*) Determine the angle α by trigonometry knowing that the component along line b-b' is to be 120 lb. (*b*) What is the corresponding value of the component along a-a'?





A trolley that moves along a horizontal beam is acted upon by two forces as shown. (*a*) Knowing that $\alpha = 25^{\circ}$, determine by trigonometry the magnitude of the force **P** so that the resultant force exerted on the trolley is vertical. (*b*) What is the corresponding magnitude of the resultant?





A disabled automobile is pulled by means of two ropes as shown. The tension in rope AB is 2.2 kN, and the angle α is 25°. Knowing that the resultant of the two forces applied at A is directed along the axis of the automobile, determine by trigonometry (*a*) the tension in rope AC, (*b*) the magnitude of the resultant of the two forces applied at A.



PROBLEM 2.8



Two forces are applied as shown to a hook support. Knowing that the magnitude of **P** is 35 N, determine by trigonometry (*a*) the required angle α if the resultant **R** of the two forces applied to the support is to be horizontal, (*b*) the corresponding magnitude of **R**.





A disabled automobile is pulled by means of two ropes as shown. Knowing that the tension in rope AB is 3 kN, determine by trigonometry the tension in rope AC and the value of α so that the resultant force exerted at A is a 4.8kN force directed along the axis of the automobile.





A trolley that moves along a horizontal beam is acted upon by two forces as shown. Determine by trigonometry the magnitude and direction of the force \mathbf{P} so that the resultant is a vertical force of 2500 N.





For the hook support shown, determine by trigonometry the magnitude and direction of the resultant of the two forces applied to the support.





The cable stays AB and AD help support pole AC. Knowing that the tension is 120 lb in AB and 40 lb in AD, determine graphically the magnitude and direction of the resultant of the forces exerted by the stays at A using (a) the parallelogram law, (b) the triangle rule.





Solve Problem 2.4 by trigonometry.

PROBLEM 2.4: Two structural members *B* and *C* are bolted to bracket *A*. Knowing that both members are in tension and that P = 6 kips and Q = 4 kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.





For the hook support of Prob. 2.9, determine by trigonometry (*a*) the magnitude and direction of the smallest force **P** for which the resultant **R** of the two forces applied to the support is horizontal, (*b*) the corresponding magnitude of **R**.





Determine the *x* and *y* components of each of the forces shown.

SOLUTION

Compute the following distances:		Y A
	$OA = (600)^2 + (800)^2$	800 N
	= 1000 mm	
	$OB = (560)^2 + (900)^2$	424 N 408 N X
	= 1060 mm	
	$OC = (\sqrt{480})^2 + (900)^2$	в
	= 1020 mm	
800-N Force:	$F_x = +(800 \text{ N}) \frac{800}{1000}$	$F_x = +640 \text{ N} \blacktriangleleft$
	$F_{y} = +(800 \text{ N}) \frac{600}{1000}$	$F_y = +480 \text{ N} \blacktriangleleft$
424-N Force:	$F_x = -(424 \text{ N}) \frac{560}{1060}$	$F_x = -224 \text{ N} \blacktriangleleft$
	$F_{y} = -(424 \text{ N}) \frac{900}{1060}$	$F_y = -360 \mathrm{N}$
408-N Force:	$F_x = +(408 \text{ N}) \frac{480}{1020}$	$F_x = +192.0 \text{ N}$
	$F_{y} = -(408 \text{ N}) \frac{900}{1020}$	$F_y = -360 \mathrm{N}$



Determine the *x* and *y* components of each of the forces shown.

SOLUTION

SOLUTION		8_ ^Y
Compute the following distances:		<u>`</u>
	$OA = \sqrt{84)^2 + (80)^2}$	50 16
	= 116 in.	2110
	$OB = (\sqrt{28})^2 + (96)^2$	° 51 16 ×
	= 100 in.	×.
	$OC = (48)^2 + (90)^2$	
	= 102 in.	
29-lb Force:	$F_x = +(29 \text{ lb}) \frac{84}{116}$	$F_x = +21.0 \text{ lb}$
	$F_{y} = +(29 \text{ lb}) \frac{80}{116}$	F_{y} = +20.0 lb
50-lb Force:	$F_x = -(50 \text{ lb}) \frac{28}{100}$	$F_x = -14.00 \text{ lb}$
	$F_{y} = +(50 \text{ lb}) \frac{96}{100}$	F_{y} = +48.0 lb
51-lb Force:	$F_x = +(51 \text{ lb}) \frac{48}{102}$	$F_x = +24.0 \text{ lb}$
	$F_{y} = -(51 \text{ lb}) \frac{90}{102}$	$F_y = -45.0 \text{ lb}$



Determine the *x* and *y* components of each of the forces shown.

SOLUTION		
40-lb Force:	$F_x = +(40 \text{ lb}) \cos 60^\circ$	$F_x = 20.0 \text{ lb}$
	$F_y = -(40 \text{ lb}) \sin 60^\circ$	$F_y = -34.6$ lb
50-lb Force:	$F_x = -(50 \text{ lb}) \sin 50^\circ$	$F_x = -38.3 \text{ lb}$
	$F_y = -(50 \text{ lb}) \cos 50^\circ$	$F_y = -32.1$ lb
60-lb Force:	$F_x = +(60 \text{ lb}) \cos 25^\circ$	$F_x = 54.4$ lb
	$F_y = +(60 \text{ lb}) \sin 25^\circ$	$F_y = 25.4 \text{ lb} \blacktriangleleft$



Determine the *x* and *y* components of each of the forces shown.

SOLUTION		
80-N Force:	$F_x = +(80 \text{ N}) \cos 40^\circ$	$F_x = 61.3 \text{ N}$
	$F_y = +(80 \text{ N}) \sin 40^\circ$	$F_y = 51.4 \text{ N}$
120-N Force:	$F_x = +(120 \text{ N}) \cos 70^\circ$	$F_x = 41.0 \text{ N} \blacktriangleleft$
	$F_y = +(120 \text{ N}) \sin 70^\circ$	$F_y = 112.8 \mathrm{N}$
150-N Force:	$F_x = -(150 \text{ N}) \cos 35^\circ$	$F_x = -122. 9 \text{ N}$
	$F_y = +(150 \text{ N}) \sin 35^\circ$	$F_y = 86.0 \text{ N} \blacktriangleleft$



Member *BD* exerts on member *ABC* a force \mathbf{P} directed along line *BD*. Knowing that \mathbf{P} must have a 300-lb horizontal component, determine (*a*) the magnitude of the force \mathbf{P} , (*b*) its vertical component.





Member *BC* exerts on member *AC* a force \mathbf{P} directed along line *BC*. Knowing that \mathbf{P} must have a 325-N horizontal component, determine (*a*) the magnitude of the force \mathbf{P} , (*b*) its vertical component.





Cable *AC* exerts on beam *AB* a force **P** directed along line *AC*. Knowing that **P** must have a 350-lb vertical component, determine (*a*) the magnitude of the force **P**, (*b*) its horizontal component.





The hydraulic cylinder *BD* exerts on member *ABC* a force **P** directed along line *BD*. Knowing that **P** must have a 750-N component perpendicular to member *ABC*, determine (*a*) the magnitude of the force **P**, (*b*) its component parallel to *ABC*.





Determine the resultant of the three forces of Problem 2.16.

PROBLEM 2.16 Determine the *x* and *y* components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.16:

Force	<i>x</i> Comp. (N)	y Comp. (N)
800 lb	+640	+480
424 lb	-224	-360
408 lb	+192	-360
	$R_x = +608$	$R_y = -240$

 $\mathbf{R} = R_x \mathbf{i} + R_y \mathbf{j}$

 R_{y}

 R_x = <u>240</u> 608 $\alpha = 21.541^{\circ}$

 $R = \frac{240 \text{ N}}{2}$

= 653.65 N

 $\tan \alpha =$

 $= (608 \text{ lb})\mathbf{i} +$

$$R_{x}\mathbf{i} + R_{y}\mathbf{j}$$
(608 lb) $\mathbf{i} + (-240 \text{ lb})\mathbf{j}$

$$\frac{R_{y}}{R_{x}}$$

$$\frac{240}{608}$$
21.541°
$$\frac{240 \text{ N}}{\sin(21.541^{\circ})}$$
653.65 N
$$\mathbf{R} = 654 \text{ N} \quad \mathbf{N} \quad \mathbf{21.5^{\circ}} \blacktriangleleft$$



Determine the resultant of the three forces of Problem 2.17.

PROBLEM 2.17 Determine the *x* and *y* components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.17:

Force	<i>x</i> Comp. (lb)	y Comp. (lb)
29 lb	+21.0	+20.0
50 lb	-14.00	+48.0
51 lb	+24.0	-45.0
	$R_x = +31.0$	$R_y = +23.0$





Determine the resultant of the three forces of Problem 2.18.

PROBLEM 2.18 Determine the *x* and *y* components of each of the forces shown.

SOLUTION				
	Force	<i>x</i> Comp. (lb)	y Comp. (lb)	
	40 lb	+20.00	-34.64	
	50 lb	-38.30	-32.14	
	60 lb	+54.38	+25.36	
		$R_x = +36.08$	$R_y = -41.42$	
$\mathbf{R} = R_x \mathbf{i} + R_y \mathbf{j}$ $= (+36.08 \text{ lb})\mathbf{i} + (-41.42 \text{ lb})\mathbf{j}$ $\tan \alpha = \frac{R_y}{R_x}$ $\tan \alpha = \frac{41.42 \text{ lb}}{36.08 \text{ lb}}$ $\tan \alpha = 1.14800$ $\alpha = 48.942^{\circ}$ $R = \frac{41.42 \text{ lb}}{\sin 48.942^{\circ}}$			i + (-41.42 lb) j	$R = 54.9 \text{ lb} = 48.9^{\circ} \blacktriangleleft$



Determine the resultant of the three forces of Problem 2.19.

PROBLEM 2.19 Determine the *x* and *y* components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.19:

I	Force	<i>x</i> Comp. (N)	y Comp. (N)]
	80 N	+61.3	+51.4	
	120 N	+41.0	+112.8	
	150 N	-122.9	+86.0	
		$R_x = -20.6$	$R_y = +250.2$	
		$\mathbf{R} = R_x \mathbf{i} + R_y$ $= (-20.6 \text{ N})$ $\tan \alpha = \frac{R_y}{R_x}$ $\tan \alpha = \frac{250.2 \text{ N}}{20.6 \text{ N}}$ $\tan \alpha = 12.1456$ $\alpha = 85.293^\circ$ $R = \frac{250.2 \text{ N}}{\sin 85.29}$. j N) i + (250.2 N) j ℝ	$\vec{R}_{x} = -20.6 \vec{c}$ $\vec{R} = 251 \text{ N} > 85.3^{\circ}$



For the collar loaded as shown, determine (*a*) the required value of α if the resultant of the three forces shown is to be vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION	
$R_x = \Sigma F_x$	
$= (100 \text{ N})\cos\alpha + (150 \text{ N})\cos(\alpha + 30^{\circ}) - (200 \text{ N})\cos\alpha$	
$R_x = -(100 \text{ N}) \cos \alpha + (150 \text{ N}) \cos (\alpha + 30^\circ)$	(1)
$R_y = \Sigma F_y$	
$= -(100 \text{ N})\sin\alpha - (150 \text{ N})\sin(\alpha + 30^{\circ}) - (200 \text{ N})\sin\alpha$	
$R_y = -(300 \text{ N}) \sin \alpha - (150 \text{ N}) \sin (\alpha + 30^\circ)$	(2)
(a) For R to be vertical, we must have $R_x = 0$. We make $R_x = 0$ in Eq. (1):	
$-100\cos\alpha + 150\cos(\alpha + 30^\circ) = 0$	
$-100\cos\alpha + 150(\cos\alpha\cos 30^\circ - \sin\alpha\sin 30^\circ) = 0$	
$29.904\cos\alpha = 75\sin\alpha$	
$\tan \alpha = \frac{29.904}{75}$	
= 0.39872	
$\alpha = 21.738^{\circ}$	$\alpha = 21.7^{\circ}$
(b) Substituting for α in Eq. (2):	
$R_y = -300 \sin 21.738^\circ - 150 \sin 51.738^\circ$	
= -228.89 N	
$R = R_y = 228.89 \text{ N}$	R = 229 N



A hoist trolley is subjected to the three forces shown. Knowing that $\alpha = 40^{\circ}$, determine (*a*) the required magnitude of the force **P** if the resultant of the three forces is to be vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION $R_x = + \Sigma F_x = P + (200 \text{ lb}) \sin 40^\circ - (400 \text{ lb}) \cos 40^\circ$ $R_x = P - 177.860$ lb (1) $R_y = + \Sigma F_y = (200 \text{ lb}) \cos 40^\circ + (400 \text{ lb}) \sin 40^\circ$ $R_v = 410.32 \text{ lb}$ (2)For **R** to be vertical, we must have $R_x = 0$. *(a)* Set $R_x = 0$ in Eq. (1) 0 = P - 177.860 lb P = 177.860 lb*P* = 177.9 lb ◀ *(b)* Since **R** is to be vertical: $R = 410 \, \text{lb}$ $R = R_y = 410 \text{ lb}$



A hoist trolley is subjected to the three forces shown. Knowing that P = 250 lb, determine (a) the required value of α if the resultant of the three forces is to be vertical, (b) the corresponding magnitude of the resultant.

SOI	LUTION		
		$R_x = + \Sigma F_x = 250 \text{ lb} + (200 \text{ lb}) \sin \alpha - (400 \text{ lb}) \cos \alpha$	
		$R_x = 250 \text{ lb} + (200 \text{ lb}) \sin \alpha - (400 \text{ lb}) \cos \alpha$	(1)
		$R_y = +\Sigma F_y = (200 \text{ lb})\cos\alpha + (400 \text{ lb})\sin\alpha$	
<i>(a)</i>	For R to be vertical, we	e must have $R_x = 0$.	
	Set	$R_x = 0$ in Eq. (1)	
		$0 = 250 \text{ lb} + (200 \text{ lb}) \sin \alpha - (400 \text{ lb}) \cos \alpha$	
	(4	$(00 \text{ lb})\cos\alpha = (200 \text{ lb})\sin\alpha + 250 \text{ lb}$	
		$2\cos\alpha = \sin\alpha + 1.25$	
		$4\cos^2\alpha = \sin^2\alpha + 2.5\sin\alpha + 1.5625$	
	4	$(1-\sin^2\alpha) = \sin^2\alpha + 2.5\sin\alpha + 1.5625$	
		$0 = 5\sin^2 \alpha + 2.5\sin \alpha - 2.4375$	
	Using the quadratic for	mula to solve for the roots gives	
		$\sin \alpha = 0.49162$	
	or	$\alpha = 29.447^{\circ}$	$\alpha = 29.4^{\circ} \blacktriangleleft$
<i>(b)</i>	Since R is to be vertica	1:	
	$R = R_y =$	$(200 \text{ lb})\cos 29.447^\circ + (400 \text{ lb})\sin 29.447^\circ$	R = 371 lb ◀



For the post loaded as shown, determine (a) the required tension in rope AC if the resultant of the three forces exerted at point C is to be horizontal, (b) the corresponding magnitude of the resultant.

SOLUTION

$$R_{x} = \Sigma F_{x} - \frac{960}{1460} \frac{T}{AC} + \frac{24}{25} (500 \text{ N}) + \frac{4}{5} (200 \text{ N})$$
$$R_{x} = -\frac{48}{73} T_{AC} + 640 \text{ N}$$
(1)

$$R_{y} = \Sigma F_{y} - \frac{1100}{1460} T_{AC} + \frac{7}{25} (500 \text{ N}) - \frac{3}{5} (200 \text{ N})$$

$$R_{y} - \frac{55}{73} T_{AC} + 20 \text{ N}$$
(2)

(a) For **R** to be horizontal, we must have $R_y = 0$.

Set
$$R_y = 0$$
 in Eq. (2):
 $-\frac{55}{73}T_{AC} + 20 \text{ N} = 0$
 $T_{AC} = 26.545 \text{ N}$
 $T_{AC} = 26.5 \text{ N}$

(b) Substituting for T_{AC} into Eq. (1) gives

$$R_x = -\frac{48}{73}(26.545 \text{ N}) + 640 \text{ N}$$

$$R_x = 622.55 \text{ N}$$

$$R = R_x = 623 \text{ N}$$

$$R = 623 \text{ N}$$



Two cables are tied together at *C* and are loaded as shown. Knowing that $\alpha = 30^{\circ}$, determine the tension (*a*) in cable *AC*, (*b*) in cable *BC*.





Two cables are tied together at C and are loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.





Two cables are tied together at C and are loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.





Two cables are tied together at C and loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.




Two cables are tied together at *C* and are loaded as shown. Knowing that $\mathbf{P} = 500$ N and $\alpha = 60^{\circ}$, determine the tension in (*a*) in cable *AC*, (*b*) in cable *BC*.





Two forces of magnitude $T_A = 8$ kips and $T_B = 15$ kips are applied as shown to a welded connection. Knowing that the connection is in equilibrium, determine the magnitudes of the forces T_C and T_D .





Two forces of magnitude $T_A = 6$ kips and $T_C = 9$ kips are applied as shown to a welded connection. Knowing that the connection is in equilibrium, determine the magnitudes of the forces T_B and T_D .





Two cables are tied together at *C* and are loaded as shown. Knowing that P = 300 N, determine the tension in cables *AC* and *BC*.





Two forces **P** and **Q** are applied as shown to an aircraft connection. Knowing that the connection is in equilibrium and that P = 500 lb and Q = 650 lb, determine the magnitudes of the forces exerted on the rods A and B.





A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable *ACB* and is pulled at a constant speed by cable *CD*. Knowing that $\alpha = 30^{\circ}$ and $\beta = 10^{\circ}$ and that the combined weight of the boatswain's chair and the sailor is 200 lb, determine the tension (*a*) in the support cable *ACB*, (*b*) in the traction cable *CD*.





A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable *ACB* and is pulled at a constant speed by cable *CD*. Knowing that $\alpha = 25^{\circ}$ and $\beta = 15^{\circ}$ and that the tension in cable *CD* is 20 lb, determine (*a*) the combined weight of the boatswain's chair and the sailor, (*b*) the tension in the support cable *ACB*.





For the cables of prob. 2.32, find the value of α for which the tension is as small as possible (*a*) in cable *bc*, (*b*) in both cables simultaneously. In each case determine the tension in each cable.





For the cables of Problem 2.36, it is known that the maximum allowable tension is 600 N in cable *AC* and 750 N in cable *BC*. Determine (*a*) the maximum force **P** that can be applied at *C*, (*b*) the corresponding value of α .





Two cables tied together at *C* are loaded as shown. Knowing that the maximum allowable tension in each cable is 800 N, determine (a) the magnitude of the largest force **P** that can be applied at *C*, (b) the corresponding value of α .





Two cables tied together at *C* are loaded as shown. Knowing that the maximum allowable tension is 1200 N in cable *AC* and 600 N in cable *BC*, determine (*a*) the magnitude of the largest force **P** that can be applied at *C*, (*b*) the corresponding value of α .





Two cables tied together at C are loaded as shown. Determine the range of values of Q for which the tension will not exceed 60 lb in either cable.





Collar *A* is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the magnitude of the force **P** required to maintain the equilibrium of the collar when (*a*) x = 4.5 in., (*b*) x = 15 in.





Collar *A* is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the distance *x* for which the collar is in equilibrium when P = 48 lb.





A movable bin and its contents have a combined weight of 2.8 kN. Determine the shortest chain sling ACB that can be used to lift the loaded bin if the tension in the chain is not to exceed 5 kN.





A 600-lb crate is supported by several ropeand-pulley arrangements as shown. Determine for each arrangement the tension in the rope. (*Hint:* The tension in the rope is the same on each side of a simple pulley. This can be proved by the methods of Ch. 4.)





Solve Parts b and d of Problem 2.51, assuming that the free end of the rope is attached to the crate.

PROBLEM 2.51 A 600-lb crate is supported by several rope-and-pulley arrangements as shown. Determine for each arrangement the tension in the rope. . (*Hint:* The tension in the rope is the same on each side of a simple pulley. This can be proved by the methods of Ch. 4.)





A 200-kg crate is to be supported by the rope-and-pulley arrangement shown. Determine the magnitude and direction of the force **P** that must be exerted on the free end of the rope to maintain equilibrium. (See the hint for Prob. 2.51.)





A load **Q** is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Knowing that P = 750 N, determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **Q**.





An 1800-N load \mathbf{Q} is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **P**.





Determine (*a*) the *x*, *y*, and *z* components of the 900-N force, (*b*) the angles θ_x , θ_y , and θ_z that the force forms with the coordinate axes.

SOLUTION $F_h = F \cos 65^\circ$ F= 900 N = (900 N)cos 65° $F_h = 380.36 \text{ N}$ $F_x = F_h \sin 20^\circ$ (a)= (380.36 N) sin 20° $F_x = -130.091$ N, $F_x = -130.1 \text{ N} \blacktriangleleft$ $F_y = F \sin 65^\circ$ = (900 N) sin 65° $F_{y} = +815.68$ N, $F_{y} = +816 \text{ N}$ $F_z = F_h \cos 20^\circ$ $= (380.36 \text{ N})\cos 20^{\circ}$ $F_z = +357.42$ N $F_z = +357 \text{ N}$ $\cos \theta_x = \frac{F_x}{F} = \frac{-130.091 \text{ N}}{900 \text{ N}}$ $\theta_r = 98.3^\circ \blacktriangleleft$ *(b)* $\cos \theta_y = \frac{F_y}{F} = \frac{+815.68 \text{ N}}{900 \text{ N}}$ $\theta_v = 25.0^\circ \blacktriangleleft$ $\cos \theta_z = \frac{F_z}{F} = \frac{+357.42 \text{ N}}{900 \text{ N}}$ $\theta_z = 66.6^\circ \blacktriangleleft$



Determine (*a*) the *x*, *y*, and *z* components of the 750-N force, (*b*) the angles θ_x , θ_y , and θ_z that the force forms with the coordinate axes.

SOLUTION		9 F= 750 N
	$F_h = F \sin 35^\circ$ = (750 N) sin35° $F_h = 430.18$ N	35° 75° × 25°
(<i>a</i>)	$F_x = F_h \cos 25^\circ$ $= (430.18 \text{ N}) \cos 25^\circ$	
	$F_x = +389.88$ N,	$F_x = +390 \text{ N} \blacktriangleleft$
	$F_y = F \cos 35^\circ$ $= (750 \text{ N}) \cos 35^\circ$	
	$F_y = +614.36 \text{ N},$	$F_y = +614 \text{ N} \blacktriangleleft$
	$F_z = F_h \sin 25^\circ$ = (430.18 N) sin 25° $F_z = +181.802$ N	$F_z = +181.8 \text{ N}$
(b)	$\cos \theta_x = \frac{F_x}{F} = \frac{+389.88 \text{ N}}{750 \text{ N}}$	$\theta_x = 58.7^\circ \blacktriangleleft$
	$\cos \theta_{y} = \frac{F_{y}}{F} = \frac{+614.36 \text{ N}}{750 \text{ N}}$	$\theta_y = 35.0^\circ \blacktriangleleft$
	$\cos \theta_z = \frac{F_z}{F} = \frac{+181.802 \text{ N}}{750 \text{ N}}$	$\theta_z = 76.0^\circ \blacktriangleleft$



The end of the coaxial cable *AE* is attached to the pole *AB*, which is strengthened by the guy wires *AC* and *AD*. Knowing that the tension in wire *AC* is 120 lb, determine (*a*) the components of the force exerted by this wire on the pole, (*b*) the angles θ_x , θ_y , and θ_z that the force forms with the coordinate axes.

SOLUTION		
(<i>a</i>)	$F_x = (120 \text{ lb}) \cos 60^{\circ} \cos 20^{\circ}$	
	$F_x = 56.382$ lb	$F_x = +56.4 \text{ lb} \blacktriangleleft$
	$F_y = -(120 \text{ lb}) \sin 60^\circ$	
	$F_y = -103.923$ lb	$F_y = -103.9$ lb \blacktriangleleft
	$F_z = -(120 \text{ lb}) \cos 60^\circ \sin 20^\circ$	
	$F_z = -20.521$ lb	$F_z = -20.5$ lb
(<i>b</i>)	$\cos \theta_x = \frac{F_x}{F} = \frac{56.382 \text{ lb}}{120 \text{ lb}}$	$\theta_x = 62.0^\circ \blacktriangleleft$
	$\cos \theta_y = \frac{F_y}{F} = \frac{-103.923 \text{ lb}}{120 \text{ lb}}$	$\theta_y = 150.0^\circ \blacktriangleleft$
	$\cos \theta_z = \frac{F_z}{F} = \frac{-20.52 \text{ lb}}{120 \text{ lb}}$	$\theta_z = 99.8^\circ \blacktriangleleft$



The end of the coaxial cable *AE* is attached to the pole *AB*, which is strengthened by the guy wires *AC* and *AD*. Knowing that the tension in wire *AD* is 85 lb, determine (*a*) the components of the force exerted by this wire on the pole, (*b*) the angles θ_x , θ_y , and θ_z that the force forms with the coordinate axes.

SOLUTION		
(<i>a</i>)	$F_x = (85 \text{ lb}) \sin 36^\circ \sin 48^\circ$	
	= 37.129 lb	$F_x = 37.1$ lb \blacktriangleleft
	$F_y = -(85 \text{ lb}) \cos 36^\circ$	
	= -68.766 lb	$F_y = -68.8 \text{ lb} \blacktriangleleft$
	$F_z = (85 \text{ lb}) \sin 36^\circ \cos 48^\circ$	
	= 33.431 lb	$F_z = 33.4 \text{ lb} \blacktriangleleft$
(b)	$\cos \theta_x = \frac{F_x}{F} = \frac{37.129 \text{ lb}}{85 \text{ lb}}$	$\theta_x = 64.1^\circ \blacktriangleleft$
	$\cos \theta_y = \frac{F_y}{F} = \frac{-68.766 \text{ lb}}{85 \text{ lb}}$	$\theta_y = 144.0^\circ \blacktriangleleft$
	$\cos\theta_z = \frac{F_z}{F} = \frac{33.431 \text{ lb}}{85 \text{ lb}}$	$\theta_z = 66.8^\circ \blacktriangleleft$

A gun is aimed at a point *A* located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the *x*, *y*, and *z* components of that force, (*b*) the values of the angles θ_x , θ_y , and θ_z defining the direction of the recoil force. (Assume that the *x*, *y*, and *z* axes are directed, respectively, east, up, and south.)



Solve Problem 2.60, assuming that point A is located 15° north of west and that the barrel of the gun forms an angle of 25° with the horizontal.

PROBLEM 2.60 A gun is aimed at a point *A* located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the *x*, *y*, and *z* components of that force, (*b*) the values of the angles θ_x , θ_y , and θ_z defining the direction of the recoil force. (Assume that the *x*, *y*, and *z* axes are directed, respectively, east, up, and south.)



Determine the magnitude and direction of the force $\mathbf{F} = (690 \text{ lb})\mathbf{i} + (300 \text{ lb})\mathbf{j} - (580 \text{ lb})\mathbf{k}$.

SOLUTION

$$F = (690 lb)i + (300 lb)j - (580 lb)k

F = F√{2x+F2y+F2z}

= √690 lb)2 + (300 lb)2 + (-580 lb)2

= 950 lb

F = 950 lb ◄

cos θx = $\frac{F_x}{F} = \frac{690 lb}{950 lb}$
 $θ_x = 43.4^\circ ◄$
 $cos θ_y = \frac{F_y}{F} = \frac{300 lb}{950 lb}$
 $θ_y = 71.6^\circ ◀$
 $cos θ_z = \frac{F_z}{F} = \frac{-580 lb}{950 lb}$
 $θ_z = 127.6^\circ ◀$$$

Determine the magnitude and direction of the force $\mathbf{F} = (650 \text{ N})\mathbf{i} - (320 \text{ N})\mathbf{j} + (760 \text{ N})\mathbf{k}$.

SOLUTION

$$\mathbf{F} = (650 \text{ N})\mathbf{i} - (320 \text{ N})\mathbf{j} + (760 \text{ N})\mathbf{k}$$

$$F = F_{y}\sqrt{2x} + F^{2}y + F^{2}z}$$

$$= (\sqrt{650 \text{ N}})^{2} + (-320 \text{ N})^{2} + (760 \text{ N})^{2}$$

$$F = 1050 \text{ N} \blacktriangleleft$$

$$\cos \theta_{x} = \frac{F_{x}}{F} = \frac{650 \text{ N}}{1050 \text{ N}}$$

$$\theta_{x} = 51.8^{\circ} \blacktriangleleft$$

$$\cos \theta_{y} = \frac{F_{y}}{F} = \frac{-320 \text{ N}}{1050 \text{ N}}$$

$$\theta_{y} = 107.7^{\circ} \blacktriangleleft$$

$$\cos \theta_{z} = \frac{F_{z}}{F} = \frac{760 \text{ N}}{1050 \text{ N}}$$

$$\theta_{z} = 43.6^{\circ} \blacktriangleleft$$

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_x = 69.3^{\circ}$ and $\theta_z = 57.9^{\circ}$. Knowing that the *y* component of the force is -174.0 lb, determine (*a*) the angle θ_y , (*b*) the other components and the magnitude of the force.

SOLUTION			
	$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$		
$\cos^2(69.3^\circ) + \cos^2\theta_y + \cos^2(57.9^\circ) = 1$			
	$\cos\theta_y = \pm 0.7699$		
(<i>a</i>)	Since $F_y < 0$, we choose $\cos\theta_y = -0.7699$	$\therefore \theta_y = 140.3^\circ \blacktriangleleft$	
(<i>b</i>)	$F_y = F \cos \Theta_y$		
	-174.0 lb = F(-0.7699)		
	F = 226.0 lb	$F = 226 \text{ lb} \blacktriangleleft$	
	$F_x = F \cos \theta_x = (226.0 \text{ lb}) \cos 69.3^\circ$	$F_x = 79.9 \text{ lb} \blacktriangleleft$	
	$F_z = F \cos \theta_z = (226.0 \text{ lb}) \cos 57.9^\circ$	$F_z = 120.1$ lb	

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_x = 70.9^{\circ}$ and $\theta_y = 144.9^{\circ}$. Knowing that the *z* component of the force is -52.0 lb, determine (*a*) the angle θ_z , (*b*) the other components and the magnitude of the force.

SOLUTION $\cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1$ $\cos^2 70.9 + \cos^2 144.9^\circ + \cos^2 \theta_z^\circ = 1$ $\cos\theta_z = \pm 0.47282$ Since $F_z < 0$, we choose $\cos \theta_z = -0.47282$ $\therefore \theta_z = 118.2^\circ \blacktriangleleft$ *(a)* $F_z = F \cos \theta_z$ *(b)* $-52.0 \ lb = F(-0.47282)$ F = 110.0 lb $F = 110.0 \text{ lb} \blacktriangleleft$ $F_x = F \cos \theta_x = (110.0 \text{ lb}) \cos 70.9^\circ$ $F_x = 36.0 \text{ lb}$ $F_y = F \cos \theta_y = (110.0 \text{ lb}) \cos 144.9^\circ$ $F_y = -90.0 \text{ lb}$

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_y = 55^\circ$ and $\theta_z = 45^\circ$. Knowing that the *x* component of the force is – 500 lb, determine (*a*) the angle θ_x , (*b*) the other components and the magnitude of the force.

SOLUTION

(*a*) We have

$$(\cos\theta_x)^2 + (\cos\theta_y)^2 + (\cos\theta_z)^2 = 1 \Longrightarrow (\cos\theta_y)^2 = 1 - (\cos\theta_y)^2 - (\cos\theta_z)^2$$

Since $F_x < 0$ we must have $\cos \theta_x$, 0

Thus, taking the negative square root, from above, we have:

$$\cos\theta_x = -\sqrt[4]{-(\cos 55)^2 - (\cos 45)^2} = 0.41353 \qquad \qquad \theta_x = 114.4^\circ \blacktriangleleft$$

(*b*) Then:

$$F = \frac{F_x}{\cos\theta_x} = \frac{500 \text{ lb}}{0.41353} = 1209.10 \text{ lb} \qquad F = 1209 \text{ lb} \blacktriangleleft$$

and

$$F_y = F \cos \theta_y = (1209.10 \text{ lb}) \cos 55^\circ$$

 $F_z = F \cos \theta_z = (1209.10 \text{ lb}) \cos 45^\circ$
 $F_z = 855 \text{ lb}$

A force **F** of magnitude 1200 N acts at the origin of a coordinate system. Knowing that $\theta_x = 65^\circ$, $\theta_y = 40^\circ$, and $F_z > 0$, determine (*a*) the components of the force, (*b*) the angle θ_z .

SOLUTION			
$\cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1$ $\cos^2 65_z + \cos^2 40^\circ + \cos^2 \theta_z \circ = 1$ $\cos \theta_z = \pm 0.48432$			
(b) Since $F_z > 0$, we choose $\cos \theta_z = 0.48432$, or $\theta_z = 61.032$.	$\therefore \ \theta_z = 61.0^\circ \blacktriangleleft$		
(<i>a</i>) $F = 1200 \text{ N}$			
$F_x = F \cos \theta_x = (1200 \text{ N}) \cos 65^{\circ}$	$F_x = 507$ N \triangleleft		
$F_y = F \cos\theta_y = (1200 \mathrm{N}) \cos 40^\circ$	$F_y = 919 \text{ N} \blacktriangleleft$		
$F_z = F \cos \theta_z = (1200 \text{ N}) \cos 61.032^\circ$	$F_z = 582 \text{ N} \blacktriangleleft$		



A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AB is 408 N, determine the components of the force exerted on the plate at B.

SOLUTION

We have:

$$\overrightarrow{BA} = +(320 \text{ mm})\mathbf{i} + (480 \text{ mm})\mathbf{j} \cdot (360 \text{ mm})\mathbf{k}$$
 $BA = 680 \text{ mm}$

Thus:

$$\mathbf{F}_{B} = T_{BA} \boldsymbol{\lambda}_{BA} = T_{BA} \frac{\overrightarrow{BA}}{BA} = T_{BA} \left(\frac{8}{17} \mathbf{i} + \frac{12}{17} \mathbf{j} - \frac{9}{17} \mathbf{k} \right)$$

$$\left(\frac{8}{17}T_{BA}\right)\mathbf{i} + \left(\frac{12}{17}T_{BA}\right)\mathbf{j} - \left(\frac{9}{17}T_{BA}\right)\mathbf{k} = 0$$

Setting $T_{BA} = 408$ N yields,

$$F_x = +192.0 \text{ N}, F_y = +288 \text{ N}, F_z = -216 \text{ N} \blacktriangleleft$$



A rectangular plate is supported by three cables as shown.

Knowing that the tension in cable AD is 429 N, determine the components of the force exerted on the plate at D.

SOLUTION

We have:

$$\vec{DA} = -(250 \text{ mm})\mathbf{i} + (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k}$$
 $DA = 650 \text{ mm}$

Thus:

$$\mathbf{F}_{D} = T_{DA} \boldsymbol{\lambda}_{DA} = T_{DA} \frac{\overrightarrow{DA}}{DA} = T_{DA} \left(-\frac{5}{13} \mathbf{i} + \frac{48}{65} \mathbf{j} + \frac{36}{65} \mathbf{k} \right)$$

$$-\left(\frac{5}{13}T_{DA}\right)\mathbf{i} + \left(\frac{48}{65}T_{DA}\right)\mathbf{j} + \left(\frac{36}{65}T_{DA}\right)\mathbf{k} = 0$$

Setting $T_{DA} = 429$ N yields,

$$F_x = -165.0 \text{ N}, F_y = +317 \text{ N}, F_z = +238 \text{ N} \blacktriangleleft$$



In order to move a wrecked truck, two cables are attached at A and pulled by winches B and C as shown. Knowing that the tension in cable AB is 2 kips, determine the components of the force exerted at A by the cable.





In order to move a wrecked truck, two cables are attached at A and pulled by winches B and C as shown. Knowing that the tension in cable AC is 1.5 kips, determine the components of the force exerted at A by the cable.




Find the magnitude and direction of the resultant of the two forces shown knowing that P = 300 N and Q = 400 N.

SOLUTION	
$\mathbf{P} = (300 \text{ N})[-\cos 30^{\circ} \sin 15^{\circ} \mathbf{i} + \sin 30^{\circ} \mathbf{j} + \cos 30^{\circ} \cos 15^{\circ} \mathbf{k}]$	
$= -(67.243 \text{ N})\mathbf{i} + (150 \text{ N})\mathbf{j} + (250.95 \text{ N})\mathbf{k}$	
$\mathbf{Q} = (400 \text{ N})[\cos 50^{\circ} \cos 20^{\circ} \mathbf{i} + \sin 50^{\circ} \mathbf{j} - \cos 50^{\circ} \sin 20^{\circ} \mathbf{k}]$	
$= (400 \text{ N})[0.60402\mathbf{i} + 0.76604\mathbf{j} - 0.21985]$	
$= (241.61 \text{ N})\mathbf{i} + (306.42 \text{ N})\mathbf{j} - (87.939 \text{ N})\mathbf{k}$	
$\mathbf{R} = \mathbf{P} + \mathbf{Q}$	
$= (174.367 \text{ N})\mathbf{i} + (456.42 \text{ N})\mathbf{j} + (163.011 \text{ N})\mathbf{k}$	
$R = \sqrt{(74.367 \text{ N})^2 + (456.42 \text{ N})^2 + (163.011 \text{ N})^2}$	
= 515.07 N	$R = 515 \text{ N} \blacktriangleleft$
$\cos\theta_{x} = \frac{R_{x}}{R} = \frac{174.367 \text{ N}}{515.07 \text{ N}} = 0.33853$	$\theta_x = 70.2^\circ \blacktriangleleft$
$\cos\theta_{y} = \frac{R_{y}}{R} = \frac{456.42 \text{ N}}{515.07 \text{ N}} = 0.88613$	$\theta_y = 27.6^\circ \blacktriangleleft$
$\cos\theta_z = \frac{R_z}{R} = \frac{163.011 \text{ N}}{515.07 \text{ N}} = 0.31648$	$\theta_z = 71.5^\circ \blacktriangleleft$



Find the magnitude and direction of the resultant of the two forces shown knowing that P = 300 N and Q = 400 N.

SOLUTION	
$\mathbf{P} = (400 \text{ N})[-\cos 30^{\circ} \sin 15^{\circ} \mathbf{i} + \sin 30^{\circ} \mathbf{j} + \cos 30^{\circ}$	cos15° k]
$= -(89.678 \text{ N})\mathbf{i} + (200 \text{ N})\mathbf{j} + (334.61 \text{ N})\mathbf{k}$	
$\mathbf{Q} = (300 \text{ N})[\cos 50^{\circ}\cos 20^{\circ}\mathbf{i} + \sin 50^{\circ}\mathbf{j} - \cos 50^{\circ}\mathbf{i}]$	sin 20° k]
= $(181.21 \text{ N})\mathbf{i} + (229.81 \text{ N})\mathbf{j} - (65.954 \text{ N})\mathbf{k}$	
$\mathbf{R} = \mathbf{P} + \mathbf{Q}$	
= $(91.532 \text{ N})\mathbf{i} + (429.81 \text{ N})\mathbf{j} + (268.66 \text{ N})\mathbf{k}$	
$R = (91.532 \text{ N})^2 + (429.81 \text{ N})^2 + (268.66 \text{ N})^2$	
= 515.07 N	$R = 515 \text{ N} \blacktriangleleft$
$\cos\theta_{x} = \frac{R_{x}}{R} = \frac{91.532 \text{ N}}{515.07 \text{ N}} = 0.177708$	$\theta_x = 79.8^\circ \blacktriangleleft$
$\cos\theta_{y} = \frac{R_{y}}{R} = \frac{429.81 \text{ N}}{515.07 \text{ N}} = 0.83447$	$\theta_y = 33.4^\circ \blacktriangleleft$
$\cos\theta_z = \frac{R_z}{R} = \frac{268.66 \text{ N}}{515.07 \text{ N}} = 0.52160$	$\theta_z = 58.6^\circ \blacktriangleleft$



Knowing that the tension is 425 lb in cable AB and 510 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION		
	$\overline{AB} = (40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$	
	$AB = (40 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2 = 85 \text{ in.}$	
	$\vec{AC} = (100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$	
	$AC = (\sqrt{100 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 125 \text{ in.}$	
	$\mathbf{T}_{AB} = T_{AB} \lambda_{AB} = T_{AB} \frac{\overline{AB}}{AB} = (425 \text{ lb}) \left[\frac{(40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (6)}{85 \text{ in.}} \right]$	$\frac{0 \text{ in.})\mathbf{k}}{2}$
	$\mathbf{T}_{AB} = (200 \text{ lb})\mathbf{i} - (225 \text{ lb})\mathbf{j} + (300 \text{ lb})\mathbf{k}$	_
	$\mathbf{T}_{AC} = T_{AC} \boldsymbol{\lambda}_{AC} = T_{AC} \frac{A_{C}^{"}}{AC} = (510 \text{ lb}) \left[\frac{(100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (45 \text{ in.})\mathbf{j}}{125 \text{ in.}} \right]$	$(\underline{60 \text{ in.})}\mathbf{k}$
	$\mathbf{T}_{AC} = (408 \text{ lb})\mathbf{i} - (183.6 \text{ lb})\mathbf{j} + (244.8 \text{ lb})\mathbf{k}$	
	$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (608)\mathbf{i} - (408.6 \text{ lb})\mathbf{j} + (544.8 \text{ lb})\mathbf{k}$	
Then:	R = 912.92 lb	$R = 913 \text{ lb} \blacktriangleleft$
and	$\cos\theta_x = \frac{608 \text{ lb}}{912.92 \text{ lb}} = 0.66599$	$\theta_x = 48.2^\circ \blacktriangleleft$
	$\cos\theta_{y} = \frac{408.6 \text{ lb}}{912.92 \text{ lb}} = -0.44757$	$\theta_y = 116.6^\circ \blacktriangleleft$
	$\cos\theta_z = \frac{544.8 \text{ lb}}{912.92 \text{ lb}} = 0.59677$	$\theta_z = 53.4^\circ \blacktriangleleft$



Knowing that the tension is 510 lb in cable AB and 425 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION				
	$AB = (40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$			
	$AB = (40 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2 = 85 \text{ in.}$			
	$AC = (100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$			
	$AC = (\sqrt{100 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 125 \text{ in.}$			
	$\mathbf{T}_{AB} = T_{AB} \lambda_{AB} = T_{AB} \frac{\frac{AB}{AB}}{AB} = (510 \text{ lb}) \left[\frac{(40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{j}}{85 \text{ in.}} \right]$	$\frac{0 \text{ in.})\mathbf{k}}{2}$		
$\mathbf{T}_{AB} = (240 \text{ lb})\mathbf{i} - (270 \text{ lb})\mathbf{j} + (360 \text{ lb})\mathbf{k}$				
	$\mathbf{T}_{AC} = T_{AC} \boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC} = (425 \text{ lb}) \left[\frac{(100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (100 \text{ in.})\mathbf{i}}{125 \text{ in.}} \right]$	$\left[\frac{60 \text{ in.} \mathbf{k}}{2} \right]$		
	$\mathbf{T}_{AC} = (340 \text{ lb})\mathbf{i} - (153 \text{ lb})\mathbf{j} + (204 \text{ lb})\mathbf{k}$			
	$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (580 \text{ lb})\mathbf{i} - (423 \text{ lb})\mathbf{j} + (564 \text{ lb})\mathbf{k}$			
Then:	R = 912.92 lb	$R = 913 \text{ lb} \blacktriangleleft$		
and	$\cos\theta_x = \frac{580 \text{ lb}}{912.92 \text{ lb}} = 0.63532$	$\theta_x = 50.6^\circ \blacktriangleleft$		
	$\cos\theta_y = \frac{-423 \text{ lb}}{912.92 \text{ lb}} = -0.46335$	θ _y =117.6° ◀		
	$\cos\theta_z = \frac{564 \text{ lb}}{912.92 \text{ lb}} = 0.61780$	$\theta_z = 51.8^\circ \blacktriangleleft$		



A frame *ABC* is supported in part by cable *DBE* that passes through a frictionless ring at *B*. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at D.

SOLUTION $\vec{BD} = -(480 \text{ mm})\mathbf{i} + (510 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k}$ $BD = (480 \text{ mm})^2 + (510 \text{ mm})^2 + (320 \text{ mm})^2 = 770 \text{ mm}$ $\mathbf{F}_{BD} = T_{BD} \boldsymbol{\lambda}_{BD} = T_{BD} \frac{BD}{BD}$ $=\frac{(385 \text{ N})}{(770 \text{ mm})}[=(480 \text{ mm})\mathbf{i} + (510 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k}]$ $= -(240 \text{ N})\mathbf{i} + (255 \text{ N})\mathbf{j} - (160 \text{ N})\mathbf{k}$ $\vec{BE} = -(270 \text{ mm})\mathbf{i} + (400 \text{ mm})\mathbf{j} - (600 \text{ mm})\mathbf{k}$ $BE = (\sqrt{270 \text{ mm}})^2 + (400 \text{ mm})^2 + (600 \text{ mm})^2 = 770 \text{ mm}$ $\mathbf{F}_{BE} = T_{BE} \boldsymbol{\lambda}_{BE} = T_{BE} \frac{\overline{BE}}{BE}$ $=\frac{(385 \text{ N})}{(770 \text{ mm})}[-(270 \text{ mm})\mathbf{i} + (400 \text{ mm})\mathbf{j} - (600 \text{ mm})\mathbf{k}]$ $= -(135 \text{ N})\mathbf{i} + (200 \text{ N})\mathbf{j} - (300 \text{ N})\mathbf{k}$ $\mathbf{R} = \mathbf{F}_{BD} + \mathbf{F}_{BE} = -(375 \text{ N})\mathbf{i} + (455 \text{ N})\mathbf{j} - (460 \text{ N})\mathbf{k}$ $R = \sqrt{(375 \text{ N})^2 + (455 \text{ N})^2 + (460 \text{ N})^2} = 747.83 \text{ N}$ R = 748 N $\cos \theta_x = \frac{-375 \text{ N}}{747.83 \text{ N}}$ $\theta_x = 120.1^\circ \blacktriangleleft$ $\cos \theta_{y} = \frac{455 \text{ N}}{747.83 \text{ N}}$ $\theta_v = 52.5^\circ \blacktriangleleft$ $\cos \theta_z = \frac{-460 \text{ N}}{747.83 \text{ N}}$ θ_z= 128.0° ◀



For the plate of Prob. 2.68, determine the tensions in cables AB and AD knowing that the tension in cable AC is 54 N and that the resultant of the forces exerted by the three cables at A must be vertical.

SOLUTION

We have:

$$\begin{array}{ll} --|l] & & \\ AB = -(320 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \\ ---LI & & \\ AC = (450 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \\ AD = (250 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} - (360 \text{ mm})\mathbf{k} \\ \end{array}$$

$$\begin{array}{ll} AB = 680 \text{ mm} \\ AC = 750 \text{ mm} \\ AD = 650 \text{ mm} \\ \end{array}$$

Thus:

$$\mathbf{T}_{AB} = T_{AB} \boldsymbol{\lambda}_{AB} = T_{AB} \frac{\overline{AB}}{AB} = \frac{T_{AB}}{680} (-320\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$
$$\mathbf{T}_{AC} = T_{AC} \boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overline{AC}}{AC} = \frac{54}{750} (450\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$
$$\mathbf{T}_{AD} = T_{AD} \boldsymbol{\lambda}_{AD} = T_{AD} \frac{\overline{AD}}{AD} = \frac{T_{AD}}{650} (250\mathbf{i} - 480\mathbf{j} - 360\mathbf{k})$$

Substituting into the Eq. $\mathbf{R} = \Sigma \mathbf{F}$ and factoring $\mathbf{i}, \mathbf{j}, \mathbf{k}$:

$$\mathbf{R} = \left(-\frac{320}{680} T_{AB} + 32.40 + \frac{250}{650} T_{AD} \right) \mathbf{i}$$
$$+ \left(\left| -\frac{480}{680} T_{AB} - 34.560 - \frac{480}{650} T_{AD} \right| \mathbf{j}$$
$$+ \left(\frac{360}{680} T_{AB} + 25.920 - \frac{360}{650} T_{AD} \right) \mathbf{k}$$

SOLUTION (Continued)

Since **R** is vertical, the coefficients of **i** and **k** are zero:

i:
$$-\frac{320}{680}T_{AB} + 32.40 + \frac{250}{650}T_{AD} = 0$$
 (1)

k:
$$\frac{360}{680}T_{AB} + 25.920 - \frac{360}{650}T_{AD} = 0$$
 (2)

Multiply (1) by 3.6 and (2) by 2.5 then add:

$$-\frac{252}{680}T_{AB} + 181.440 = 0$$
$$T_{AB} = 489.60 \text{ N}$$

 $T_{AB} = 490 \text{ N} \blacktriangleleft$

Substitute into (2) and solve for T_{AD} :

$$\frac{360}{680} (489.60 \text{ N}) + 25.920 - \frac{360}{650} T_{AD} = 0$$

 $T_{AD} = 514.80 \text{ N}$

 $T_{AD} = 515 \text{ N} \blacktriangleleft$



The boom *OA* carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable *AB* is 183 lb and that the resultant of the load **P** and of the forces exerted at *A* by the two cables must be directed along *OA*, determine the tension in cable *AC*.





For the boom and loading of Problem. 2.78, determine the magnitude of the load **P**.

PROBLEM 2.78 The boom *OA* carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable *AB* is 183 lb and that the resultant of the load **P** and of the forces exerted at *A* by the two cables must be directed along *OA*, determine the tension in cable *AC*.

SOLUTION

See Problem 2.78. Since resultant must be directed along OA, i.e., the x-axis, we write

$$R_y = 0: \Sigma F = (87 \text{ lb}) + \frac{25}{65} \frac{T}{AC} - P = 0$$

 T_{AC} = 130.0 lb from Problem 2.97.

Then
$$(87 \text{ lb}) + \frac{25}{65}(130.0 \text{ lb}) - P = 0$$
 $P = 137.0 \text{ lb} \blacktriangleleft$



A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AB is 6 kN.



SOLUTION (Continued)

Equilibrium condition: $\Sigma F = 0$: \therefore $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = 0$ Substituting the expressions obtained for \mathbf{T}_{AB} , \mathbf{T}_{AC} , and \mathbf{T}_{AD} ; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

From i:
$$-\frac{45}{75}T_{AB} + \frac{50}{86}T_{AD} = 0$$
 (1)

From **j**:
$$\frac{60}{75}T_{AB} + \frac{60}{68}T_{AC} + \frac{60}{86}T_{AD} - W = 0$$
(2)

From **k**: $-\frac{32}{68}T_{AC} + \frac{36}{86}T_{AD} = 0$

Setting $T_{AB} = 6$ kN in (1) and (2), and solving the resulting set of equations gives

$$T_{AC} = 6.1920 \,\mathrm{kN}$$

 $T_{AC} = 5.5080 \,\mathrm{kN}$ $W = 13.98 \,\mathrm{kN}$

(3)



A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AD is 4.3 kN.



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PROBLEM 2.81 (Continued)

Equilibrium condition: $\Sigma F = 0$: \therefore $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = 0$ Substituting the expressions obtained for \mathbf{T}_{AB} , \mathbf{T}_{AC} , and \mathbf{T}_{AD} ; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:From **i**: $-\frac{45}{75}T_{AB} + \frac{50}{86}T_{AD} = 0$ From **j**: $\frac{60}{75}T_{AB} + \frac{60}{68}T_{AC} + \frac{60}{86}T_{AD} - W = 0$ From **k**: $-\frac{32}{68}T_{AC} + \frac{36}{86}T_{AD} = 0$ Setting $T_{AD} = 4.3$ kN into the above equations gives $T_{AB} = 4.1667$ kN $T_{AC} = 3.8250$ kNW = 9.71 kN



Three cables are used to tether a balloon as shown. Knowing that the balloon exerts an 800-N vertical force at A, determine the tension in each cable.



PROBLEM 2.82 (Continued)

Equilibrium condition $\Sigma F = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$ Substituting the expressions obtained for T_{AB} , T_{AC} , and T_{AD} and factoring i, j, and k: $(-0.6T_{AB}+0.32432T_{AC})\mathbf{i} + (-0.8T_{AB}-0.75676T_{AC}-0.86154T_{AD}+P)\mathbf{j}$ $+ (0.56757T_{AC} - 0.50769T_{AD})\mathbf{k} = 0$ Equating to zero the coefficients of **i**, **j**, **k**: $-0.6T_{AB} + 0.32432T_{AC} = 0$ (1) $-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0$ (2) $0.56757T_{AC} - 0.50769T_{AD} = 0$ (3)From Eq. (1) $T_{AB} = 0.54053T_{AC}$ From Eq. (3) $T_{AD} = 1.11795T_{AC}$ Substituting for T_{AB} and T_{AD} in terms of T_{AC} into Eq. (2) gives: $-0.8(0.54053T_{AC}) - 0.75676T_{AC} - 0.86154(1.11795T_{AC}) + P = 0$ $2.1523T_{AC} = P; P = 800 \text{ N}$ $T_{AC} = \frac{800 \text{ N}}{2.1523}$ = 371.69 N Substituting into expressions for T_{AB} and T_{AD} gives: $T_{AB} = 0.54053(371.69 \text{ N})$ $T_{AD} = 1.11795(371.69 \,\mathrm{N})$ $T_{AB} = 201$ N, $T_{AC} = 372$ N, $T_{AD} = 416$ N \triangleleft



A crate is supported by three cables as shown. Determine the weight of the crate knowing that the tension in cable AD is 616 lb.

SOLUTION

and

The forces applied at *A* are:

 \mathbf{T}_{AB} , \mathbf{T}_{AC} , \mathbf{T}_{AD} and \mathbf{W}

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors \mathbf{i} , \mathbf{j} , \mathbf{k} , we write

and

$$\begin{aligned}
\overrightarrow{AB} &= -(36 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k} \\
AB &= 75 \text{ in.} \\
\overrightarrow{AC} &= (60 \text{ in.})\mathbf{j} + (32 \text{ in.})\mathbf{k} \\
AC &= 68 \text{ in.} \\
\overrightarrow{AD} &= (40 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k} \\
AD &= 77 \text{ in.} \\
\mathbf{T}_{AB} &= T_{AB}\lambda_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} \\
&= (-0.48\mathbf{i} + 0.8\mathbf{j} - 0.36\mathbf{k})T_{AB} \\
\mathbf{T}_{AC} &= T_{AC}\lambda_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} \\
&= (0.88235\mathbf{j} + 0.47059\mathbf{k})T_{AC} \\
\mathbf{T}_{AD} &= T_{AD}\lambda_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} \\
&= (0.51948\mathbf{i} + 0.77922\mathbf{j} - 0.35065\mathbf{k})T_{AD}
\end{aligned}$$
Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$
 $\Sigma F = 0; \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$

PROBLEM 2.83 (Continued)

Substituting the expressions obtained for T_{AB} , T_{AC} , and T_{AD} and factoring **i**, **j**, and **k**:

$$(-0.48T_{AB} + 0.51948T_{AD})\mathbf{i} + (0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W)\mathbf{j} + (-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD})\mathbf{k} = 0$$

 $-0.48T_{AB} + 0.51948T_{AD} = 0$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0$$

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0$$

Substituting $T_{AD} = 616$ lb in Equations (1), (2), and (3) above, and solving the resulting set of

equations, gives:

 $T_{AC} = 969.00 \text{ lb } W = 1868 \text{ lb } \blacktriangleleft$



SOLUTION

See Problem 2.83 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \tag{1}$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0$$
⁽²⁾

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0$$
⁽³⁾

Substituting T_{AC} = 544 lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives:

$$T_{AB} = 374.27 \text{ lb}$$

 $T_{AD} = 345.82 \text{ lb}$ $W = 1049 \text{ lb} \blacktriangleleft$



SOLUTION

See Problem 2.83 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \tag{1}$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0$$
⁽²⁾

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0 \tag{3}$$

Substituting W = 1600 lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives

- $T_{AB} = 571 \text{ lb} \blacktriangleleft$
- $T_{AC} = 830 \text{ lb} \blacktriangleleft$
- $T_{AD} = 528 \text{ lb} \blacktriangleleft$



Three wires are connected at point D, which is located 18 in. below the T-shaped pipe support *ABC*. Determine the tension in each wire when a 180-lb cylinder is suspended from point D as shown.



and

SOLUTION (Continued)

$$T_{DA} = T_{Da} \lambda_{DA} = T_{Da} \frac{DA}{DA}$$

$$= (0.63324 \mathbf{j} + 0.77397 \mathbf{k}) T_{DA}$$

$$T_{DB} = T_{DB} \lambda_{DB} = T_{DB} \frac{DB}{DB}$$

$$= (-0.70588 \mathbf{i} + 0.52941 \mathbf{j} - 0.47059 \mathbf{k}) T_{DB}$$

$$T_{DC} = T_{DC} \lambda_{DC} = T_{DC} \frac{DC}{DC}$$

$$= (0.70588 \mathbf{i} + 0.52941 \mathbf{j} - 0.47059 \mathbf{k}) T_{DC}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} - W\mathbf{j} = 0$$

Substituting the expressions obtained for T_{DA} , T_{DB} , and T_{DC} and factoring i, j, and k:

$$(-0.70588T_{DB} + 0.70588T_{DC})$$
i
 $(0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W)$ **j**
 $(0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC})$ **k**

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.70588T_{DB} + 0.70588T_{DC} = 0 \tag{1}$$

$$0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W = 0$$
⁽²⁾

$$0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC} = 0 \tag{3}$$

Substituting W = 180 lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives,

- $T_{DA} = 119.7$ lb \blacktriangleleft
- $T_{DB} = 98.4$ lb \blacktriangleleft
- $T_{DC} = 98.4 \text{ lb}$



A 36-lb triangular plate is supported by three wires as shown. Determine the tension in each wire, knowing that a = 6 in.



SOLUTION (Continued)

 Equilibrium condition:
 $\Sigma F = 0$: $\mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} + (36 \text{ lb})\mathbf{j} = 0$

 Substituting the expressions obtained for \mathbf{T}_{DA} , \mathbf{T}_{DB} , and \mathbf{T}_{DC} and factoring \mathbf{i} , \mathbf{j} , and \mathbf{k} :

 $(0.55471T_{DA} - 0.30769T_{DB} - 0.30769T_{DC})\mathbf{i} + (-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb})\mathbf{j}$
 $+ (0.23077T_{DB} - 0.23077T_{DC})\mathbf{k} = 0$

 Equating to zero the coefficients of \mathbf{i} , \mathbf{j} , \mathbf{k} :

 $0.55471T_{DA} - 0.30769T_{DC} = 0$ (1)

 $-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb} = 0$ (2)

 $0.23077T_{DB} - 0.23077T_{DC} = 0$ (3)

 Equation (3) confirms that $T_{DB} = T_{DC}$. Solving simultaneously gives,

 $T_{DA} = 14.42$ lb; $T_{DB} = T_{DC} = 13.00$ lb



A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AC is 60 N, determine the weight of the plate.

SOLUTION

We note that the weight of the plate is equal in magnitude to the force \mathbf{P} exerted by the support on Point *A*.



We have:

$$\frac{AB}{AB} = -(320 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad AB = 680 \text{ mm}$$
$$\frac{AC}{AD} = (450 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad AC = 750 \text{ mm}$$
$$AD = (250 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} - (360 \text{ mm})\mathbf{k} \qquad AD = 650 \text{ mm}$$



Free Body A :

Thus:

$$\mathbf{T}_{AB} = T_{AB} \boldsymbol{\lambda}_{AB} = T_{AB} \frac{\overline{AB}}{AB} = \left(-\frac{8}{17} \mathbf{i} - \frac{12}{17} \mathbf{j} + \frac{9}{17} \mathbf{k} \right)_{AB} \qquad \text{Dimensions in mm}$$
$$\mathbf{T}_{AC} = T_{AC} \boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overline{AC}}{AC} = \left(0.6\mathbf{i} - 0.64\mathbf{j} + 0.48\mathbf{k} \right) T_{AC}$$
$$\mathbf{T}_{AD} = T_{AD} \boldsymbol{\lambda}_{AD} = T_{AD} \frac{\overline{AD}}{AD} = \left(\frac{5}{13} \mathbf{i} - \frac{9.6}{13} \mathbf{j} - \frac{7.2}{13} \mathbf{k} \right) T_{AD}$$

Substituting into the Eq. $\Sigma F = 0$ and factoring **i**, **j**, **k** :

$$\left(-\frac{8}{17} T_{AB} + 0.6 T_{AC} + \frac{5}{13} T_{AD} \right) \mathbf{i}$$

+ $\left(-\frac{12}{17} T_{AB} - 0.64 T_{AC} - \frac{9.6}{13} T_{AD} + P \right) \mathbf{j}$
+ $\left(\frac{9}{17} T_{AB} + 0.48 T_{AC} - \frac{7.2}{13} T_{AD} \right) \mathbf{k} = 0$

SOLUTION (Continued)

Setting the coefficient of **i**, **j**, **k** equal to zero:

i:
$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0$$
 (1)

j:
$$-\frac{12}{7}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0$$
 (2)

k:
$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0$$
 (3)

Making $T_{AC} = 60$ N in (1) and (3):

$$-\frac{8}{17}T_{AB} + 36 \text{ N} + \frac{5}{13}T_{AD} = 0$$
 (1')

$$\frac{9}{17}T_{AB} + 28.8 \text{ N} - \frac{7.2}{13}T_{AD} = 0 \tag{3'}$$

Multiply (1') by 9, (3') by 8, and add:

554.4 N
$$-\frac{12.6}{13}T_{AD} = 0$$
 $T_{AD} = 572.0$ N

Substitute into (1') and solve for T_{AB} :

$$T_{AB} = \frac{17}{8} \left(36 + \frac{5}{13} \times 572 \right) \qquad T_{AB} = 544.0 \text{ N}$$

Substitute for the tensions in Eq. (2) and solve for P:

$$P = \frac{12}{17}(544 \text{ N}) + 0.64(60 \text{ N}) + \frac{9.6}{13}(572 \text{ N})$$

= 844.8 N Weight of plate = P = 845 N



A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AD is 520 N, determine the weight of the plate.

SOLUTION

See Problem 2.88 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0$$
(1)

$$-\frac{12}{17}T_{AB} + 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0$$
⁽²⁾

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0$$
(3)

Making T_{AD} = 520 N in Eqs. (1) and (3):

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + 200 \text{ N} = 0 \tag{1'}$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - 288 \text{ N} = 0 \tag{3'}$$

Multiply (1') by 9, (3') by 8, and add:

$$9.24T_{AC} - 504$$
 N = 0 $T_{AC} = 54.5455$ N

Substitute into (1') and solve for T_{AB} :

$$T_{AB} = \frac{17}{8} (0.6 \times 54.5455 + 200)$$
 $T_{AB} = 494.545$ N

Substitute for the tensions in Eq. (2) and solve for *P*:

$$P = \frac{12}{17} (494.545 \text{ N}) + 0.64(54.5455 \text{ N}) + \frac{9.6}{13} (520\text{N})$$

= 768.00 N Weight of plate = P = 768 N <



In trying to move across a slippery icy surface, a 175-lb man uses two ropes AB and AC. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.



SOLUTION (Continued)

Substituting the expressions obtained for T_{AB} , T_{AC} , N, and W; factoring i, j, and k; and equating each of the coefficients to zero gives the following equations:

From **i**:
$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0$$
 (1)

$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175 \text{ lb}) = 0$$
(2)

From **k**:
$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} = 0$$
 (3)

Solving the resulting set of equations gives:

$$T_{AB} = 30.8$$
 lb; $T_{AC} = 62.5$ lb



Solve Problem 2.90, assuming that a friend is helping the man at *A* by pulling on him with a force $\mathbf{P} = -(45 \text{ lb})\mathbf{k}$.

PROBLEM 2.90 In trying to move across a slippery icy surface, a 175-lb man uses two ropes *AB* and *AC*. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.

SOLUTION

Refer to Problem 2.90 for the figure and analysis leading to the following set of equations, Equation (3) being modified to include the additional force $\mathbf{P} = (-45 \text{ lb})\mathbf{k}$.

$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0 \tag{1}$$

$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175 \text{ lb}) = 0$$
(2)

$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} - (45 \text{ lb}) = 0$$
(3)

Solving the resulting set of equations simultaneously gives:

$$T_{AB} = 81.3 \text{ lb} \blacktriangleleft$$
$$T_{AC} = 22.2 \text{ lb} \blacktriangleleft$$



SOLUTION			
$\Sigma \mathbf{F}_{A} = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{P} = 0$ where $\mathbf{P} = P\mathbf{i}$			
$AB = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k}$ $AB = 1060 \text{ mm}$			
$\vec{A}_{\rm T} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k}$ $AC = 1040 \text{ mm}$			
$AD = -(960 \text{ mm})\mathbf{i} + (720 \text{ mm})\mathbf{j} - (220 \text{ mm})\mathbf{k}$ $AD = 1220 \text{ mm}$			
$\mathbf{T}_{AB} = T_{AB} \boldsymbol{\lambda}_{AB} = T_{AB} \frac{\overline{AB}}{\overline{AB}} = T_{AB} \left(-\frac{48}{53} \mathbf{i} - \frac{12}{53} \mathbf{j} + \frac{19}{53} \mathbf{k} \right)$			
$\mathbf{T}_{AC} = T_{AC} \boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC} = T_{AC} \left(-\frac{12}{13} \mathbf{i} - \frac{3}{13} \mathbf{j} - \frac{4}{13} \mathbf{k} \right)$			
$\mathbf{T}_{AD} = T_{AD} \mathbf{\hat{h}}_{D} = \frac{305 \text{ N}}{1220 \text{ mm}} [(-960 \text{ mm})\mathbf{i} + (720 \text{ mm})\mathbf{j} - (220 \text{ mm})\mathbf{k}]$			
$= -(240 \text{ N})\mathbf{i} + (180 \text{ N})\mathbf{j} - (55 \text{ N})\mathbf{k}$			
Substituting into $\Sigma \mathbf{F}_A = 0$, factoring i , j , k , and setting each coefficient equal to ϕ gives:			
$\mathbf{i}: P = \frac{48}{53} T_{AB} + \frac{12}{13} T_{AC} + 240 \text{ N}$ (1)			
j : $\frac{12}{53}T_{AB} + \frac{3}{13}T_{AC} = 180 \text{ N}$ (2)			
$\mathbf{k}: \qquad \frac{19}{53} T_{AB} - \frac{4}{13} T_{AC} = 55 \text{ N} $ (3)			
Solving the system of linear equations using conventional algorithms gives:			
$T_{AB} = 446.71 \text{ N}$			
$T_{AC} = 341.71 \text{ N}$ $P = 960 \text{ N} \blacktriangleleft$			



Three cables are connected at *A*, where the forces **P** and **Q** are applied as shown. Knowing that P = 1200 N, determine the values of *Q* for which cable *AD* is taut.

SOLUTION

We assume that $T_{AD} = 0$ and write $\Sigma \mathbf{F}_{A} = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + Q\mathbf{j} + (1200 \text{ N})\mathbf{i} = 0$ $AB = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k}$ AB = 1060 mm $AC = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} AC = 1040 \text{ mm}$ $\mathbf{T}_{AB} = T_{AB} \,\boldsymbol{\lambda}_{AB} = T_{AB} \,\frac{\overline{AB}}{\overline{AB}} = \left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right) T_{AB}$ $\mathbf{T}_{AC} = T_{AC} \,\boldsymbol{\lambda}_{AC} = T_{AC} \,\frac{\overrightarrow{AC}}{AC} = \left(\left| -\frac{12}{13} \,\mathbf{i} - \frac{3}{13} \,\mathbf{j} - \frac{4}{13} \,\mathbf{k} \right| \right) \mathbf{T}_{AC}$ Substituting into $\Sigma \mathbf{F}_A = 0$, factoring **i**, **j**, **k**, and setting each coefficient equal to ϕ gives: i: $-\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} + 1200 \text{ N} = 0$ (1)**j**: $-\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + Q = 0$ (2) $\mathbf{k}: \quad \frac{19}{53} T_{AB} - \frac{4}{13} T_{AC} = 0$ (3)Solving the resulting system of linear equations using conventional algorithms gives: $T_{AB} = 605.71 \,\mathrm{N}$ $T_{AC} = 705.71 \text{ N}$

$$Q = 300.00 \text{ N}$$
 $0 \le Q < 300 \text{ N}$

Note: This solution assumes that Q is directed upward as shown ($Q \ge 0$), if negative values of Q are considered, cable AD remains taut, but AC becomes slack for Q = -460 N.



A container of weight *W* is suspended from ring *A*. Cable *BAC* passes through the ring and is attached to fixed supports at *B* and *C*. Two forces $\mathbf{P} = P\mathbf{i}$ and \mathbf{Q} = $Q\mathbf{k}$ are applied to the ring to maintain the container in the position shown. Knowing that W = 376 N, determine *P* and *Q*. (*Hint:* The tension is the same in both portions of cable *BAC*.)

SOLUTION

 $\mathbf{T}_{AB} = T \boldsymbol{\lambda}_{AB}$ Free-Body A: $= T \frac{\overline{AB}}{AB}$ $= T \frac{(-130 \text{ mm})\mathbf{i} + (400 \text{ mm})\mathbf{j} + (160 \text{ mm})\mathbf{k}}{450 \text{ mm}}$ TAB = T $=T\left(-\frac{13}{45}\mathbf{i}+\frac{40}{45}\mathbf{j}+\frac{16}{45}\mathbf{k}\right)$ = - (376 N) J $\mathbf{T}_{AC} = T \boldsymbol{\lambda}_{AC}$ $= T \frac{\overline{AC}}{AC}$ $= T \frac{(-150 \text{ mm})\mathbf{i} + (400 \text{ mm})\mathbf{j} + (-240 \text{ mm})\mathbf{k}}{490 \text{ mm}}$ $=T\left(-\frac{15}{49}\mathbf{i}+\frac{40}{49}\mathbf{j}-\frac{24}{49}\mathbf{k}\right)$ $\Sigma F = 0: \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{Q} + \mathbf{P} + \mathbf{W} = 0$ Setting coefficients of i, j, k equal to zero: $\mathbf{i} : -\frac{13}{45}T - \frac{15}{49}T + P = 0$ 0.59501T = P(1) $\mathbf{j}: + \frac{40}{45} + \frac{40}{49} - W = 0 \qquad 1.70521T = W$ (2) $\mathbf{k}: + \frac{16}{45}T - \frac{24}{49}T + Q = 0 \qquad 0.134240T = Q$ (3)

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PROBLEM 2.94 (Continued)

Data:

W = 376 N 1.70521T = 376 N T = 220.50 N

0.59501(220.50 N) = P

 $P = 131.2 \text{ N} \blacktriangleleft$ $Q = 29.6 \text{ N} \blacktriangleleft$

0.134240(220.50 N) = Q



For the system of Problem 2.94, determine W and Q knowing that P = 164 N.

PROBLEM 2.94 A container of weight *W* is suspended from ring *A*. Cable *BAC* passes through the ring and is attached to fixed supports at *B* and *C*. Two forces $\mathbf{P} = P\mathbf{i}$ and $\mathbf{Q} = Q\mathbf{k}$ are applied to the ring to maintain the container in the position shown. Knowing that W = 376 N, determine *P* and *Q*. (*Hint:* The tension is the same in both portions of cable *BAC*.)

SOLUTION

Refer to Problem 2.94 for the figure and analysis resulting in Equations (1), (2), and (3) for *P*, *W*, and *Q* in terms of *T* below. Setting P = 164 N we have:

Eq. (1):	0.59501T = 164 N	T = 275.63 N
Eq. (2):	1.70521(275.63 N) = W	$W = 470$ N \triangleleft
Eq. (3):	0.134240(275.63 N) = Q	Q = 37.0 N



Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load **P** is applied to ring *A*, determine the tension in each of the three cables.



SOLUTION Continued

Substituting into $\Sigma \mathbf{F}_A = 0$, setting $\mathbf{P} = (-200 \text{ lb})\mathbf{j}$, and setting the coefficients of \mathbf{i} , \mathbf{j} , \mathbf{k} equal to ϕ , we obtain the following three equilibrium equations:

From **i**:
$$-\frac{17.5}{62.5}T_{BAC} + \frac{4}{5}T_{AD} = 0$$
 (1)

From

j:
$$\left(\frac{60}{62.5} + \frac{60}{65}\right)_{BAC} + \frac{3}{5}T_{AD} + \frac{4}{5}T_{AE} - 200 \text{ lb} = 0$$
 (2)

From $\mathbf{k}: \quad \frac{25}{65}T_{BAC} - \frac{3}{5}T_{AE} = 0$

Solving the system of linear equations using conventional algorithms gives:

$$T_{BAC} = 76.7$$
 lb; $T_{AD} = 26.9$ lb; $T_{AE} = 49.2$ lb

(3)


Knowing that the tension in cable AE of Prob. 2.96 is 75 lb, determine (*a*) the magnitude of the load **P**, (*b*) the tension in cables *BAC* and *AD*.

PROBLEM 2.96 Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load \mathbf{P} is applied to ring *A*, determine the tension in each of the three cables.

SOLUTION

Refer to the solution to Problem 2.96 for the figure and analysis leading to the following set of equilibrium equations, Equation (2) being modified to include *P***j** as an unknown quantity:

$$-\frac{17.5}{62.5}T_{BAC} + \frac{4}{5}T_{AD} = 0 \tag{1}$$

$$\left(\frac{60}{62.5} + \frac{60}{65}\right)_{BAC} + \frac{3}{5}T_{AD} + \frac{4}{5}T_{AE} - P = 0$$
(2)

$$\frac{25}{65}T_{BAC} - \frac{3}{5}T_{AE} = 0 \quad (3)$$

Substituting for T_{AE} = 75 lb and solving simultaneously gives:

(a)
$$P = 305 \text{ lb} \blacktriangleleft$$

(b) $T_{BAC} = 117.0 \text{ lb}; T_{AD} = 40.9 \text{ lb} \blacktriangleleft$

SOLUTION Continued Then from the specifications of the problem, y = 155 mm = 0.155 m $z^2 = 0.23563 \text{ m}^2 - (0.155 \text{ m})^2$ z = 0.46 m and $T_{AB} = \frac{341 \text{ N}}{0.155(1.90476)}$ *(a)* = 1155.00 N or $T_{AB} = 1155$ N \triangleleft and $Q = \frac{341 \text{ N}(0.46 \text{ m})(0.866)}{(0.155 \text{ m})}$ *(b)* =(1012.00 N) $Q = 1012 \text{ N} \blacktriangleleft$ or



A container of weight *W* is suspended from ring *A*, to which cables *AC* and *AE* are attached. A force **P** is applied to the end *F* of a third cable that passes over a pulley at *B* and through ring *A* and that is attached to a support at *D*. Knowing that W = 1000 N, determine the magnitude of *P*. (*Hint:* The tension is the same in all portions of cable *FBAD*.)

SOLUTION

The (vector) force in each cable can be written as the product of the (scalar) force and the unit vector along the cable. That is, with

$$\mathcal{AB} = -(0.78 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (0 \text{ m})\mathbf{k}$$

$$AB = \sqrt{(-0.78 \text{ m})^2 + (1.6 \text{ m})^2 + (0)^2}$$

$$= 1.78 \text{ m}$$

$$\mathbf{T}_{AB} = T\lambda_{AB} = T_{AB} \frac{\overline{AB}}{AB}$$

$$= \frac{T_{AB}}{1.78 \text{ m}} [-(0.78 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (0 \text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AB} = T_{AB} (-0.4382\mathbf{i} + 0.8989\mathbf{j} + 0\mathbf{k})$$

$$\overline{AC} = (0)\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (1.2 \text{ m})\mathbf{k}$$

$$AC = (\sqrt{0} \text{ m})^2 + (1.6 \text{ m})^2 + (1.2 \text{ m})^2 = 2 \text{ m}$$

$$\mathbf{T}_{AC} = T\lambda_{AC} = T_{AC} \frac{\overline{AC}}{AC} = \frac{T_{AC}}{2 \text{ m}} [(0)\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (1.2 \text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AC} = T\lambda_{AC} = (0.8\mathbf{j} + 0.6\mathbf{k})$$

$$\overline{AD} = (1.3 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (0.4 \text{ m})\mathbf{k}$$

$$AD = (\sqrt{1.3 \text{ m}}^2 + (1.6 \text{ m})^2 + (0.4 \text{ m})^2 = 2.1 \text{ m}$$

$$\mathbf{T}_{AD} = T\lambda_{AD} = T_{AD} \frac{\overline{AD}}{AD} = \frac{T_{AD}}{2.1 \text{ m}} [(1.3 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} + (0.4 \text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AD} = T\lambda_{AD} = T_{AD} (0.6190\mathbf{i} + 0.7619\mathbf{j} + 0.1905\mathbf{k})$$

and

and

SOLUTION Continued

Finally,

$$AE = (0.4 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} - (0.86 \text{ m})\mathbf{k}$$

$$AE = \sqrt{(-0.4 \text{ m})^2 + (1.6 \text{ m})^2 + (-0.86 \text{ m})^2} = 1.86 \text{ m}$$

$$\mathbf{T}_{AE} = T\lambda_{AE} = T_{AE} \frac{\overline{AE}}{AE}$$

$$= \frac{T_{AE}}{1.86 \text{ m}} [-(0.4 \text{ m})\mathbf{i} + (1.6 \text{ m})\mathbf{j} - (0.86 \text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AE} = T_{AE} (-0.2151\mathbf{i} + 0.8602\mathbf{j} - 0.4624\mathbf{k})$$

With the weight of the container

 $\mathbf{W} = -W\mathbf{j}$, at A wehave:

$$\Sigma \mathbf{F} = 0: \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

Equating the factors of **i**, **j**, and **k** to zero, we obtain the following linear algebraic equations:

$$-0.4382T_{AB} + 0.6190T_{AD} - 0.2151T_{AE} = 0 \tag{1}$$

$$0.8989T_{AB} + 0.8T_{AC} + 0.7619T_{AD} + 0.8602T_{AE} - W = 0$$
⁽²⁾

$$0.6T_{AC} + 0.1905T_{AD} - 0.4624T_{AE} = 0 \tag{3}$$

Knowing that W = 1000 N and that because of the pulley system at $BT_{AB} = T_{AD} = P$, where *P* is the externally applied (unknown) force, we can solve the system of linear Equations (1), (2) and (3) uniquely for *P*.

 $P = 378 \text{ N} \blacktriangleleft$



Using two ropes and a roller chute, two workers are unloading a 200-lb cast-iron counterweight from a truck. Knowing that at the instant shown the counterweight is kept from moving and that the positions of Points *A*, *B*, and *C* are, respectively, A(0, -20 in., 40 in.), B(-40 in., 50 in., 0), and C(45 in., 40 in., 0), and assuming that no friction exists between the counterweight and the chute, determine the tension in each rope. (*Hint*: Since there is no friction, the force exerted by the chute on the counterweight must be perpendicular to the chute.)

B (-40,50,0

C (45,40,0)

SOLUTION

From the geometry of the chute:

$$\mathbf{N} = \frac{N}{\sqrt{5}} (2\mathbf{j} + \mathbf{k})$$
$$= N (0.8944\mathbf{j} + 0.4472\mathbf{k})$$

The force in each rope can be written as the product of the magnitude of the force and the unit vector along the cable. Thus, with

$$AB = (40 \text{ in.})\mathbf{i} + (70 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}$$

$$AB = \sqrt{40 \text{ in.}}^2 + (70 \text{ in.})^2 + (40 \text{ in.})^2$$

$$= 90 \text{ in.}$$

$$\mathbf{T}_{AB} = T\lambda_{AB} = T_{AB}\frac{\overline{AB}}{\overline{AB}}$$

$$= \frac{T_{AB}}{90 \text{ in.}}[(-40 \text{ in.})\mathbf{i} + (70 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}]$$

$$\mathbf{T}_{AB} = T_{AB}\left(-\frac{4}{9}\mathbf{i} + \frac{7}{9}\mathbf{j} - \frac{4}{9}\mathbf{k}\right)$$

 $AC = (45 \text{ in.})^2 + (60 \text{ in.})^2 + (40 \text{ in.})^2 = 85 \text{ in.}$

 $=\frac{T_{AC}}{85 \text{ in}} [(45 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}]$

 $AC = (45 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}$

 $\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC}$

 $\mathbf{T}_{AC} = T_{AC} \left(\frac{9}{17} \mathbf{i} + \frac{12}{17} \mathbf{j} - \frac{8}{17} \mathbf{k} \right)$

 $\Sigma \mathbf{F} = 0: \mathbf{N} + \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{W} = 0$

and

Then:

SOLUTION Continued

With W = 200 lb, and equating the factors of **i**, **j**, and **k** to zero, we obtain the linear algebraic equations:

$$\mathbf{i:} \quad -\frac{4}{9}T_{AB} + \frac{9}{17}T_{AC} = 0 \tag{1}$$

$$\mathbf{j}: \qquad \frac{7}{9}T_{AB} + \frac{12}{17}T_{AC} + \frac{2}{\sqrt{5}} 200 \text{ lb} = 0 \tag{2}$$

$$\mathbf{k}: \quad -\frac{4}{9}T_{AB} - \frac{8}{17}T_{AC} + \frac{1}{\sqrt{5}} = 0 \tag{3}$$

Using conventional methods for solving linear algebraic equations we obtain:

$$T_{AB} = 65.6 \text{ lb} \blacktriangleleft$$

$$T_{AC} = 55.1 \text{ lb} \blacktriangleleft$$



Collars *A* and *B* are connected by a 25-in.-long wire and can slide freely on frictionless rods. If a 60-lb force **Q** is applied to collar *B* as shown, determine (*a*) the tension in the wire when x = 9 in., (*b*) the corresponding magnitude of the force **P** required to maintain the equilibrium of the system.





Collars *A* and *B* are connected by a 25-in.-long wire and can slide freely on frictionless rods. Determine the distances x and z for which the equilibrium of the system is maintained when P = 120 lb and Q = 60 lb.

SOLUTION

See Problem 2.100 for the diagrams and analysis leading to Equations (1) and (2) below:

$$P = \frac{T_{AB}x}{25 \text{ in.}} = 0 \tag{1}$$

$$60 \text{ lb} - \frac{T_{AB}z}{25 \text{ in.}} = 0 \tag{2}$$

For P = 120 lb, Eq. (1) yields (1') $T_{AB} x = (25 \text{ in.})(20 \text{ lb})$

From Eq. (2):
$$T_{AB \ Z} = (25 \text{ in.})(60 \text{ lb})$$
 (2')
Dividing Eq. (1') by (2'), $\frac{x}{-} = 2$ (3)

z

Dividing Eq. (1') by (2'),

Now write

 $x^{2} + z^{2} + (20 \text{ in.})^{2} = (25 \text{ in.})^{2}$ (4)

Solving (3) and (4) simultaneously,

$$4z^{2} + z^{2} + 400 = 625$$

$$z^{2} = 45$$

$$z = 6.7082 \text{ in.}$$
From Eq. (3):
$$x = 2z = 2(6.7082 \text{ in.})$$

$$= 13.4164 \text{ in.}$$

$$x = 13.42 \text{ in.}, \quad z = 6.71 \text{ in.} \blacktriangleleft$$



Collars *A* and *B* are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341 \text{ N})\mathbf{j}$ is applied to collar *A*, determine (*a*) the tension in the wire when y = 155 mm, (*b*) the magnitude of the force \mathbf{Q} required to maintain the equilibrium of the system.





Solve Problem 2.102 assuming that y = 275 mm.

PROBLEM 2.102 Collars *A* and *B* are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341 \text{ N})\mathbf{j}$ is applied to collar *A*, determine (*a*) the tension in the wire when y = 155 mm, (*b*) the magnitude of the force \mathbf{Q} required to maintain the equilibrium of the system.

SOLUTION

From the analysis of Problem 2.102, particularly the results:

$$y^{2} + z^{2} = 0.23563 \text{ m}^{2}$$

 $T_{AB} = \frac{341 \text{ N}}{1.90476 y}$
 $Q = \frac{341 \text{ N}}{y} z$

With y = 275 mm = 0.275 m, we obtain:

$$z^2 = 0.23563 \text{ m}^2 - (0.275 \text{ m})^2$$

 $z = 0.40 \text{ m}$

and

(a)

$$T_{AB} = \frac{341 \text{ N}}{(1.90476)(0.275 \text{ m})} = 651.00$$

or
and
(b)
 $Q = \frac{341 \text{ N}(0.40 \text{ m})}{(0.275 \text{ m})}$
or
 $Q = 496 \text{ N} \blacktriangleleft$



Two structural members A and B are bolted to a bracket as shown. Knowing that both members are in compression and that the force is 15 kN in member A and 10 kN in member B, determine by trigonometry the magnitude and direction of the resultant of the forces applied to the bracket by members A and B.

SOLUTION

Using the force triangle and the laws of cosines and sines,		50° p
we have	$\gamma = 180^{\circ} - (40^{\circ} + 20^{\circ})$	40°
	= 120°	(X 15 KN
Then	$R^2 = (15 \text{ kN})^2 + (10 \text{ kN})^2$	$R \setminus I$
	$-2(15 \text{ kN})(10 \text{ kN}) \cos 120^{\circ}$	
	$= 475 \text{ kN}^2$	20
	R = 21.794 kN	* IOKN
and	10 kN = 21.794 kN	
und	sinα sin120°	
	$\sin \alpha = \left(\frac{10 \text{ kN}}{10 \text{ km}} \right) \sin 120^{\circ}$	
	$(21.794 \text{ kN})^{-1120}$	
	= 0.39737	
	$\alpha = 23.414$	
Hence:	$\phi = \alpha + 50^\circ = 73.414$	$\mathbf{R} = 21.8 \text{ kN} \ \overline{\ \ } 73.4^{\circ} \ \overline{\ \ }$







The hydraulic cylinder *BC* exerts on member *AB* a force **P** directed along line *BC*. Knowing that **P** must have a 600-N component perpendicular to member *AB*, determine (*a*) the magnitude of the force **P**, (*b*) its component along line *AB*.





Knowing that $\alpha = 40^{\circ}$, determine the resultant of the three forces shown.

SOLUTION

60-lb Force:	$F_x = (60 \text{ lb}) \cos 20^\circ = 56.382 \text{ lb}$ $F_y = (60 \text{ lb}) \sin 20^\circ =$	
80-lb Force:	$F_x = (80 \text{ lb}) \cos 60^\circ = 40.000 \text{ lb}$ $F_y = (80 \text{ lb}) \sin 60^\circ =$	Ry=(29.80316) j ~ R
120-lb Force:	$F_x = (120 \text{ lb})\cos 30^\circ =$ $F_y = -(120 \text{ lb})\sin 30^\circ = -60.000 \text{ lb}$	$R_{x} = (200.3051b)i$
and	$R_x = \Sigma F_x = 200.305$ lb $R_y = \Sigma F_y = 29.803$ lb	
	$R = (200.305 \text{ lb})^2 + (29.803 \text{ lb})^2$ = 202.510 lb	
Further:	$\tan \alpha = \frac{29.803}{200.305}$	
	$\alpha = \tan^{-1} \frac{29.803}{200.305}$ $= 8.46^{\circ}$	$\mathbf{R} = 203 \text{ lb} \checkmark 8.46^{\circ} \blacktriangleleft$







For W = 800 N, P = 200 N, and d = 600 mm, determine the value of *h* consistent with equilibrium.

SOLUTION Free-Body Diagram $T_{AC} = T_{BC} = 800 \text{ N}$ $AC = BC = \left(\sqrt{p^2 + d^2}\right)$ $\Sigma F_y = 0: 2(800 \text{ N}) \frac{h}{\sqrt{h^2 + d^2}} - P = 0$ $800 = \frac{P}{2} \sqrt{1 + \left(\frac{d}{h}\right)^2}$ Data: P = 200 N, d = 600 mm and solving for h $800 \text{ N} = \frac{200 \text{ N}}{2} \sqrt{1 + \left(\frac{600 \text{ mm}}{h}\right)^2}$ $h = 75.6 \text{ mm} \blacktriangleleft$



Three forces are applied to a bracket as shown. The directions of the two 150-N forces may vary, but the angle between these forces is always 50°. Determine the range of values of α for which the magnitude of the resultant of the forces acting at *A* is less than 600 N.





Cable *AB* is 65 ft long, and the tension in that cable is 3900 lb. Determine (*a*) the *x*, *y*, and *z* components of the force exerted by the cable on the anchor *B*, (*b*) the angles θ_x , θ_y , and θ_z defining the direction of that force.





Three cables are used to tether a balloon as shown. Determine the vertical force \mathbf{P} exerted by the balloon at *A* knowing that the tension in cable *AB* is 259 N.



SOLUTION Continued

Equilibrium condition $\Sigma F = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$ Substituting the expressions obtained for T_{AB} , T_{AC} , and T_{AD} and factoring i, j, and k: $(-0.6T_{AB} + 0.32432T_{AC})\mathbf{i} + (-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P)\mathbf{j}$ + $(0.56757T_{AC} - 0.50769T_{AD})\mathbf{k} = 0$ Equating to zero the coefficients of **i**, **j**, **k**: $-0.6T_{AB} + 0.32432T_{AC} = 0$ (1) $-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0$ (2) $0.56757T_{AC} - 0.50769T_{AD} = 0$ (3) Setting $T_{AB} = 259$ N in (1) and (2), and solving the resulting set of equations gives $T_{AC} = 479.15 \text{ N}$ $T_{AD} = 535.66 \,\mathrm{N}$ $P = 1031 \text{ N}^{\dagger} \blacktriangleleft$



Three cables are used to tether a balloon as shown. Determine the vertical force \mathbf{P} exerted by the balloon at *A* knowing that the tension in cable *AC* is 444 N.

SOLUTION

See Problem 2.112 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \tag{1}$$

$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0$$
⁽²⁾

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \tag{3}$$

Substituting T_{AC} = 444 N in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives

$$T_{AB} = 240 \text{ N}$$

 $T_{AD} = 496.36 \text{ N}$ **P** = 956 N



A transmission tower is held by three guy wires attached to a pin at A and anchored by bolts at B, C, and D. If the tension in wire AB is 630 lb, determine the vertical force **P** exerted by the tower on the pin at A.



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PROBLEM 2.114 (Continued)

Setting the coefficients of **i**, **j**, **k**, equal to zero:

$$\mathbf{i:} \quad -\frac{3}{7}T_{AB} + \frac{6}{23}T_{AC} + \frac{2}{11}T_{AD} = 0 \tag{1}$$

$$\mathbf{j}: \qquad -\frac{6}{7}T_{AB} - \frac{18}{23}T_{AC} - \frac{9}{11}T_{AD} + P = 0$$
(2)

$$\mathbf{k}: \qquad \frac{2}{7}T_{AB} + \frac{13}{23}T_{AC} - \frac{6}{11}T_{AD} = 0 \tag{3}$$

Set $T_{AB} = 630$ lb in Eqs. (1) – (3):

$$-270 \text{ lb} + \frac{6}{23} T_{AC} + \frac{2}{11} T_{AD} = 0$$
^(1')

$$-540 \text{ lb} - \frac{18}{23}T_{AC} - \frac{9}{11}T_{AD} + P = 0$$
^(2')

$$180 \text{ lb} + \frac{13}{23}T_{AC} - \frac{6}{11}T_{AD} = 0 \tag{3'}$$

Solving,
$$T_{AC} = 467.42 \text{ lb}$$
 $T_{AD} = 814.35 \text{ lb}$ $P = 1572.10 \text{ lb}$ $P = 1572 \text{ lb}$



A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AD is 520 N, determine the weight of the plate.

SOLUTION

See Problem 2.114 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0$$
(1)

$$-\frac{12}{17}T_{AB} + 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0$$
(2)

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0$$
(3)

Making T_{AD} = 520 N in Eqs. (1) and (3):

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + 200 \text{ N} = 0 \tag{1'}$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - 288 \text{ N} = 0 \tag{3'}$$

Multiply (1') by 9, (3') by 8, and add:

$$9.24T_{AC} - 504$$
 N = 0 $T_{AC} = 54.5455$ N

Substitute into (1') and solve for T_{AB} :

$$T_{AB} = \frac{17}{8} (0.6 \times 54.5455 + 200) \quad T_{AB} = 494.545 \text{ N}$$

Substitute for the tensions in Eq. (2) and solve for *P*:

$$P = \frac{12}{17} (494.545 \text{ N}) + 0.64(54.5455 \text{ N}) + \frac{9.6}{13} (520 \text{ N})$$

= 768.00 N Weight of plate = P = 768 N <